

Proposed solutions 7b

$$1) a) E_x = -\frac{1}{K_{mn}^2} K_m K_p A \cos K_m x \sin K_n y \sin K_p z$$

$$E_y = -\frac{1}{K_{mn}^2} K_n K_p A \sin K_m x \cos K_n y \sin K_p z$$

$$E_z = A \sin K_m x \sin K_n y \cos K_p z$$

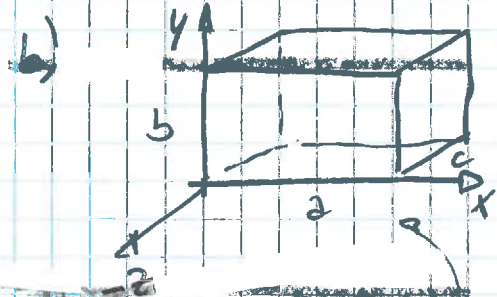
~~$$H_x = \frac{j\omega\epsilon}{K_{mn}^2} K_m A \sin K_m x \cos K_n y \cos K_p z$$~~

$$H_y = -\frac{j\omega\epsilon}{K_{mn}^2} K_n A \cos K_m x \sin K_n y \cos K_p z$$

$$H_z = 0$$

$$m, n = 1, 2, 3, \dots$$

$$p = 0, 1, 2, 3, \dots$$

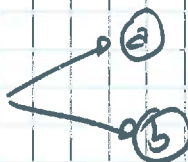


(out of scale...)

$$a = c = 2b$$

For this system of coordinates the dominant mode is the TE_{101} mode

$$c) f_{101} = \frac{c}{\sqrt{\epsilon_r} 2} \sqrt{\frac{2}{a^2}}$$



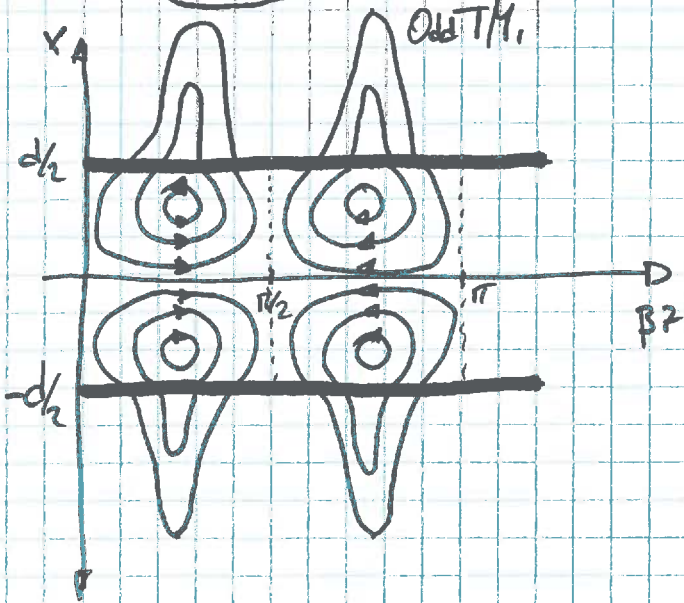
$$a = 21.21 \text{ cm}$$

$$a = 13.26 \text{ cm}$$

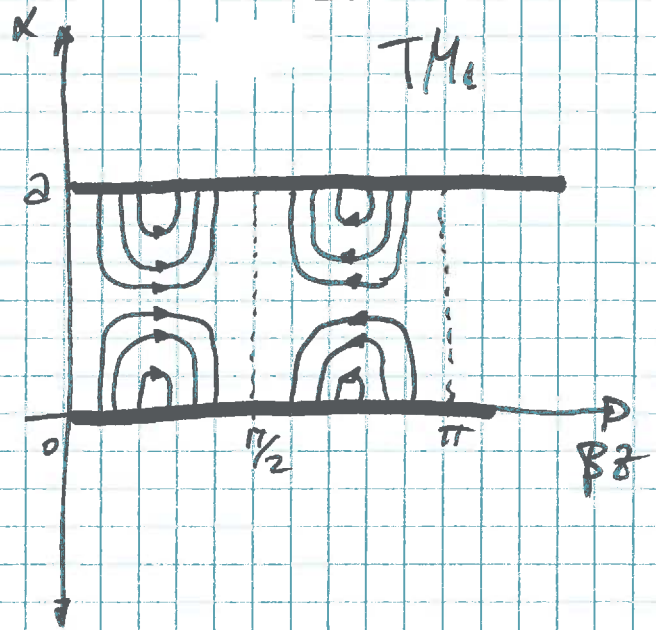
d) See the scan attached at the end

2) a) For the sake of a better comparison, only TM_1 and TM_2 are depicted.

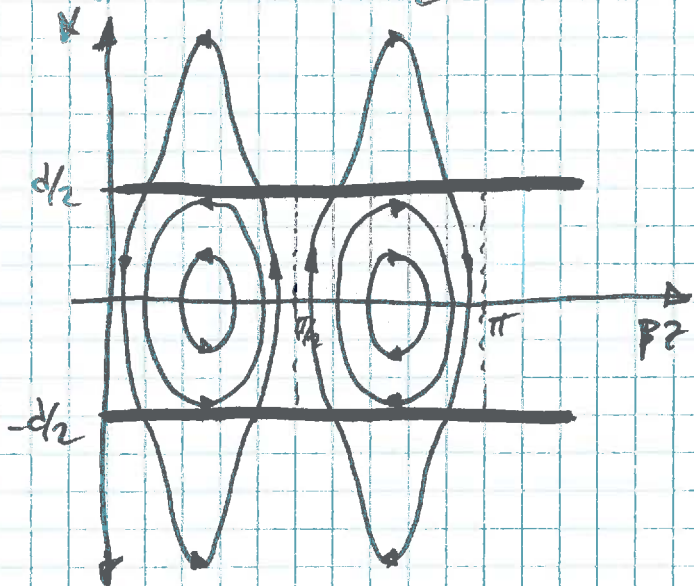
DWG



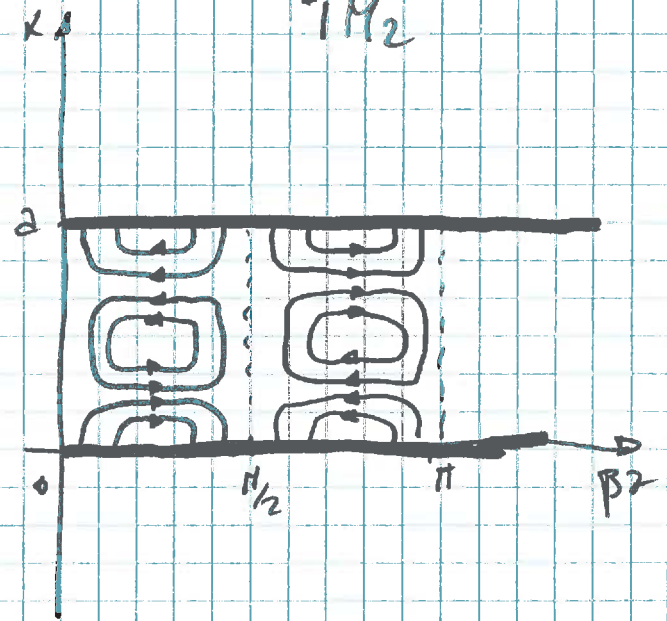
PPW



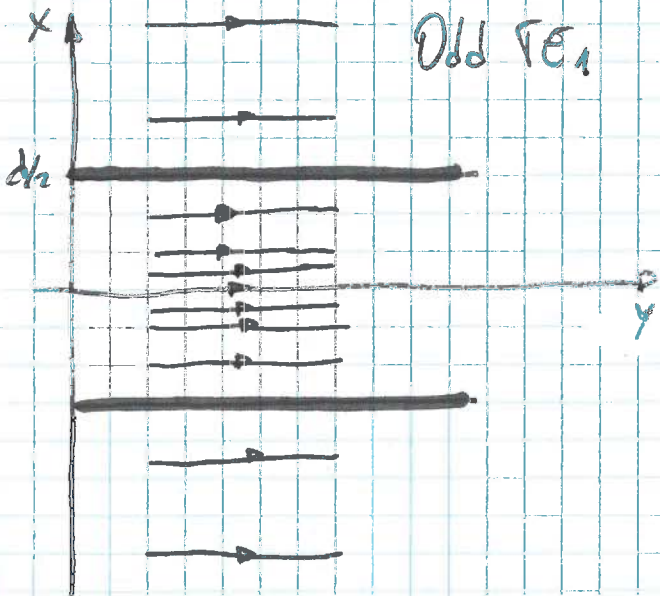
Even TM_2



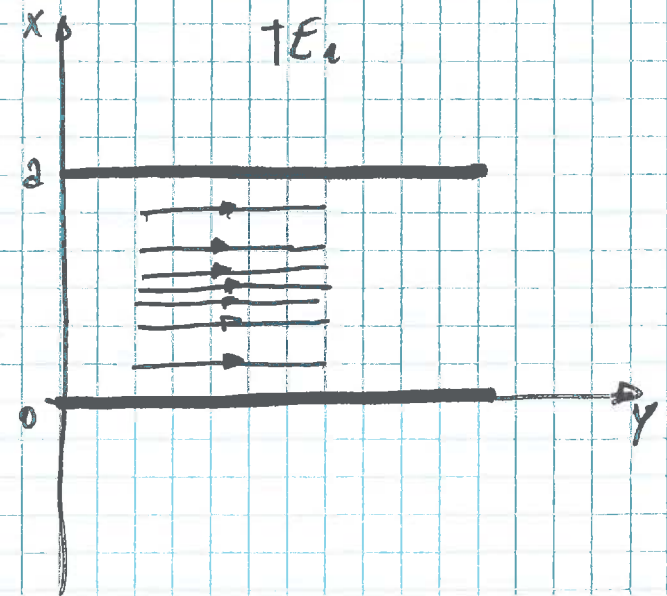
TM_2

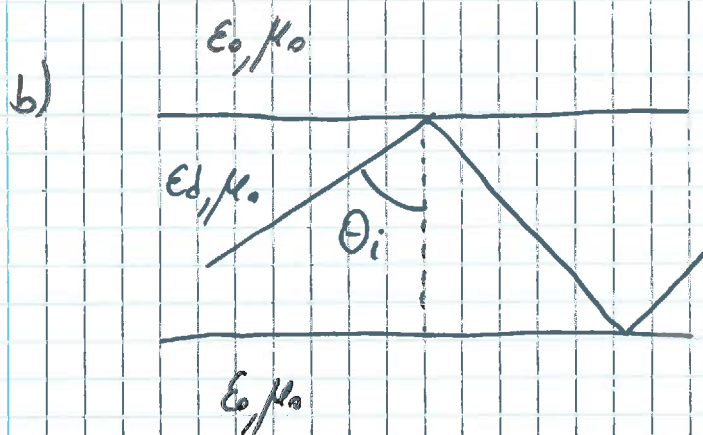
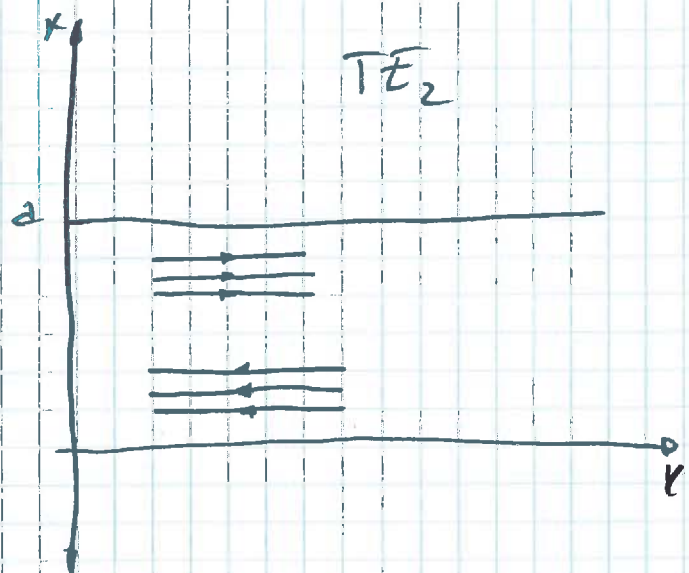
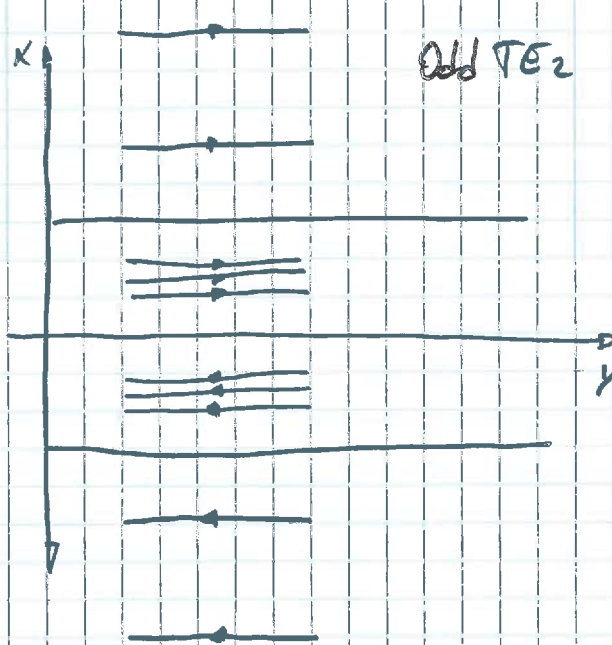


Odd TE_1



TE_1





If θ_i is chosen such that $\theta_i \geq \theta_c$, then there is T.I.R. at the dielectric-air interface. Therefore, only inhomogeneous waves exist in air and the wave is "confined" \Rightarrow can be guided

c) i) $f = \frac{c}{\lambda} = 187,5 \text{ THz}$

$$f_{\text{cTH}_m} = \frac{m-1}{2d\sqrt{\epsilon_1\mu_1 - \epsilon_2\mu_2}}$$

of modes excited is maximum m such that

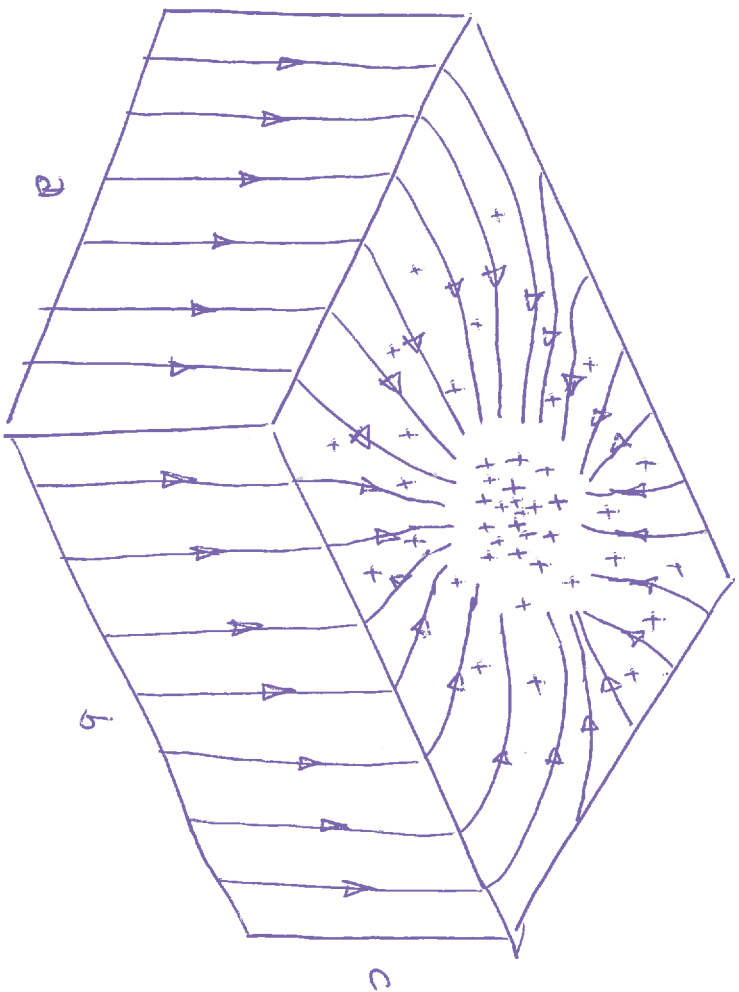
$$f_{\text{cTH}_{m_{\text{max}}}} < f$$

$$m_{\text{max}} < \left\lfloor f 2d \sqrt{\epsilon_1\mu_1 - \epsilon_2\mu_2} + 1 \right\rfloor = \boxed{7}$$

Since cutoffs freqs. for TE modes are the same, then the total amount of propagating modes is $\boxed{14}$

2) \nexists d such that the DWG propagates only one mode
(TE and TM are always degenerate modes in a DWG)

$$\frac{p}{\rho_s} \bar{I}_s$$



(You can picture the bottom side and the hidden walls)