

⑬ Rearranjando R_1 e R_2 :

$$R_1 = \sum_{i=0}^{n/2-1} \frac{2h}{2} f(x_{2i}) + f(x_{2i+1}) = \frac{2h}{2} (f(a) + f(b) + 2 \sum_{i=1}^{n/2-1} f(x_{2i}))$$

$$R_2 = \sum_{i=0}^{n-1} \frac{h}{2} f(x_i) + f(x_{i+1}) = \frac{h}{2} (f(a) + f(b) + 2 \sum_{i=1}^{n-1} f(x_i))$$

$$S = \frac{4R_2 - R_1}{3}$$

$$= \left[2h(f(a) + 2 \sum_{i=1}^{n-1} f(x_i) + f(b)) - h(f(a) + 2 \sum_{i=1}^{n/2-1} f(x_{2i}) + f(b)) \right] \cdot \frac{1}{3}$$

$$= \frac{h}{3} \left[2f(a) + 4 \sum_{i=1}^{n-1} f(x_i) + 2f(b) - f(a) - 2 \sum_{i=1}^{n/2-1} f(x_{2i}) - f(b) \right] \quad (*)$$

$$= \frac{h}{3} \left(f(a) + 4 \left(\sum_{i=1}^{n/2} f(x_{2i-1}) + \sum_{i=1}^{n/2-1} f(x_{2i}) \right) - 2 \sum_{i=1}^{n/2-1} f(x_{2i}) + f(b) \right)$$

$$= \frac{h}{3} \left(f(a) + 4 \sum_{i=1}^{n/2} f(x_{2i-1}) + 2 \sum_{i=1}^{n/2-1} f(x_{2i}) + f(b) \right)$$

⊛ Pois é possível separar a soma de R_2 em pares e ímpares

$$\sum_{i=1}^{n/2-1} f(x_{2i}) + \sum_{i=1}^{n/2-1} f(x_{2i+1})$$