

# OpenGeoProver Output for conjecture “geothm\_zadatak”

Wu’s method used

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## 1 Invoking the theorem prover

The used proving method is Wu’s method.

The input system is:

$$\begin{aligned} p_1 &= 2x_1 - \\ p_2 &= 2x_2 - \\ p_3 &= -x_4x_1 - x_3x_2 + x_2x_1 \\ p_4 &= x_6x_5x_2 + x_6x_5x_1 - x_5x_2x_1 - x_4x_1 - x_3x_2 + x_2x_1 \\ p_5 &= x_7x_5x_2 + x_7x_5x_1 - x_5x_2x_1 - x_4x_1 - x_3x_2 + x_2x_1 \\ p_6 &= x_8x_5x_2 + x_8x_5x_1 - x_5x_2 - x_5x_1 \end{aligned}$$

### 1.1 Triangulation, step 1

**Choosing variable:** Trying the variable with index 6.

**Variable  $x_6$  selected:** The number of polynomials with this variable, with indexes from 1 to 6, is 1.

**Single polynomial with chosen variable:** Chosen polynomial is  $p_4$ . No reduction needed.

The triangular system has not been changed.

### 1.2 Triangulation, step 2

**Choosing variable:** Trying the variable with index 5.

**Variable  $x_5$  selected:** The number of polynomials with this variable, with indexes from 1 to 5, is 2.

**Minimal degrees:** 2 polynomial(s) with degree 1.

**Polynomial with linear degree:** Removing variable  $x_5$  from all other polynomials by reducing them with polynomial  $p_4$  from previous step.

Finished a triangulation step, the current system is:

$$\begin{aligned}
p_1 &= 2x_1 - \\
p_2 &= 2x_2 - \\
p_3 &= -x_4x_1 - x_3x_2 + x_2x_1 \\
p_4 &= x_8x_4x_2x_1 + x_8x_4x_1^2 + x_8x_3x_2^2 + x_8x_3x_2x_1 \\
&\quad - x_8x_2^2x_1 - x_8x_2x_1^2 - x_4x_2x_1 - x_4x_1^2 - x_3x_2^2 \\
&\quad - x_3x_2x_1 + x_2^2x_1 + x_2x_1^2 \\
p_5 &= x_7x_5x_2 + x_7x_5x_1 - x_5x_2x_1 - x_4x_1 - x_3x_2 + x_2x_1 \\
p_6 &= x_6x_5x_2 + x_6x_5x_1 - x_5x_2x_1 - x_4x_1 - x_3x_2 + x_2x_1
\end{aligned}$$

### 1.3 Triangulation, step 3

**Choosing variable:** Trying the variable with index 4.

**Variable  $x_4$  selected:** The number of polynomials with this variable, with indexes from 1 to 4, is 2.

**Minimal degrees:** 2 polynomial(s) with degree 1.

**Polynomial with linear degree:** Removing variable  $x_4$  from all other polynomials by reducing them with polynomial  $p_3$  from previous step.

Finished a triangulation step, the current system is:

$$\begin{aligned}
p_1 &= 2x_1 - \\
p_2 &= 2x_2 - \\
p_3 &= 0 \\
p_4 &= -x_4x_1 - x_3x_2 + x_2x_1 \\
p_5 &= x_7x_5x_2 + x_7x_5x_1 - x_5x_2x_1 - x_4x_1 - x_3x_2 + x_2x_1 \\
p_6 &= x_6x_5x_2 + x_6x_5x_1 - x_5x_2x_1 - x_4x_1 - x_3x_2 + x_2x_1
\end{aligned}$$

### 1.4 Triangulation, step 4

**Choosing variable:** Trying the variable with index 3.

**Error:** Variable with index 3 not found in polynomial system.

## 2 Prover results

**Status:** Proving failed - general error occurred.