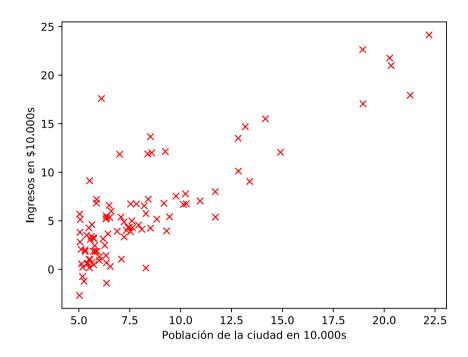
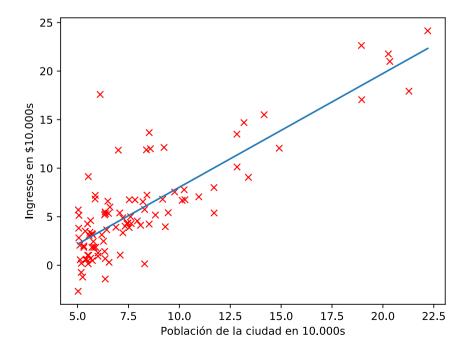
### Práctica 0: vectorización

solución vectorizada

```
def integra_mc_vec(fun, a, b, num_puntos=100):
    """Calcula la integral de f entre a y b por el método de
    Monte Carlo sin usar bucles
    eje_x = np.linspace(a, b, num_puntos)
    eje_y = fun(eje_x)
    max_f = max(eje_y)
    min_f = 0
    random_x = np.random.uniform(a, b, num_puntos)
    random_y = np.random.uniform(min_f, max_f, num_puntos)
    f_random_x = fun(random_x)
    plt.figure()
    plt.plot(random_x, random_y, 'x', c='red')
    plt.plot(eje_x, eje_y, '-')
    plt.savefig('mc.pdf')
    plt.close()
    debajo = sum(random_y < f_random_x)</pre>
    area_total = abs(b - a) * abs(max_f - min_f)
    return area_total * (debajo / num_puntos)
```



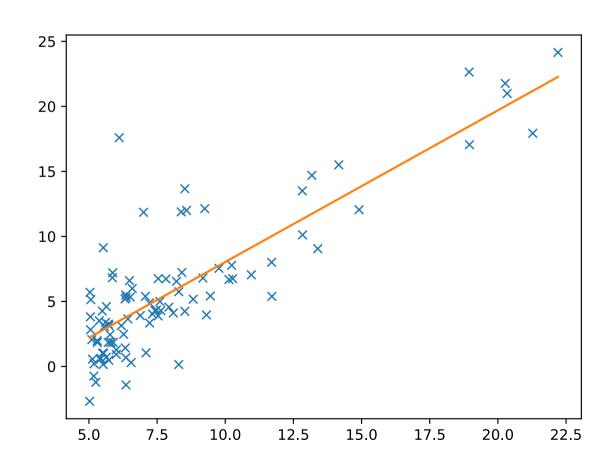


```
import numpy as np
from pandas.io.parsers import read_csv
def carga_csv(file_name):
    """carga el fichero csv especificado y lo
       devuelve en un array de numpy
    11 11 11
    valores = read_csv(file_name, header=None).to_numpy()
    # suponemos que siempre trabajaremos con float
    return valores.astype(float)
            array([[ 6.1101 , 17.592 ],
                   [ 5.5277 , 9.1302 ],
                   [ 8.5186 , 13.662 ],
                   [ 7.0032 , 11.854 ],
                   [ 5.3054 , 1.9869 ],
                   [ 8.2934 , 0.14454],
                   [13.394 , 9.0551],
                   [ 5.4369 , 0.61705]])
```

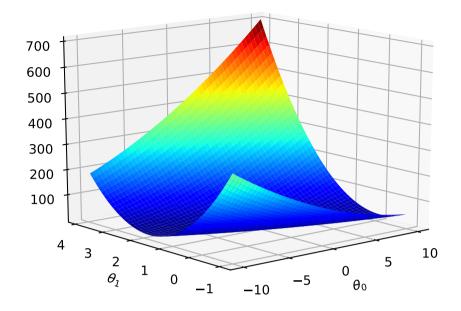
solución de la primera parte

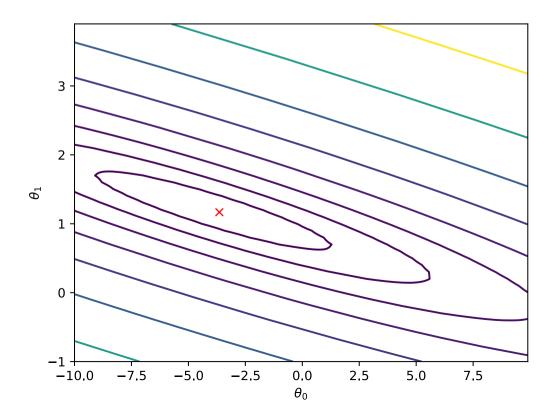
```
repeat until convergence {
                                                                  update
  \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m \left( h_\theta(x^{(i)}) - y^{(i)} \right) \qquad \text{update} \\ \theta_0 \text{ and } \theta_1 \\ \theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m \left( h_\theta(x^{(i)}) - y^{(i)} \right) \cdot x^{(i)} \qquad \text{simultaneously}
                                                  array([[ 6.1101 , 17.592 ],
                                                            [ 5.5277 , 9.1302 ],
   datos = carga_csv('ex1data1.csv')
                                                            [ 8.5186 , 13.662 ],
   X = datos[:, 0]
                                                            [ 7.0032 , 11.854 ],
   Y = datos[:, 1]
   m = len(X)
                                                            [ 5.3054 , 1.9869 ],
   alpha = 0.01
                                                            [ 8.2934 , 0.14454],
   theta_0 = theta_1 = 0
                                                            [13.394 , 9.0551],
   for _ in range(1500):
                                                            [ 5.4369 , 0.61705]])
        sum_0 = sum_1 = 0
        for i in range(m):
              sum_0 += (theta_0 + theta_1 * X[i]) - Y[i]
              sum_1 += ((theta_0 + theta_1 * X[i]) - Y[i]) * X[i]
        theta_0 = theta_0 - (alpha / m) * sum_0
        theta_1 = theta_1 - (alpha / m) * sum_1
```

```
plt.plot(X, Y, "x")
min_x = min(X)
max_x = max(X)
min_y = theta_0 + theta_1 * min_x
max_y = theta_0 + theta_1 * max_x
plt.plot([min_x, max_x], [min_y, max_y])
plt.savefig("resultado.pdf")
```



gráficas en 3D





```
import numpy as np
In [3]: x = np.array([1,2,3])
In [4]: y = np.array([4,5,6])
In [5]: xx, yy = np.meshgrid(x,y)
In [6]: xx
Out[6]:
array([[1, 2, 3],
      [1, 2, 3],
       [1, 2, 3]]
In [7]: yy
Out[7]:
array([[4, 4, 4],
      [5, 5, 5],
       [6, 6, 6]
```

```
from mpl toolkits.mplot3d import Axes3D
import matplotlib.pvplot as plt
from matplotlib import cm
from matplotlib.ticker import LinearLocator, FormatStrFormatter
import numpy as np
fig = plt.figure()
ax = fig.gca(projection='3d') # ax = Axes3D(fig)
# Make data.
X = np.arange(-5, 5, 0.25)
Y = np.arange(-5, 5, 0.25)
X, Y = np.meshgrid(X, Y)
R = np.sqrt(X**2 + Y**2)
                                                                <sup>-4</sup> <sub>-2</sub> <sub>0</sub>
Z = np.sin(R)
# Plot the surface.
surf = ax.plot_surface(X, Y, Z, cmap=cm.coolwarm,
                        linewidth=0, antialiased=False)
# Customize the z axis.
ax.set_zlim(-1.01, 1.01)
ax.zaxis.set_major_locator(LinearLocator(10))
ax.zaxis.set major formatter(FormatStrFormatter('%.02f'))
# Add a color bar which maps values to colors.
fig.colorbar(surf, shrink=0.5, aspect=5)
plt.show()
```

1.01

0.79

0.56

0.11

-0.11

-0.34

-0.56

-0.79

-1.01

0.75

0.50

0.25

0.00

-0.25

-0.50

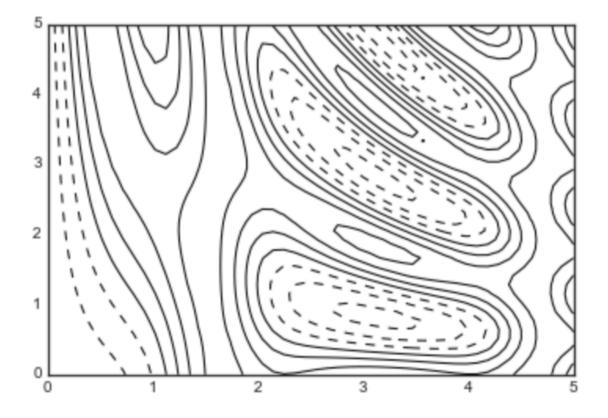
-0.75

```
def f(x, y):
    return np.sin(x) ** 10 + np.cos(10 + y * x) * np.cos(x)
```

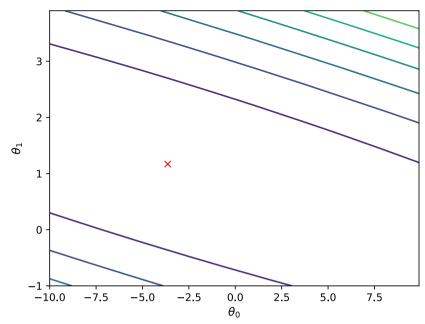
```
x = np.linspace(0, 5, 50)
y = np.linspace(0, 5, 40)

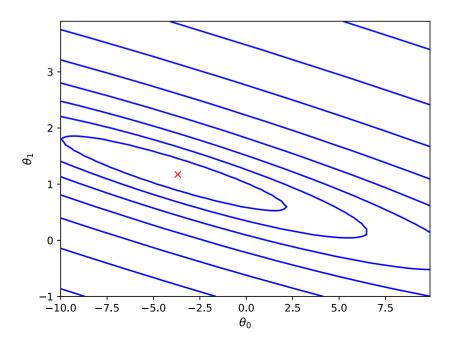
X, Y = np.meshgrid(x, y)
Z = f(X, Y)
```

```
plt.contour(X, Y, Z, colors='black');
```



plt.contour(Theta0, Theta1, Coste)





```
def make_data(t0_range, t1_range, X, Y):
    """Genera las matrices X,Y,Z para generar un plot en 3D
    ** ** **
    step = 0.1
    Theta0 = np.arange(t0_range[0], t0_range[1], step)
    Theta1 = np.arange(t1_range[\emptyset], t1_range[1], step)
    Theta0, Theta1 = np.meshgrid(Theta0, Theta1)
    # Theta0 y Theta1 tienen las misma dimensiones, de forma que
    # cogiendo un elemento de cada uno se generan las coordenadas x,y
    # de todos los puntos de la rejilla
    Coste = np.empty_like(Theta0)
    for ix, iy in np.ndindex(Theta0.shape):
        Coste[ix, iy] = coste(X, Y, [Theta0[ix, iy], Theta1[ix, iy]])
    return [Theta0, Theta1, Coste]
```

solución vectorizada

#### Gradient descent algorithm

```
repeat until convergence {
    \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m \left( h_\theta(x^{(i)}) - y^{(i)} \right) \qquad \text{update} \\ \theta_0 \text{ and } \theta_1 \\ \theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m \left( h_\theta(x^{(i)}) - y^{(i)} \right) \cdot x^{(i)} \qquad \text{simultaneously}
Repeat {
       \theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \dots, \theta_n)
                                                   (simultaneously update for every j = 0, \dots, n)
      \theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}
                                                                                                  h_{\theta}(x) = \theta^T x
             h_{\theta}(x) = \theta_0 + \theta_1 x
```

```
datos = carga_csv('ex1data1.csv')
X = datos[:, :-1]
np.shape(X) # (97, 1)
Y = datos[:, -1]
np.shape(Y) # (97,)
m = np.shape(X)[0]
n = np.shape(X)[1]
# añadimos una columna de 1's a la X
X = np.hstack([np.ones([m, 1]), X])
alpha = 0.01
Thetas, costes = descenso_gradiente(X, Y, alpha)
```

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} \left( h_{\theta}(x^{(i)}) - y^{(i)} \right)^{2}$$

$$X heta = \left[ egin{array}{c} (x^{(1)})^T heta \ (x^{(2)})^T heta \ dots \ (x^{(m)})^T heta \end{array} 
ight] = \left[ egin{array}{c} heta^T(x^{(1)}) \ heta^T(x^{(2)}) \ dots \ heta^T(x^{(m)}) \end{array} 
ight]$$

$$J(\theta) = \frac{1}{2m} (X\theta - \vec{y})^T (X\theta - \vec{y})$$

$$J(\theta) = \frac{1}{2m} (X\theta - \vec{y})^T (X\theta - \vec{y})$$

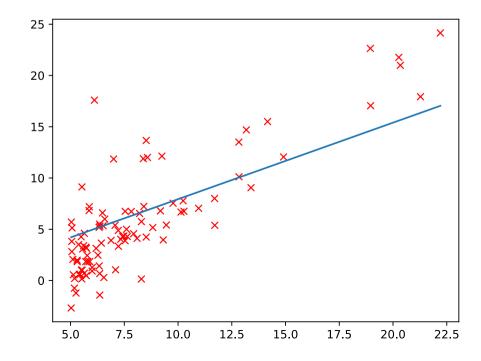
```
def coste(X, Y, Theta):
    H = np.dot(X, Theta)
    Aux = (H - Y) ** 2
    return Aux.sum() / (2 * len(X))
```

$$\frac{\partial J(\theta)}{\partial \theta_j} = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

$$\begin{bmatrix} \frac{\partial J(\theta)}{\partial \theta_{0}} \\ \frac{\partial J(\theta)}{\partial \theta_{1}} \\ \vdots \\ \frac{\partial J(\theta)}{\partial \theta_{n}} \end{bmatrix} = \frac{1}{m} \begin{bmatrix} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_{0}^{(i)} \\ \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_{1}^{(i)} \\ \vdots \\ \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_{n}^{(i)} \end{bmatrix} \quad h_{\theta}(x) - y = \begin{bmatrix} h_{\theta}(x^{(1)}) - y^{(1)} \\ h_{\theta}(x^{(2)}) - y^{(2)} \\ \vdots \\ h_{\theta}(x^{(m)}) - y^{(m)} \end{bmatrix} \\ = \frac{1}{m} \sum_{i=1}^{m} \left( (h_{\theta}(x^{(i)}) - y^{(i)}) x^{(i)} \right) \\ = \frac{1}{m} X^{T} (h_{\theta}(x) - y)$$

$$\frac{\delta J(\theta)}{\delta \theta_i} = \frac{1}{m} X^T (h_{\theta}(x) - y)$$

```
def gradiente(X, Y, Theta, alpha):
    NuevaTheta = Theta
    m = np.shape(X)[0]
    n = np.shape(X)[1]
    H = np.dot(X, Theta)
    Aux = (H - Y)
    for i in range(n):
        Aux_i = Aux * X[:, i]
        NuevaTheta -= (alpha / m) * Aux_i.sum()
    return NuevaTheta
```



```
def gradiente(X, Y, Theta, alpha):
    NuevaTheta = Theta
    m = np.shape(X)[0]
    n = np.shape(X)[1]
    H = np.dot(X, Theta)
    Aux = (H - Y)
    for i in range(n):
        Aux_i = Aux * X[:, i]
        NuevaTheta[i] -= (alpha / m) * Aux_i.sum()
    return NuevaTheta
```

