

Задача 4

Для языка $L = \{\varepsilon, 110, 111, 011, 11\}$ определена подстановка $\sigma(0) = \{1, 11\}$; $\sigma(1) = \{\varepsilon, 0\}$.
Вычислить $\sigma(L)$.

$$\sigma(\varepsilon) = \varepsilon$$

$$\sigma(110) = \sigma(1)\sigma(1)\sigma(0) = \{\varepsilon, 0\}\{\varepsilon, 0\}\{1, 11\} = \{1, 11, 01, 011, 001, 0011\}$$

$$\sigma(111) = \sigma(1)\sigma(1)\sigma(1) = \{\varepsilon, 0\}\{\varepsilon, 0\}\{\varepsilon, 0\} = \{0, 00, 000\}$$

$$\sigma(011) = \sigma(0)\sigma(1)\sigma(1) = \{1, 11\}\{\varepsilon, 0\}\{\varepsilon, 0\} = \{10, 1, 100, 11, 110, 1100\}$$

$$\sigma(11) = \sigma(1)\sigma(1) = \{\varepsilon, 0\}\{\varepsilon, 0\} = \{0, 00\}$$

$$\sigma(L) = \{1, 11, 01, 011, 001, 0011, 0, 00, 000, 10, 100, 110, 1100\}$$

Задача 5 Для языков $L_1 = \{01, 11, 12\}$ и $L_2 = \{120, 011, 112\}$ найти языки:

$$L_1^4/L_2 = \{01010, 01011, 01110, 01111, 01120, 01121, 11010, 11011, 11110, 11111, 11120, 11121, 12010, 12011, 12110, 12111, 12120, 12121\}$$

$$L_2 \setminus L_1^3 = \{011101, 101, 011111, 111, 011112, 112, 011201, 201, 011211, 211, 011212, 212, 120101, 120111, 120112\}$$

$$L_1^R \setminus L_2^2 = \{112120, 2120, 112011, 2011, 11211, 2112\}$$

$$L_2^2/L_1 = \{1200, 0110, 1120, 1201, 0111, 1121\}$$

$$\{1\} \setminus ((L_1 + L_2)^2 / \{12\}) = \{1\} \setminus (\{01, 11, 12, 120, 011, 112\}^2 / \{12\}) = \{1\} \setminus \{01, 11, 12, 120, 011, 112, 111, 121, 1201, 0111, 1121\} = \{1, 2, 20, 12, 11, 21, 201, 121\}$$