

Elastocapillary Crease

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A material under compression often forms creases. When the material is elastic and soft, the nucleation of creases depends on both elasticity and capillarity. Here we introduce a model of elastocapillary creases. The model assumes that the surface tension remains constant on the free surface, but may change upon self-contact. In particular, surface tension vanishes upon self-contact for a pristine surface of elastomers and gels. The model predicts that the nucleation of creases depends on the sizes of surface defects relative to the elastocapillary length, and happens over a well-defined range of strains, instead of a specific strain. The loss of surface tension upon self-contact lowers the energy barrier for nucleation, and widens the range of nucleation strains for materials of any thickness relative to the elastocapillary length. We test this model by conducting experiments with materials of various elastocapillary lengths, along with the data available in the literature.

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Buckling a bar and blowing a bubble are elastic and capillary instabilities. Such familiar instabilities have long appealed to researchers for broad applications, as well as in developing concepts and tools for studying diverse—and often less familiar—instabilities in physics, chemistry, and biology. Much attention has also been paid to elastocapillary phenomena, such as fracture [1,2], adhesion [3–9], cavitation [10–12], compositional patterns [13,14], and morphological changes [9,15–17].

This Letter focuses on an elastocapillary instability: creases nucleated on soft and elastic materials under compression. Creases are commonly observed on rubbers [18,19], gels [20–24], and soft tissues [25,26]. Creases have been used to demonstrate stimuli-responsive displays of bimolecular patterns [27], stem cell differentiation [28], tunable adhesion [29], and switchable chemical patterns [30]. As ubiquitous as creases are, their scientific studies have led to conflicting findings. When capillary effect is weak, the crease forms at a specific strain [18,31,32], much below the critical strain predicted by a linear perturbation analysis [15]. When capillary effect is strong, one experiment reports that a crease nucleates near a specific strain predicted by the linear perturbation analysis [16], but another experiment reports that a crease extends at a specific strain much below the prediction of the linear perturbation analysis [17]. Existing models of elastocapillary creases characterize the strength of capillary effect by the elastocapillary length relative to the thickness of materials, but not relative to the size of defects [16,17,23]. The situation is puzzling, as one expects that the nucleation of creases is defect sensitive.

Here we reconcile the conflicting findings by a new model of elastocapillary creases. The model assumes that surface tension is constant on the free surface, but may change upon self-contact. In particular, the surface tension vanishes upon self-contact for a pristine surface of elastomers and gels. The model predicts that the nucleation of creases depends on the sizes of surface defects relative to the elastocapillary length, and happens in a range of strains, instead of at a specific strain. The range of nucleation strains is well-defined by the thickness of materials relative to the elastocapillary length. The loss of surface tension upon self-contact lowers the energy barrier for nucleation and widens the range of nucleation strains for materials of any size and elastocapillary length. We test this model by conducting experiments with materials of varying elastocapillary lengths, along with the data available in the literature.

We compare four models of surface instability (Fig. 1). Corresponding to each model is a distinct bifurcation diagram, which we sketch on the plane of the applied strain ϵ and the amplitude of deviation from the flat surface A . The former is a loading parameter, and the latter a proxy for the state of deformation. A state of equilibrium corresponds to a point in the ϵ - A plane. A stable state corresponds to a local energy minimum, and an unstable state corresponds to a local energy maximum. As the applied strain changes, a sequence of equilibrium states forms a path. (The applied strain is the compressive displacement divided by the undeformed length of the sample. Unless otherwise stated, the material is taken to deform under the plane strain condition.) This Letter

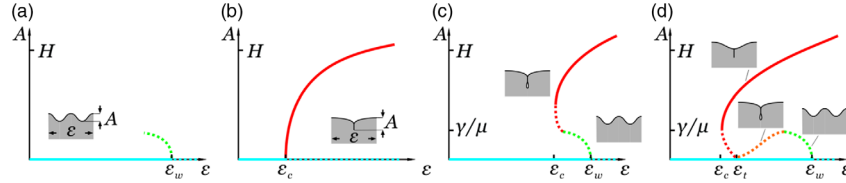


FIG. 1. Bifurcation diagrams of four models of instability. In the bifurcation diagrams, different colors mean different surface morphologies. Solid lines mean stable states and dotted lines mean unstable states. (a) Elastic wrinkles. (b) Elastic creases. (c) Elastocapillary creases of constant surface tension. (d) Elastocapillary creases with vanishing surface tension upon self-contact.

focuses on the nucleation of creases, not the subsequent evolution of the creases. The theory assumes that the soft material is elastic, and neglects any migration of solvent in the material.

In the absence of surface tension, the onset of wrinkle and the onset of crease are two distinct elastic instabilities. A wrinkle is a smooth undulation of the surface, the calculated strain for the onset of the wrinkle is $\varepsilon_w = 0.46$ [15], and the wrinkled state is unstable [33] [Fig. 1(a)]. A crease is a self-contact of the surface, the calculated strain for the onset of crease is $\varepsilon_c = 0.35$ [31,32], and the creased state is stable [34] [Fig. 1(b)]. Since crease has lower critical strain and is stable, crease is the only observable surface instability.

The model of elastic creases makes a remarkable prediction: creases nucleate at a specific strain. This prediction is understood as follows. The model assumes neo-Hookean elasticity, which well describes the soft elastic materials used in experiments (elastomers and gels) at the level of strain for crease nucleation. The model has a single material parameter, the shear modulus, and has no material-specific length. The size of the specimen is irrelevant to the onset of a crease, because the crease can be arbitrarily small. Consequently, the nucleation of the crease is scale-free, fully determined by the local state of strain. The model has no other dimensionless parameter, and predicts that the nucleation strain is independent of material, specimen geometry, and surface defects.

In the presence of surface tension, a material-specific length emerges: the elastocapillary length γ/μ , where γ is the surface tension and μ is the shear modulus. We neglect the change in surface tension due to deformation. For a defect-free elastic film of thickness H in the stress-free state, the elastocapillary number $\gamma/\mu H$ and the applied strain ε are the only dimensionless parameters in this elastocapillary boundary value problem.

We assume that the surface tension of a soft material does not change with deformation, but may change upon self-contact [35]. For an elastomer, segments of a polymer chain far away from crosslinkers behave as if in a polymer melt. Upon self-contact, the polymer segments mix across the contact. For a highly swollen gel, the surface tension is dominated by that of the solvent [8,40]. Upon self-contact, the solvent mixes across the interface. Consequently, a clean surface of an elastomer or a gel completely loses surface tension upon self-contact. A contaminated surface

may retain some surface tension upon self-contact. As will become clear, the loss of surface tension upon self-contact profoundly affects the nucleation of creases.

We first consider a model of elastocapillary creases with constant surface tension γ everywhere [Fig. 1(c)]. When the surface is curved with a local radius of curvature R , the surface tension produces the Laplace pressure $p = \gamma/R$. If the self-contact retains the surface tension, a crease must have a rounded tip since a sharp crease tip would result in a diverging Laplace pressure. The size of the round tip must scale with the only length scale γ/μ . Consequently, an infinitesimal crease is no longer possible. Accordingly, the previously derived bifurcation to form sharp-tip crease of arbitrarily small size does not exist anymore. The surface can only become unstable and bifurcates into a wrinkle at a higher critical strain ε_w . As we will show later by finite element simulation, this wrinkle is unstable, corresponding to the green portion of the postbifurcation path in Fig. 1(c). The neighboring peaks contact each other when the amplitude of the wrinkle A is comparable to the elastocapillary length γ/μ . The self-contact stabilizes the undulated surface and turns the post-bifurcation path around [Fig. 1(c) red line]. We identify the point where the postbifurcation path turns around as the critical point of crease, with the strain ε_c . In the presence of surface tension, creasing and wrinkling are no longer different instabilities, but are different stages of the same instability.

We next consider the model of elastocapillary creases with vanishing surface tension upon self-contact [Fig. 1(d)]. Before the surface self-contacts, the two models of elastocapillary creases have the same behavior. Once the surface self-contacts, the loss of surface tension in the second model zips up the contact. Since the size of the crease tip scales with γ/μ , the vanishing surface tension implies a crease of a sharp tip. A triple line forms where the free surface and the self-contact meet. Since the free surface has constant surface tension and the self-contact has vanishing surface tension, the balance of forces at the triple line requires that the free surface be flat and that the self-contact be vertical to the free surface. Since the zipped crease can continuously shrink to infinitesimal size, a surface with infinitesimal crease is on the postbifurcation path. As an infinitesimal crease only infinitesimally perturbs the free energy from a flat state, the postbifurcation path representing crease [Fig. 1(d) red] and the fundamental path representing the flat surface

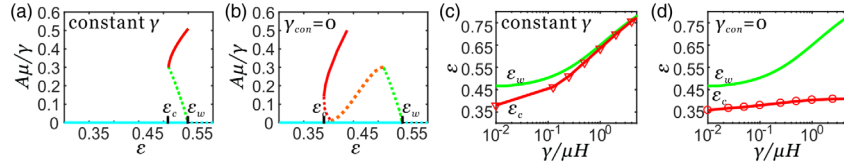


FIG. 2. Finite element simulation of the two models of elastocapillary creases. Bifurcation diagrams for the elastocapillary crease of (a) constant surface tension, and (b) vanishing surface tension upon self-contact. The unzipping portion of the postbifurcation path (orange) is not simulated, but is schematically drawn to connect the simulated parts of the postbifurcation path. Critical strains as functions of the elastocapillary number predicted by the model of elastocapillary crease of (c) constant surface tension, and (d) vanishing surface tension upon self-contact.

[Fig. 1(d) blue] must touch. Although an infinitesimal crease and the flat surface have the same free energy at the touch point (at strain ϵ_t), the touch point is not a bifurcation point because surface tension imposes an energy barrier between the flat state and the creased state. This is similar to the first order phase transition observed in water boiling, where the liquid phase and the vapor phase have the same free energy at boiling temperature, but a vapor bubble has to overcome an energy barrier to nucleate from the liquid phase. We again identify the point where the postbifurcation path becomes stable as the critical point of crease.

We compute the bifurcation diagrams of the two models of elastocapillary creases using the finite element method [41]. For example, consider the computed bifurcation diagrams for the elastocapillary number $\gamma/\mu H = 0.25$ [Figs. 2(a) and 2(b)]. The wrinkle forms at $\epsilon_w = 0.55$, in agreement with the analytical result obtained from the linear perturbation analysis [43]. The wrinkle is subcritical. For the model of constant γ , the self-contact point and the critical point of crease coincide at $\epsilon_c = 0.51$, although the two points may separate for other values of the elastocapillary number (Fig. S2 [41]). For the model with $\gamma_{\text{con}} = 0$, the postbifurcation path of the zipped crease [Fig. 2(b) red] touches the horizontal line of the fundamental path. The critical strain for crease predicted by the model of elastocapillary creases with vanishing surface tension upon self-contact is $\epsilon_c = 0.39$, which is much below the value 0.51 predicted by the model of elastocapillary creases with constant surface tension and is somewhat above the value 0.35 predicted by the model of elastic creases.

To appreciate the significance of the loss of surface tension upon self-contact, we compare the critical strains of the two models of elastocapillary creases [Figs. 2(c) and 2(d)]. The critical strain of wrinkle ϵ_w is the same for both models, and is calculated analytically [43]. However, the critical strain of crease ϵ_c differs for the two models. When $\gamma/\mu H \rightarrow 0$, both elastocapillary models recover the predictions of the models of elastic crease and elastic wrinkle. But as $\gamma/\mu H$ increases, the model of constant surface tension predicts increasingly high ϵ_c , close to ϵ_w , because the surface tension greatly penalizes the increased surface area in the crease. The difference between ϵ_c and ϵ_w is less than 0.02 for $\gamma/\mu H > 1$. For the model of vanishing surface tension upon self-contact, ϵ_c also increases with $\gamma/\mu H$,

but asymptotes to a value of 0.41. The asymptote exists because when the surface tension is high, the free surface becomes hard to deform and effectively remains flat as the crease forms (Fig. S3 [44]). Forming a crease while maintaining a flat free surface is a pure elastic problem independent of the elastocapillary number $\gamma/\mu H$. A comparison of the two models shows that the loss of surface tension upon self-contact does not change the gap between ϵ_c and ϵ_w when $\gamma/\mu H$ is small, but greatly widens the gap when $\gamma/\mu H$ is large.

Our model predicts that defects affect nucleation strains (Fig. 3). In the presence of a defect of size d , a new dimensionless number emerges, the elastocapillary number of the defect, $\gamma/\mu d$, in addition to the other two dimensionless numbers, the elastocapillary number of the specimen, $\gamma/\mu H$, and the applied strain ϵ . If $d \ll \gamma/\mu$, the surface tension smoothens the defect, so that the surface only becomes unstable near ϵ_w , and then snaps into a crease. If $d \gg \gamma/\mu$, the strain at the defect is much higher than the overall strain in the material, so that the defect can be compressed into self-contact at a relatively low overall strain, and deepens substantially near ϵ_c . For a defect of arbitrary size, the nucleation strain of a crease should be bounded by these two limits, ϵ_c and ϵ_w .

We characterize the strength of capillary effect by comparing the elastocapillary length both to the thickness of the specimen, $\gamma/\mu H$, and to the size of the defect, $\gamma/\mu d$. The former sets the range of nucleation strains, and the latter the observed nucleation strain. A stiff elastomer, of $\gamma = 10$ mN/m and $\mu = 1$ Mpa, has an elastocapillary length of $\gamma/\mu = 10$ mN. It is common to have $d \gg 10$ and $H \gg 10$ nm, so that the model of elastic creases prevails: creases nucleate on the stiff elastomer at the specific strain of $\epsilon_c = 0.35$. By contrast, a soft hydrogel, of $\gamma = 70$ mN/m and $\mu = 100$ pa, has an elastocapillary length of $\gamma/\mu = 0.7$ mm. Defects of sizes smaller than the elastocapillary length are obtained with common laboratory procedures, so that the nucleation of creases is defect insensitive, at a specific strain ϵ_w , set by the value of $\gamma/\mu H$. Between the two extreme cases, a hydrogel of $\gamma = 70$ mN/m and $\mu = 10$ kpa has an elastocapillary length of $\gamma/\mu = 7$ μ m. Defects of sizes both larger and smaller than the elastocapillary length are readily available, so that the nucleation of creases is defect sensitive, and

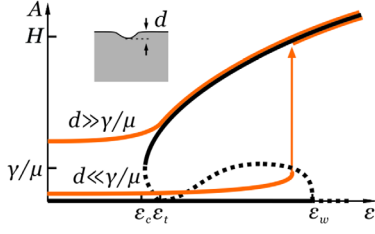


FIG. 3. The observed nucleation strain for a crease depends on the size of a defect relative to the elastocapillary length. (a) If $d \ll \gamma/\mu$, a crease nucleates near ϵ_w . (b) If $d \gg \gamma/\mu$, a crease nucleates near ϵ_c .

happens in a range of strains. Whereas constant surface tension causes a wide range of nucleation strains only for small values of $\gamma/\mu H$ [Fig. 2(c)], the loss of surface tension causes a wide range of nucleation strains for all values of $\gamma/\mu H$ [Fig. 2(d)].

We experimentally verify our model of elastocapillary creases [45]. We cure a polyacrylamide hydrogel, thickness $H = 1$ mm, shear modulus between 0.16 and 8.7 kPa, on a prestretched polyurethane “mounting layer.” The surface tension of the hydrogel is taken as that of the precursor solution, which is about 65 mN/m. Consequently, the elastocapillary length γ/μ varies from 7.3 μm to 0.4 mm (Table S2), and the elastocapillary number $\mu/\gamma H$ of the specimen varies from 0.0073 to 0.4. The prestretch is later released to compress the hydrogel layer, while the surface of the hydrogel is monitored by a high-speed camera. The nucleation of each crease is then identified by analyzing the video recording. All the experiments are conducted in a humidity chamber to limit the drying of the hydrogel.

We observed crease nucleation from both visible defects [Fig. 4(a), video S1] and invisible defects [Fig. 4(b), video S2]. The visible defects were larger than the invisible defects. The visible defects led to lower nucleation strain, in accord with our model. Our experiments, as well as the data in the literature [16,17], did not contaminate the surfaces. Consequently, we compare the experimentally measured nucleation strains to our theoretical predictions of ϵ_w and ϵ_c according to the model of vanishing surface tension upon contact [Fig. 4(c)]. Since the strain in the hydrogel film is not homogeneous after the first nucleation of the crease or at the edge of the hydrogel, we only plot the nucleation strain of the first crease that nucleates from the center of each sample. Our finite element simulations are under the plane strain condition, but our experiments are conducted under uniaxial force. We convert the nucleation strain under the plane strain condition to that under uniaxial force [46].

As predicted by our model, for a given value of $\gamma/\mu H$, creases nucleated in a range of strains, rather than at a specific strain, and the distribution was confined between ϵ_w and ϵ_c [Fig. 4(c)]. As $\gamma/\mu H \rightarrow 1$, more creases nucleated near ϵ_w , probably because naturally occurring defects were much smaller than the film thickness of 1 mm, so that $d \ll \gamma/\mu$. The nucleation strains reported in Mora *et al.* [16]

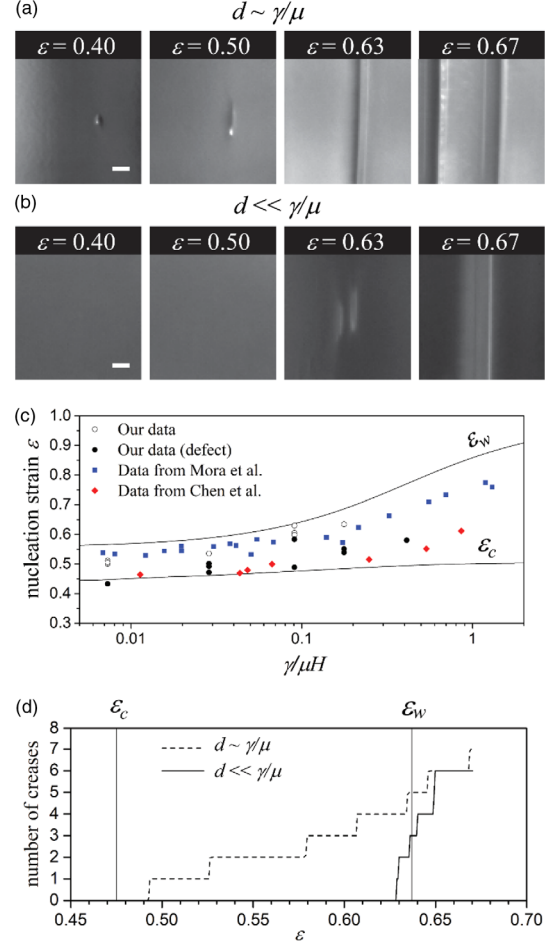


FIG. 4. Defect sensitivity is demonstrated by comparing (a) a sample with visible defects $d \sim \gamma/\mu$, and (b) crease nucleated from the center part of the sample without visible defects $d \ll \gamma/\mu$. For both samples, $\gamma/\mu = 0.091$ and $H = 1.0$ mm. The scale bar is 0.3 mm. (c) Experimentally measured nucleation strains are compared with theoretically predicted range of nucleation strains assuming vanishing surface tension upon self-contact. In the legend, (defect) means a first crease formed from the center of the sample associated with a visible defect. (d) The nucleation history of the samples of (a) and (b).

are close to higher limit ϵ_w , possibly because the soft hydrogels they used (12–4200 Pa) result in elastocapillary lengths much larger than defects. Chen *et al.* [17] reported the channeling strain in an elastomer with thickness gradient. The data are close to the lower limit ϵ_c because channeling creases come from existing creases, which act as large defects.

After the nucleation of the first crease, more creases nucleate as the sample is further compressed [Fig. 4(d)]. Since the strain on the hydrogel is no longer homogeneous after the nucleation of the first crease, the exact nucleation strain of these subsequent creases cannot be determined from our experiment. We may nevertheless make some qualitative observation based on the distribution of the nucleation strains. For $H = 1.0$ mm and $\gamma/\mu = 90 \mu\text{m}$,

defects larger than $90\text{ }\mu\text{m}$ occur rather scarcely. Consequently, even if we have visible defects [Fig. 4(a), video S1], few creases nucleate from defects of $d \sim \gamma/\mu$ at a strain much below ε_w while most creases nucleate from defects of $d \ll \gamma/\mu$, at a strain close to ε_w . On the other hand, if there is no visible defect, which means that all the defects have size $d \ll \gamma/\mu$, all creases nucleate almost simultaneously near ε_w [Fig. 4(b), video S2]. Since the earlier forming crease would locally relax the compressive strain, we always observe the last few creases nucleating above ε_w of the mounting layer. This observation should not be taken as a violation of the theory.

In summary, we have developed a model of elastocapillary crease, and tested the model with experiments reported here and available in the literature. So long as surface defects have a statistical distribution and can be both larger and smaller than the elastocapillary length, creases nucleate in a range of strains, instead of at a specific strain. The range of nucleation strain is well defined for a given material thickness relative to the elastocapillary length. The loss of surface tension upon self-contact lowers the energy barrier for nucleation, and widens the range of nucleation strains for materials of any thickness relative to the elastocapillary length.

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- [44] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.122.098003> for the finite element simulation of when surface energy vanishes upon self-contact.
- [45] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.122.098003> for detailed description on experimental verification.
- [46] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.122.098003> for a discussion on generalized plane strain condition in elastocapillary problems, which includes Ref. [32].