

$$\frac{\partial l}{\partial \beta} = \sum_{i=1}^m \frac{\partial l}{\partial y_i} \quad ; \quad \frac{\partial l}{\partial \gamma} = \sum_{i=1}^m \frac{\partial l}{\partial y_i} \hat{x}_i$$

$$\frac{\partial l}{\partial x_i} = \frac{\partial l}{\partial y_i} \times \gamma \times \left\{ \frac{\partial \hat{x}_i}{\partial x_i} \right\}$$

$$\frac{\partial \hat{x}_i}{\partial x_i} = \frac{\partial}{\partial x_i} \left(\frac{x_i - \mu_B}{\sqrt{\sigma_B^2 + \epsilon}} \right) = \frac{\sqrt{\sigma_B^2 + \epsilon} \left(1 - \frac{1}{m}\right) \left\{ (x_i - \mu_B) \times \frac{1}{2\sqrt{\sigma_B^2 + \epsilon}} \times \frac{\partial \sigma_B^2}{\partial x_i} \right\}}{\sigma_B^2 + \epsilon}$$

$$= \frac{\left(1 - \frac{1}{m}\right)}{\sqrt{\sigma_B^2 + \epsilon}} \left\{ \frac{x_i - \mu_B}{2(\sigma_B^2 + \epsilon)^{3/2}} \times \frac{\partial \sigma_B^2}{\partial x_i} \right\}$$

$$\frac{\partial \sigma_B^2}{\partial x_i} = \frac{1}{m} \sum_{i=1}^m \left(1 - \frac{1}{m}\right) 2(x_i - \mu_B)$$

$$= \frac{1}{m} 2 \sum_{i=1}^m (x_i - \mu_B) - \frac{1}{m} 2 \left(\sum_{i=1}^m \frac{x_i}{m} - \sum_{i=1}^m \frac{\mu_B}{m} \right)$$

$$= \frac{2}{m} \sum_{i=1}^m (x_i - \mu_B) - \frac{2}{m} \left(\mu_B - \frac{m \mu_B}{m} \right)$$

$$= \frac{2}{m} \sum_{i=1}^m (x_i - \mu_B)$$

$$\frac{\partial \hat{x}_i}{\partial x_i} = \frac{1}{\sqrt{\sigma_B^2 + \epsilon}} - \frac{1}{m \sqrt{\sigma_B^2 + \epsilon}} - \frac{(x_i - \mu_B)}{2(\sigma_B^2 + \epsilon)^{3/2}} \times \frac{2}{m} \sum_{i=1}^m (x_i - \mu_B)$$

$$\frac{\partial l}{\partial x_i} = \gamma \left\{ \frac{\partial l}{\partial y_i} \frac{1}{\sqrt{\sigma_B^2 + \epsilon}} - \frac{\partial l}{\partial y_i} \frac{1}{m \sqrt{\sigma_B^2 + \epsilon}} - \frac{\sum_{i=1}^m \frac{\partial l}{\partial y_i} (x_i - \mu_B)}{m \times (\sigma_B^2 + \epsilon)^{3/2}} \times (x_i - \mu_B) \right\}$$