Introduction to Data Science (IDS) course

## Data Quality & Preprocessing

Lecture 17 Instruction – without solutions (Lisa Mannel)

# IDS-I-L17





## **Outliers & Missing Values**

## Outlier detection techniques based on previous lectures:

- Boxplots (Lecture 2)
- Decision Trees (Lecture 3)
- Regression (Lecture 4)
- SVMs (Lecture 5)
- Clustering (Lecture 9)



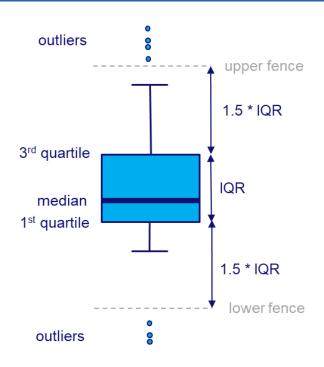
## **Outliers & Missing Values**

We can handle outliers/missing values in several ways, depending on our needs, e.g.:

- Ignore the feature or instance
- Fill in the correct value (domain knowledge)
- Fill in a value based on other data
  - Mean, median, min, max, most frequent... (possibly focus on similar data)
  - Prediction model (regression, SVM, decision tree, NN, ...)



## **Outliers & Missing Values - Boxplots**



Instances outside the fences can be considered outliers.

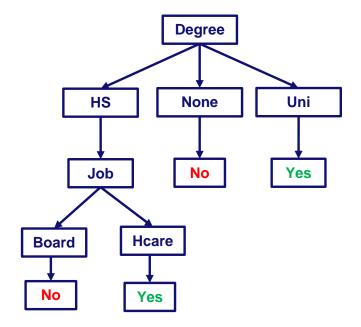
See Instruction 3 for exercises.



### **Outliers & Missing Values – Decision trees**

|    | Experience | Degree | Job   | Class |  |
|----|------------|--------|-------|-------|--|
| 1  | Exp >10    | HS     | Board | No    |  |
| 2  | 5< Exp <10 | Uni    | Board | Yes   |  |
| 3  | Exp >10    | HS     | Board | No    |  |
| 4  | 5< Exp <10 | HS     | Hcare | Yes   |  |
| 5  | Exp < 5    | HS     | Hcare | Yes   |  |
| 6  | Exp < 5    | HS     | Board | No    |  |
| 7  | Exp < 5    | None   | Edu   | No    |  |
| 8  | Exp >10    | None   | Hcare | No    |  |
| 9  | Exp < 5    | Uni    | Edu   | Yes   |  |
| 10 | Exp >10    | Uni    | Board | Yes   |  |
| 11 | Exp >10    | HS     | Board | Yes   |  |
|    |            |        |       |       |  |

Consider the following data about accepting or rejecting job applications based on "Experience", "Degree", and "Job", as well as the corresponding decision tree (extension of Instruction 3).





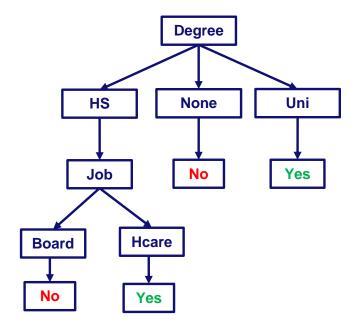
### **Outliers & Missing Values – Decision trees**

|    | Experience | Degree | Job   | Class |
|----|------------|--------|-------|-------|
| 1  | Exp >10    | HS     | Board | No    |
| 2  | 5< Exp <10 | Uni    | Board | Yes   |
| 3  | Exp >10    | HS     | Board | No    |
| 4  | 5< Exp <10 | HS     | Hcare | Yes   |
| 5  | Exp < 5    | HS     | Hcare | Yes   |
| 6  | Exp < 5    | HS     | Board | No    |
| 7  | Exp < 5    | None   | Edu   | No    |
| 8  | Exp >10    | None   | Hcare | No    |
| 9  | Exp < 5    | Uni    | Edu   | Yes   |
| 10 | Exp >10    | Uni    | Board | Yes   |
| 11 | Exp >10    | HS     | Board | Yes   |

#### **Exercise 1**

Consider the given the data table and corresponding decision tree.

- a) Which instances can be identified as outliers based on the given decision tree?
- b) Using the decision tree as predictive model to replace the outliers target features values, what would be the resulting data table?





## **Outliers & Missing Values – Regression**

| Age<br>[months] | Weight<br>[kg] | Size<br>[cm] |
|-----------------|----------------|--------------|
| 0               | 2.5            | 46.4         |
| 0               | 3.8            | 52.9         |
| 1               | 3.2            | 50.4         |
| 3               | 6.7            | 63.4         |
| 9               | 7.5            | 68           |
| 9               | 10.2           | 75           |
| 12              | 8.4            | 71.7         |
| 12              | 11.2           | 79.1         |
| 18              | 9.6            | 77.5         |
| 18              | 12.8           | 86.1         |
| 24              | 10.5           | 82.3         |
| 24              | 14.1           | 92           |

#### **Exercise 2**

Consider the given baby data and corresponding regression function  $\mathbb{M}_{\mathbf{w}}(d)$ , predicting Age based on Weight and Size.

- a) For an error threshold of 3, (using the absolute error), which data points will be identified as outliers?
- Use the regression function to replace the outliers target feature values by the predicted values.

$$\mathbb{M}_{\mathbf{w}}(d) = -8.4 + 1 \times \text{WEIGHT} + 0.12 \times \text{SIZE}$$



#### **Outlier Detection - SVMs**

| Class       | Age      | Weight |
|-------------|----------|--------|
| Class       | [months] | [kg]   |
| underweight | 0        | 2.5    |
| overweight  | 0        | 4.2    |
| underweight | 0        | 2.4    |
| overweight  | 0        | 3.8    |
| underweight | 1        | 3.2    |
| overweight  | 1        | 5.4    |
| underweight | 1        | 3      |
| overweight  | 1        | 4.9    |
| underweight | 3        | 4.4    |
| overweight  | 3        | 7.4    |
| underweight | 3        | 4.2    |
| overweight  | 3        | 6.7    |
| underweight | 6        | 6.2    |
| overweight  | 6        | 9.5    |
| underweight | 6        | 5.8    |
| overweight  | 6        | 8.7    |
|             |          |        |

#### **Exercise 3**

Consider the given data table and corresponding separating hyperplane.

- a) Based on this hyperplane, which instances can be considered outliers?
- b) Replace the outliers target feature values by the values predicted by the SVM.

$$0 = 0.4 \cdot AGE - WEIGHT + 4.0$$
  
 $\Leftrightarrow (w_1, w_2) = (-1.0, 0.4), b = 4.0$ 



## **Outlier Detection - Clustering**

| Class       | Age<br>[months] | Weight [kg] |
|-------------|-----------------|-------------|
| underweight | 0               | 2.5         |
| overweight  | 0               | 4.2         |
| underweight | 0               | 2.4         |
| overweight  | 0               | 2.7         |
| underweight | 1               | 3.2         |
| overweight  | 1               | 5.4         |
| underweight | 1               | 3           |
| overweight  | 1               | 4.9         |
| underweight | 3               | 4.4         |
| overweight  | 3               | 7.4         |
| underweight | 3               | 4.2         |
| overweight  | 3               | 6.7         |
| underweight | 6               | 6.2         |
| overweight  | 6               | 9.5         |
| underweight | 6               | 5.8         |
| overweight  | 6               | 8.7         |
|             |                 |             |

#### **Exercise 4**

Consider the given data clustered into the blue, red, yellow and purple clusters. Which instances can be considered outliers?



#### **Transformation**

Getting the right data type, e.g.

- One-hot encoding: categorical to numerical
- Binning: numerical to categorical (ordinal)

**Known from earlier lectures!** 



## **Transformation - Binning**

#### **Introduced in Lecture 2!**

#### Many details can vary in real applications:

- What to do, if there is not enough data to 'fill the last bin'?
- What to do, if the data is not dividable into bins according to requested parameters?
- Do we define interval limits closed or open ?

•



## **Transformation - Binning**

Weight [kg] 2.5 3.8 3.2 4.9 4.4 6.7 6.2 7.5 8.4 9.6 12.8 10.5 14.1

#### **Exercise 5**

Apply equal-width binning to the given data. Your lowest bin interval should have 0 as open lower limit, and your highest interval should have 16 as closed upper limit.

- Give a mapping of the data to two bins. Indicate the interval limits as well as the bins boundary values.
- 2) Give a mapping of the data to four bins. Indicate the interval limits as well as the bins boundary values.



## **Transformation - Binning**

Weight [kg] 2.5 3.2 3.8 4.4 4.9 6.2 6.7 7.5 8.4 10.5

(sorted)

12.8 14.1

#### **Exercise 6**

Apply equal-frequency binning to the given data.

- Give a mapping of the data to two bins. Indicate the interval limits as well as the bins boundary values.
- 2) Give a mapping of the data such that the bin size is four. Indicate the interval limits as well as the bins boundary values.



#### **Normalization**

Adjusting the influence of features.

#### Introduced in the lecture:

- Min-Max Normalization
- Standard Score Normalization
- Decimal Scaling



#### **Normalization – Min-Max**

| Age<br>[months] | Weight [kg] | Size<br>[cm] |
|-----------------|-------------|--------------|
| 0               | 2.5         | 46.4         |
| 0               | 3.8         | 52.9         |
| 1               | 3.2         | 50.4         |
| 1               | 4.9         | 56.9         |
| 3               | 4.4         | 56.7         |
| 3               | 6.7         | 63.4         |
| 6               | 6.2         | 63.4         |
| 6               | 8.7         | 70.2         |
| 9               | 7.5         | 68           |
| 9               | 10.2        | 75           |
| 12              | 8.4         | 71.7         |
| 12              | 11.2        | 79.1         |
| 18              | 9.6         | 77.5         |
| 18              | 12.8        | 86.1         |
| 24              | 10.5        | 82.3         |
| 24              | 14.1        | 92           |

#### **Exercise 7**

Apply Min-Max Normalization for each feature of the given data with a target interval of [1,10].



### Normalization – Standard Score

| Age<br>[months] | Weight [kg] | Size<br>[cm] |
|-----------------|-------------|--------------|
| 0               | 2.5         | 46.4         |
| 0               | 3.8         | 52.9         |
| 1               | 3.2         | 50.4         |
| 1               | 4.9         | 56.9         |
| 3               | 4.4         | 56.7         |
| 3               | 6.7         | 63.4         |
| 6               | 6.2         | 63.4         |
| 6               | 8.7         | 70.2         |
| 9               | 7.5         | 68           |
| 9               | 10.2        | 75           |
| 12              | 8.4         | 71.7         |
| 12              | 11.2        | 79.1         |
| 18              | 9.6         | 77.5         |
| 18              | 12.8        | 86.1         |
| 24              | 10.5        | 82.3         |
| 24              | 14.1        | 92           |

#### **Exercise 8**

Scale each feature of the given data points using Standard Score Normalization.



## Normalization – Decimal Scaling

| Age      | Weight | Size |
|----------|--------|------|
| [months] | [kg]   | [cm] |
| 0        | 2.5    | 46.4 |
| 0        | 3.8    | 52.9 |
| 1        | 3.2    | 50.4 |
| 1        | 4.9    | 56.9 |
| 3        | 4.4    | 56.7 |
| 3        | 6.7    | 63.4 |
| 6        | 6.2    | 63.4 |
| 6        | 8.7    | 70.2 |
| 9        | 7.5    | 68   |
| 9        | 10.2   | 75   |
| 12       | 8.4    | 71.7 |
| 12       | 11.2   | 79.1 |
| 18       | 9.6    | 77.5 |
| 18       | 12.8   | 86.1 |
| 24       | 10.5   | 82.3 |
| 30       | 17.1   | 102  |

#### **Exercise 9**

Scale each feature of the given data points using Decimal Scaling.



#### Reduction

Making the data smaller for analysis, but produce the same or similar analysis results.

- Two types of reduction:
  - Feature reduction (keep all the rows, but reduce the number of columns in dataset)
  - Instance reduction (store summary, remove or reduce the number of rows)



## **Reduction - Aggregation**

| Weight<br>[kg] | Age<br>[months] | Class       |
|----------------|-----------------|-------------|
|                |                 |             |
| 2.5            | 0               | underweight |
| 4.2            | 0               | overweight  |
| 2.4            | 0               | underweight |
| 2.7            | 0               | overweight  |
| 3.2            | 1               | underweight |
| 5.4            | 1               | overweight  |
| 3              | 1               | underweight |
| 4.9            | 1               | overweight  |
| 4.4            | 3               | underweight |
| 7.4            | 3               | overweight  |
| 4.2            | 3               | underweight |
| 6.7            | 3               | overweight  |
| 6.2            | 6               | underweight |
| 9.5            | 6               | overweight  |
| 5.8            | 6               | underweight |
| 8.7            | 6               | overweight  |

#### **Exercise 10**

Consider the data table on the left. Reduce the data by dropping features and applying aggregation to

- Show the minimum weight of overweight babies, for each age class.
- b) For each age class, show the average weight.
- c) For age class, show the summarized weight of all underweight babies and of all overweight babies.

