# OpenGeoProver Output for conjecture "geothm\_zadatak"

Wu's method used

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# 1 Invoking the theorem prover

The used proving method is Wu's method. The input system is:

 $p_1 = x_1 - p_2 = x_2 + 1$   $p_3 = x_3 - p_4 = x_4$   $p_5 = x_5 - p_6 = x_6 + x_3$ 

#### 1.1 Triangulation, step 1

Choosing variable: Trying the variable with index 6.

Variable  $x_6$  selected: The number of polynomials with this variable, with indexes from 1 to 6, is 1.

Single polynomial with chosen variable: Chosen polynomial is  $p_6$ . No reduction needed.

The triangular system has not been changed.

#### 1.2 Triangulation, step 2

Choosing variable: Trying the variable with index 5.

**Variable**  $x_5$  **selected:** The number of polynomials with this variable, with indexes from 1 to 5, is 1.

Single polynomial with chosen variable: Chosen polynomial is  $p_5$ . No reduction needed.

The triangular system has not been changed.

#### 1.3 Triangulation, step 3

Choosing variable: Trying the variable with index 4.

Variable  $x_4$  selected: The number of polynomials with this variable, with indexes from 1 to 4, is 1.

Single polynomial with chosen variable: Chosen polynomial is  $p_4$ . No reduction needed.

The triangular system has not been changed.

#### 1.4 Triangulation, step 4

Choosing variable: Trying the variable with index 3.

Variable  $x_3$  selected: The number of polynomials with this variable, with indexes from 1 to 3, is 1.

Single polynomial with chosen variable: Chosen polynomial is  $p_3$ . No reduction needed.

The triangular system has not been changed.

#### 1.5 Triangulation, step 5

Choosing variable: Trying the variable with index 2.

Variable  $x_2$  selected: The number of polynomials with this variable, with indexes from 1 to 2, is 1.

Single polynomial with chosen variable: Chosen polynomial is  $p_2$ . No reduction needed.

The triangular system has not been changed.

#### 1.6 Triangulation, step 6

Choosing variable: Trying the variable with index 1.

Variable  $x_1$  selected: The number of polynomials with this variable, with indexes from 1 to 1, is 1.

Single polynomial with chosen variable: Chosen polynomial is  $p_1$ . No reduction needed.

The triangular system has not been changed.

The triangular system is:

 $\begin{array}{rcl} p_1 & = & x_1 - \\ p_2 & = & x_2 + 1 \\ p_3 & = & x_3 - \\ p_4 & = & x_4 \\ p_5 & = & x_5 - \end{array}$ 

 $p_6 = x_6 + x_3$ 

## 2 Final Remainder

## 2.1 Final remainder for conjecture geothm\_zadatak

Calculating final remainder of the conclusion:

$$g = x_5 x_2 + x_3 x_1$$

with respect to the triangular system.

1. Pseudo remainder with  $p_6$  over variable  $x_6$ :

$$g = x_5 x_2 + x_3 x_1$$

2. Pseudo remainder with  $p_5$  over variable  $x_5$ :

$$g = x_3x_1 + x_2$$

3. Pseudo remainder with  $p_4$  over variable  $x_4$ :

$$g = x_3x_1 + x_2$$

4. Pseudo remainder with  $p_3$  over variable  $x_3$ :

$$g = x_2 + x_1$$

5. Pseudo remainder with  $p_2$  over variable  $x_2$ :

$$g = x_1 -$$

6. Pseudo remainder with  $p_1$  over variable  $x_1$ :

$$g = 0$$

# 3 Prover results

Status: Theorem has been proved.

Space Complexity: The biggest polynomial obtained during prover execution

contains 2 terms.

**Time Complexity:** Time spent by the prover is 0.031 seconds.

# 4 NDG Conditions

## NDG Conditions in readable form

• There are no NDG conditions for this theorem