



Robótica Móvel e Inteligente

Mobile Robot Mapping

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Contents

- 1 Mapping
- 2 Occupance grid
- 3 SLAM
- 4 Bibliography

Navigation

Questions and topics

- Where am I?
 - localization
- **Where have I been?**
 - **mapping**
- Where should I going?
 - decision
- What's the best way to get there?
 - Path planning
- How do I get there?
 - Path following and obstacle avoidance (Motion)

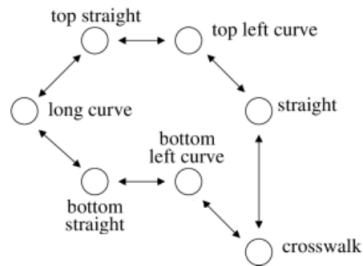
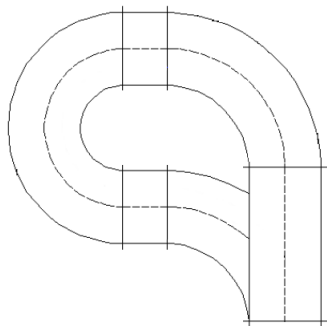
Mapping

Purpose

- **Mapping** is the process of building an internal estimate of the map of the environment
 - What does the world look like (for navigation purposes)?
- Approaches
 - Topological map
 - Features map
 - Metric map
 - Occupancy grid map

Mapping

Example of metric and topological maps



Occupancy Grid Method

- Map is composed of cells of equal dimension
- Every cell may be occupied or free
- Every cell keeps the probability of being occupied
 - Probability that each cell is occupied $P(H)$ and probability that each cell is unoccupied $P(\sim H)$

$$0 \leq P(H) \leq 1$$

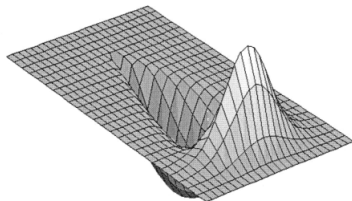
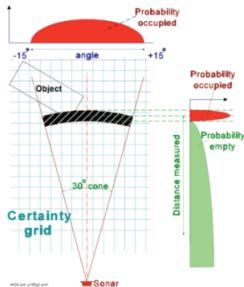
$$P(\sim H) = 1 - P(H)$$

- Other methods store 2 different functions: one for occupied probability and another for empty probability

Occupancy Grid

Mapping problem

- We want to determine $P(H|s)$
 - Probability cell H is occupied given a certain measure s
- Let's start by determining $P(s|H)$
 - Probability of getting measure s if H is occupied
 - This is the sensor model



Occupancy Grid

Mapping problem (2)

- One can determine $P(H|s)$ from $P(s|H)$
- From Bayes' Rule

$$P(H|s) = \frac{P(s|H) * P(H)}{P(s)} = \frac{P(s|H) * P(H)}{P(s|H) * P(H) + P(s|\sim H) * P(\sim H)}$$

- $P(s|H)$ and $P(s|\sim H)$ are known from the sensor model
- $P(H)$ and $P(\sim H)$ are unconditional probabilities or prior probabilities
 - If no information is available, one can assume $P(H) = P(\sim H) = 0.5$

Occupancy Grid

Mapping problem (3)

- Updating with the Bayes' rule

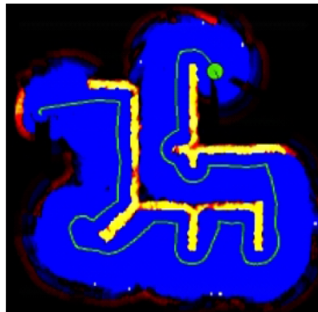
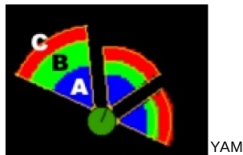
$$P(H|s_n) = \frac{P(s_n|H) * P(H|s_{n-1})}{P(s_n|H) * P(H|s_{n-1}) + P(s_n|\sim H) * P(\sim H|s_{n-1})}$$

- This is the recursive version of the update formula
- Each time a new observation is made that can be employed to update the occupancy grid

Occupancy Grid

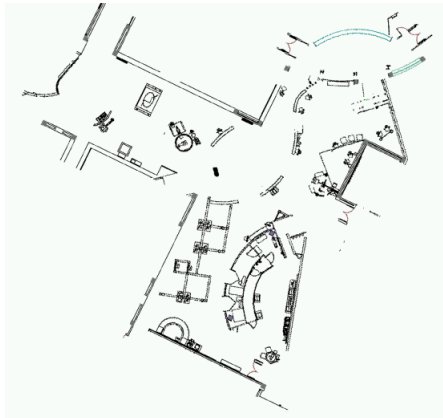
Mapping example – YAM algorithm

- Probabilities (?) may be positive or negative
 - Positive means probably occupied
 - Negative means probably empty
- Estimated position of the robot is assigned minimum probability
- Field of view of obstacle sensors is divided in 3 regions:
 - Cells in Region A are assigned a low probability
 - Cells in Region B decrease their probability
 - Cells in Region C increase their probability
 - Increase in region C is 4 times the value of decrease in region B



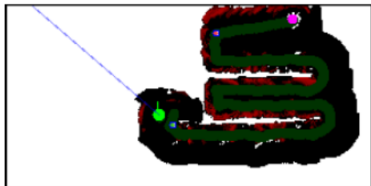
Occupancy Grid

Mapping example – laser range finder sensor



Occupancy Grid

Mapping example – XIP approach



SLAM

Simultaneous Localization and Mapping

- Mapping, as presented in the previous slides, assumes the pose of the robot is known
- Often this is not true and, while mapping, the robot must simultaneously estimate its pose
 - To estimate its pose it may use the already known map
- The general problem is denoted as the **Simultaneous Localization and Mapping (SLAM)** problem

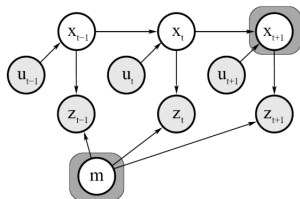
- **SLAM problem**
 - A robot is exploring an unknown, static environment
- **Inputs**
 - The robot's controls
 - Observations of nearby features
- **Estimate**
 - Map
 - Pose or path of the robot

SLAM

Online and full SLAM

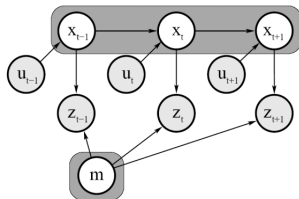
- **Online SLAM** – estimates map and current position given measures and controls

$$p(x_t, m | z_{1:t}, u_{1:t})$$



- **Full SLAM** – estimates map and the whole robot path given measures and controls

$$p(x_{1:t}, m | z_{1:t}, u_{1:t})$$



- SLAM techniques: Scan matching, EKF SLAM, Fast-SLAM, Graph-SLAM, SEIFs, **Gmapping**, **LAMA**
- <https://www.openslam.org/>

Bibliography

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