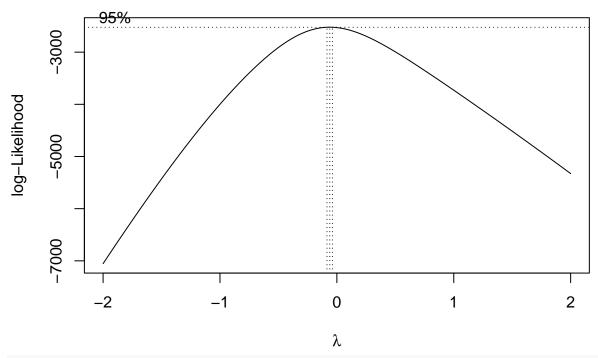
```
library(car)
## Loading required package: carData
library(reshape2)
library(ggplot2)
library(MASS)
library(interactions)
source("clean_data.R")
df <- remove_cols(df, c("Color", "Model"))</pre>
# Remove columns with only one observation and affected rows
res <- convert_categorical(df, categorical)</pre>
design <- as.data.frame(res$dummy)</pre>
singles <- c()
bad_idx <- c()</pre>
for (col in colnames(design)) {
 if (sum(design[, col] != 0) <= 1) {</pre>
    singles <- c(singles, col)</pre>
    bad_idx <- c(bad_idx, which(design[, col] != 0))</pre>
  }
}
singles
## [1] "MakeFiat"
                                                           "Fuel.TypePetrol + CNG"
                                  "MakeLexus"
## [4] "LocationDak. Kannada" "LocationFaizabad"
                                                           "LocationGorakhpur"
## [7] "LocationPurnea"
                                                           "LocationRudrapur"
                                 "LocationRohtak"
## [10] "LocationSamastipur" "LocationValsad"
bad_idx
## [1] 662 1009 1169 1077 779 569 728 245 510 264 162
df <- df[-bad_idx, ]</pre>
```

### Box Cox

```
bc <- boxcox(Price ~., data = df)</pre>
```



bc\$x[which.max(bc\$y)]

## [1] -0.06060606

For the sake of interpretability, we will use a log transformation, since  $\lambda \approx 0$ .

# Iteratively Remove Multicollinear Regressors

```
x \leftarrow df
model \leftarrow lm(log(Price) \sim ., data = x)
removed <- c()
finished <- F
while(!finished) {
  temp <- car::vif(model)[, "GVIF^(1/(2*Df))"]</pre>
  worst <- names(which.max(temp))</pre>
  if (length(temp) > 0 && temp[worst] > sqrt(5)) {
    x <- remove_cols(x, c(worst))</pre>
    model <- lm(log(Price) ~., data = x)</pre>
    removed <- c(removed, worst)</pre>
  } else {
    finished <- T
}
removed
                                                       "Max.Power.Value"
## [1] "Max.Torque.Value"
                               "Max.Power.RPM"
## [4] "Engine"
                               "Fuel.Tank.Capacity" "Height"
which(abs(rstudent(model)) > 4)
```

```
## 39 268 345 1071 1171
```

After inspecting these data points, we do not find a good reason to remove them (i.e., they are not clerical errors).

#### Add Interactions

We consider only numerical interactions due to data sparsity; including categorical values produces NA's for most interactions. We do not expect kilometers driven to interact with torque or width, so those interactions are not considered.

names (model \$coefficients) [names (model \$coefficients) %in% numerical] ## [1] "Year" "Kilometer" "Max.Torque.RPM" "Length" ## [5] "Width" model <- lm( log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM + Year:Length + Year:Width + Max.Torque.RPM:Length + Max.Torque.RPM:Width + Length: Width, data = x) anova(model) ## Analysis of Variance Table ## ## Response: log(Price) ## Df Sum Sq Mean Sq F value Pr(>F) ## Make 25 354.44 14.178 482.1594 < 2.2e-16 \*\*\* ## Year 1 178.52 178.525 6071.3552 < 2.2e-16 \*\*\* ## Kilometer 1 0.98 0.982 33.3800 9.430e-09 \*\*\* ## Fuel.Type 2 19.23 9.615 326.9979 < 2.2e-16 \*\*\* ## Transmission 1 20.31 20.313 690.7982 < 2.2e-16 \*\*\* 63 16.76 ## Location 0.266 9.0458 < 2.2e-16 \*\*\* ## Owner 3 0.46 0.153 5.2143 0.001397 \*\* ## Seller.Type 2 0.33 0.165 5.6238 0.003697 \*\* ## Max.Torque.RPM 1 1.67 1.669 56.7628 9.050e-14 \*\*\* ## Drivetrain 2 5.81 98.7875 < 2.2e-16 \*\*\* 2.905 1 51.72 51.724 1759.0668 < 2.2e-16 \*\*\* ## Length ## Width 5.06 5.063 172.1998 < 2.2e-16 \*\*\* ## Seating.Capacity 0.02 0.6507 0.419991 1 0.019 ## Year:Kilometer 1 1.10 1.100 37.4187 1.251e-09 \*\*\* ## Year:Max.Torque.RPM 0.99 0.993 33.7868 7.690e-09 \*\*\* 1 ## Year:Length 1 2.04 2.038 69.2926 < 2.2e-16 \*\*\* ## Year:Width 0.08 2.5959 0.107377 1 0.076 ## Max.Torque.RPM:Length 1 0.28 0.276 9.3872 0.002229 \*\* ## Max.Torque.RPM:Width 1 0.01 0.012 0.3960 0.529287 ## Length:Width 1 0.01 0.014 0.4748 0.490893 ## Residuals 1329 39.08 0.029 ## ---

Interactions with width don't seem to be significant; remove them.

## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

```
model <- lm(
 log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM
                  + Year:Length + Max.Torque.RPM:Length,
 data = x
)
anova(model)
## Analysis of Variance Table
## Response: log(Price)
##
                          Df Sum Sq Mean Sq
                                              F value
                                                         Pr(>F)
## Make
                          25 354.44 14.178 481.9160 < 2.2e-16 ***
## Year
                           1 178.52 178.525 6068.2914 < 2.2e-16 ***
## Kilometer
                           1 0.98
                                      0.982
                                              33.3632 9.505e-09 ***
## Fuel.Type
                           2 19.23
                                      9.615 326.8329 < 2.2e-16 ***
## Transmission
                           1 20.31 20.313 690.4496 < 2.2e-16 ***
## Location
                          63 16.76
                                     0.266
                                               9.0412 < 2.2e-16 ***
## Owner
                           3
                              0.46
                                      0.153
                                               5.2117 0.001402 **
## Seller.Type
                           2 0.33
                                               5.6210 0.003708 **
                                      0.165
                           1 1.67
                                              56.7341 9.165e-14 ***
## Max.Torque.RPM
                                      1.669
                           2 5.81
                                              98.7377 < 2.2e-16 ***
## Drivetrain
                                      2.905
## Length
                           1 51.72 51.724 1758.1791 < 2.2e-16 ***
## Width
                           1 5.06
                                      5.063 172.1129 < 2.2e-16 ***
## Seating.Capacity
                           1 0.02
                                      0.019
                                              0.6504 0.420108
## Year:Kilometer
                           1 1.10
                                              37.3998 1.262e-09 ***
                                      1.100
## Year:Max.Torque.RPM
                           1 0.99
                                      0.993
                                              33.7697 7.752e-09 ***
## Year:Length
                           1
                               2.04
                                      2.038
                                              69.2576 < 2.2e-16 ***
## Max.Torque.RPM:Length
                           1
                               0.27
                                      0.270
                                               9.1768 0.002498 **
## Residuals
                        1332 39.19
                                      0.029
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Seems reasonable now. We will double check our assumptions
vif(model, type = "predictor")
## GVIFs computed for predictors
##
                         GVIF Df GVIF^(1/(2*Df))
## Make
                   119.109068 25
                                        1.100320
## Year
                    75.935730 8
                                        1.310774
## Kilometer
                   330.635985 3
                                        2.629612
## Fuel.Type
                     5.334325 2
                                        1.519742
## Transmission
                     1.851632 1
                                        1.360747
## Location
                    16.448508 63
                                        1.022473
## Owner
                    1.673586 3
                                        1.089619
## Seller.Type
                     1.341372 2
                                        1.076186
## Max.Torque.RPM
                  207.518246 6
                                        1.559869
## Drivetrain
                     4.003689 2
                                        1.414539
## Length
                   207.518246 6
                                        1.559869
## Width
                                        2.150498
                     4.624641 1
## Seating.Capacity 2.882982 1
                                        1.697934
##
                                      Interacts With
```

## Make

```
## Kilometer
                                                   Year
## Fuel.Type
## Transmission
## Location
## Owner
## Seller.Type
                                          Year, Length
## Max.Torque.RPM
## Drivetrain
## Length
                                  Year, Max.Torque.RPM
## Width
## Seating.Capacity
## Make
                    Year, Kilometer, Fuel. Type, Transmission, Location, Owner, Seller. Type, Max. Torque.
## Year
                                                         Make, Fuel. Type, Transmission, Location, Owner,
## Kilometer
                                Make, Fuel. Type, Transmission, Location, Owner, Seller. Type, Max. Torque.
## Fuel.Type
                         Make, Year, Kilometer, Transmission, Location, Owner, Seller. Type, Max. Torque.
                             Make, Year, Kilometer, Fuel. Type, Location, Owner, Seller. Type, Max. Torque.
## Transmission
                        Make, Year, Kilometer, Fuel. Type, Transmission, Owner, Seller. Type, Max. Torque.
## Location
## Owner
                     Make, Year, Kilometer, Fuel. Type, Transmission, Location, Seller. Type, Max. Torque.
## Seller.Type
                           Make, Year, Kilometer, Fuel. Type, Transmission, Location, Owner, Max. Torque.
## Max.Torque.RPM
                                             Make, Kilometer, Fuel. Type, Transmission, Location, Owner,
## Drivetrain
                          Make, Year, Kilometer, Fuel. Type, Transmission, Location, Owner, Seller. Type,
                                             Make, Kilometer, Fuel. Type, Transmission, Location, Owner,
## Length
## Width
                     Make, Year, Kilometer, Fuel. Type, Transmission, Location, Owner, Seller. Type, Max.
## Seating.Capacity
                                 Make, Year, Kilometer, Fuel. Type, Transmission, Location, Owner, Seller
```

We get that  $GVIF^{(1/(2*Df))} > 2.236068 \approx \sqrt{5}$ , for "Kilometer," but this is known to be important is does not exceed the threshold by a lot, so we keep it.

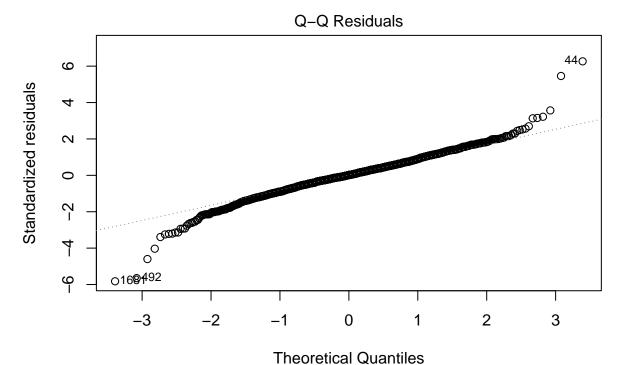
Kilometer, Max. Torque. RPM, Length

#### plot(model)

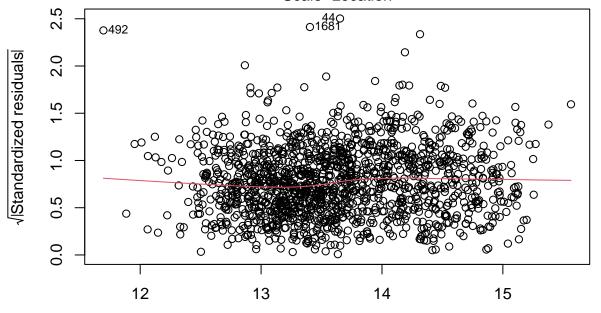
## Year

# Residuals vs Fitted 0 440 0 2 o. Residuals 0.0 S ġ. 0 0492 01681 12 13 14 15

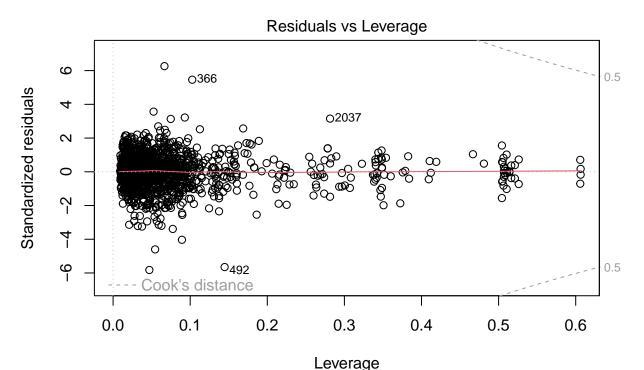
Fitted values
Im(log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM + Year:Length + Ma ...



Im(log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM + Year:Length + Ma ... Scale-Location



Fitted values Im(log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM + Year:Length + Ma ...



Im(log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM + Year:Length + Ma ...

# Backwards Stepwise Search

We do a backwards search since our model already conforms to the linear assumptions and is performing well. We simply wish to reduce the model size now.

```
reduced_model <- step(model, direction = "backward", data = x, trace = 0, k = log(nrow(x)))
old <- names(model$coefficients)
new <- names(reduced_model$coefficients)

old[!(old %in% new)]

## [1] "LocationAhmedabad" "LocationAllahabad" "LocationAmbala Cantt"
## [4] "LocationAmritsar" "LocationAurangabad" "LocationBangalore"</pre>
```

```
"LocationBhubaneswar"
                                                           "LocationBulandshahar"
##
    [7]
        "LocationBhopal"
##
   [10]
        "LocationChandigarh"
                                  "LocationChennai"
                                                           "LocationCoimbatore"
        "LocationDehradun"
                                  "LocationDelhi"
                                                           "LocationDharwad"
   [13]
        "LocationErnakulam"
                                  "LocationFaridabad"
                                                           "LocationGhaziabad"
   [16]
                                                           "LocationGuwahati"
        "LocationGoa"
                                  "LocationGurgaon"
   [19]
   [22]
        "LocationHaldwani"
                                  "LocationHyderabad"
                                                           "LocationIndore"
##
   [25]
        "LocationJaipur"
                                  "LocationJalandhar"
                                                           "LocationJamshedpur"
        "LocationKanpur"
                                  "LocationKarnal"
                                                           "LocationKharar"
   [28]
                                                           "LocationKollam"
        "LocationKheda"
                                  "LocationKolkata"
   [31]
        "LocationKota"
                                  "LocationLucknow"
                                                           "LocationLudhiana"
   [34]
##
        "LocationMangalore"
                                  "LocationMeerut"
                                                           "LocationMirzapur"
   [40]
        "LocationMohali"
                                  "LocationMumbai"
                                                           "LocationMuzaffurpur"
   [43]
        "LocationMysore"
                                  "LocationNagpur"
                                                           "LocationNashik"
        "LocationNavi Mumbai"
                                  "LocationNoida"
                                                           "LocationPanchkula"
   [46]
        "LocationPatna"
                                  "LocationPune"
                                                           "LocationRaipur"
                                  "LocationRanga Reddy"
        "LocationRanchi"
                                                           "LocationRoorkee"
   Γ521
   [55] "LocationSalem"
                                  "LocationSurat"
                                                           "LocationThane"
```

```
## [58] "LocationUdupi" "LocationVadodara" "LocationVaranasi"
## [61] "LocationWarangal" "LocationYamunanagar" "LocationZirakpur"
## [64] "OwnerSecond" "OwnerThird" "OwnerUnRegistered Car"
## [67] "Seller.TypeCorporate" "Seller.TypeIndividual" "Seating.Capacity"
```

## **Inspect Model Coefficients**

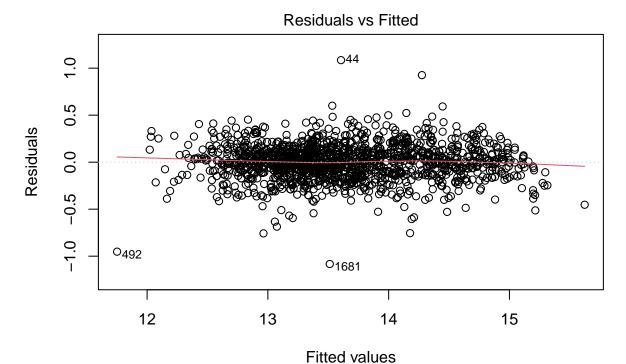
```
summary(reduced_model)
```

```
##
## Call:
##
  lm(formula = log(Price) ~ Make + Year + Kilometer + Fuel.Type +
##
       Transmission + Max.Torque.RPM + Drivetrain + Length + Width +
##
       Year:Kilometer + Year:Max.Torque.RPM + Year:Length + Max.Torque.RPM:Length,
##
       data = x)
##
  Residuals:
##
##
       Min
                 1Q
                      Median
                                   30
                                            Max
   -1.08307 -0.10778 0.00302 0.11095
##
  Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
                          9.510e+01 4.616e+01
                                                2.060 0.039566 *
## (Intercept)
## MakeBMW
                         1.874e-02 4.321e-02
                                                0.434 0.664637
## MakeChevrolet
                        -8.118e-01 9.967e-02 -8.144 8.35e-16 ***
## MakeDatsun
                        -9.312e-01 7.499e-02 -12.418 < 2e-16 ***
## MakeFord
                        -5.886e-01 4.134e-02 -14.237
                                                       < 2e-16 ***
                        -5.243e-01 3.348e-02 -15.659 < 2e-16 ***
## MakeHonda
## MakeHyundai
                        -4.913e-01 2.934e-02 -16.744 < 2e-16 ***
## MakeIsuzu
                        -4.104e-01 1.386e-01
                                               -2.960 0.003124 **
                         4.304e-02 8.415e-02
                                                0.511 0.609111
## MakeJaguar
## MakeJeep
                        -3.526e-01 5.495e-02
                                               -6.418 1.89e-10 ***
                         -4.353e-01 4.853e-02
## MakeKia
                                               -8.970 < 2e-16 ***
## MakeLand Rover
                         8.907e-02 1.132e-01
                                                0.787 0.431440
                        -6.243e-01 3.534e-02 -17.663 < 2e-16 ***
## MakeMahindra
## MakeMaruti Suzuki
                        -5.409e-01 3.008e-02 -17.979 < 2e-16 ***
## MakeMercedes-Benz
                         1.231e-01 3.561e-02
                                                3.457 0.000563 ***
## MakeMG
                         -6.054e-01 5.996e-02 -10.095
                                                       < 2e-16 ***
## MakeMINI
                                                8.645
                         7.174e-01 8.298e-02
                                                       < 2e-16 ***
## MakeMitsubishi
                        -2.063e-01 1.137e-01 -1.814 0.069817 .
## MakeNissan
                         -7.579e-01 5.559e-02 -13.634
                                                       < 2e-16 ***
## MakeRenault
                        -7.602e-01 4.110e-02 -18.499
                                                       < 2e-16 ***
## MakeSkoda
                        -4.933e-01 4.013e-02 -12.292 < 2e-16 ***
                        -8.659e-01 1.144e-01 -7.570 6.74e-14 ***
## MakeSsangyong
## MakeTata
                         -7.449e-01 3.963e-02 -18.799
                                                       < 2e-16 ***
                        -2.811e-01 3.210e-02 -8.757
                                                       < 2e-16 ***
## MakeToyota
## MakeVolkswagen
                        -5.047e-01
                                    4.029e-02 -12.525
                                                       < 2e-16 ***
## MakeVolvo
                         4.204e-02 6.144e-02
                                                0.684 0.493988
## Year
                         -4.268e-02
                                    2.289e-02
                                               -1.865 0.062445
## Kilometer
                        -3.578e-04 1.296e-04
                                               -2.761 0.005844 **
## Fuel.TypeDiesel
                        -1.317e-01 4.020e-02 -3.277 0.001075 **
## Fuel.TypePetrol
                        -1.608e-01 3.648e-02 -4.409 1.12e-05 ***
## TransmissionManual
                         -1.581e-01 1.340e-02 -11.799 < 2e-16 ***
## Max.Torque.RPM
                         1.250e-02 3.153e-03
                                               3.965 7.72e-05 ***
```

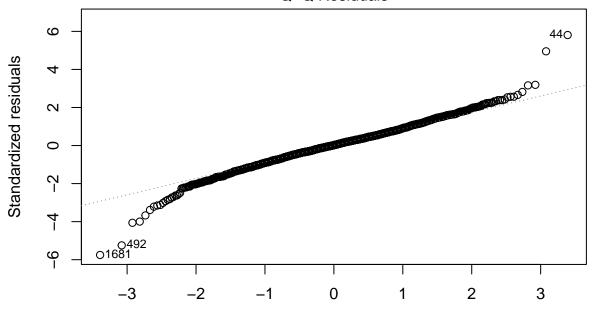
```
## DrivetrainFWD
                        -2.699e-01 2.396e-02 -11.268 < 2e-16 ***
## DrivetrainRWD
                       -2.116e-01 2.905e-02 -7.283 5.44e-13 ***
## Length
                        -7.724e-02 1.032e-02 -7.484 1.26e-13 ***
## Width
                        1.540e-03 1.163e-04 13.239 < 2e-16 ***
## Year:Kilometer
                         1.768e-07 6.427e-08
                                               2.751 0.006026 **
## Year:Max.Torque.RPM
                       -6.132e-06 1.559e-06 -3.933 8.82e-05 ***
## Year:Length
                         3.866e-05 5.116e-06
                                              7.555 7.51e-14 ***
## Max.Torque.RPM:Length -3.970e-08 1.460e-08 -2.719 0.006627 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1905 on 1401 degrees of freedom
## Multiple R-squared: 0.9273, Adjusted R-squared: 0.9253
## F-statistic: 458.2 on 39 and 1401 DF, p-value: < 2.2e-16
anova(reduced_model)
## Analysis of Variance Table
## Response: log(Price)
##
                          Df Sum Sq Mean Sq
                                             F value
## Make
                          25 354.44 14.178 390.8754 < 2.2e-16 ***
## Year
                           1 178.52 178.525 4921.9071 < 2.2e-16 ***
## Kilometer
                              0.98
                                     0.982
                                             27.0604 2.265e-07 ***
                          1
## Fuel.Type
                           2 19.23
                                     9.615 265.0896 < 2.2e-16 ***
                          1 20.31 20.313 560.0141 < 2.2e-16 ***
## Transmission
## Max.Torque.RPM
                          1
                             1.14
                                     1.139
                                             31.4057 2.518e-08 ***
                          2 6.53
## Drivetrain
                                     3.267
                                             90.0706 < 2.2e-16 ***
## Length
                          1 56.67 56.670 1562.3991 < 2.2e-16 ***
## Width
                                     5.636 155.3813 < 2.2e-16 ***
                          1 5.64
                          1 0.92
## Year:Kilometer
                                     0.922
                                             25.4311 5.184e-07 ***
## Year:Max.Torque.RPM
                          1 1.25
                                             34.3901 5.618e-09 ***
                                     1.247
## Year:Length
                           1 2.19
                                     2.187
                                             60.3045 1.559e-14 ***
## Max.Torque.RPM:Length
                           1
                              0.27
                                     0.268
                                              7.3935 0.006627 **
## Residuals
                        1401 50.82
                                     0.036
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

#### Final Model Verification

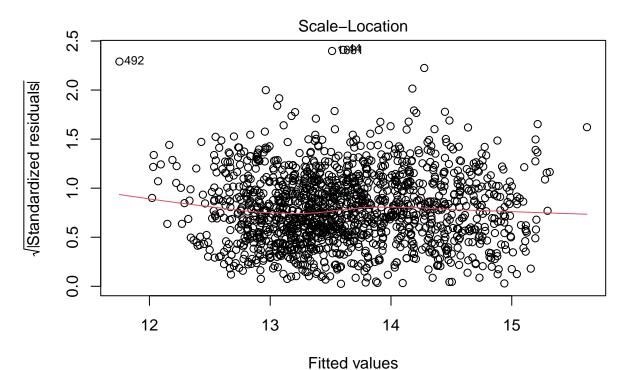
```
plot(reduced_model)
```



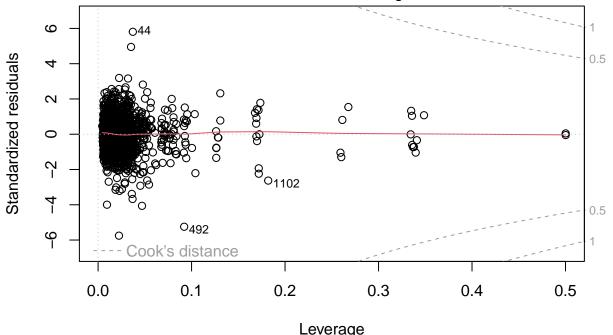
Im(log(Price) ~ Make + Year + Kilometer + Fuel.Type + Transmission + Max.To ...
Q-Q Residuals



Theoretical Quantiles Im(log(Price) ~ Make + Year + Kilometer + Fuel.Type + Transmission + Max.To ...



Im(log(Price) ~ Make + Year + Kilometer + Fuel.Type + Transmission + Max.To ... Residuals vs Leverage



Im(log(Price) ~ Make + Year + Kilometer + Fuel.Type + Transmission + Max.To ...

## Normalized Coefficients

```
normalized <- remove_cols(x, old[!(old %in% new)]) # removed from multicollinearity test
normalized <- remove_cols(x, c("Seating.Capacity", "Seller.Type"))</pre>
```

```
for (col in colnames(normalized)) {
  if (col != "Price" && !(col %in% categorical)) {
    normalized[, col] <- (normalized[, col] - mean(normalized[, col])) / sd(normalized[, col])</pre>
  }
}
normalized_model <- lm(log(Price) ~ . + Year:Kilometer + Year:Max.Torque.RPM</pre>
                    + Year:Length + Max.Torque.RPM:Length, data = normalized)
sort(abs(normalized_model$coefficients), decreasing = T)
##
              (Intercept)
                                   MakeSsangyong
                                                             MakeDatsun
##
            14.479239336
                                     0.872512749
                                                            0.857115032
##
           MakeChevrolet
                                     MakeRenault
                                                             MakeNissan
##
             0.798238688
                                     0.749256440
                                                            0.733447399
##
                 MakeTata
                                        MakeMINI
                                                                  MakeMG
##
             0.718998608
                                     0.704054157
                                                            0.596345412
##
            MakeMahindra
                                        MakeFord
                                                      MakeMaruti Suzuki
##
             0.596297888
                                     0.572746578
                                                            0.523222676
##
          MakeVolkswagen
                                       MakeSkoda
                                                              MakeHonda
##
             0.518324656
                                     0.509078901
                                                            0.485869081
             MakeHyundai
                                                          LocationSalem
##
                                       MakeIsuzu
##
             0.465042221
                                     0.437700433
                                                            0.420870279
##
                  MakeKia
                                        MakeJeep
                                                         LocationMysore
##
             0.415501427
                                     0.333574675
                                                            0.320886296
##
                     Year
                           LocationBulandshahar
                                                     LocationAurangabad
##
             0.313783661
                                     0.313704055
                                                            0.293113281
##
      LocationCoimbatore
                                   DrivetrainFWD
                                                         MakeMitsubishi
##
             0.269393557
                                     0.263692508
                                                            0.249563035
##
              MakeToyota
                                     LocationGoa
                                                      LocationBangalore
##
              0.248826742
                                     0.248093841
                                                            0.246496783
##
          LocationKollam
                                                          DrivetrainRWD
                                          Length
##
             0.226788237
                                     0.226439416
                                                            0.221018253
##
         LocationChennai
                                  LocationIndore
                                                      LocationErnakulam
##
             0.216077914
                                     0.209724881
                                                            0.208988890
##
         LocationDharwad
                                 Fuel.TypePetrol
                                                      LocationHyderabad
##
             0.207341744
                                     0.189472148
                                                            0.185525949
##
       LocationJalandhar
                                  MakeLand Rover
                                                         LocationNagpur
##
             0.181224043
                                     0.180846132
                                                            0.167588274
##
        LocationGuwahati
                                 Fuel.TypeDiesel
                                                          LocationUdupi
##
             0.167182283
                                     0.164673775
                                                            0.148042941
##
       MakeMercedes-Benz
                             TransmissionManual
                                                                   Width
##
                                                            0.135371333
             0.145432782
                                     0.143902253
##
            LocationPune
                                  LocationJaipur
                                                       LocationAmritsar
##
             0.131030713
                                     0.122967074
                                                            0.121805119
##
              OwnerThird
                                    LocationKota
                                                         LocationMohali
##
             0.121210169
                                     0.117146416
                                                            0.115934495
##
           LocationThane
                                  LocationMumbai
                                                         LocationRaipur
##
             0.102055354
                                     0.100701797
                                                            0.099272043
##
        LocationMirzapur
                                  LocationKarnal
                                                          LocationNoida
##
             0.098291704
                                     0.096670247
                                                            0.095972455
##
    LocationAmbala Cantt
                            LocationNavi Mumbai
                                                      LocationAllahabad
##
             0.092130013
                                     0.092020794
                                                            0.090599537
```

##	LocationKheda		OwnerUnRegistered Car
##	0.088221751	0.086058622	0.082215522
##	LocationBhubaneswar	${\tt Location}{\tt Kolkata}$	LocationDelhi
##	0.080119830	0.076002757	0.071607021
##	${ t Location} { t Faridabad}$	${\tt Location Muzaffur pur}$	LocationRanga Reddy
##	0.069764717	0.068179314	0.066742019
##	MakeJaguar	LocationWarangal	${ t Location Ahmedabad}$
##	0.065901543	0.063180846	0.062246218
##	LocationPatna	LocationDehradun	LocationNashik
##	0.062160128	0.059305473	0.058196769
##	${ t Max.Torque.RPM}$	LocationMangalore	LocationKharar
##	0.056697498	0.056620215	0.056298195
##	LocationVaranasi	LocationRoorkee	LocationRanchi
##	0.048878372	0.047629067	0.046096495
##	LocationLudhiana	Year:Length	LocationSurat
##	0.043273053	0.041510876	0.041112278
##	LocationMeerut	Kilometer	${ t Location Chandigarh }$
##	0.038541407	0.034232361	0.031825300
##	MakeVolvo	${ t Location Bhopal}$	LocationPanchkula
##	0.030938615	0.029053023	0.027400801
##	${ t Location Zirakpur}$	${\tt LocationGhaziabad}$	${ t Location Yamunanagar}$
##	0.026027821	0.023076512	0.023015393
##	LocationLucknow	OwnerSecond	Year:Max.Torque.RPM
##	0.021634758	0.020113875	0.018733584
##	Max.Torque.RPM:Length	Year:Kilometer	${\tt LocationJamshedpur}$
##	0.017715033	0.017494262	0.017254036
##	${ t MakeBMW}$	LocationHaldwani	${\tt LocationGurgaon}$
##	0.012673995	0.010949026	0.010276737
##	${ t Location Vadodara}$		

# Confidence Intervals

##

# confint(reduced\_model, level = 0.95)

0.009552204

```
##
                                 2.5 %
                                              97.5 %
## (Intercept)
                          4.547396e+00 1.856477e+02
## MakeBMW
                         -6.602817e-02 1.035016e-01
## MakeChevrolet
                         -1.007281e+00 -6.162404e-01
## MakeDatsun
                         -1.078298e+00 -7.841001e-01
## MakeFord
                         -6.697386e-01 -5.075326e-01
## MakeHonda
                         -5.900076e-01 -4.586369e-01
## MakeHyundai
                         -5.488761e-01 -4.337524e-01
## MakeIsuzu
                         -6.823497e-01 -1.384600e-01
                         -1.220379e-01 2.081188e-01
## MakeJaguar
## MakeJeep
                         -4.604327e-01 -2.448569e-01
                         -5.305453e-01 -3.401349e-01
## MakeKia
## MakeLand Rover
                         -1.329586e-01 3.111020e-01
## MakeMahindra
                         -6.936231e-01 -5.549561e-01
## MakeMaruti Suzuki
                         -5.998648e-01 -4.818426e-01
## MakeMercedes-Benz
                          5.324385e-02 1.929706e-01
## MakeMG
                         -7.229815e-01 -4.877246e-01
                          5.546073e-01 8.801579e-01
## MakeMINI
## MakeMitsubishi
                         -4.293712e-01 1.673447e-02
```

```
## MakeNissan
                        -8.669420e-01 -6.488544e-01
## MakeRenault
                        -8.408366e-01 -6.796076e-01
## MakeSkoda
                        -5.720421e-01 -4.145890e-01
## MakeSsangyong
                        -1.090227e+00 -6.414793e-01
## MakeTata
                        -8.226646e-01 -6.671974e-01
## MakeToyota
                        -3.440356e-01 -2.181091e-01
## MakeVolkswagen
                        -5.837269e-01 -4.256451e-01
## MakeVolvo
                        -7.849495e-02 1.625703e-01
## Year
                        -8.757891e-02 2.221399e-03
## Kilometer
                        -6.120361e-04 -1.035533e-04
## Fuel.TypeDiesel
                        -2.106099e-01 -5.288107e-02
## Fuel.TypePetrol
                        -2.323631e-01 -8.925600e-02
## TransmissionManual
                        -1.843935e-01 -1.318227e-01
## Max.Torque.RPM
                         6.315101e-03 1.868420e-02
## DrivetrainFWD
                        -3.169270e-01 -2.229383e-01
## DrivetrainRWD
                        -2.685680e-01 -1.545884e-01
## Length
                        -9.748973e-02 -5.699824e-02
## Width
                        1.311510e-03 1.767784e-03
## Year:Kilometer
                         5.069930e-08 3.028336e-07
## Year:Max.Torque.RPM -9.190592e-06 -3.073084e-06
## Year:Length
                         2.861917e-05 4.869220e-05
## Max.Torque.RPM:Length -6.834755e-08 -1.105992e-08
```