Introduction to Structural Causal Models

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Motivation



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Introduction (1)

- Machine learning has provided many insights into different problems
- One issue is the consideration of 'What are we actually predicting?'
- Mainstream tools are build on association-based learning
- Associations are not enough for high stake settings
- We want causation and not correlation

Introduction (2)

Causal assumptions differentiate causal models from association learning methods.

Association-based Concepts	Causal Concepts
Correlation	Randomization
Regression	Confounding
Conditional Independence	Disturbance
Likelihood	Error Terms
Odds Ratio	Structural Coefficients
Propensity Score	Spurious Correlation

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Foundations of SCMs (1)

- System of equations
- Assignment equation ':=' rather than regular equation '='
- Nonparametric SEM
- Functional form rather than using conditional probabilities
- SCM = PO + Graphical Tools
- Exogenous factors are part of the model specification

SCM vs SEM

Error terms

Regression: Omittable outside factor SCM/SEM; Latent influential factor that is pivotal for the model specification but not observable

Consists of graph and assignments: Baseline:

$$C := N_c$$
$$E := f_E(C, N_E)$$

source: Peters, Janzing, and Schölkopf (2017)

Assumptions

- First, there was no sign to express the assignment equation and people used the '=' and one would e.g. write A = B.
- Treating an equation as a **algebraic equation** led to confusion because those have no causal information.
- This algebraic equation would imply that B = A because the order has no concrete meaning in algebraic equations.
- The problem is that the equation is symmetric.
- The initial '=' sign was replaced with the :=' which is asymmetric (Pearl, 2009) and called an **assignment**.
- This misconception has caused a lot of challenges.¹
- As mentioned, we define variables as functions e.g. $A = f_A(B, U_A)$.

¹For more information see Pearl (2009)

Assumptions in Causality

Established Conditions:

Definition: SUTVA

'The treatment that one unit receives does not change the effect of treatment for any other unit.' (Hardt and Recht 2021)

Definition: Consistency

The outcome Y agrees with the potential outcome corresponding to the treatment indicator.' (Hardt and Recht 2021)

Definition: Ignorability

The potential outcomes are conditionally independent of treatment given some set of de-confounding variables. (Hardt and Recht 2021) (perfect RCT)

- First tow hold for SCM counterfactuals
- third not testable but can check via backdoor criterion in SCM

SCM Applications:

- Flexible simulations for higher order problems (intervention, counterfactual)
- Graphical visualization via directed acyclic graph

Fundamental Differences (1)

- conflict whether to use graphs or not
- A SEM is a parametric specification used in applied sciences (parameters contested)
- A Bayesian causal network is another popular causal model using conditional probabilities and NO functions
- Differences in performance between BCN and SCM# Performance Evaluation

Implications

Method	CBN	SCM
Prediction	 Unstable Volatile to parameter changes Re-Estimate entire model	$ \begin{array}{c} \cdot \; \text{Stable} \\ \cdot \; \text{More Natural Specification} \\ \cdot \; \text{Only estimate } \Delta \; \text{CM} \end{array} $
Intervention	 Costly for Non-Markovian Models Unstable(Nature CP) Only generic estimates(Δ CP) 	Pot. Cyclic RepresentationStableContext specific
Counterfactuals	$ \begin{array}{c} \cdot \ \mathbf{Impossible} \\ \cdot \ \mathbf{no} \ \mathbf{information} \ \mathbf{on} \ \mathbf{latent} \\ \mathbf{factors}(\epsilon) \end{array} $	PossibleInclusion of latent factors

Pearls Causal Hierachy

Table 3: Pearls Hierarchy of Causation (2009)

Method	Action	Example	Usage
Association $P(a b)$	Co-occurrence	What happened	(Un-)Supervised ML, BN, Reg.
Intervention $P(a do(b), c)$	Do- manipulation	What happens if	CBN,MDP,RL
Counterfactual $P(a_b a^i,b^i)$	Hypotheticals	What would have happened if	SCM ,PO

Prediction

- ML, BN and regression are at the lowest level in the causal hierarchy
- Prediction methods demand the least information and depend on association alone
- Associational methods ignore external changes outside of our data.
- intervention distribution has information on these external changes.
- intervention distribution is only defined in high level causal methods.

Intervention

- The second query deals with interventions
- Mathematical Tool: do-calculus
- The do-calculus enables us to study the manipulation of parent nodes
- There are various types of intervention
- One example is atomic intervention, where we set a variable to a constant
- In policy intervention we specify a different function for an equation
- Off-policy intervention models different intervention that is not in our historical data
- CBN, MDP and reinforcement learning model intervention.

Example Intevention

Counterfactuals

Process is described as follows:

- **a** Abduction: Cast probability P(u) as conditional probability $P(u|\epsilon)$
- **1** Action: Exchange (X = x)
- **1** Prediction: Compute (Y = y)

Graphical Tools

- Nodes
- Edges
- Parents/Ancestors/Descendents
- (Missing) Arrows

Graphical Illustration - Probabilisitic Model

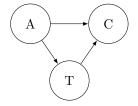


Figure 1: Probabilistic Model

Graphical Illustration - Structural Causal Model

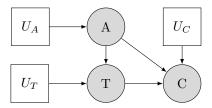


Figure 2: Structural Causal Model

Causality and Time

- Time in Physical Sciences: Mechanical and exact
- Time in Social Sciences: Often Vague
- Regular Time Specification is also more vague
- To accommodate that issue, research on differential equation based SCMs started

Graphical Overview

model	predict in IID setting	predict under changing distributions / interventions	answer counter- factual questions	obtain physical insight	automatically learn from data
mechanistic model	Y	Y	Y	Y	?
structural causal model	Y	Y	Y	N	Y??
causal graphical model	Y	Y	N	N	Y?
statistical model	Y	N	N	N	Y

References

Hardt, Moritz, and Benjamin Recht. 2021. *Patterns, Predictions, and Actions: A Story about Machine Learning*. https://mlstory.org. http://arxiv.org/abs/2102.05242.

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