

Analysis

Imports

```
library(mgcv)
library(tidyverse)
library(caret)
library(mice)
library(quantreg)

df <- read.csv("data/train_simple.csv", stringsAsFactors = TRUE)

train_idx <- read.csv("data/X_train.csv")$X
train_df <- df[train_idx, ]
test_df <- df[-train_idx, ]
rm(df)
```

Define metric

```
mean_abs_err <- function(y_hat, y){
  sum(abs(y_hat - y)) / length(y_hat)
}
```

Fit linear regression without imputing income

As lots of the incomes are zero, it makes sense to impute these, as employment status is a categorical variable anyway which accounts for those with no income. First we can get a baseline without imputing income.

```
mod <- lm(total_claim_amount ~ vehicle_class + income +
          employment_status*monthly_premium_auto +
          location_code*monthly_premium_auto, data = train_df)
```

```
y_hat <- predict(mod, newdata = test_df)
```

```
summary(mod)
```

```
##
## Call:
## lm(formula = total_claim_amount ~ vehicle_class + income + employment_status *
##     monthly_premium_auto + location_code * monthly_premium_auto,
##     data = train_df)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -540.40  -64.47  -25.83   57.67 1357.87
##
## Coefficients:
##                                     Estimate Std. Error
```

```

## (Intercept) -5.416e+01 2.503e+01
## vehicle_classLuxury Car 3.358e+01 1.752e+01
## vehicle_classLuxury SUV 2.560e+01 1.691e+01
## vehicle_classSports Car -6.369e+00 8.201e+00
## vehicle_classSUV 6.486e-01 5.864e+00
## vehicle_classTwo-Door Car 2.863e+00 4.098e+00
## income -1.446e-04 9.090e-05
## employment_statusEmployed 7.421e+01 2.242e+01
## employment_statusMedical Leave -3.799e+01 3.220e+01
## employment_statusRetired 1.210e+02 3.358e+01
## employment_statusUnemployed -1.059e+01 2.330e+01
## monthly_premium_auto 1.832e+00 2.570e-01
## location_codeSuburban 9.448e+00 1.293e+01
## location_codeUrban 1.094e+01 1.616e+01
## employment_statusEmployed:monthly_premium_auto -7.923e-01 2.208e-01
## employment_statusMedical Leave:monthly_premium_auto 7.679e-01 3.312e-01
## employment_statusRetired:monthly_premium_auto -1.459e+00 3.407e-01
## employment_statusUnemployed:monthly_premium_auto 1.157e+00 2.319e-01
## monthly_premium_auto:location_codeSuburban 4.173e+00 1.338e-01
## monthly_premium_auto:location_codeUrban 2.322e+00 1.703e-01
## t value Pr(>|t|)
## (Intercept) -2.163 0.030556 *
## vehicle_classLuxury Car 1.917 0.055300 .
## vehicle_classLuxury SUV 1.513 0.130213
## vehicle_classSports Car -0.777 0.437429
## vehicle_classSUV 0.111 0.911930
## vehicle_classTwo-Door Car 0.699 0.484775
## income -1.591 0.111674
## employment_statusEmployed 3.309 0.000941 ***
## employment_statusMedical Leave -1.180 0.238188
## employment_statusRetired 3.603 0.000317 ***
## employment_statusUnemployed -0.455 0.649413
## monthly_premium_auto 7.127 1.14e-12 ***
## location_codeSuburban 0.731 0.465086
## location_codeUrban 0.677 0.498324
## employment_statusEmployed:monthly_premium_auto -3.588 0.000336 ***
## employment_statusMedical Leave:monthly_premium_auto 2.319 0.020454 *
## employment_statusRetired:monthly_premium_auto -4.284 1.87e-05 ***
## employment_statusUnemployed:monthly_premium_auto 4.987 6.29e-07 ***
## monthly_premium_auto:location_codeSuburban 31.179 < 2e-16 ***
## monthly_premium_auto:location_codeUrban 13.632 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 123.4 on 6206 degrees of freedom
## Multiple R-squared: 0.8159, Adjusted R-squared: 0.8153
## F-statistic: 1447 on 19 and 6206 DF, p-value: < 2.2e-16
mae <- mean_abs_err(y_hat, test_df$total_claim_amount)
print(paste("MAE of:", round(mae, 2)))

## [1] "MAE of: 89.55"

```

Try imputing income variable

```
df_big <- read.csv("data/train.csv", stringsAsFactors = TRUE)
df_big <- df_big %>% select(-Country, -Customer)
df_big$Income[df_big$Income == 0] <- NA
```

```
imputations <- complete(mice(df_big, method = "pmm", seed=1))
```

```
## Warning: Number of logged events: 26
```

```
train_df$income <- imputations$Income[train_idx]
test_df$income <- imputations$Income[-train_idx]
```

Linear regression with “missing” income values imputed

```
mod <- lm(total_claim_amount ~ vehicle_class + income +
          employment_status*monthly_premium_auto +
          location_code*monthly_premium_auto, data = train_df)
```

```
y_hat <- predict(mod, newdata = test_df)
```

```
summary(mod)
```

```
##
```

```
## Call:
```

```
## lm(formula = total_claim_amount ~ vehicle_class + income + employment_status *
##     monthly_premium_auto + location_code * monthly_premium_auto,
##     data = train_df)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max
## -541.14  -64.46  -25.83   57.05 1357.81
```

```
##
```

```
## Coefficients:
```

```
##                                     Estimate Std. Error
## (Intercept)                       -5.465e+01  2.503e+01
## vehicle_classLuxury Car              3.350e+01  1.752e+01
## vehicle_classLuxury SUV              2.560e+01  1.691e+01
## vehicle_classSports Car             -6.376e+00  8.202e+00
## vehicle_classSUV                     6.430e-01  5.864e+00
## vehicle_classTwo-Door Car            2.852e+00  4.098e+00
## income                             -1.255e-04  8.981e-05
## employment_statusEmployed             7.356e+01  2.242e+01
## employment_statusMedical Leave       -3.793e+01  3.221e+01
## employment_statusRetired              1.210e+02  3.358e+01
## employment_statusUnemployed          -7.692e+00  2.322e+01
## monthly_premium_auto                  1.832e+00  2.570e-01
## location_codeSuburban                  9.536e+00  1.293e+01
## location_codeUrban                     1.093e+01  1.616e+01
## employment_statusEmployed:monthly_premium_auto -7.923e-01  2.209e-01
## employment_statusMedical Leave:monthly_premium_auto 7.672e-01  3.312e-01
## employment_statusRetired:monthly_premium_auto -1.459e+00  3.407e-01
## employment_statusUnemployed:monthly_premium_auto  1.157e+00  2.319e-01
## monthly_premium_auto:location_codeSuburban  4.174e+00  1.339e-01
```

```
## monthly_premium_auto:location_codeUrban          2.322e+00  1.703e-01
## t value Pr(>|t|)
## (Intercept) -2.183 0.029065 *
## vehicle_classLuxury Car 1.912 0.055880 .
## vehicle_classLuxury SUV 1.513 0.130207
## vehicle_classSports Car -0.777 0.436984
## vehicle_classSUV 0.110 0.912690
## vehicle_classTwo-Door Car 0.696 0.486475
## income -1.398 0.162250
## employment_statusEmployed 3.281 0.001041 **
## employment_statusMedical Leave -1.178 0.238935
## employment_statusRetired 3.602 0.000318 ***
## employment_statusUnemployed -0.331 0.740481
## monthly_premium_auto 7.126 1.15e-12 ***
## location_codeSuburban 0.737 0.460942
## location_codeUrban 0.676 0.498785
## employment_statusEmployed:monthly_premium_auto -3.587 0.000337 ***
## employment_statusMedical Leave:monthly_premium_auto 2.316 0.020570 *
## employment_statusRetired:monthly_premium_auto -4.283 1.87e-05 ***
## employment_statusUnemployed:monthly_premium_auto 4.989 6.25e-07 ***
## monthly_premium_auto:location_codeSuburban 31.182 < 2e-16 ***
## monthly_premium_auto:location_codeUrban 13.633 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 123.4 on 6206 degrees of freedom
## Multiple R-squared:  0.8159, Adjusted R-squared:  0.8153
## F-statistic: 1447 on 19 and 6206 DF, p-value: < 2.2e-16

mae <- mean_abs_err(y_hat, test_df$total_claim_amount)
print(paste("MAE of:", round(mae, 2)))

## [1] "MAE of: 89.55"
```

Doesn't seem to make much difference.

GAM

Does using a GAM improve performance? Again using the data with imputed income (even though it probably doesn't make much difference).

```
mod <- gam(total_claim_amount ~ employment_status + location_code +
           vehicle_class + s(income) +
           s(monthly_premium_auto, by = employment_status) +
           s(monthly_premium_auto, by = location_code), data = train_df)

y_hat <- predict(mod, newdata = test_df)
summary(mod)

##
## Family: gaussian
## Link function: identity
##
## Formula:
## total_claim_amount ~ employment_status + location_code + vehicle_class +
##       s(income) + s(monthly_premium_auto, by = employment_status) +
```

```

##      s(monthly_premium_auto, by = location_code)
##
## Parametric coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      1.152e+02  9.195e+00  12.529 < 2e-16 ***
## employment_statusEmployed      2.937e-01  9.318e+00   0.032  0.975
## employment_statusMedical Leave -1.114e+03  1.946e+02  -5.724 1.09e-08 ***
## employment_statusRetired      -1.533e+01  1.170e+01  -1.310  0.190
## employment_statusUnemployed      1.014e+02  8.091e+00  12.532 < 2e-16 ***
## location_codeSuburban      3.953e+02  4.391e+00  90.021 < 2e-16 ***
## location_codeUrban      2.258e+02  5.106e+00  44.219 < 2e-16 ***
## vehicle_classLuxury Car      -5.028e-02  2.113e+01  -0.002  0.998
## vehicle_classLuxury SUV      -2.738e+01  2.125e+01  -1.288  0.198
## vehicle_classSports Car      -8.804e+00  8.591e+00  -1.025  0.305
## vehicle_classSUV      -2.575e-02  6.383e+00  -0.004  0.997
## vehicle_classTwo-Door Car      2.757e+00  4.033e+00   0.684  0.494
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
##              edf Ref.df      F
## s(income)              7.4640 8.4172  3.205
## s(monthly_premium_auto):employment_statusDisabled      5.8737 6.6539  5.855
## s(monthly_premium_auto):employment_statusEmployed      0.8751 0.8752 30.943
## s(monthly_premium_auto):employment_statusMedical Leave  8.8384 8.8738 13.373
## s(monthly_premium_auto):employment_statusRetired      0.8750 0.8751 30.902
## s(monthly_premium_auto):employment_statusUnemployed      8.7841 8.8698  9.449
## s(monthly_premium_auto):location_codeRural      8.6420 8.8407  5.320
## s(monthly_premium_auto):location_codeSuburban      3.9079 4.7932  6.517
## s(monthly_premium_auto):location_codeUrban      0.8754 0.8757 30.681
##              p-value
## s(income)              0.00127 **
## s(monthly_premium_auto):employment_statusDisabled      2.00e-06 ***
## s(monthly_premium_auto):employment_statusEmployed      8.17e-07 ***
## s(monthly_premium_auto):employment_statusMedical Leave < 2e-16 ***
## s(monthly_premium_auto):employment_statusRetired      8.38e-07 ***
## s(monthly_premium_auto):employment_statusUnemployed < 2e-16 ***
## s(monthly_premium_auto):location_codeRural      1.20e-07 ***
## s(monthly_premium_auto):location_codeSuburban      1.18e-05 ***
## s(monthly_premium_auto):location_codeUrban      9.41e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Rank: 92/93
## R-sq.(adj) =  0.822   Deviance explained = 82.3%
## GCV = 14856   Scale est. = 14717      n = 6226
mae <- mean_abs_err(y_hat, test_df$total_claim_amount)
print(paste("MAE of:", round(mae, 2)))

## [1] "MAE of: 91.34"

```

Default GAM does worse during cross-validation! Not too surprising when you see the plots though as they look very linear. Although I could also be doing something wrong...

Quantile regression

Since we are aiming to minimize the mean absolute error. Perhaps fitting a linear model using median regression will likely perform better. This is optimal for minimizing mean absolute error, whereas the mean is optimal for the squared error loss function.

```
mod <- rq(total_claim_amount ~ vehicle_class + income +
  employment_status*monthly_premium_auto +
  location_code*monthly_premium_auto, data = train_df)

y_hat <- predict(mod, newdata = test_df)

summary.rq(mod, se = "boot") # bootstrap se estimates
```

```
##
## Call: rq(formula = total_claim_amount ~ vehicle_class + income + employment_status *
##   monthly_premium_auto + location_code * monthly_premium_auto,
##   data = train_df)
##
## tau: [1] 0.5
##
## Coefficients:
##                                     Value      Std. Error
## (Intercept)                        8.84868      35.06114
## vehicle_classLuxury Car             0.00000       8.11257
## vehicle_classLuxury SUV             0.00000       5.18898
## vehicle_classSports Car             0.00000       1.22768
## vehicle_classSUV                    0.00000       0.00000
## vehicle_classTwo-Door Car           0.15345       2.89356
## income                             0.00000       0.00000
## employment_statusEmployed           6.54929      30.71381
## employment_statusMedical Leave      6.54929      44.37370
## employment_statusRetired            6.54929      30.71381
## employment_statusUnemployed        -130.86191     35.55818
## monthly_premium_auto                1.08339       0.52058
## location_codeSuburban               -15.39797     15.59786
## location_codeUrban                  -2.98427     21.69061
## employment_statusEmployed:monthly_premium_auto -0.10396       0.48050
## employment_statusMedical Leave:monthly_premium_auto -0.10396       0.69153
## employment_statusRetired:monthly_premium_auto -0.10396       0.48050
## employment_statusUnemployed:monthly_premium_auto  2.96634       0.49763
## monthly_premium_auto:location_codeSuburban      3.82057       0.18314
## monthly_premium_auto:location_codeUrban          2.52061       0.26221
##                                     t value      Pr(>|t|)
## (Intercept)                        0.25238       0.80076
## vehicle_classLuxury Car             0.00000       1.00000
## vehicle_classLuxury SUV             0.00000       1.00000
## vehicle_classSports Car             0.00000       1.00000
## vehicle_classSUV                    1.40577       0.15984
## vehicle_classTwo-Door Car           0.05303       0.95771
## income                             -3.20966       0.00134
## employment_statusEmployed           0.21324       0.83115
## employment_statusMedical Leave      0.14759       0.88267
## employment_statusRetired            0.21324       0.83115
## employment_statusUnemployed        -3.68022       0.00024
```

```
## monthly_premium_auto                2.08112    0.03746
## location_codeSuburban                -0.98718    0.32359
## location_codeUrban                   -0.13758    0.89057
## employment_statusEmployed:monthly_premium_auto -0.21635    0.82872
## employment_statusMedical Leave:monthly_premium_auto -0.15033    0.88051
## employment_statusRetired:monthly_premium_auto -0.21635    0.82872
## employment_statusUnemployed:monthly_premium_auto  5.96094    0.00000
## monthly_premium_auto:location_codeSuburban    20.86150    0.00000
## monthly_premium_auto:location_codeUrban      9.61313    0.00000
```

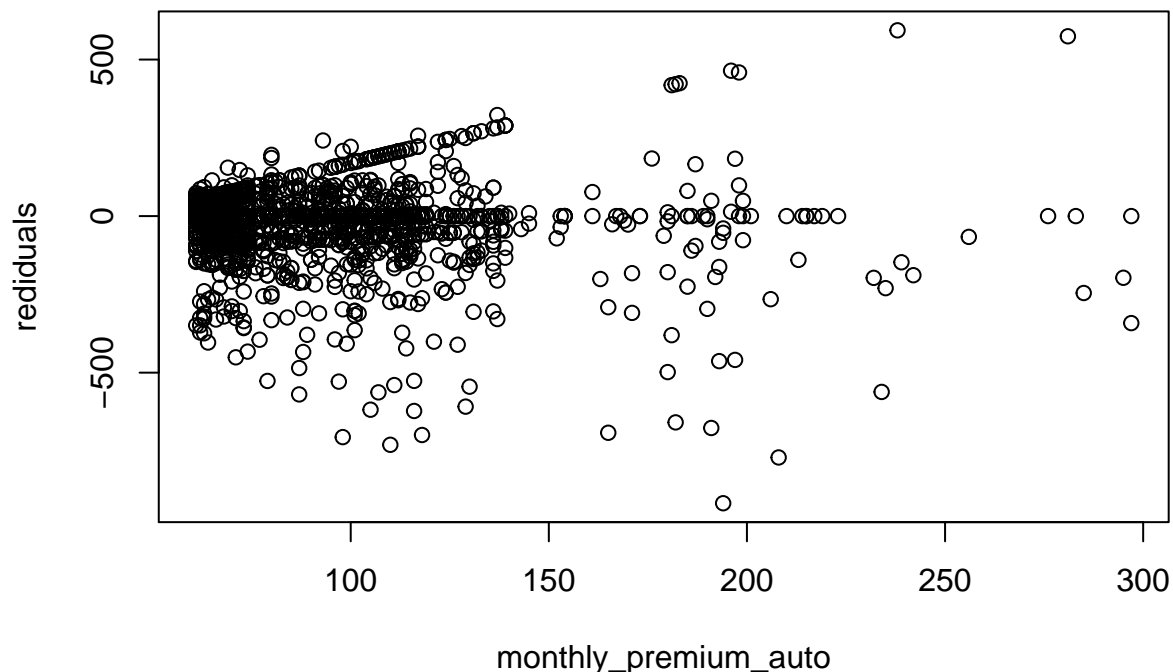
```
mae <- mean_abs_err(y_hat, test_df$total_claim_amount)
print(paste("MAE of:", round(mae, 2)))
```

```
## [1] "MAE of: 79.4"
```

This performs a lot better. We should be able to simplify things further based on the zero coefficients above.

Note that here we use the pairwise bootstrap estimate of the standard errors. This is more robust to heteroscedasticity than the standard method (e.g. see this paper). We can see that we have heteroscedasticity here:

```
plot(test_df$monthly_premium_auto, (y_hat-test_df$total_claim_amount),
      xlab = "monthly_premium_auto", ylab = "rediduals")
```



We will slim things down and simplify the model to make a final model:

Final Model

Simplify using the following:

- Simplify `employment_status` into a boolean `is_employed`, as being unemployed was the only significant factor level.
- Drop income and vehicle class

```

train_df_simple <- train_df %>%
  mutate(is_unemployed = employment_status == "Unemployed") %>%
  select(-employment_status, -income, -vehicle_class)

test_df_simple <- test_df %>%
  mutate(is_unemployed = employment_status == "Unemployed") %>%
  select(-employment_status, -income, -vehicle_class)

head(train_df_simple)

```

```

##      location_code monthly_premium_auto total_claim_amount is_unemployed
## 1352          Urban                67          172.5185         FALSE
## 7760        Suburban               129          928.8000          TRUE
## 4393        Suburban               112         1169.4098         FALSE
## 2182        Suburban                66          344.2016         FALSE
## 2219        Suburban                65          468.0000         FALSE
## 1966          Rural                65          117.4504         FALSE

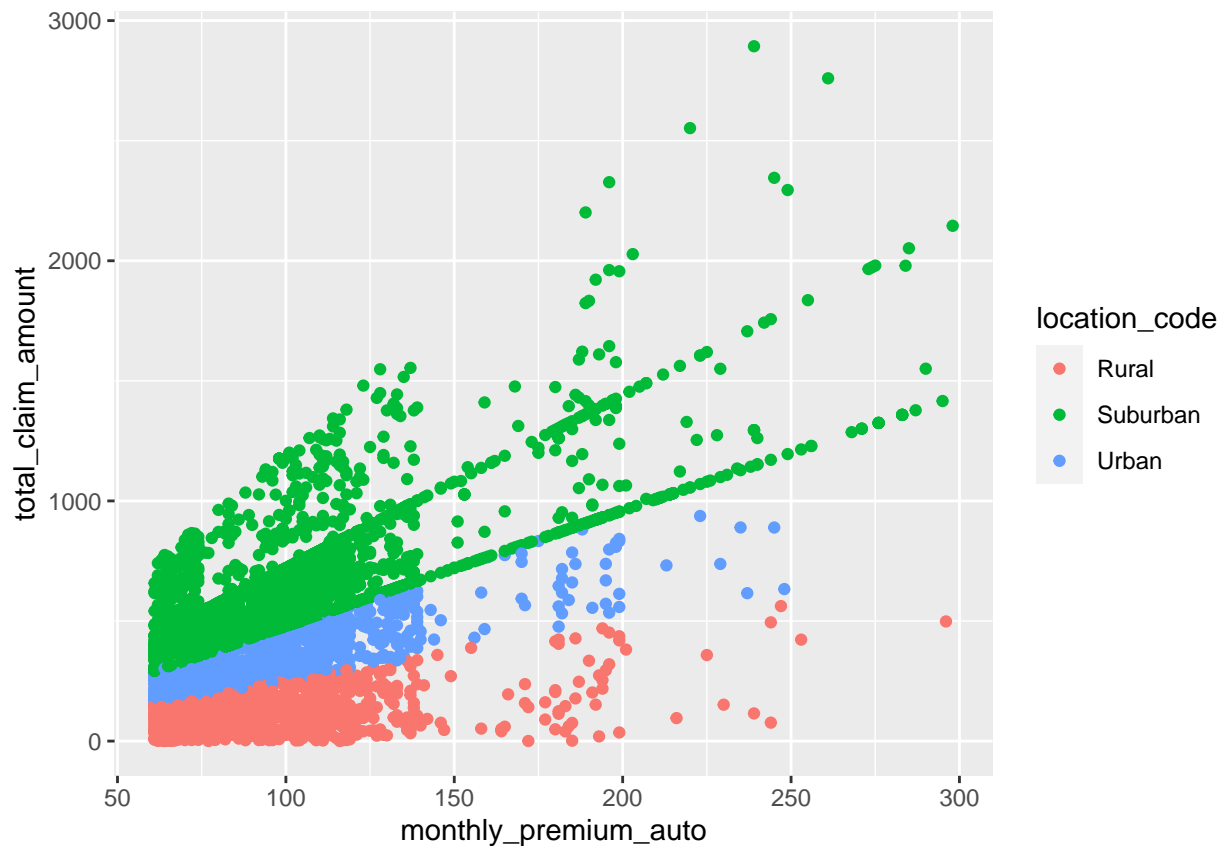
```

Note that these are primary variables identified in the EDA. We observed that the factor variables `is_unemployed` and `location_code` show a strong interaction with the `monthly_premium_auto` variable:

```

train_df %>%
  ggplot(aes(x = monthly_premium_auto, y = total_claim_amount,
             col = location_code)) +
  geom_point()

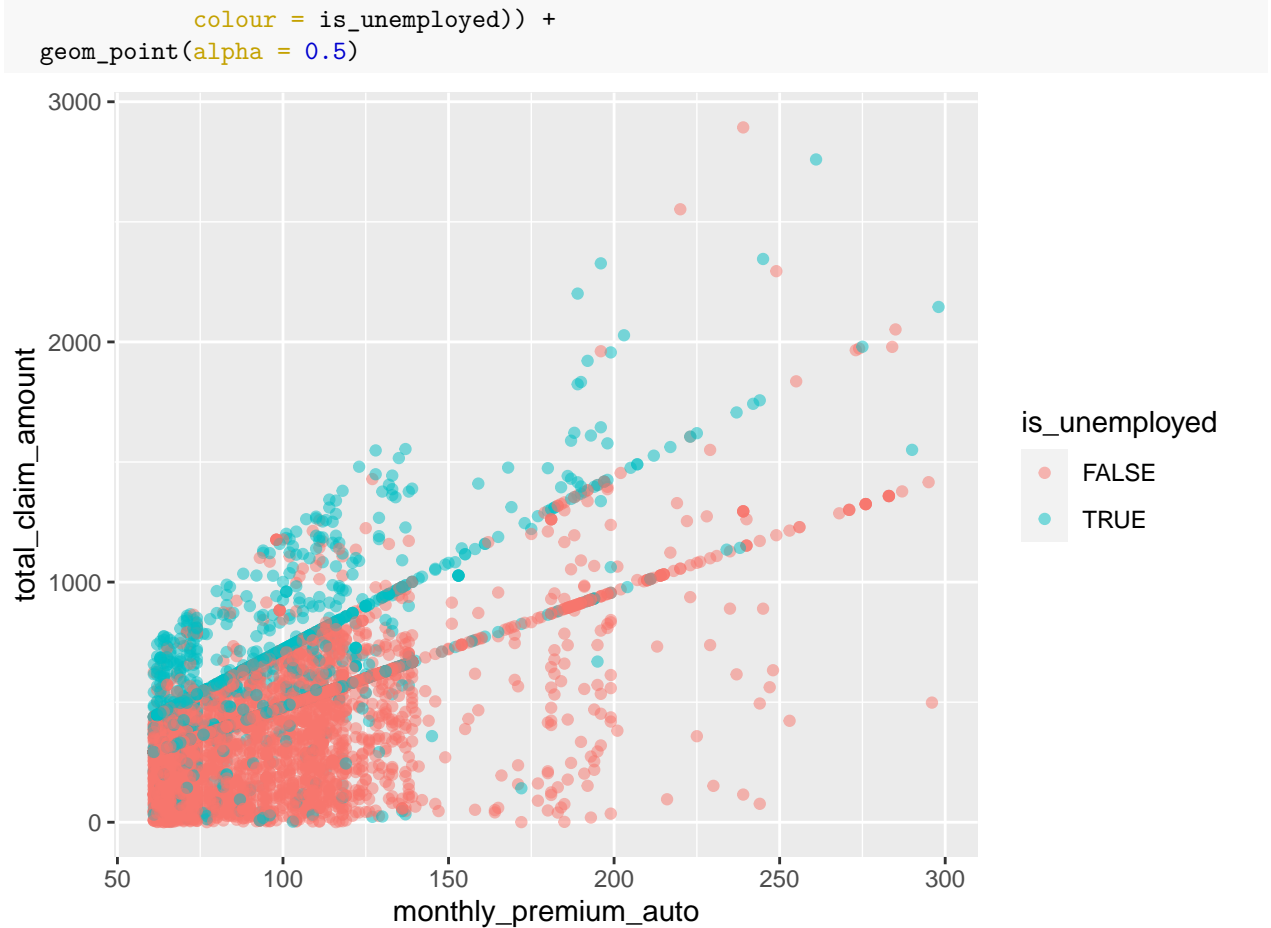
```



```

train_df_simple %>%
  ggplot(aes(x = monthly_premium_auto, y = total_claim_amount,

```

The final, very simple model, using just three features is below:

```
mod <- rq(total_claim_amount ~
  is_unemployed*monthly_premium_auto +
  location_code*monthly_premium_auto, data = train_df_simple)

y_hat <- predict(mod, test_df_simple)

summary.rq(mod, se = "boot")
```

```
##
## Call: rq(formula = total_claim_amount ~ is_unemployed * monthly_premium_auto +
##      location_code * monthly_premium_auto, data = train_df_simple)
##
## tau: [1] 0.5
##
## Coefficients:
##              Value      Std. Error t value
## (Intercept)    15.58546    14.63297   1.06509
## is_unemployedTRUE -137.59246    19.33962  -7.11454
## monthly_premium_auto    0.97845     0.17734   5.51743
## location_codeSuburban  -15.58546    14.63297  -1.06509
## location_codeUrban    -2.97803    20.97822  -0.14196
## is_unemployedTRUE:monthly_premium_auto    3.07118     0.11322  27.12592
```

```
## monthly_premium_auto:location_codeSuburban    3.82155    0.17734    21.54963
## monthly_premium_auto:location_codeUrban       2.52053    0.25301     9.96209
##                                               Pr(>|t|)
## (Intercept)                                0.28688
## is_unemployedTRUE                          0.00000
## monthly_premium_auto                      0.00000
## location_codeSuburban                     0.28688
## location_codeUrban                        0.88712
## is_unemployedTRUE:monthly_premium_auto      0.00000
## monthly_premium_auto:location_codeSuburban  0.00000
## monthly_premium_auto:location_codeUrban     0.00000
```

```
mae <- mean_abs_err(y_hat, test_df$total_claim_amount)
print(paste("MAE of:", round(mae, 2)))
```

```
## [1] "MAE of: 79.36"
```

Now we have the best model. I will retrain it on the whole data set. Then this can be used to predict on the test set when it is released:

```
df <- rbind(train_df_simple, test_df_simple)

mod <- rq(total_claim_amount ~
  is_unemployed*monthly_premium_auto +
  location_code*monthly_premium_auto +
  is_unemployed*location_code, data = df)
```

```
## Warning in rq.fit.br(x, y, tau = tau, ...): Solution may be nonunique
```

```
# Put test data here...
```