OpenGeoProver Output for conjecture "geothm_zadatak"

Wu's method used

October 1, 2016

1 Invoking the theorem prover

The used proving method is Wu's method. The input system is:

 $p_1 = 2x_1$ $p_2 = 2x_2$ $p_3 = 2x_4$ $p_4 = 2x_5 - x_1$ $p_5 = 2x_6 - x_2$ $p_6 = 2x_7 - x_3$ $p_7 = x_{11}x_2 + x_9 - x_2$ $p_8 = x_{11}x_3 + x_{10} - x_3$ $= -x_{12}x_5 + x_8$ $p_{10} = -x_{12}x_6 + x_9$ $p_{11} = -x_{12}x_7 + x_{10}$ $p_{12} = 2x_{13} - 2$ $p_{13} = 2x_{14}$ $p_{14} = -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2$ $p_{15} = x_{18}x_3 + x_{17} - x_3$ $p_{16} = -x_{19}x_5 + x_{19} + x_{15}$ $p_{17} = -x_{19}x_6 + x_{19} + x_{16} = -x_{19}x_7 + x_{17}$

1.1 Triangulation, step 1

Choosing variable: Trying the variable with index 18.

Variable x_{18} selected: The number of polynomials with this variable, with indexes from 1 to 18, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{18} from all other polynomials by reducing them with polynomial p_{14} from previous step.

Finished a triangulation step, the current system is:

1.2 Triangulation, step 2

Choosing variable: Trying the variable with index 17.

Variable x_{17} selected: The number of polynomials with this variable, with indexes from 1 to 17, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{17} from all other polynomials by reducing them with polynomial p_{16} from previous step.

$$\begin{array}{rcl}
p_1 & = & 2x_1 - \\
p_2 & = & 2x_2 - \\
p_3 & = & 2x_4 - \\
p_4 & = & 2x_5 - x_1 - \\
p_5 & = & 2x_6 - x_2 \\
p_6 & = & 2x_7 - x_3
\end{array}$$

$$\begin{array}{rcl} p_7 & = & x_{11}x_2 + x_9 - x_2 \\ p_8 & = & x_{11}x_3 + x_{10} - x_3 \\ p_9 & = & -x_{12}x_5 + x_8 \\ p_{10} & = & -x_{12}x_6 + x_9 \\ p_{11} & = & -x_{12}x_7 + x_{10} \\ p_{12} & = & 2x_{13} - 2 \\ p_{13} & = & 2x_{14} - \\ p_{14} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{15} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{16} & = & -x_{19}x_{14}x_7 + x_{19}x_7x_2 - x_{16}x_3 + x_{14}x_3 \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

1.3 Triangulation, step 3

Choosing variable: Trying the variable with index 16.

Variable x_{16} selected: The number of polynomials with this variable, with indexes from 1 to 16, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{16} from all other polynomials by reducing them with polynomial p_{15} from previous step.

$$\begin{array}{rclcrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 2x_6 - x_2 \\ p_6 & = & 2x_7 - x_3 \\ p_7 & = & x_{11}x_2 + x_9 - x_2 \\ p_8 & = & x_{11}x_3 + x_{10} - x_3 \\ p_9 & = & -x_{12}x_5 + x_8 \\ p_{10} & = & -x_{12}x_6 + x_9 \\ p_{11} & = & -x_{12}x_7 + x_{10} \\ p_{12} & = & 2x_{13} - 2 \\ p_{13} & = & 2x_{14} - \\ p_{14} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{15} & = & -x_{19}x_{14}x_7 + x_{19}x_7x_2 - x_{19}x_6x_3 + x_{19}x_3 + x_{14}x_3 - x_3 \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \end{array}$$

$$p_{18} = -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2$$

1.4 Triangulation, step 4

Choosing variable: Trying the variable with index 15.

Variable x_{15} selected: The number of polynomials with this variable, with indexes from 1 to 15, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_{14} . No reduction needed.

The triangular system has not been changed.

1.5 Triangulation, step 5

Choosing variable: Trying the variable with index 14.

Variable x_{14} selected: The number of polynomials with this variable, with indexes from 1 to 14, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{14} from all other polynomials by reducing them with polynomial p_{13} from previous step.

$$\begin{array}{rclcrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 2x_6 - x_2 \\ p_6 & = & 2x_7 - x_3 \\ p_7 & = & x_{11}x_2 + x_9 - x_2 \\ p_8 & = & x_{11}x_3 + x_{10} - x_3 \\ p_9 & = & -x_{12}x_5 + x_8 \\ p_{10} & = & -x_{12}x_6 + x_9 \\ p_{11} & = & -x_{12}x_7 + x_{10} \\ p_{12} & = & 2x_{13} - 2 \\ p_{13} & = & 2x_{19}x_7x_2 - x_{19}x_7 - 2x_{19}x_6x_3 + 2x_{19}x_3 - x_3 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

1.6 Triangulation, step 6

Choosing variable: Trying the variable with index 13.

Variable x_{13} selected: The number of polynomials with this variable, with indexes from 1 to 13, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_{12} . No reduction needed.

The triangular system has not been changed.

1.7 Triangulation, step 7

Choosing variable: Trying the variable with index 12.

Variable x_{12} selected: The number of polynomials with this variable, with indexes from 1 to 12, is 3.

Minimal degrees: 3 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{12} from all other polynomials by reducing them with polynomial p_9 from previous step.

$$\begin{array}{rclcrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 2x_6 - x_2 \\ p_6 & = & 2x_7 - x_3 \\ p_7 & = & x_{11}x_2 + x_9 - x_2 \\ p_8 & = & x_{11}x_3 + x_{10} - x_3 \\ p_9 & = & 2x_{19}x_7x_2 - x_{19}x_7 - 2x_{19}x_6x_3 + 2x_{19}x_3 - x_3 \\ p_{10} & = & -x_9x_5 + x_8x_6 \\ p_{11} & = & -x_{10}x_5 + x_8x_7 \\ p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

1.8 Triangulation, step 8

Choosing variable: Trying the variable with index 11.

Variable x_{11} selected: The number of polynomials with this variable, with indexes from 1 to 11, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{11} from all other polynomials by reducing them with polynomial p_7 from previous step.

Finished a triangulation step, the current system is:

$$\begin{array}{rclcrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 2x_6 - x_2 \\ p_6 & = & 2x_7 - x_3 \\ p_7 & = & 2x_{19}x_7x_2 - x_{19}x_7 - 2x_{19}x_6x_3 + 2x_{19}x_3 - x_3 \\ p_8 & = & -x_9x_5 + x_8x_6 \\ p_9 & = & -x_{10}x_5 + x_8x_7 \\ p_{10} & = & x_{10}x_2 - x_9x_3 \\ p_{11} & = & x_{11}x_2 + x_9 - x_2 \\ p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

1.9 Triangulation, step 9

Choosing variable: Trying the variable with index 10.

Variable x_{10} selected: The number of polynomials with this variable, with indexes from 1 to 10, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_{10} from all other polynomials by reducing them with polynomial p_9 from previous step.

$$\begin{array}{rclcrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 2x_6 - x_2 \\ p_6 & = & 2x_7 - x_3 \\ p_7 & = & 2x_{19}x_7x_2 - x_{19}x_7 - 2x_{19}x_6x_3 + 2x_{19}x_3 - x_3 \\ p_8 & = & -x_9x_5 + x_8x_6 \\ p_9 & = & x_9x_5x_3 - x_8x_7x_2 \\ p_{10} & = & -x_{10}x_5 + x_8x_7 \\ p_{11} & = & x_{11}x_2 + x_9 - x_2 \\ p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

1.10 Triangulation, step 10

Choosing variable: Trying the variable with index 9.

Variable x_9 selected: The number of polynomials with this variable, with indexes from 1 to 9, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_9 from all other polynomials by reducing them with polynomial p_8 from previous step.

$$\begin{array}{llll} p_1 & = & 2x_1 - & & & \\ p_2 & = & 2x_2 - & & & \\ p_3 & = & 2x_4 - & & & \\ p_4 & = & 2x_5 - x_1 - & & & \\ p_5 & = & 2x_6 - x_2 & & & \\ p_6 & = & 2x_7 - x_3 & & & \\ p_7 & = & 2x_{19}x_7x_2 - x_{19}x_7 - 2x_{19}x_6x_3 + 2x_{19}x_3 - x_3 \\ p_8 & = & x_8x_7x_5x_2 - x_8x_6x_5x_3 \\ p_9 & = & -x_9x_5 + x_8x_6 \end{array}$$

$$\begin{array}{lll} p_{10} & = & -x_{10}x_5 + x_8x_7 \\ p_{11} & = & x_{11}x_2 + x_9 - x_2 \\ p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \end{array}$$

1.11 Triangulation, step 11

Choosing variable: Trying the variable with index 8.

Variable x_8 selected: The number of polynomials with this variable, with indexes from 1 to 8, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_8 . No reduction needed.

The triangular system has not been changed.

1.12 Triangulation, step 12

Choosing variable: Trying the variable with index 7.

Variable x_7 selected: The number of polynomials with this variable, with indexes from 1 to 7, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_7 from all other polynomials by reducing them with polynomial p_6 from previous step.

$$\begin{array}{rclcrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 2x_6 - x_2 \\ p_6 & = & -4x_{19}x_6x_3 + 2x_{19}x_3x_2 + 3x_{19}x_3 - 2x_3 \\ p_7 & = & 2x_7 - x_3 \\ p_8 & = & x_8x_7x_5x_2 - x_8x_6x_5x_3 \\ p_9 & = & -x_9x_5 + x_8x_6 \\ p_{10} & = & -x_{10}x_5 + x_8x_7 \\ p_{11} & = & x_{11}x_2 + x_9 - x_2 \end{array}$$

$$\begin{array}{lll} p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \end{array}$$

1.13 Triangulation, step 13

Choosing variable: Trying the variable with index 6.

Variable x_6 selected: The number of polynomials with this variable, with indexes from 1 to 6, is 2.

Minimal degrees: 2 polynomial(s) with degree 1.

Polynomial with linear degree: Removing variable x_6 from all other polynomials by reducing them with polynomial p_5 from previous step.

Finished a triangulation step, the current system is:

$$\begin{array}{rclrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 2x_4 - \\ p_4 & = & 2x_5 - x_1 - \\ p_5 & = & 6x_{19}x_3 - 4x_3 \\ p_6 & = & 2x_6 - x_2 \\ p_7 & = & 2x_7 - x_3 \\ p_8 & = & x_8x_7x_5x_2 - x_8x_6x_5x_3 \\ p_9 & = & -x_9x_5 + x_8x_6 \\ p_{10} & = & -x_{10}x_5 + x_8x_7 \\ p_{11} & = & x_{11}x_2 + x_9 - x_2 \\ p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

1.14 Triangulation, step 14

Choosing variable: Trying the variable with index 5.

Variable x_5 **selected:** The number of polynomials with this variable, with indexes from 1 to 5, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_4 . No reduction needed.

The triangular system has not been changed.

1.15 Triangulation, step 15

Choosing variable: Trying the variable with index 4.

Variable x_4 selected: The number of polynomials with this variable, with indexes from 1 to 4, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_3 . No reduction needed.

The triangular system has not been changed.

1.16 Triangulation, step 16

Choosing variable: Trying the variable with index 3.

Variable x_3 selected: The number of polynomials with this variable, with indexes from 1 to 3, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_3 . No reduction needed.

The triangular system has not been changed.

1.17 Triangulation, step 17

Choosing variable: Trying the variable with index 2.

Variable x_2 selected: The number of polynomials with this variable, with indexes from 1 to 2, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_2 . No reduction needed.

The triangular system has not been changed.

1.18 Triangulation, step 18

Choosing variable: Trying the variable with index 1.

Variable x_1 selected: The number of polynomials with this variable, with indexes from 1 to 1, is 1.

Single polynomial with chosen variable: Chosen polynomial is p_1 . No reduction needed.

The triangular system has not been changed.

The triangular system is:

$$\begin{array}{rclrcl} p_1 & = & 2x_1 - \\ p_2 & = & 2x_2 - \\ p_3 & = & 6x_{19}x_3 - 4x_3 \\ p_4 & = & 2x_4 - \\ p_5 & = & 2x_5 - x_1 - \\ p_6 & = & 2x_6 - x_2 \\ p_7 & = & 2x_7 - x_3 \\ p_8 & = & x_8x_7x_5x_2 - x_8x_6x_5x_3 \\ p_9 & = & -x_9x_5 + x_8x_6 \\ p_{10} & = & -x_{10}x_5 + x_8x_7 \\ p_{11} & = & x_{11}x_2 + x_9 - x_2 \\ p_{12} & = & -x_{12}x_5 + x_8 \\ p_{13} & = & 2x_{13} - 2 \\ p_{14} & = & 2x_{14} - \\ p_{15} & = & -x_{19}x_5 + x_{19} + x_{15} - \\ p_{16} & = & -x_{19}x_6 + x_{19} + x_{16} - \\ p_{17} & = & -x_{19}x_7 + x_{17} \\ p_{18} & = & -x_{18}x_{14} + x_{18}x_2 + x_{16} - x_2 \\ \end{array}$$

2 Final Remainder

2.1 Final remainder for conjecture geothm_zadatak

Calculating final remainder of the conclusion:

$$g = 4x_{17}^2 - 8x_{17}x_{10} + 4x_{16}^2 - 8x_{16}x_9 + 4x_{15}^2 - 8x_{15}x_8 + 4x_{10}^2 + 4x_9^2 + 4x_8^2 -$$

with respect to the triangular system.

1. Pseudo remainder with p_{18} over variable x_{18} :

$$g = 4x_{17}^2 - 8x_{17}x_{10} + 4x_{16}^2 - 8x_{16}x_9 + 4x_{15}^2 - 8x_{15}x_8 + 4x_{10}^2 + 4x_{19}^2 + 4x_{19}^2 - 4x_{10}^2 + 4x_{10$$

2. Pseudo remainder with p_{17} over variable x_{17} :

$$g = 4x_{19}^2 x_7^2 - 8x_{19}x_{10}x_7 + 4x_{16}^2 - 8x_{16}x_9 + 4x_{15}^2 - 8x_{15}x_8 + 4x_{10}^2 + 4x_9^2 + 4x_8^2 -$$

3. Pseudo remainder with p_{16} over variable x_{16} :

$$g = 4x_{19}^2x_7^2 + 4x_{19}^2x_6^2 - 8x_{19}^2x_6 + 4x_{19}^2 - 8x_{19}x_{10}x_7$$
$$-8x_{19}x_9x_6 + 8x_{19}x_9 + 8x_{19}x_6 - 8x_{19} + 4x_{15}^2 - 8x_{15}x_8 + 4x_{10}^2 + 4x_{19}^2 - 8x_9 + 4x_{19}^2 + 3$$

4. Pseudo remainder with p_{15} over variable x_{15} :

$$g = 4x_{19}^2x_7^2 + 4x_{19}^2x_6^2 - 8x_{19}^2x_6 + 4x_{19}^2x_5^2$$

$$-8x_{19}^2x_5 + 8x_{19}^2 - 8x_{19}x_{10}x_7 - 8x_{19}x_{9}x_6 + 8x_{19}x_9$$

$$-8x_{19}x_8x_5 + 8x_{19}x_8 + 8x_{19}x_6 + 8x_{19}x_5 - 16x_{19} + 4x_{10}^2 + 4x_9^2$$

$$-8x_9 + 4x_8^2 - 8x_8 + 7$$

5. Pseudo remainder with p_{14} over variable x_{14} :

$$g = 4x_{19}^2x_7^2 + 4x_{19}^2x_6^2 - 8x_{19}^2x_6 + 4x_{19}^2x_5^2$$

$$-8x_{19}^2x_5 + 8x_{19}^2 - 8x_{19}x_{10}x_7 - 8x_{19}x_{9}x_6 + 8x_{19}x_9$$

$$-8x_{19}x_8x_5 + 8x_{19}x_8 + 8x_{19}x_6 + 8x_{19}x_5 - 16x_{19} + 4x_{10}^2 + 4x_9^2$$

$$-8x_9 + 4x_8^2 - 8x_8 + 7$$

6. Pseudo remainder with p_{13} over variable x_{13} :

$$g = 4x_{19}^2x_7^2 + 4x_{19}^2x_6^2 - 8x_{19}^2x_6 + 4x_{19}^2x_5^2$$

$$-8x_{19}^2x_5 + 8x_{19}^2 - 8x_{19}x_{10}x_7 - 8x_{19}x_{9}x_6 + 8x_{19}x_9$$

$$-8x_{19}x_8x_5 + 8x_{19}x_8 + 8x_{19}x_6 + 8x_{19}x_5 - 16x_{19} + 4x_{10}^2 + 4x_9^2$$

$$-8x_9 + 4x_8^2 - 8x_8 + 7$$

7. Pseudo remainder with p_{12} over variable x_{12} :

$$g = 4x_{19}^2x_7^2 + 4x_{19}^2x_6^2 - 8x_{19}^2x_6 + 4x_{19}^2x_5^2$$

$$-8x_{19}^2x_5 + 8x_{19}^2 - 8x_{19}x_{10}x_7 - 8x_{19}x_{9}x_6 + 8x_{19}x_9$$

$$-8x_{19}x_8x_5 + 8x_{19}x_8 + 8x_{19}x_6 + 8x_{19}x_5 - 16x_{19} + 4x_{10}^2 + 4x_9^2$$

$$-8x_9 + 4x_8^2 - 8x_8 + 7$$

8. Pseudo remainder with p_{11} over variable x_{11} :

$$g = 4x_{19}^2x_7^2 + 4x_{19}^2x_6^2 - 8x_{19}^2x_6 + 4x_{19}^2x_5^2$$

$$-8x_{19}^2x_5 + 8x_{19}^2 - 8x_{19}x_{10}x_7 - 8x_{19}x_{9}x_6 + 8x_{19}x_9$$

$$-8x_{19}x_8x_5 + 8x_{19}x_8 + 8x_{19}x_6 + 8x_{19}x_5 - 16x_{19} + 4x_{10}^2 + 4x_9^2$$

$$-8x_9 + 4x_8^2 - 8x_8 + 7$$

9. Pseudo remainder with p_{10} over variable x_{10} :

$$\begin{array}{lll} g & = & 4x_{19}^2x_7^2x_5^2 + 4x_{19}^2x_6^2x_5^2 - 8x_{19}^2x_6x_5^2 + \\ & & 4x_{19}^2x_5^4 - 8x_{19}^2x_5^3 + 8x_{19}^2x_5^2 - 8x_{19}x_9x_6x_5^2 + \\ & & 8x_{19}x_9x_5^2 - 8x_{19}x_8x_7^2x_5 - 8x_{19}x_8x_5^3 + \\ & & 8x_{19}x_8x_5^2 + 8x_{19}x_6x_5^2 + 8x_{19}x_5^3 - 16x_{19}x_5^2 + \\ & 4x_9^2x_5^2 - 8x_9x_5^2 + 4x_8^2x_7^2 + 4x_8^2x_5^2 - 8x_8x_5^2 + \\ & & 7x_5^2 \end{array}$$

10. Pseudo remainder with p_9 over variable x_9 :

$$\begin{array}{lll} g & = & 4x_{19}^2x_7^2x_5^4 + 4x_{19}^2x_6^2x_5^4 - 8x_{19}^2x_6x_5^4 + \\ & & 4x_{19}^2x_5^6 - 8x_{19}^2x_5^5 + 8x_{19}^2x_5^4 \\ & & -8x_{19}x_8x_7^2x_5^3 - 8x_{19}x_8x_6^2x_5^3 + 8x_{19}x_8x_6x_5^3 \\ & & -8x_{19}x_8x_5^5 + 8x_{19}x_8x_5^4 + 8x_{19}x_6x_5^4 + 8x_{19}x_5^5 \\ & & -16x_{19}x_5^4 + 4x_8^2x_7^2x_5^2 + 4x_8^2x_6^2x_5^2 + \\ & & 4x_8^2x_5^4 - 8x_8x_6x_5^3 - 8x_8x_5^4 + 7x_5^4 \end{array}$$

11. Pseudo remainder with p_8 over variable x_8 :

$$\begin{array}{lll} g&=&4x_{19}^2x_7^4x_5^6x_2^2-8x_{19}^2x_7^3x_6x_5^6x_3x_2+\\ &4x_{19}^2x_7^2x_6^2x_5^6x_3^2+\\ &4x_{19}^2x_7^2x_6^2x_5^6x_2^2\\ &-8x_{19}^2x_7^2x_6x_5^6x_2^2+4x_{19}^2x_7^2x_5^8x_2^2\\ &-8x_{19}^2x_7^2x_5^7x_2^2+8x_{19}^2x_7^2x_5^6x_2^2\\ &-8x_{19}^2x_7x_6^3x_5^6x_3x_2+16x_{19}^2x_7x_6^2x_5^6x_3x_2\\ &-8x_{19}^2x_7x_6x_5^8x_3x_2+16x_{19}^2x_7x_6x_5^7x_3x_2\\ &-8x_{19}^2x_7x_6x_5^8x_3x_2+4x_{19}^2x_7x_6x_5^8x_3^2\\ &-16x_{19}^2x_7x_6x_5^6x_3x_2+4x_{19}^2x_6^4x_5^6x_3^2\\ &-8x_{19}^2x_6^3x_5^6x_3^2+4x_{19}^2x_6^2x_5^8x_3^2\\ &-8x_{19}^2x_6^2x_5^7x_3^2+8x_{19}^2x_6^2x_5^6x_3^2+\\ &8x_{19}x_7^2x_6x_5^6x_2^2+8x_{19}x_7^2x_5^7x_2^2\\ &-16x_{19}x_7x_6x_5^7x_3x_2+32x_{19}x_7x_6x_5^6x_3x_2+\\ &8x_{19}x_6^3x_5^6x_3^2+8x_{19}x_6^2x_5^7x_3^2\\ &-16x_{19}x_6^2x_5^6x_3^2+7x_7^2x_5^6x_2^2\\ &-14x_7x_6x_5^6x_3x_2+7x_6^2x_5^6x_3^2\\ &-14x_7x_6x_5^6x_3x_2+7x_6^2x_5^6x_3^2\\ \end{array}$$

12. Pseudo remainder with p_7 over variable x_7 :

$$\begin{array}{lll} g&=&64x_{19}^2x_6^4x_5^6x_3^2-64x_{19}^2x_6^3x_5^6x_3^2x_2\\ &-128x_{19}^2x_6^2x_5^5x_3^2+64x_{19}^2x_6^2x_5^8x_3^2\\ &-128x_{19}^2x_6^2x_5^5x_3^2+16x_{19}^2x_6^2x_5^6x_3^4+\\ &16x_{19}^2x_6^2x_5^6x_3^2x_2^2+\\ &128x_{19}^2x_6^2x_5^6x_3^2x_2+128x_{19}^2x_6x_5^6x_3^2\\ &-64x_{19}^2x_6x_5^8x_3^2x_2+128x_{19}^2x_6x_5^7x_3^2x_2\\ &-16x_{19}^2x_6x_5^6x_3^4x_2-32x_{19}^2x_6x_5^6x_3^2x_2^2\\ &-128x_{19}^2x_6x_5^6x_3^2x_2+16x_{19}^2x_5^8x_3^2x_2^2\\ &-128x_{19}^2x_5x_3^2x_2^2+4x_{19}^2x_5^6x_3^4x_2^2+\\ &32x_{19}^2x_5^6x_3^2x_2^2+128x_{19}x_6^2x_5^6x_3^2x_2\\ &-256x_{19}x_6^2x_5^6x_3^2-128x_{19}x_6x_5^6x_3^2x_2+\\ &32x_{19}x_6x_5^6x_3^2x_2^2+256x_{19}x_6x_5^6x_3^2x_2+\\ &32x_{19}x_5^7x_3^2x_2^2-64x_{19}x_6x_5^6x_3^2x_2+\\ &32x_{19}x_5^7x_3^2x_2^2-64x_{19}x_5^6x_3^2x_2^2+\\ &112x_6^2x_5^6x_3^2-112x_6x_5^6x_3^2x_2+\\ &28x_5^6x_3^2x_2^2\end{array}$$

13. Pseudo remainder with p_6 over variable x_6 :

$$g = 0$$

14. Pseudo remainder with p_5 over variable x_5 :

$$g = 0$$

15. Pseudo remainder with p_4 over variable x_4 :

$$g = 0$$

16. Pseudo remainder with p_3 over variable x_3 :

$$g = 0$$

17. Pseudo remainder with p_2 over variable x_2 :

$$g = 0$$

18. Pseudo remainder with p_1 over variable x_1 :

$$g = 0$$

3 Prover results

Status: Theorem has been proved.

Space Complexity: The biggest polynomial obtained during prover execution

contains 34 terms.

Time Complexity: Time spent by the prover is 0.11 seconds.

4 NDG Conditions

NDG Conditions in readable form

• Failed to translate NDG Conditions to readable form