

# Operating Systems (2INC0)

## Deadlock (08) Terminology

**Dr. Geoffrey Nelissen**

Courtesy of Prof. Dr. Johan Lukkien and  
Dr. Tanir Ozcelebi

(also thanks to Bic & Shaw, Silberschatz, Galvin & Gagne)



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Resource-aware  
Intelligent Systems

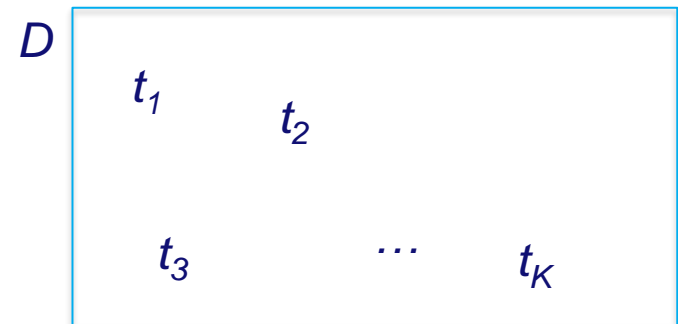
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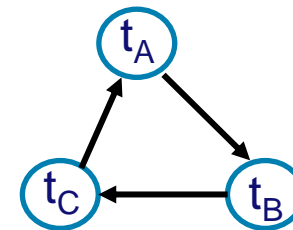
# Formal definitions

- We call a task ***blocked*** if:
  - it is **waiting on a blocking synchronization action**
- A set  $D$  of tasks is called ***deadlocked*** if
  - **all tasks in  $D$  are blocked or terminated** (normally or abnormally),
  - there is **at least one non-terminated** task in  $D$ , and
  - for each non-terminated task  $t$  in  $D$ , any **task that might unblock  $t$  is also in  $D$** .



# Deadlock: conditions

- Program behaviors that may lead to deadlock
  - mutual exclusion
  - greediness: hold and wait
    - incrementally reserving some resources while waiting for other resources to become available (e.g., dining philosophers).
  - absence of preemption mechanism
  - circular waiting
    - e.g., tasks  $t_A$ ,  $t_B$  and  $t_C$  waiting on each other:



A wait-for graph  
(explained next).

- These all play a role and can be (should be) addressed explicitly in the solution.
  - i.e., deadlock is addressed by *avoiding / working better with these behaviors*

# Deadlock: type of resources

- Deadlock is usually associated with access to resources.
- **consumable resources**: resource is taken away upon use  
(→ number of resources varies)
  - typical producer / consumer problems
  - example: characters typed using a keyboard, blocks of data from the network
- **reusable resources**: resource is given back after use  
(→ number of resources is fixed)
  - Typically, **mutual exclusion (critical section)** or **readers/writers type of problems**
  - example: processor, memory blocks, physical entities, variables

# Deadlock: analysis

## Next video:

- **Deadlock detection algorithm** depends on the type of resource:
  - **Consumable:** *wait-for graph*
  - **Reusable:** *dependency graph*

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## Deadlock analysis

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# Model for analysis: graphs

- **Analysis of deadlocks:**
  - **Consumable resources** and **condition synchronizations:**  
*wait-for graph*
  - **Reusable resources** and **action synchronizations:**  
*dependency graph*

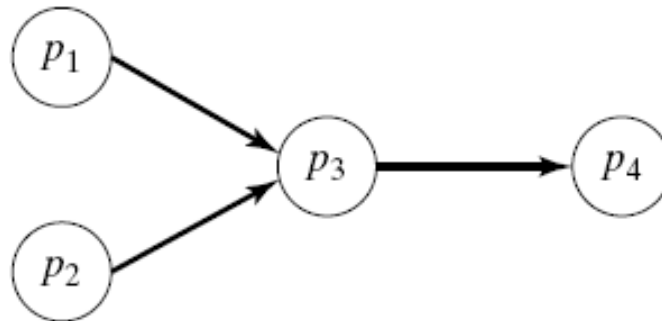
# Model for analysis: graphs

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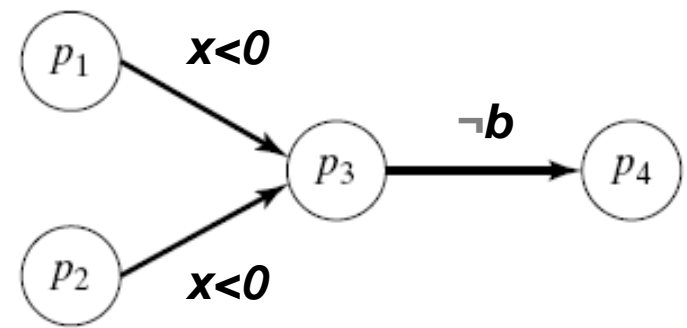
# Wait-for graph

- **Wait-for graph:**
  - **Nodes = tasks**
    - i.e., the activities, thread/process
  - **Edges = a *wait-for* (i.e. *blocked-on*) relationship**
    - an edge  $p_1 \rightarrow p_3$  means that  $p_1$  may unblock  $p_3$  (*textbook uses it differently*)



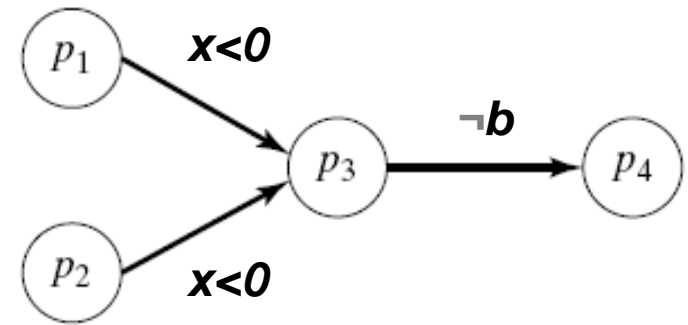
# Wait-for graph

## Example



- $p_1$ : ...  $P(m)$ ;  $x := x+y$ ; **sigall(c)**;  $V(m)$  ...
  - $p_2$ : ...  $P(m)$ ;  $x := a$ ; **sigall(c)**;  $V(m)$  ...
  - $p_3$ : ...  $P(m)$ ; **while**  $x < 0$  **do** **wait(m,c)** **od**;  $x := x-1$ ;  $b := \text{true}$ ; **signal(d)**;  $V(m)$  ...
  - $p_4$ : ...  $P(m)$ ; **while** **not**  $b$  **do** **wait(m,d)** **od**; ...  $b := \text{false}$ ;  $V(m)$  ...
- 
- The graph captures a *possible dynamic* situation (reachable system state),
    - We must **prove the possibility of existence** of the graph
      - e.g., if  $a$  is always negative, there is never a state with an arrow  $p_2 \rightarrow p_3$
    - We **label** the edges with corresponding **blocking conditions**
      - i.e., information about the state that gives the specific blocking
      - e.g., at this state  $p_3$  is blocked due to  $x < 0$  and  $p_4$  is blocked due to  $\neg b$
  - Note:
    - We **leave out the dependency on the mutex  $m$**  since we know mutual exclusion does not add to deadlock provided that the critical sections terminate as it is the case in the example.

# Wait-for graph Analysis



- **Deadlock** possible **only if** there is a **cycle** in the wait-for graph
- How to prove the absence of deadlock?
  - Proof by contradiction:
    - **Assume there is a deadlock** between the **tasks involved in a cycle**
    - **Prove that at least one task can be unblocked by a task that is not involved in that cycle**

# Model for analysis: graphs

- **Analysis of deadlocks:**
  - **Consumable resources** and **condition synchronizations:**  
*wait-for graph*
  - **Reusable resources** and **action synchronizations:**  
*dependency graph*

# Resource dependency graph

- **Resource dependency graph:**

- bipartite graph with **two classes of nodes** = **tasks** and **resources**

- **three types of edges**

- Type1: **task** has **requested** and now waits for the **resource**
- Type2: **resource acquired (held) by task**
- Type3: **task may request** the **resource**

$p \longrightarrow R : p \text{ requests } R$

$R \longrightarrow p : p \text{ holds } R$

$p \dashrightarrow R : p \text{ may request } R$

- A **resource dependency graph** represents a **particular state of the system**
- **Three type of events may change the state**
  - *request* (by a task),
  - *acquire* (response to a request by the system, according to a policy),
  - *release* (by the task)

# Resource dependency graph

## Example

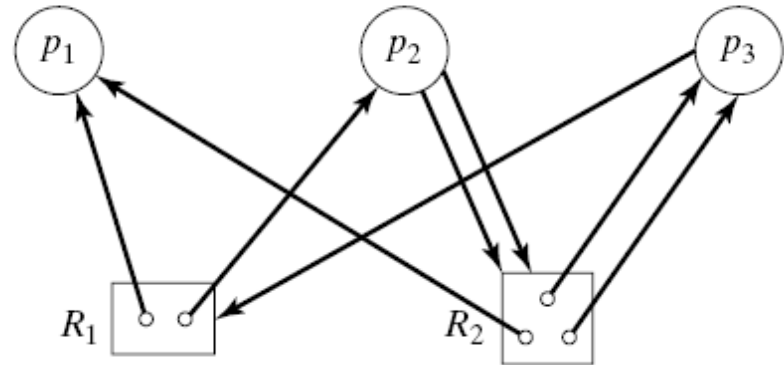
- Edges

- $p \xrightarrow{\text{solid}} R$ :  $p$  requests  $R$
- $R \xrightarrow{\text{solid}} p$ :  $p$  holds  $R$
- $p \xrightarrow{\text{dashed}} R$ :  $p$  may request  $R$

- Example (graph shown)

- $p_1$  holds one of  $R_1$  and one of  $R_2$
- $p_2$  holds one of  $R_1$  and requests two of  $R_2$
- ...

- $p$  is **blocked** if it has an outgoing edge that is not directly removable
  - i.e., for which **the requested resource is free**



# Resource dependency graph

## Example

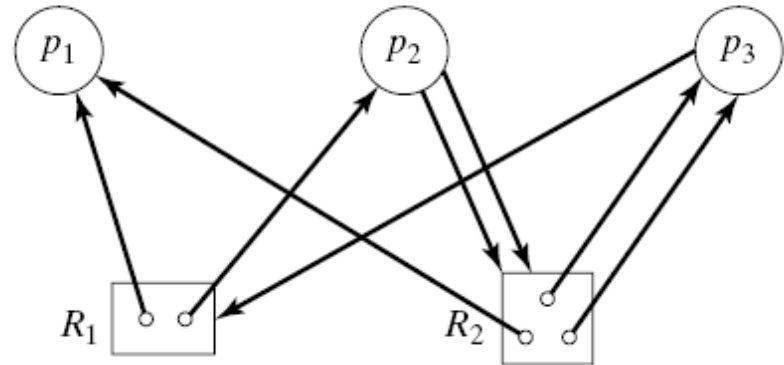
- Edges

- $p \longrightarrow R$ :  $p$  requests  $R$
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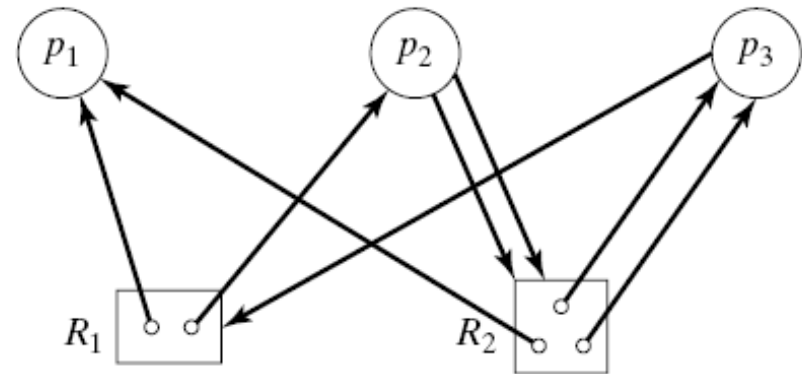
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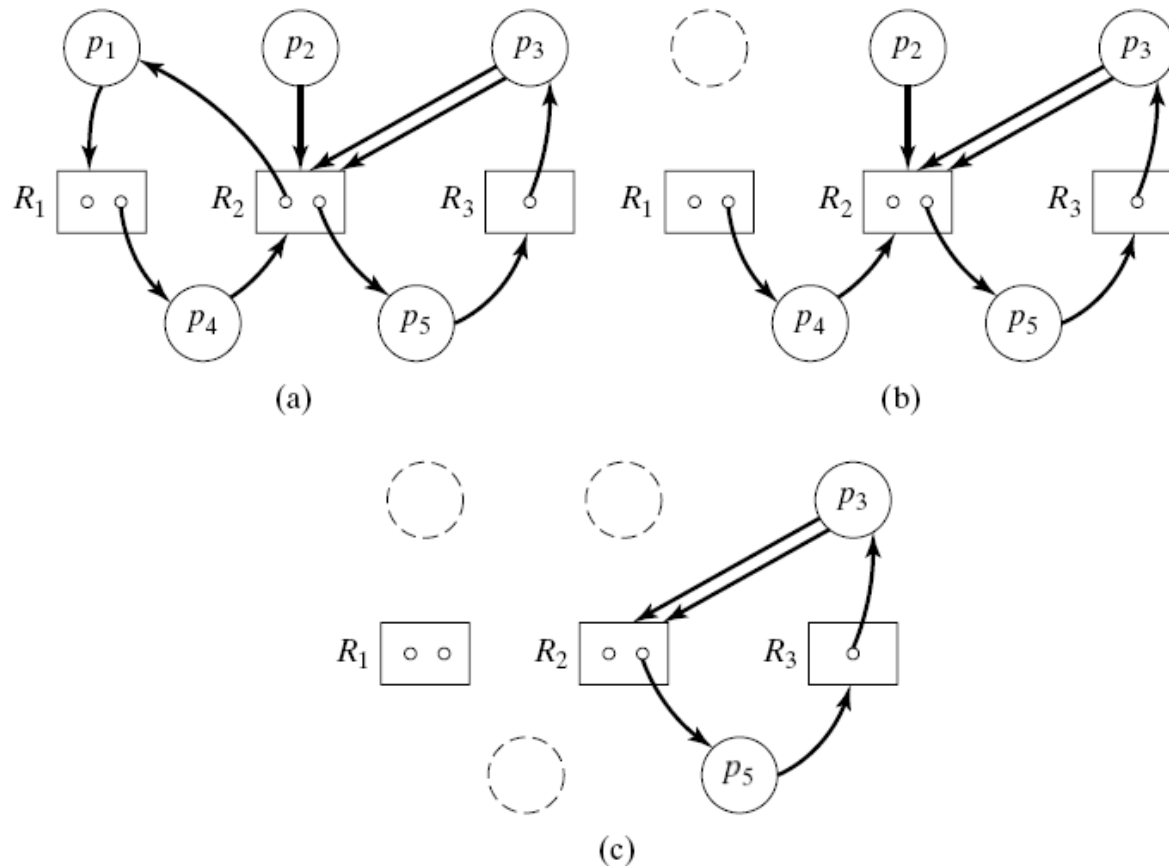
# Resource dependency: reduction

- Assume that the graph represents a *stable* state, **repeatedly remove a non-blocked task** and all its incoming connections
  - Simulates the completion of that task critical section
- If there is a **remaining set** after reduction = **deadlocked**
  - Called a *knot*





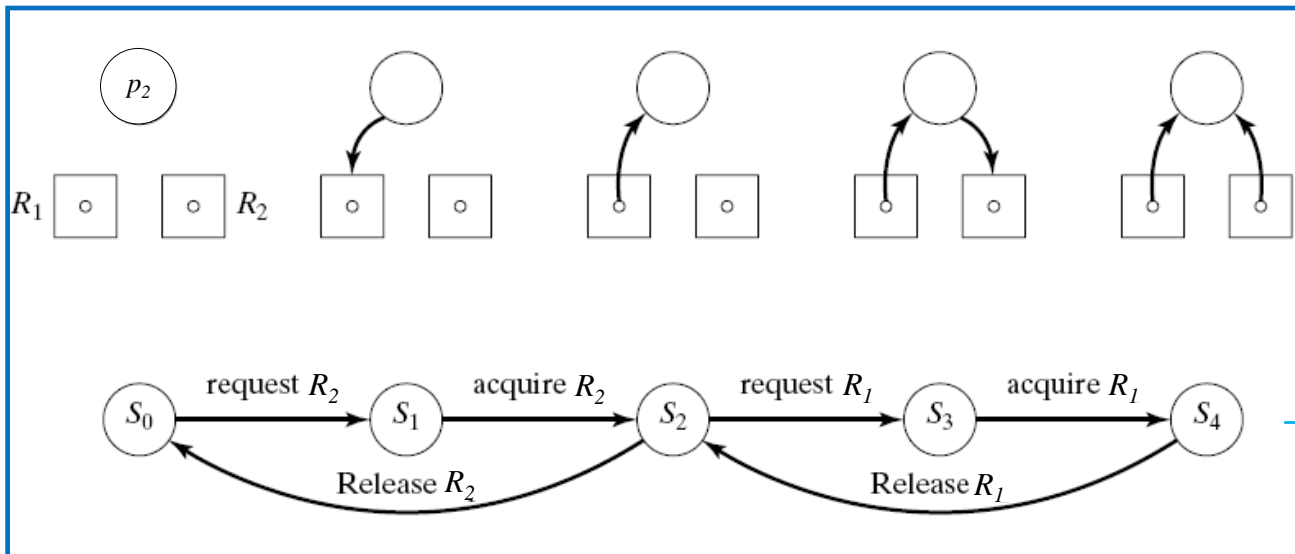
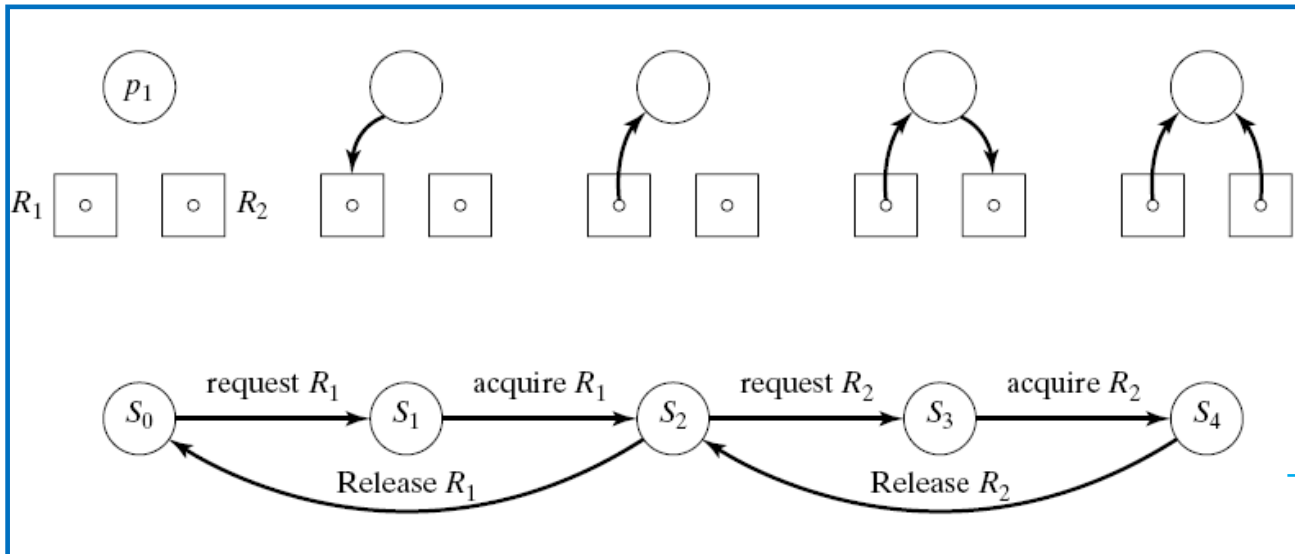
# Resource dependency: Reduction in progress...

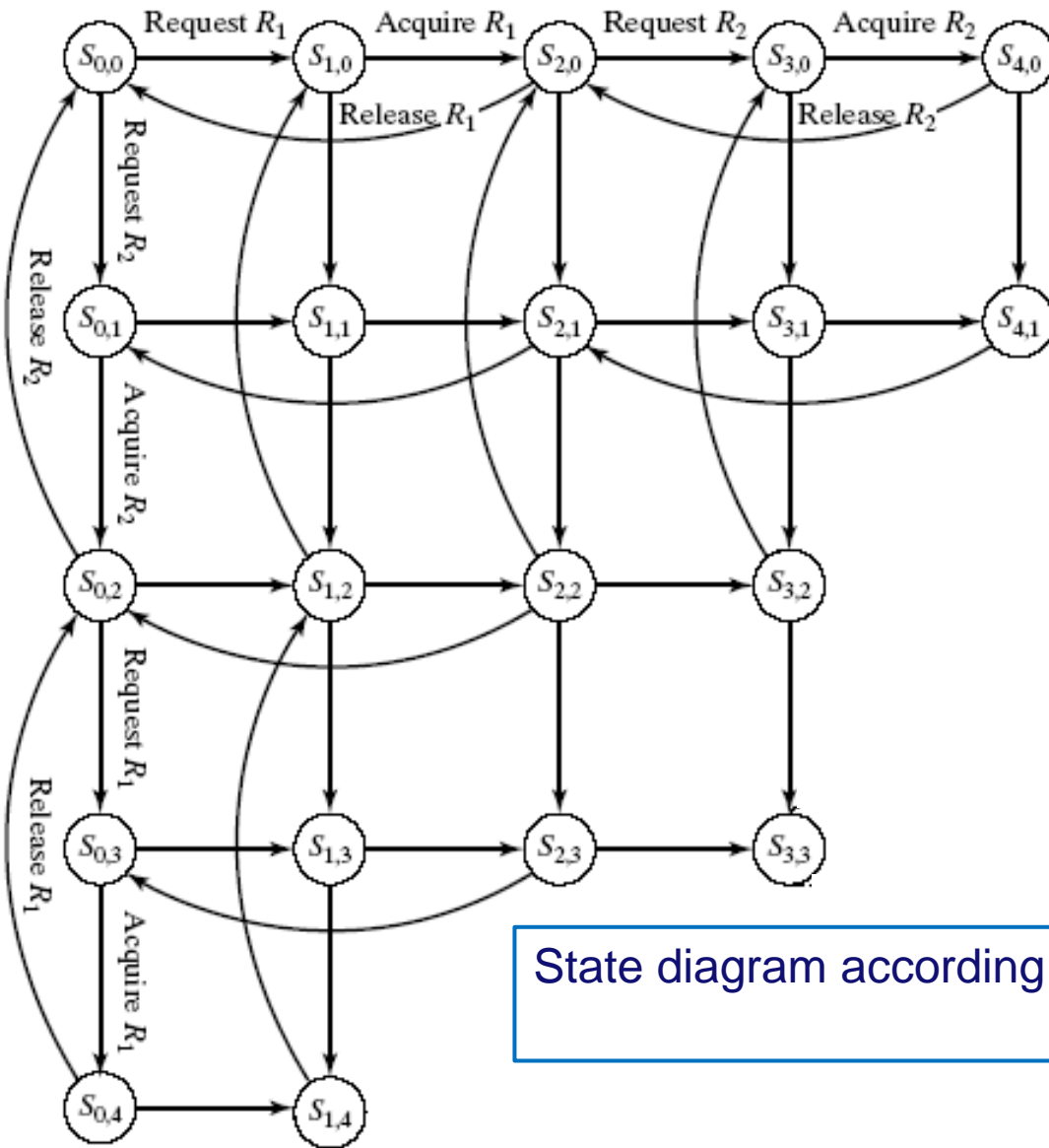


# Resource dependency: Sufficient condition for deadlock

- If we have a **greedy allocation algorithm**:
  - **Allocate resources as soon as they are available**
    - could be implemented just with a semaphore (counting the resources)
  - **Show the existence of a knot** in one of the dependency graphs that can be generated **by allocating the resources arbitrarily**
- **More generally**, examine the reachable states of the **Finite State Machine** corresponding to the request/acquisition sequences

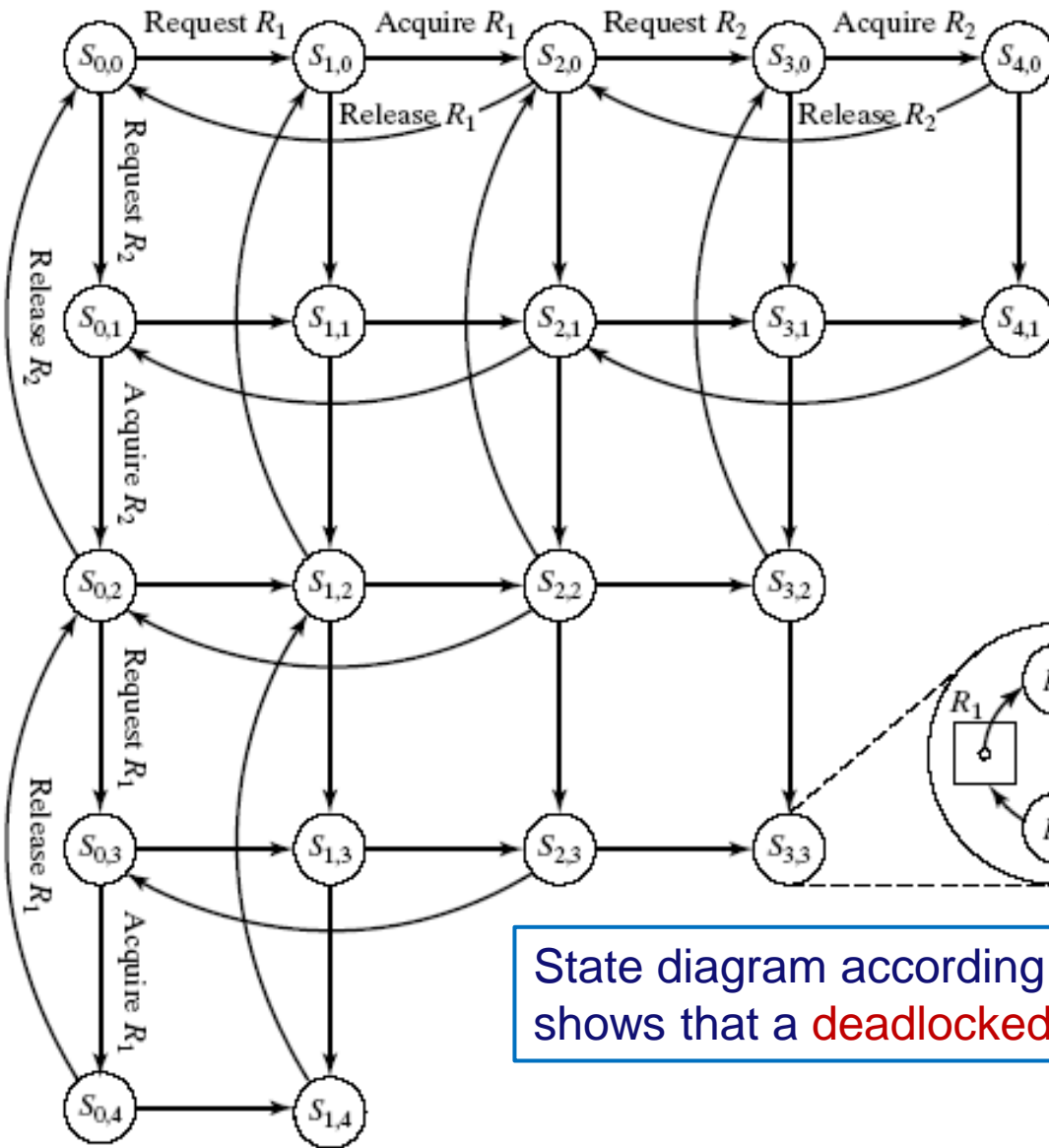
# Example: state diagrams and reachable states





Joint state space (FSM for it).

State diagram according to all possible traces



Joint state space (FSM for it).

