# Supplementary Materials for "The Effect of Legislature Size on Public Spending: A Meta-Analysis"

Huzeyfe Alptekin\* Danilo Freire<sup>†</sup> Umberto Mignozzetti<sup>‡</sup> Catarina Roman<sup>§</sup>

17 March 2021

## **Contents**

A	Sear	ch Criteria	3
В	Arti	cle Selection	3
	B.1	Exclusion Analysis	4
	B.2	Flow Chart	4
С	Met	a-Analysis Dataset	5
D	Des	criptive Statistics	5
	D.1	Study Year	6
	D.2	Frequency of Published Papers	6
	D.3	Electoral System	7
	D.4	Dependent Variables	7
	D.5	Independent Variables	8
	D.6	Histogram of the Coefficients and the Standard Errors	8
	D.7	Sign Coefficients	9
E	Desc	criptive Statistics of Moderators	.0
F	Bino	omial Tests for Coefficient Signs	.1

<sup>\*</sup>Research Associate, Contemporary Brazilian History Research and Documentation Center, School of Social Sciences, Fundação Getulio Vargas, huzeyfealptekin@gmail.com.

<sup>†</sup>Independent Researcher, danilofreire@gmail.com, https://danilofreire.github.io.

<sup>&</sup>lt;sup>‡</sup>Visiting Assistant Professor, Quantitative Theory and Methods Department, Emory University, umberto.mignozzetti@emory.edu, http://umbertomig.com.

<sup>§</sup>Research Associate, School of International Relations, Fundação Getulio Vargas, catarinamroman@gmail.com, http://catarinaroman.github.io.

G	Meta	a-Analysis	12
	G.1	Estimation Method	12
	G.2	Lower House Size and Expenditure per Capita	14
	G.3	Log Lower House Size and Expenditure per Capita	17
	G.4	Upper House Size and Expenditure per Capita	17
	G.5	Lower House Size and Log Expenditure Per Capita	19
	G.6	Log of Lower House Size and Log of Expenditure Per Capita	21
	G.7	Upper House Size and Log of Expenditure Per Capita	23
	G.8	Lower House Size and Expenditure as Percentage of GDP	23
	G.9	Log Lower House Size and Expenditure as Percentage of GDP	24
	G.10	Upper House Size and Expenditure as Percentage of GDP	26
	G.11	Lower House Size and Expenditure per Capita (IV)	28
	G.12	Lower House Size and Log of Expenditure per Capita (RDD)	30
Н	Meta	a-Analysis (All Coefficients)	32
	H.1	Lower House Size and Expenditure Per Capita	32
	H.2	Log of Lower House Size and Expenditure Per Capita	37
	H.3	Upper House Size and Expenditure Per Capita	37
	H.4	Lower House Size and Log of Expenditure Per Capita	39
	H.5	Log of Lower House Size and Log of Expenditure Per Capita	41
	H.6	Upper House Size and Log of Expenditure Per Capita	43
	H.7	Lower House Size and Expenditure as Percentage of GDP	43
	H.8	Log of Lower House Size and Expenditure as Percentage of GDP	45
	H.9	Upper House Size and Expenditure as Percentage of GDP	47
	H.10	Lower House Size and Expenditure per Capita (IV)	49
	H.11	Lower House Size and Log of Expenditure per Capita (RDD)	50
I	Meta	a-Regressions	52
	I.1	Meta-Regressions for Expenditure Per Capita	52
	I.2	Meta-Regressions for Log of Expenditure Per Capita	54
	I.3	Meta-Regressions for Expenditure as a Percentage of the GDP	56
J	Rob	ustness: Meta-Regressions (All Coefficients)	58
K	Sess	ion Information	60

### A Search Criteria

The first step in our systematic review consisted in gathering a study sample. We started our data collection with a manual search based on a set of keywords we scouted from the distributive politics literature. This search produced a database with many entries that were unrelated to our subject of investigation. To reduce the number of false positives in our sample, we restricted our search to studies that cited Weingast, Shepsle and Johnsen's 1981 paper "*The Political Economy of Benefits and Costs: A Neoclassical Approach to Distributive Politics*", which is a seminal contribution to the field. Although Google Scholar reports the article has received 2,180 citations, our search resulted in 2,664 records on the 21<sup>st</sup> of November 2019.

We webscraped three large academic databases: Google Scholar (n = 1001); Microsoft Academic (n = 927); and Scopus (n = 736). The R script we wrote extracted the article title, abstract, authors, year, journal of publication, and database from which the record originated. Our code is available in section ?? below. We screened these results with an English language and article restriction, that is, we excluded all records written in other languages and all that were not academic papers, such as book chapters or doctoral theses. We set no restriction to unpublished articles. XXXX CATARINA AND HUZEYFE: FIX THIS

#### **B** Article Selection

The selection process was conducted by two authors in three phases. In the first round, we excluded all titles that were clearly unrelated to our topic of interest. For instance, we curiously found articles about car motors amidst our sample. We consider this a preliminary step, since we were not able to eliminate a large number of entries. Then, we read all abstracts. We chose to maintain those which indicated that either government expenditure or legislative structures were the main subject of the paper. For instance, if the paper sought to identify variables that increased government size, it was maintained. Abstracts that indicated the paper discussed or estimated the impacts of representative institutions, elections, or chamber dynamics were also included. This allowed us to significantly reduce our sample to 376 records.

In the second phase, we assessed full texts. To remain in our sample, the paper should (i) conduct a quantitative analysis, (ii) report data on the number of legislators, and (iii) also include data on public expenditure. If the publication had all three, it was maintained. Disagreements in this phase were discussed among the authors, and a third investigator was consulted when needed.

The third phase consisted of filling out tables for each of the remaining 47 articles to systematically evaluate their eligibility. Since authors use different measures for government spending and the number of lower/upper house members, we extracted all coefficients that provided this information. We decided which variables to keep by following the current practices of the literature. In this phase, we also collected information on

whether or not the paper had been published, and if it explicitly discussed the *law of 1/n*. Upon choosing the variables, we excluded the non-conforming studies, arriving at our final sample of 31 articles.

**B.1** Exclusion Analysis

We selected the final pool of articles based on two criteria regarding their reported coefficients:

1. Matched treatment variable:

• *N*: Number Legislators in the Lower House

• *logN*: Log Number Legislators in the Lower House

• *K*: Number Legislators in the Upper House

2. Matched outcome variable:

• ExpPC: Expenditure Per Capita

• logExpPC: Log Expenditure Per Capita

• PCTGDP: Percent GDP Public Expenditure

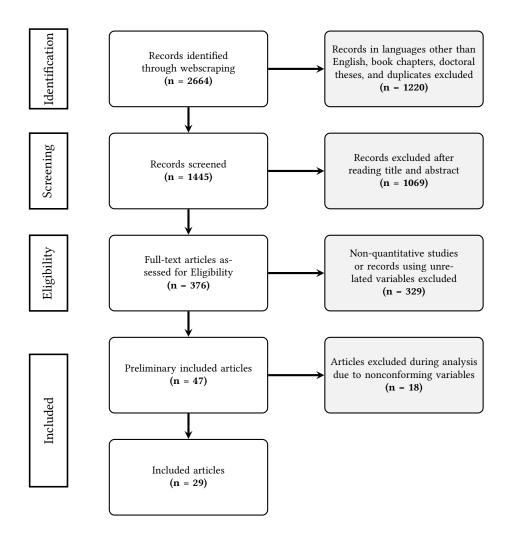
If a paper did not use a combination of these variables, we excluded it from the meta-analysis.

**B.2** Flow Chart

The diagram below shows each step of our article selection process. We followed the Preferred Reporting Items for Systematic Reviews and Meta-Analyses (PRISMA) statement to conduct our study<sup>1</sup>. The column to the right depicts the amount of articles excluded in each phase, and the one to the left shows the number of records evaluated.

 $^1\mathrm{More}$  information about the PRISMA statement is available at http://www.prisma-statement.org.

4



## C Meta-Analysis Dataset

Our data are comprised of two datasets. The first dataset has the main coefficients reported in the studies. These data include only the most rigorous model from each paper, that is, those estimated with the largest sample size, most control variables, and fixed effects if the authors added them. If the article employed a regression discontinuity design, we chose the coefficient from the optimal bandwidth or from the intermediate one. This sample encompasses 44 estimates, as 13 articles analysed two dependent or independent variables of interest. Our second sample, in contrast, contains all the 148 effect sizes reported in the 31 papers.

In the main text, we focus on the results for our restricted sample as we consider them more robust, but the findings are very similar when we use the extended dataset. Here we present the results of all tests performed in both reduced and full samples.

# **D** Descriptive Statistics

In this section, we show the descriptive statistics for our sample. We focus on the following paper characteristics: study year, whether the paper has been published or not, the electoral system of the country discussed in

the original study, the data aggregation level, as well as the distribution of the dependent and independent variables of interest.

## D.1 Study Year

For study year, we have an average of 2009.18, with standard deviation of 6.55. The oldest study included in the paper is from 1998, while the most recent paper was written in 2019. Therefore, we cover 21 years of tests of the *law of 1/n*.

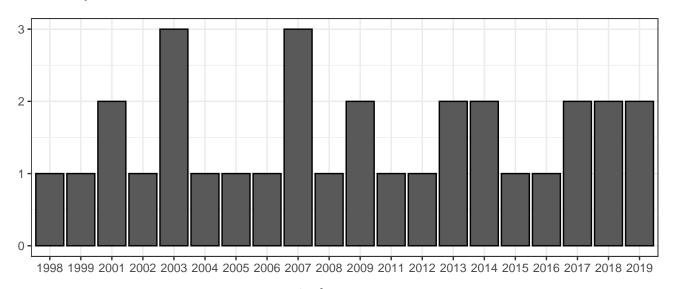


Figure 1: Study Year Frequencies

### D.2 Frequency of Published Papers

Studies were included in our sample regardless of their publication status. From the 31 papers in the sample, 5 were published while 26 were not published.

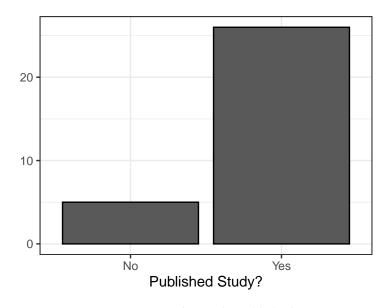


Figure 2: Was the study published?

#### **D.3** Electoral System

Our sample differs considerably in regards to research design. One remarkable difference is that several authors apply the logics of the *law of 1/n*, which was built with majoritarian systems in mind, to non-majoritarian democracies. In the sample, 15 of the papers study *Majoritarian* systems while 16 study *Non-Majoritarian* electoral systems. $^2$ 

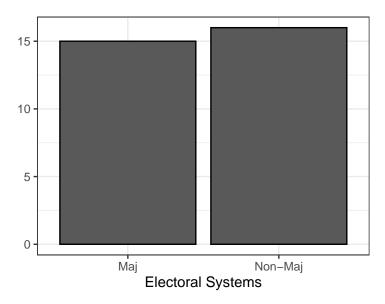


Figure 3: Electoral Systems

## **D.4** Dependent Variables

The outcome variables included in the paper are:

- 16 Per Capita Expenditure papers
- 8 Natural Log of Per Capita Expenditure papers
- 9 Expenditure as a Percentage of the GDP papers

 $<sup>^{2}</sup>$ Note that for the *law of 1/n* to be valid in a non-majoritarian system, we need to assume that despite the fact that politicians are able to campaign in every place in the district, the votes are geographically concentrated. The concentration facilitates politicians to use pork-barrel projects to captivate their electoral supporters.

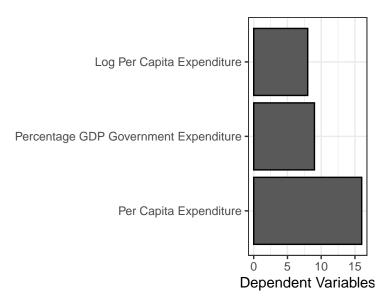


Figure 4: Dependent variables across the law of 1/n studies

### **D.5** Independent Variables

Most papers in our sample analyse the number of legislators in the lower house (7). The second most frequent independent variable is the number of legislators in the upper house (12). Finally, the minority of papers use the natural log of the number of legislators in the lower house as an independent variable (25). As we noted above, some papers had multiple coefficients, and thus the total number of coefficients is 44, while the number of papers is only 31.

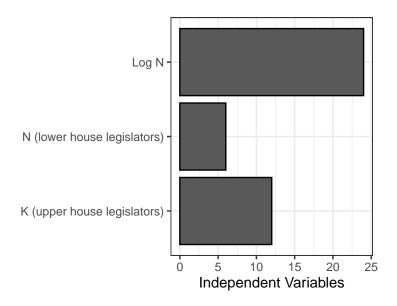
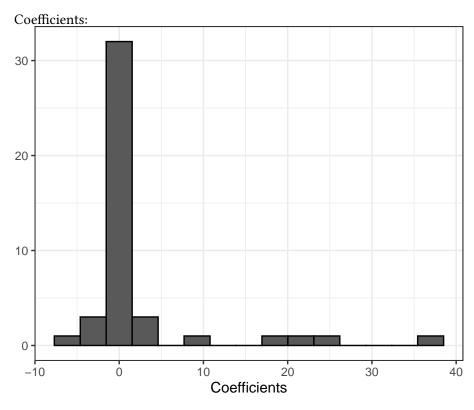
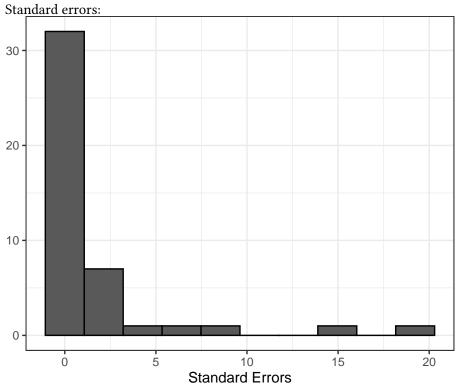


Figure 5: Independent variables across the law of 1/n studies

## D.6 Histogram of the Coefficients and the Standard Errors

The coefficients in the papers vary considerably. In this section, we plot a histogram of the coefficients for all measurements included in the meta-analytic dataset.





# D.7 Sign Coefficients

One simple statistic that we can compute to assess the validity of the law of 1/n is the frequency of positive and negative estimates in the study sample. Below we plot the frequency for all the papers included in the meta-analytic dataset.

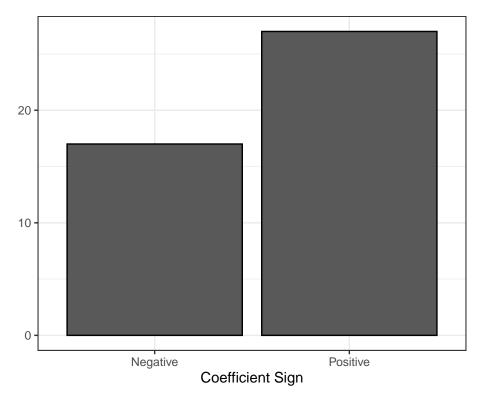


Figure 6: Coefficient Sign

# **E** Descriptive Statistics of Moderators

We chose a set of moderators that frequently appear in the literature and may help us interpret our results. We included them in our meta-regressions alongside an indicator for the type of independent variable used in the original study  $(n, \log(n), \text{ or } k)$ . The additional moderators are: 1) electoral system; 2) data aggregation level; 3) estimation method; 4) publication year; 5) paper publication in an academic journal. The table below presents descriptive statistics for these moderators in our selection of articles.

Table 1: Descriptive Statistics of Moderators

	[ALL]	Other Coefficients	Main Coefficients
	N=148	N=104	N=44
Independent Variables:			
K	45 (30.4%)	33 (31.7%)	12 (27.3%)
logN	22 (14.9%)	15 (14.4%)	7 (15.9%)
N	81 (54.7%)	56 (53.8%)	25 (56.8%)
Year	2008 (6.04)	2008 (5.81)	2009 (6.55)
Published work:			
No	15 (10.1%)	8 (7.69%)	7 (15.9%)
Yes	133 (89.9%)	96 (92.3%)	37 (84.1%)

Table 1: Descriptive Statistics of Moderators (continued)

	[ALL]	Other Coefficients	Main Coefficients
Electoral system:			
Maj	72 (48.6%)	49 (47.1%)	23 (52.3%)
Non-Maj	76 (51.4%)	55 (52.9%)	21 (47.7%)
Estimation method:			
OLS	47 (31.8%)	36 (34.6%)	11 (25.0%)
PANEL	78 (52.7%)	54 (51.9%)	24 (54.5%)
IV	12 (8.11%)	7 (6.73%)	5 (11.4%)
RDD	11 (7.43%)	7 (6.73%)	4 (9.09%)

## F Binomial Tests for Coefficient Signs

The *law of 1/n* posits that we should expect a positive influence of legislature size on public expenditures. A general test of the theory could investigate whether the papers tend to find a higher frequency of positive coefficients in their estimations. In statistical terms, consider a random variable representing the coefficient sign for the papers. As each sign of the paper is a Bernoulli trial, the aggregate result for all papers follows a Binomial distribution with parameters n equals the number of papers, and p the chance of a positive sign. The *law of 1/n* can be reformulated as the chance of p > 0.5, which facilitates the testing of the theory. The null hypothesis for such a test is that:

•  $H_0$ : the proportion of positive and negative signs are indistinguishable (p = 0.5).

As we are taking an agnostic approach, we acknowledge that either the *law of 1/n* (p > 0.5), or the *reverse law of 1/n* (p < 0.5) could be true. In this case, the alternative hypothesis is  $p \neq 0.5$ . To perform this test, we run binomial tests in R, using the function binom.test(.).

This test has two advantages. First, it is robust to the design of the paper. This is an important feature as papers analyse different countries, samples, and have distinct characteristics, such as whether they were published or not. All these factors increase the levels of study heterogeneity. The binomial test ignores the design discrepancies and focuses on the overall reported effect. Second, this test has the advantage of being straightforward and easy to interpret. It requires very few assumption and has a direct statistical formulation. The disadvantage is that we can extract more information from the articles with meta-regressions, as we see in the next sections.

For the number of legislators in the lower house (*N*), the results follow below.

method	alternative	estimate	p.value
Exact binomial test	two.sided	0.44	0.69

Under the null hypothesis of p=0.5, we find that 11 studies, out of 25, had a positive sign. The chance of a distribution with p=0.5 generate this sample is equal to p-value = 0.69. Therefore, we reject the hypothesis that  $p \neq 0.5$ .

For the log of the number of legislators in the lower house  $(\log(N))$ , the results follow below.

method	alternative	estimate	p.value
Exact binomial test	two.sided	0.8571	0.125

Out of 7, 6 had a positive sign. The chance of a distribution with p = 0.5 generate this sample is equal to p-value = 0.125. So we reject the hypothesis that  $p \neq 0.5$ .

Finally, for the number of legislators in the upper house (*K*), the results are:

method	alternative	estimate	p.value
Exact binomial test	two.sided	0.8333	0.03857

Here we see that 10 out of 12 had a positive sign. The p-value for this test is 0.039. Therefore, we accept the hypothesis that  $p \neq 0.5$ . This is the only test that presents evidence of an association between the legislature size and expenditure.

# G Meta-Analysis

#### **G.1** Estimation Method

In general terms, there are two main ways to conduct a meta-analysis, either by using fixed effects or by employing random effects models. The fixed effects model assumes that there exists only one true effect, and that all estimates are an attempt to uncover this effect. The random effects model, in contrast, assumes that there is a distribution of true effects, and that the coefficients vary based on sampling and tests characteristics.

In this paper, we a random-effects model. The empirical papers testing the law of 1/n are very diverse. We tried to capture some of this diversity by considering the main dependent and independent variables separately, but they have at least three other important sources of dispersion:

1. Subjects: Counties, Municipalities, States, Provinces, Countries.

- 2. Electoral systems: Majoritarian, PR, Mixed.
- 3. Modelling strategies: Panel data, Standard OLS, IV, RDD.

These sources of heterogeneity have two implications. First, they make our estimates notably disperse. All but one of our heterogeneity tests are significant. When the sample sizes are large enough, we removed more heterogeneous studies, but we still had considerable dispersion in our estimates. Second, the amount of heterogeneity makes fixed effects estimates unrealistic and biased. Thus, we opt for random effects model.

Let each study having an effect of  $T_i$ . In a random effects model, we can decompose this effect into two components, the true effect that the study with the same specifications as i comes from,  $\theta_i$ , and a within-study error  $\varepsilon_i$ :

$$T_i = \theta_i + \varepsilon_i$$

And the random effects model assumes that the  $\theta_i$  varies from study to study, having a true parameter  $\mu$ , plus a between-study error,  $\xi_i$ :

$$T_i = \mu + \xi_i + \varepsilon_i$$

And the random effects model estimates the parameter  $\mu$ , under the challenge of estimating both the within-and-between-study sampling errors.

Another crucial assumption in the meta-analysis is the independence between the results (Harrer et al. (2019), Cheung (2019), Veroniki et al. (2016), Borenstein et al. (2011)). This assumption states that for our findings be consistent and efficient, the coefficients used in the meta-analysis have to come from different sources of variation. However, in the political economy literature, authors frequently use similar datasets, and almost all papers fit more than one model for the same variable. While our short dataset contains 44 estimates, our full dataset has 148 coefficients. This because the papers report an average of 4.7741935 coefficients. Between robustness tests, multiple dependent and independent variables, and the papers that share similar datasets, the independence assumption is violated. To correct for this problem, we use a multi-level random effects model (Cheung (2014)). The main difference from the single-level random effects model is that we add two extra levels of dependence: the participants and the studies levels. All these levels are assumed to absorb the dependence in the data, leaving for the main coefficient, the independent effect of legislature size on public spending.

There are two levels in the main models. First, we build a common index for papers that share the same dataset specifications. The papers with common indexing are:

Paper IDs	Source of Dependence
3, 42, 132, 165, 439, 441, 467, 505	US States Dataset
408, 208, A258	US Municipalities Dataset
849, 578	US Municipalities Datasetand Same Author in twoDifferent Studies

All the remaining papers receive a unique index. As the number of the papers with these dependencies are not very high, and many characteristics within papers vary (e. g., state-wise ad-hoc exclusions, start and end points variations, region selection, etc.), we show that it makes little difference to change from this index to the paper IDs. In the case of the full dataset, the results change considerably, because authors fit several models within the same paper. In the case In any case, we use multi-level random effects for all the estimated models in this paper.

To study the possibility of of publication bias, for all models we add a funnel plot and an Egger et al. (1997) test for distribution asymmetry. The funnel plot displays the possibility of having a file-drawer effect, meaning that null results are disproportionately less represented in our sample. In this plot, under the assumption of no file-drawer effect, the coefficients are expected to lie symmetrically around the mean observed outcome. If they are asymmetric, it evidences a possible file-drawer effect.

In all empirical estimates, we use the package meta, and the package dmetar, described in (Harrer et al. 2019)(https://bookdown.org/MathiasHarrer/Doing\_Meta\_Analysis\_in\_R/random.html). To empirically implement the random effects model, we need to choose a method to estimate the true effect size variance,  $\tau^2$ , which in our formulation, represents the variance of  $\xi_i$ . We selected the **Restricted Maximum Likelihood Estimator**, as the literature regards it the most precise when analysing continuous measures, such as we have in our data (Veroniki et al. (2016)).

We combined the three independent variables  $(N, \log(N), \text{ and } K)$  with our dependent variables of interest (Expenditure Per Capita, Log of Expenditure Per Capita, Expenditure as a Percentage of the GDP). This formed a  $3 \times 3$  table, and in the following pages we present the results for each of these combinations.

#### G.2 Lower House Size and Expenditure per Capita

```
##
## Multivariate Meta-Analysis Model (k = 15; method: REML)
##
## Variance Components:
##
## estim sqrt nlvls fixed factor
```

```
## sigma^2.1 0.1614 0.4018 8 no id_level1
## sigma^2.2 0.0000 0.0000 15 no id_level1/id_level2
##
## Test for Heterogeneity:
## Q(df = 14) = 215.1021, p-val < .0001
##
## Model Results:
##
## estimate se tval pval ci.lb ci.ub
## 0.0385 0.1590 0.2418 0.8125 -0.3027 0.3796
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1</pre>
```

#### The forest plot:

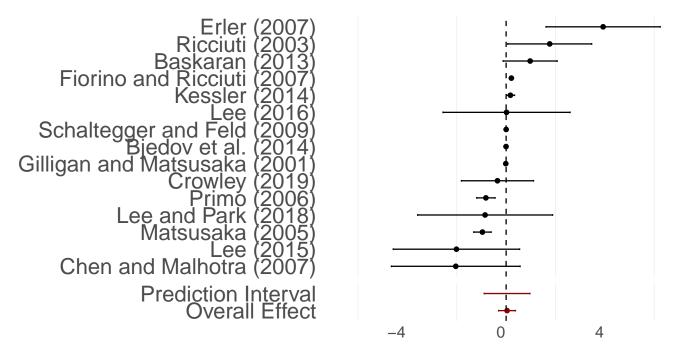


Figure 7: Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

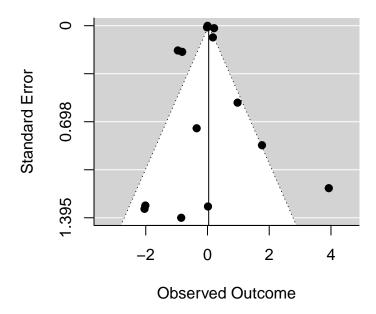


Figure 8: Funnel Plot – Effect of Lower House Size (N) on Per Capita Expenditure (ExpPC)

### Highlights:

- 1. The results are highly heterogeneous: Q = 215.1.
- 2. The estimated SMD in the random effects model is g = 0.04 (SE = 0.159).
- 3. The prediction interval ranges from -0.89 to 0.97. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

### **G.2.1** Electoral System Subgroup Analysis

The *law of 1/n* was created for majoritarian systems. In the theoretical section below, we explain why the argument have potential issues when applied to non-majoritarian electoral systems. We estimated a subgroup analysis using a binary electoral system.

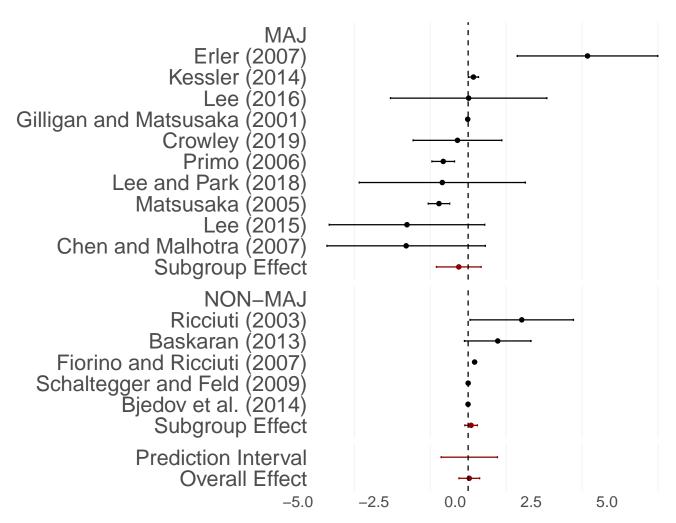


Figure 9: Subgroup Analysis of (N) x (ExpPC), controlling by electoral system

Therefore, we can see that the hypothesis that majoritarian systems produce systematic positive effects was disproved. Both are non-significant, and they reassure us that the absense of effect is not caused by pooling multiple types of electoral systems.

### G.3 Log Lower House Size and Expenditure per Capita

There are no studies that have per capita expenditure as the dependent variable and log of lower house size as the treatment variable.

## G.4 Upper House Size and Expenditure per Capita

Now, we look into the upper house size (K). In this model, we investigate the effect of upper house size on expenditure per capita (ExpPC).

```
##
## Multivariate Meta-Analysis Model (k = 9; method: REML)
##
## Variance Components:
```

```
##
## estim sqrt nlvls fixed factor
## sigma^2.1 32.4170 5.6936  4  no   id_level1
## sigma^2.2 52.2149 7.2260  9  no id_level1/id_level2
##
## Test for Heterogeneity:
## Q(df = 8) = 42.6588, p-val < .0001
##
## Model Results:
##
## estimate se tval pval ci.lb ci.ub
## 3.8171 4.2570 0.8967 0.3961 -5.9995 13.6337
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1</pre>
```

### And the forest plot:

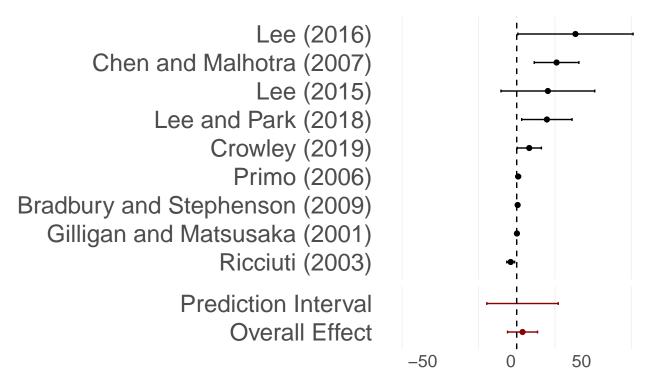


Figure 10: Effect of upper house size (K) on the per capita government expenditure (ExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

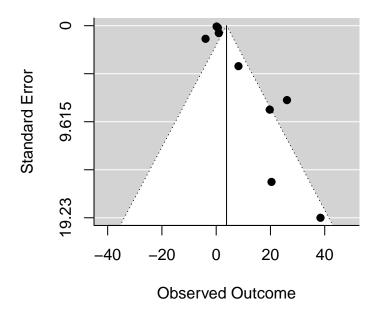


Figure 11: Funnel Plot – Effect of upper house size (K) on per capita government expenditure (ExpPC)

#### Highlights:

- 1. The results are highly heterogeneous: Q = 42.66.
- 2. The estimated SMD in the random effects model is g = 3.82 (SE = 4.257).
- 3. The prediction interval ranges from -19.56 to 27.19. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## G.5 Lower House Size and Log Expenditure Per Capita

This model estimates the Log of Per Capita Expenditure as the dependent variable, and the number of lower house legislators as the treatment variable.

```
##
## Multivariate Meta-Analysis Model (k = 5; method: REML)
##
  Variance Components:
##
                                                         factor
               estim
                             nlvls fixed
  sigma^2.1 0.0050 0.0706
                                                      id_level1
## sigma^2.2 0.0050 0.0706
                                        no id_level1/id_level2
                                  5
## Test for Heterogeneity:
## Q(df = 4) = 50.0612, p-val < .0001
## Model Results:
```

```
## estimate se tval pval ci.lb ci.ub
## -0.0543 0.0462 -1.1746 0.3053 -0.1827 0.0741
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The forest plot is as follows:

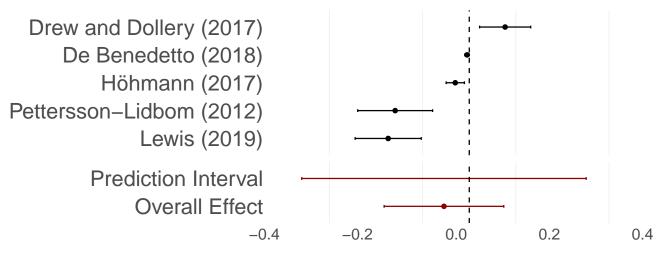


Figure 12: Effect of lower houses size (N) on log of per capita expenditure (logExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

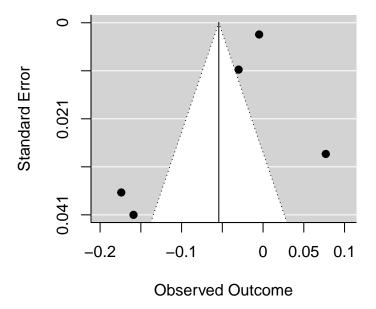


Figure 13: Funnel Plot – Effect of lower houses size (N) on log of per capita expenditure (logExpPC)

### Highlights:

- 1. The results are highly heterogeneous: Q = 50.06.
- 2. The estimated SMD in the random effects model is g = -0.05 (SE = 0.046).
- 3. The prediction interval ranges from -0.36 to 0.25. Therefore, it emcompasses zero.

4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

# G.6 Log of Lower House Size and Log of Expenditure Per Capita

In this specification, we study the log of per capita expenditure (logExpPC) as a function of the log of lower house size (logN).

```
##
## Multivariate Meta-Analysis Model (k = 4; method: REML)
## Variance Components:
##
              estim sqrt nlvls fixed
                                                       factor
## sigma^2.1 0.0000 0.0000
                                2
                                                    id_level1
                                      no
                                   no id_level1/id_level2
## sigma^2.2 0.0058 0.0763
                                4
## Test for Heterogeneity:
## Q(df = 3) = 14.2923, p-val = 0.0025
## Model Results:
##
## estimate
                      tval
                             pval ci.lb ci.ub
    0.1815  0.0434  4.1868  0.0248  0.0435  0.3195 *
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The forest plot is available below:

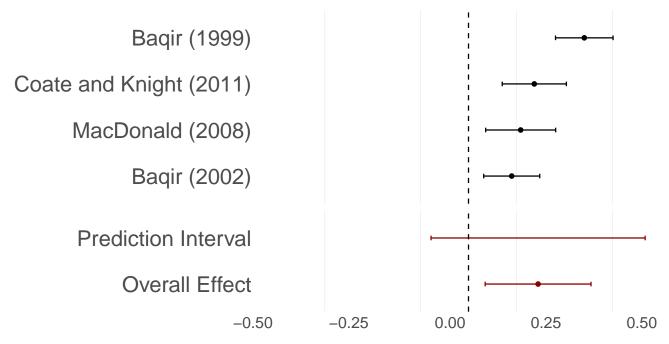


Figure 14: Effect of log lower houses size (logN) on the log of per capita government expenditure (logExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

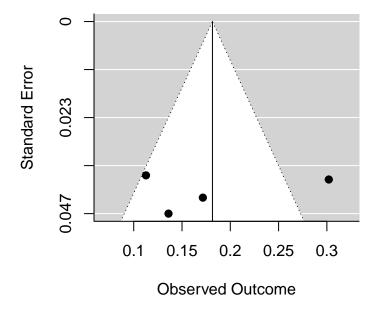


Figure 15: Funnel Plot – Effect of log lower houses size (N) on log of per capita government expenditure (logExpPC)

#### Highlights:

- 1. The results are highly heterogeneous: Q = 14.29.
- 2. The estimated SMD in the random effects model is q = 0.18 (SE = 0.043).
- 3. The prediction interval ranges from -0.1 to 0.46. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

### G.7 Upper House Size and Log of Expenditure Per Capita

No studies correlate the log of per capita expenditure with the size of upper house (K).

## G.8 Lower House Size and Expenditure as Percentage of GDP

This model fits the random effects for the percentage of GDP as public expenditure as the main outcome, and the size of lower house as the treatment variable.

```
##
## Multivariate Meta-Analysis Model (k = 5; method: REML)
## Variance Components:
                       sqrt nlvls fixed
                                                        factor
              estim
## sigma^2.1 0.0004 0.0195
                                       no
                                                     id_level1
## sigma^2.2 0.0004 0.0195
                                       no id_level1/id_level2
## Test for Heterogeneity:
## Q(df = 4) = 30.9717, p-val < .0001
## Model Results:
## estimate
                       tval
                               pval
                                       ci.lb
                                              ci.ub
   -0.0083 0.0132 -0.6251 0.5658 -0.0449 0.0284
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Below, you may find the forest plot:

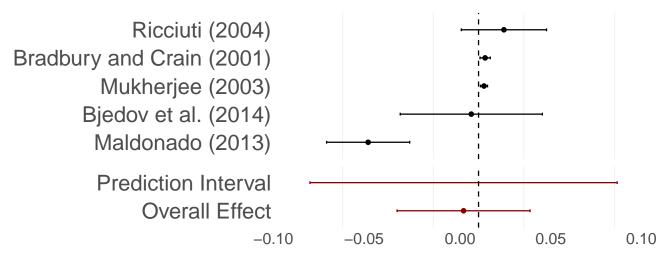


Figure 16: Effect of lower houses size (N) on percentage of public expenditure GDP (PCTGDP)

And to assess the possibility of publication bias, we add funnel plot below:

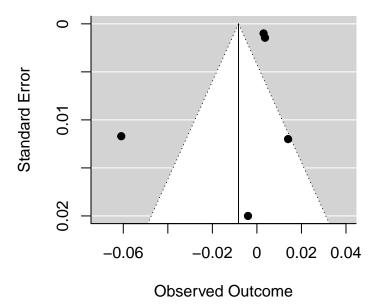


Figure 17: Funnel Plot – Effect of lower houses size (N) on percentage of public expenditure GDP (PCTGDP)

### Highlights:

- 1. The results are highly heterogeneous: Q = 30.97.
- 2. The estimated SMD in the random effects model is q = -0.01 (SE = 0.013).
- 3. The prediction interval ranges from -0.09 to 0.08. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## G.9 Log Lower House Size and Expenditure as Percentage of GDP

This model investigates the percentage of GDP as public expenditure as the dependent variable and the log lower house size (logN) as the treatment variable.

```
##
## Multivariate Meta-Analysis Model (k = 3; method: REML)
##
   Variance Components:
##
##
               estim
                             nlvls
                                     fixed
                                                         factor
## sigma^2.1 2.6578 1.6303
                                                      id_level1
  sigma^2.2 2.6578 1.6303
                                  3
                                        no id_level1/id_level2
## Test for Heterogeneity:
## Q(df = 2) = 51.6470, p-val < .0001
##
## Model Results:
```

```
## estimate se tval pval ci.lb ci.ub
## 0.0203 1.4854 0.0137 0.9903 -6.3707 6.4114
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The forest plot follows below:

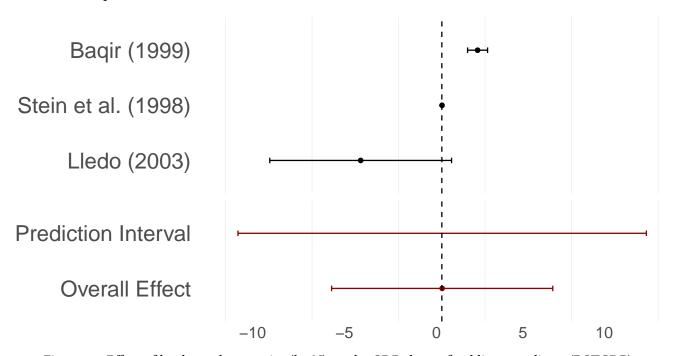


Figure 18: Effect of log lower houses size (logN) on the GDP share of public expenditure (PCTGDP)

And to assess the possibility of publication bias, we add funnel plot below:

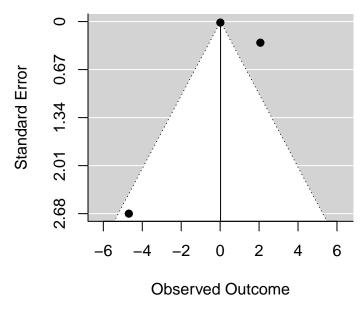


Figure 19: Funnel Plot – Effect of log lower houses size (N) on the GDP share of public expenditure (PCTGDP)

Highlights:

- 1. The results are highly heterogeneous: Q = 51.65.
- 2. The estimated SMD in the random effects model is g = 0.02 (SE = 1.485).
- 3. The prediction interval ranges from -11.78 to 11.82. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## G.10 Upper House Size and Expenditure as Percentage of GDP

This model looks into the effect of upper house size (K) on the public expenditure share of the GDP (PCTGDP).

```
##
## Multivariate Meta-Analysis Model (k = 3; method: REML)
## Variance Components:
##
               estim sqrt nlvls fixed
                                                          factor
## sigma^2.1 0.0004 0.0201
                                                       id_level1
                                     no id_level1/id_level2
## sigma^2.2 0.0004 0.0201
                                3
##
## Test for Heterogeneity:
## Q(df = 2) = 14.0739, p-val = 0.0009
##
## Model Results:
## estimate
                        tval
                                pval
                                        ci.lb ci.ub
             se
    -0.0027 \quad 0.0175 \quad -0.1570 \quad 0.8896 \quad -0.0781 \quad 0.0726
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The forest plot follows below:

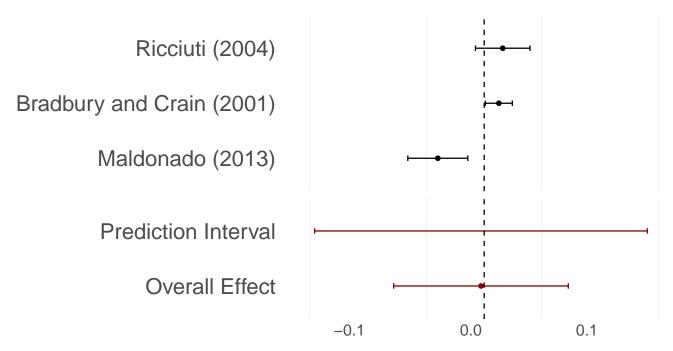


Figure 20: Effect of upper house size (K) on the public expenditure share of the GDP (PCTGDP)

And to assess the possibility of publication bias, we add funnel plot below:

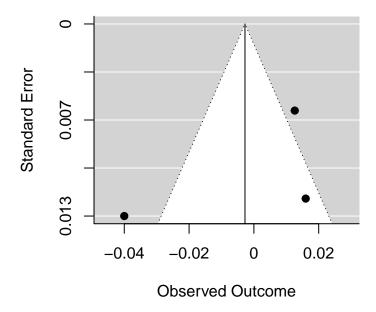


Figure 21: Funnel Plot – Effect of upper house size (K) on the public expenditure share of the GDP (PCTGDP)

## Highlights:

- 1. The results are highly heterogeneous: Q = 14.07.
- 2. The estimated SMD in the random effects model is g = 0 (SE = 0.018).
- 3. The prediction interval ranges from -0.15 to 0.14. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## G.11 Lower House Size and Expenditure per Capita (IV)

```
## Multivariate Meta-Analysis Model (k = 4; method: REML)
## Variance Components:
##
              estim
                       sqrt nlvls fixed
                                                        factor
## sigma^2.1 0.8028 0.8960
                                                     id_level1
## sigma^2.2 0.0000 0.0000
                                       no id_level1/id_level2
##
## Test for Heterogeneity:
## Q(df = 3) = 46.8325, p-val < .0001
## Model Results:
                                       ci.lb ci.ub
## estimate
                       tval
                               pval
   -0.0105 0.5472 -0.0192 0.9859 -1.7518 1.7308
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

#### And the forest plot:

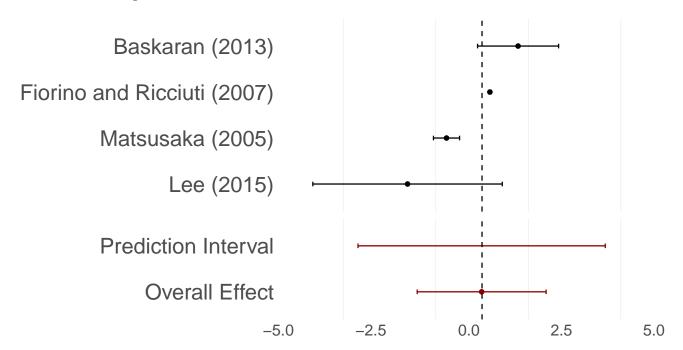


Figure 22: Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

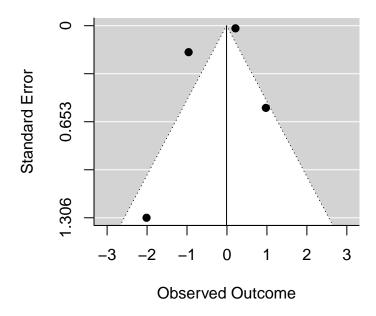


Figure 23: Funnel Plot – Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

### Highlights:

- 1. The results are highly heterogeneous: Q = 215.1.
- 2. The estimated SMD in the random effects model is g = 0.04 (SE = 0.159).
- 3. The prediction interval ranges from -0.89 to 0.97. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

### **G.11.1** Regression Method Subgroup Analysis

Over time, the literature evolved to use causally identified techniques for determine the effect of legislature size on the expenduture per capita. To study whether the method had an effect on the estimated coefficients, we fit a subgroup analysis using the method employed in each paper.

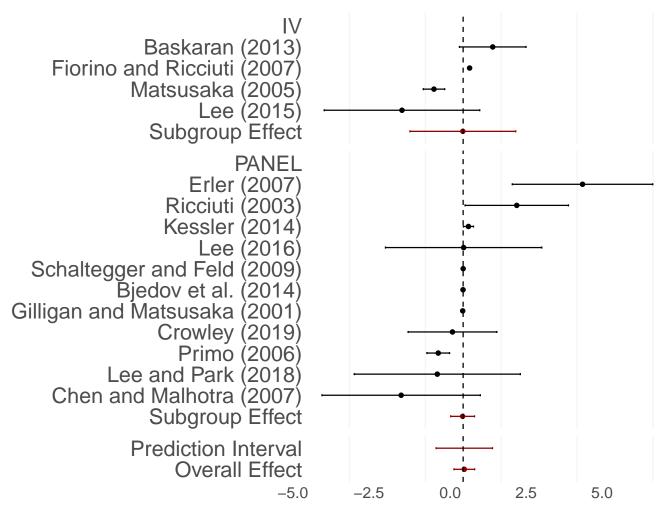


Figure 24: Subgroup Analysis of (N) x (ExpPC), controlling by regression methods

Although all methods generate a null effect, the IV method seems to be well distributed, with two papers with positive effects and two papers negative displaying negative effects. The random effects model for the subgroup is 0.22, which is negative but non-significant. Improve the estimation technique, for the case of IVs, render still a null effect of legislature size on per capita government expenditure.

#### G.12 Lower House Size and Log of Expenditure per Capita (RDD)

```
## ## Multivariate Meta-Analysis Model (k = 4; method: REML)
##
## Variance Components:
##
## estim sqrt nlvls fixed factor
## sigma^2.1 0.0034 0.0583 4 no id_level1
## sigma^2.2 0.0034 0.0583 4 no id_level1/id_level2
##
## Test for Heterogeneity:
## Q(df = 3) = 41.0086, p-val < .0001</pre>
```

```
##
## Model Results:
##
## estimate se tval pval ci.lb ci.ub
## -0.0849 0.0433 -1.9594 0.1449 -0.2228 0.0530
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

#### Forest plot:

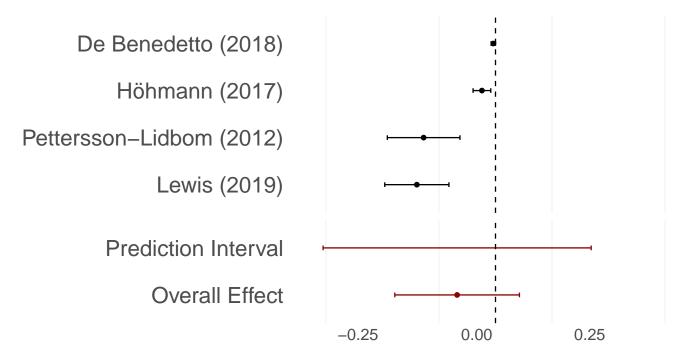


Figure 25: Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

#### Highlights:

- 1. The results are highly heterogeneous: Q = 41.01.
- 2. The estimated SMD in the random effects model is g = -0.08 (SE = 0.043).
- 3. The prediction interval ranges from -0.38 to 0.21. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

#### **G.12.1** Regression Method Subgroup Analysis

Over time, the literature evolved to use causally identified techniques for determine the effect of legislature size on the log of expenditure per capita. To study whether the method had an effect on the estimated coefficients, we fit a subgroup analysis using the method employed in each paper.

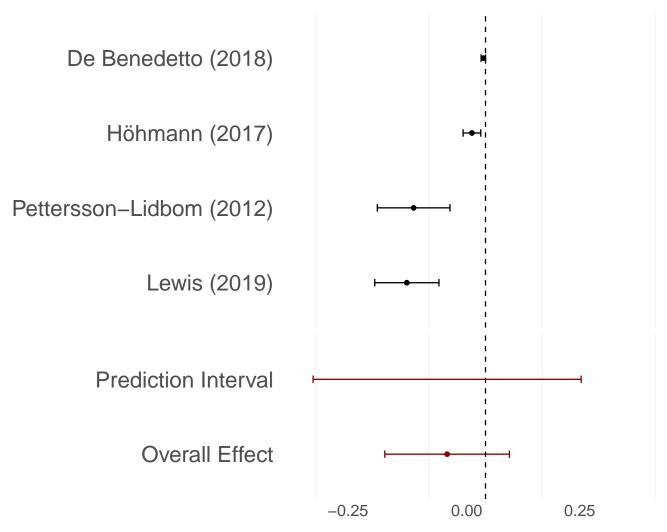


Figure 26: Subgroup Analysis of (N) x (logExpPC), controlling by the regression methods

For the RDD subgroup analysis, we can see a much clearer picture. The subgroup effect is -0.085. This suggests that improving the estimation renders to a negative result that is likely to hold conditional on more papers using the technique displaying the same effect size and sign.

```
## pdf
## 2
## pdf
```

##

# H Meta-Analysis (All Coefficients)

### H.1 Lower House Size and Expenditure Per Capita

Here we estimate the relationship between expenditure per capita as a dependent variable, and the lower house size as the independent variable.

```
## Multivariate Meta-Analysis Model (k = 43; method: REML)
##
## Variance Components:
           estim sqrt nlvls fixed
                                                factor
## sigma^2.1 0.4631 0.6805
                                             id_level1
                            8 no
## sigma^2.2 0.0088 0.0939
                          43 no id_level1/id_level2
## Test for Heterogeneity:
## Q(df = 42) = 753.4012, p-val < .0001
## Model Results:
## estimate se tval pval ci.lb ci.ub
## 0.1443 0.2553 0.5651 0.5750 -0.3709 0.6595
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The forest plot:

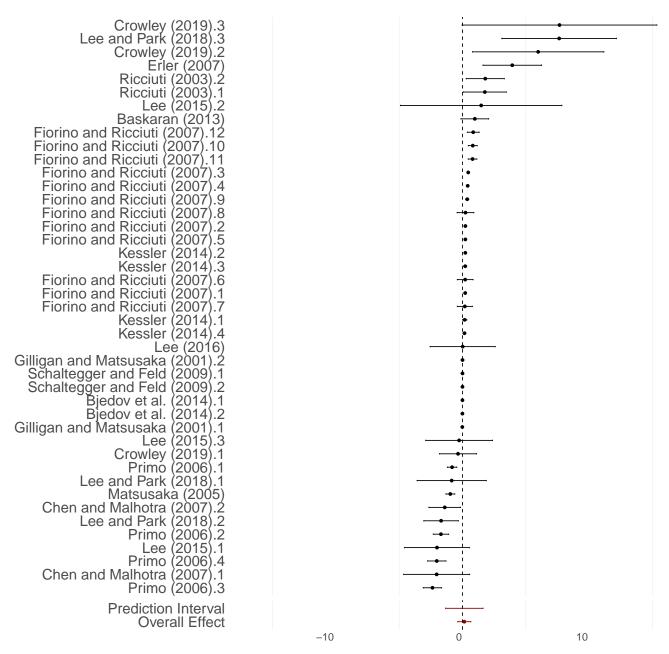


Figure 27: Effect of Lower House Size (N) on Per Capita Expenditure (ExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

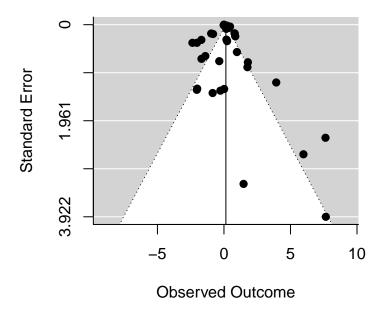


Figure 28: Funnel Plot – Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

### Highlights:

- 1. The results are highly heterogeneous: Q = 753.4.
- 2. The estimated SMD in the random effects model is g = 0.14 (SE = 0.255).
- 3. The prediction interval ranges from -1.33 to 1.62. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

#### H.1.1 Electoral System Subgroup Analysis

The *law of 1/n* was formulated to analyse the budgetary allocation in majoritarian systems. In the theoretical section below, we explain why the argument have potential issues when applied to non-majoritarian electoral systems. We estimated a subgroup analysis using a dummy variable indicating the electoral system included in each model.

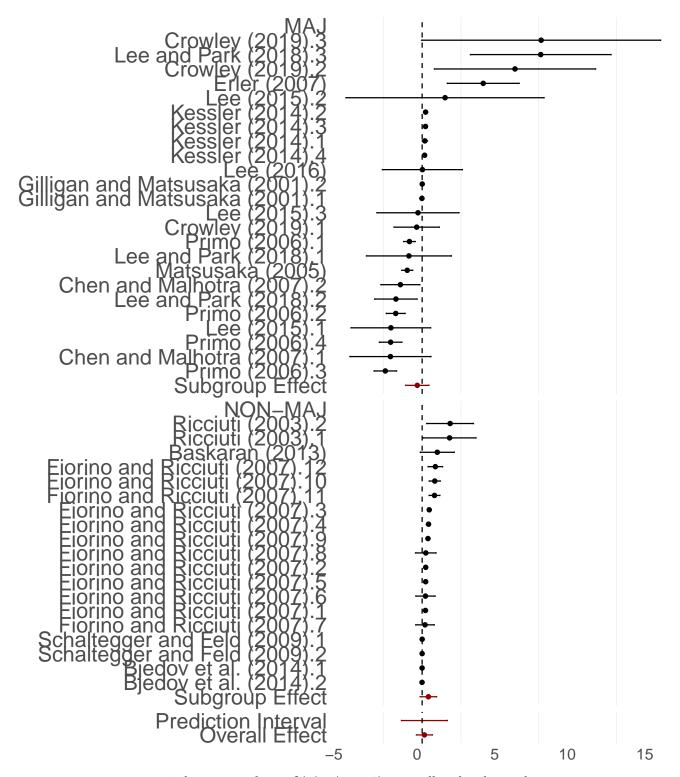


Figure 29: Subgroup Analysis of (N) x (ExpPC), controlling by electoral system

Therefore, we see that majoritarian systems do not have a clear positive effect on budgetary spending. The majoritarian systems in the sample had a random effects model estimate of -0.25, while the random effects model in the non-majoritarian subgroup fitted a value of 0.08. Both are not statistically significant, but they reassure us that the absence of effect is not caused by pooling multiple types of electoral systems.

## H.2 Log of Lower House Size and Expenditure Per Capita

There are no studies that have per capita expenditure as the dependent variable and log of lower house size as the treatment variable.

## H.3 Upper House Size and Expenditure Per Capita

Now we investigate the effect of the upper house size (K) on government spending. In the model below, we evaluate the relationship between upper house size and expenditure per capita (ExpPC).

```
##
## Multivariate Meta-Analysis Model (k = 31; method: REML)
## Variance Components:
##
              estim
                     sqrt nlvls fixed
                                                       factor
## sigma^2.1 19.2324 4.3855
                                                    id_level1
                                      no
## sigma^2.2 5.3579 2.3147
                             31 no id_level1/id_level2
## Test for Heterogeneity:
## Q(df = 30) = 150.2534, p-val < .0001
## Model Results:
               se
                    tval
                            pval
                                    ci.lb ci.ub
   1.1563 2.3581 0.4904 0.6274 -3.6596 5.9722
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

And the forest plot:

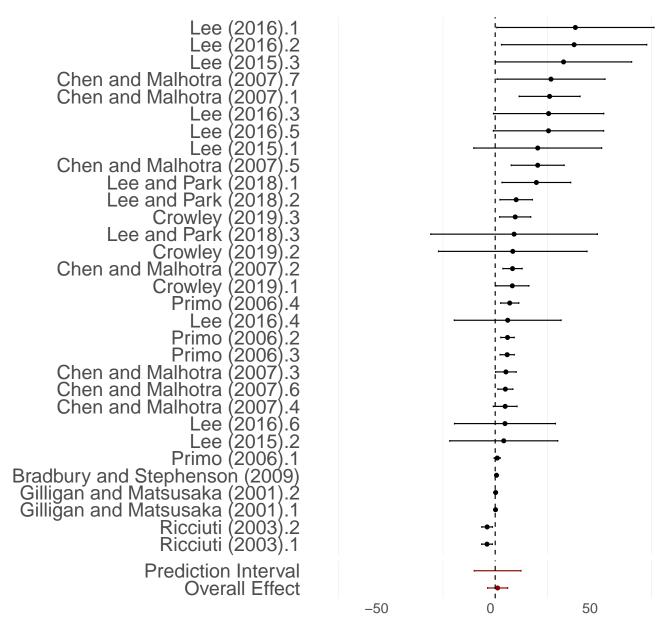


Figure 30: Effect of upper house size (K) on the per capita government expenditure (ExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

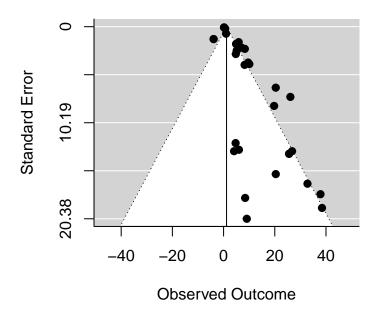


Figure 31: Funnel Plot – Effect of upper houses size (K) on Per Capita Expenditure (ExpPC)

## Highlights:

- 1. The results are highly heterogeneous: Q = 150.25.
- 2. The estimated SMD in the random effects model is g = 1.16 (SE = 2.358).
- 3. The prediction interval ranges from -10.06 to 12.37. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## H.4 Lower House Size and Log of Expenditure Per Capita

This model estimates the log of per capita expenditure as the dependent variable, and the number of lower house legislators as the treatment variable.

```
##
## Multivariate Meta-Analysis Model (k = 17; method: REML)
##
  Variance Components:
##
                                                         factor
               estim
                             nlvls fixed
  sigma^2.1 0.0000 0.0000
                                                      id_level1
## sigma^2.2 0.0121 0.1101
                                        no id_level1/id_level2
                                 17
## Test for Heterogeneity:
## Q(df = 16) = 233.7588, p-val < .0001
## Model Results:
```

```
## estimate se tval pval ci.lb ci.ub
## -0.0408 0.0277 -1.4717 0.1605 -0.0995 0.0180
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The forest plot is shown below:

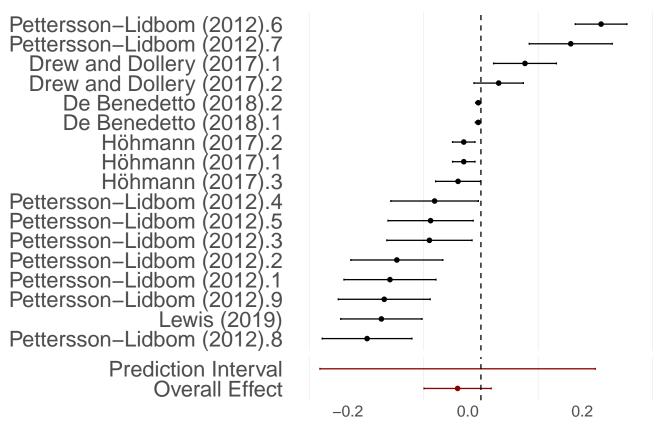


Figure 32: Effect of lower houses size (N) on log of per capita expenditure (logExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

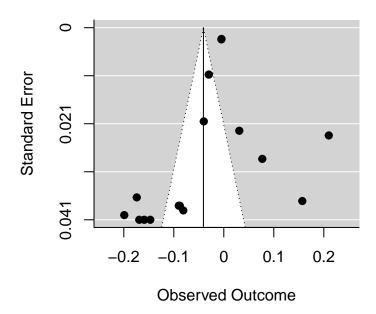


Figure 33: Funnel Plot – Effect of lower houses size (N) on log of Per Capita Expenditure (logExpPC)

## Highlights:

- 1. The results are highly heterogeneous: Q = 233.76.
- 2. The estimated SMD in the random effects model is q = -0.04 (SE = 0.028).
- 3. The prediction interval ranges from -0.28 to 0.2. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## H.5 Log of Lower House Size and Log of Expenditure Per Capita

In this specification, we study the log of per capita expenditure (logExpPC) as a function of the log of lower house size (logN).

```
##
## Multivariate Meta-Analysis Model (k = 16; method: REML)
##
## Variance Components:
##
               estim
                        sqrt nlvls fixed
                                                         factor
## sigma^2.1 0.0037 0.0608
                                                      id_level1
## sigma^2.2 0.0015 0.0392
                                        no id_level1/id_level2
                                 16
## Test for Heterogeneity:
## Q(df = 15) = 43.3297, p-val = 0.0001
## Model Results:
```

```
## estimate se tval pval ci.lb ci.ub
## 0.2230 0.0454 4.9143 0.0002 0.1263 0.3197 ***
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The forest plot:

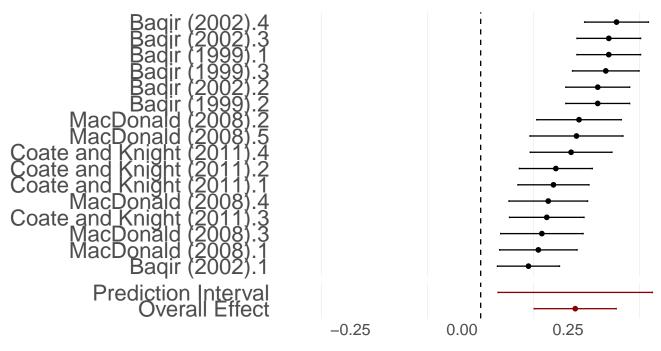


Figure 34: Effect of log lower houses size (logN) on the log of per capita government expenditure (logExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

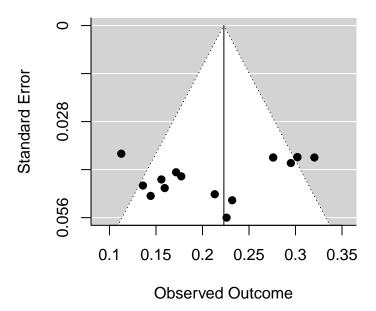


Figure 35: Funnel Plot – Effect of log of lower houses size (logN) on log of Per Capita Expenditure (logExpPC)

Highlights:

- 1. The results are highly heterogeneous: Q = 43.33.
- 2. The estimated SMD in the random effects model is g = 0.22 (SE = 0.045).
- 3. The prediction interval ranges from 0.04 to 0.4. Therefore, it does not emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## H.6 Upper House Size and Log of Expenditure Per Capita

No studies related the log of per capita expenditure with the size of upper house (K).

# H.7 Lower House Size and Expenditure as Percentage of GDP

This model fits the random effects for the percentage of GDP as public expenditure as the main outcome, and the size of lower house as the treatment variable.

```
##
## Multivariate Meta-Analysis Model (k = 21; method: REML)
## Variance Components:
##
              estim sqrt nlvls fixed
                                                     factor
## sigma^2.1 0.0007 0.0260
                               5
                                                  id_level1
                                     no
## sigma^2.2 0.0001 0.0107
                              21
                                  no id_level1/id_level2
## Test for Heterogeneity:
## Q(df = 20) = 1314.5409, p-val < .0001
## Model Results:
##
                                     ci.lb
## estimate se
                      tval
                             pval
   -0.0046 0.0125 -0.3692 0.7158 -0.0306 0.0214
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Here is the forest plot:

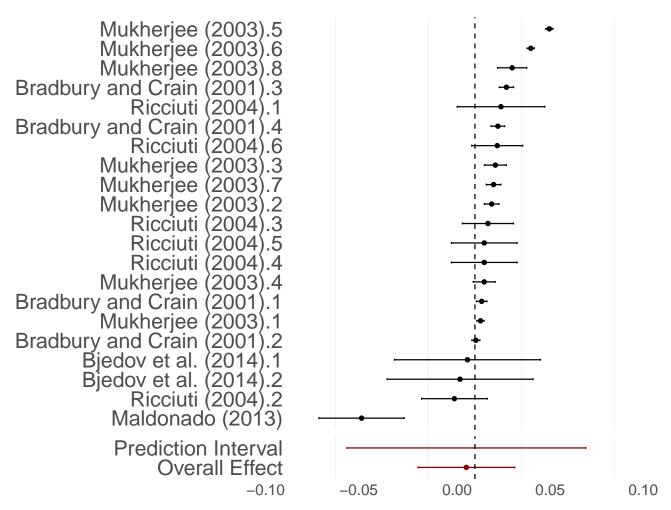


Figure 36: Effect of lower houses size (N) on percentage of public expenditure GDP (PCTGDP)

And to assess the possibility of publication bias, we add funnel plot below:

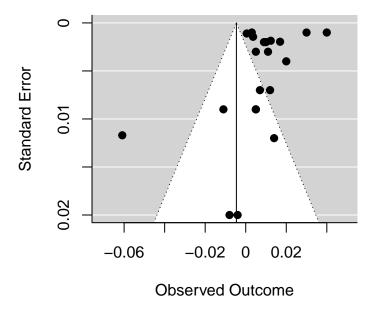


Figure 37: Funnel Plot – Effect of lower houses size (N) on percentage of public expenditure GDP (PCTGDP)

#### Highlights:

1. The results are highly heterogeneous: Q = 1314.54.

- 2. The estimated SMD in the random effects model is q = 0 (SE = 0.012).
- 3. The prediction interval ranges from -0.07 to 0.06. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## H.8 Log of Lower House Size and Expenditure as Percentage of GDP

This meta-regression investigates the percentage of GDP as public expenditure as the dependent variable and the natural logarithm of lower house size  $(\log(N))$  as the treatment variable.

```
##
## Multivariate Meta-Analysis Model (k = 6; method: REML)
## Variance Components:
##
              estim sqrt nlvls fixed
                                                      factor
## sigma^2.1 5.8712 2.4231
                                                   id_level1
## sigma^2.2 0.0000 0.0000
                             6 no id_level1/id_level2
##
## Test for Heterogeneity:
## Q(df = 5) = 163.0025, p-val < .0001
##
## Model Results:
                             pval ci.lb ci.ub
## estimate se
                   tval
    0.0300 \ 1.5497 \ 0.0193 \ 0.9853 \ -3.9537 \ 4.0136
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The forest plot:

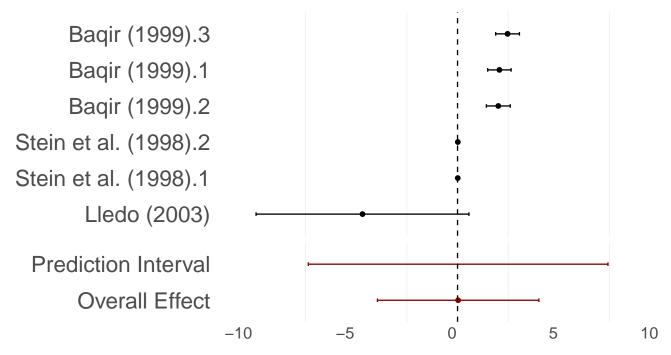


Figure 38: Effect of log lower houses size (logN) on the GDP share of public expenditure (PCTGDP)

And to assess the possibility of publication bias, we add funnel plot below:

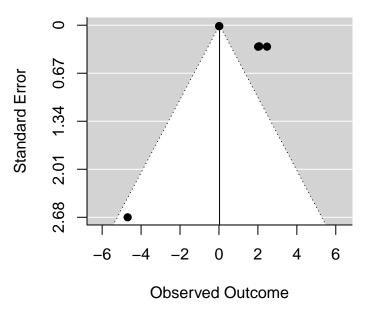


Figure 39: Funnel Plot – Effect of log of lower houses size (logN) on log of Per Capita Expenditure (logExpPC)

## Highlights:

- 1. The results are highly heterogeneous: Q = 163.
- 2. The estimated SMD in the random effects model is q = 0.03 (SE = 1.55).
- 3. The prediction interval ranges from -7.36 to 7.42. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

# H.9 Upper House Size and Expenditure as Percentage of GDP

This model looks into the effect of upper house size (*K*) on the public expenditure share of the GDP (PCTGDP).

```
## Multivariate Meta-Analysis Model (k = 14; method: REML)
## Variance Components:
##
             estim sqrt nlvls fixed
                                                  factor
## sigma^2.1 0.0006 0.0240
                            3
                                 no
                                               id_level1
                           14 no id_level1/id_level2
## sigma^2.2 0.0001 0.0077
## Test for Heterogeneity:
## Q(df = 13) = 65.0192, p-val < .0001
##
## Model Results:
##
## estimate se tval pval ci.lb ci.ub
## -0.0057 0.0148 -0.3856 0.7060 -0.0376 0.0262
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

And the forest plot:

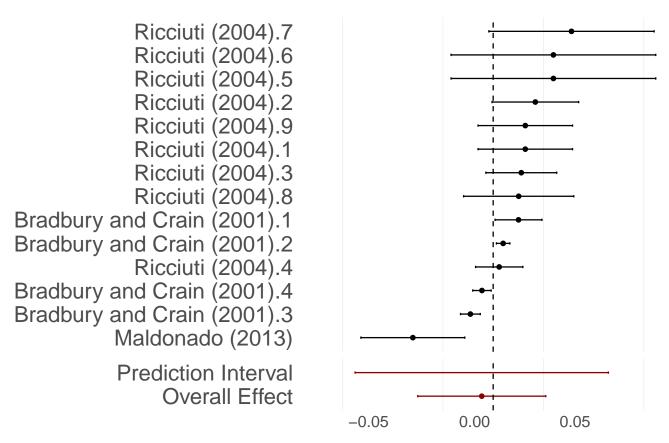


Figure 40: Effect of upper house size (K) on the public expenditure share of the GDP (PCTGDP)

And to assess the possibility of publication bias, we add funnel plot below:

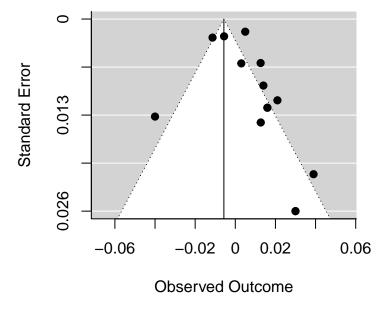


Figure 41: Funnel Plot – Effect of upper houses size (K) on the public expenditure share of GDP (PCTGDP)

#### Highlights:

- 1. The results are highly heterogeneous: Q = 65.02.
- 2. The estimated SMD in the random effects model is q = -0.01 (SE = 0.015).
- 3. The prediction interval ranges from -0.07 to 0.06. Therefore, it emcompasses zero.

4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## H.10 Lower House Size and Expenditure per Capita (IV)

```
##
## Multivariate Meta-Analysis Model (k = 9; method: REML)
## Variance Components:
                                                     factor
              estim
                    sgrt nlvls fixed
## sigma^2.1 0.8114 0.9008
                                                  id_level1
## sigma^2.2 0.0141 0.1188
                              9 no id_level1/id_level2
## Test for Heterogeneity:
## Q(df = 8) = 94.2338, p-val < .0001
## Model Results:
                                   ci.lb ci.ub
                            pval
    0.0398 0.5526 0.0720 0.9443 -1.2345 1.3141
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

#### And the forest plot:

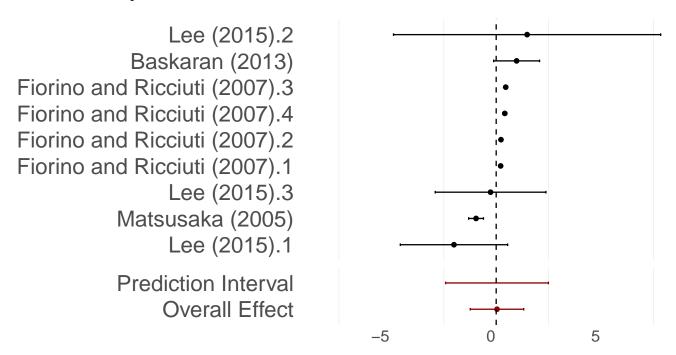


Figure 42: Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

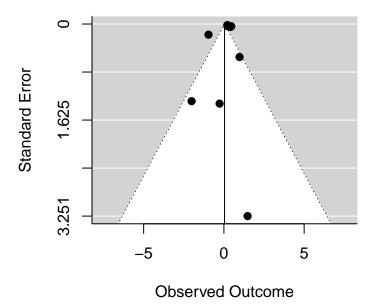


Figure 43: Funnel Plot – Effect of lower houses size (N) on Per Capita Expenditure (ExpPC)

#### Highlights:

##

- 1. The results are highly heterogeneous: Q = 94.23.
- 2. The estimated SMD in the random effects model is g = 0.04 (SE = 0.553).
- 3. The prediction interval ranges from -2.41 to 2.49. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

## H.11 Lower House Size and Log of Expenditure per Capita (RDD)

```
## Multivariate Meta-Analysis Model (k = 11; method: REML)
##
## Variance Components:
##
                                                        factor
                            nlvls fixed
               estim
## sigma^2.1 0.0051 0.0712
                                                     id_level1
                                       no
  sigma^2.2 0.0000 0.0000
                                11
                                       no id_level1/id_level2
##
## Test for Heterogeneity:
## Q(df = 10) = 74.4929, p-val < .0001
## Model Results:
##
## estimate
                       tval
                               pval
                                       ci.lb
  -0.0747 0.0369 -2.0237 0.0705 -0.1569 0.0075 .
```

```
## ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

#### And the forest plot:

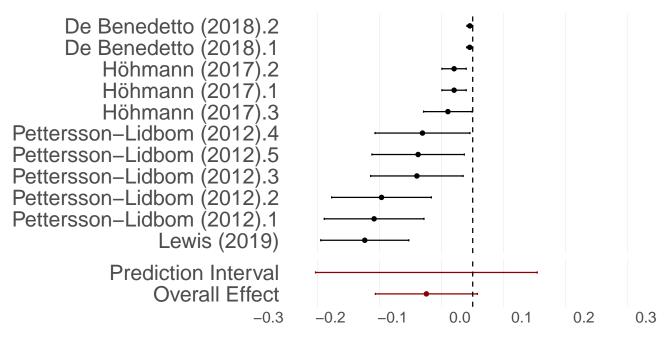


Figure 44: Effect of lower houses size (N) on log of Per Capita Expenditure (logExpPC)

And to assess the possibility of publication bias, we add funnel plot below:

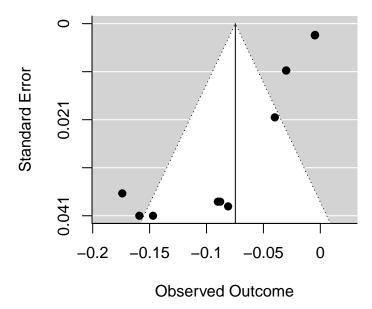


Figure 45: Funnel Plot – Effect of lower houses size (N) on log of Per Capita Expenditure (ExpPC)

#### Highlights:

- 1. The results are highly heterogeneous: Q = 74.49.
- 2. The estimated SMD in the random effects model is q = -0.07 (SE = 0.037).

- 3. The prediction interval ranges from -0.25 to 0.1. Therefore, it emcompasses zero.
- 4. The Egger et al. (1997) test rejected the hypothesis of publication bias.

# I Meta-Regressions

In the meta-regressions, we study the effects of a group of moderators on the reported government spending data. We select the following moderators:

- 1. The independent variable (variable indepvar2):
- K: Upper House Size
- N: Lower House Size
- logN: Log of Lower House Size
- 2. Year that the paper was published (for working papers, the year it was posted online; variable year)
- 3. A dummy indicating whether the paper was published or not (variable published).
- 4. A dummy for non-majoritarian electoral systems (variable elecsys2).
- 5. The estimation method used in the papers (variable method):
- OLS: Ordinary-Least Squares in Cross-Sectional data.
- PANEL: Time-Series Cross-Section models, with estimated fixed effects.
- IV: Instrumental Variables models.
- RDD: Regression Discontinuity Designs.

The results follows below, for the three combinations of dependent variables: Expenditure Per Capita, Log of Expenditure Per Capita, and Expenditure as a Percentage of the GDP.

### I.1 Meta-Regressions for Expenditure Per Capita

Here we study the expenditure per capita as the main outcome, aggregating all types of independent variables.

```
##
## Multivariate Meta-Analysis Model (k = 24; method: REML)
##
## logLik Deviance AIC BIC AICC
## -51.2403 102.4807 120.4807 127.9796 146.1950
##
## Variance Components:
```

```
sqrt nlvls fixed
                                                       factor
##
              estim
## sigma^2.1 0.0000 0.0001
                                 9
                                                    id_level1
## sigma^2.2 2.4576 1.5677
                                      no id_level1/id_level2
                               24
## Test for Residual Heterogeneity:
## QE(df = 17) = 124.7931, p-val < .0001
##
## Test of Moderators (coefficients 2:7):
## F(df1 = 6, df2 = 17) = 0.3022, p-val = 0.9272
##
## Model Results:
##
                                                           ci.lb
                                                                    ci.ub
                   estimate
                                         tval
                                                 pval
## intrcpt
                   -66.0931 163.0215 -0.4054 0.6902 -410.0384 277.8522
## indepvar2N
                    -1.0416
                              1.2006 -0.8675 0.3977
                                                                   1.4915
                    0.0325
                              0.0814 0.3991 0.6948
                                                         -0.1392
                                                                   0.2042
## year
## publishedYes
                    1.4630
                              1.7724 0.8254 0.4206
                                                         -2.2764
                                                                   5.2023
## elecsys2Non-Maj
                    0.4147
                              1.0195 0.4067 0.6893
                                                         -1.7363
                                                                   2.5657
## methodPANEL
                     0.5012
                               1.9040 0.2632 0.7955
                                                         -3.5159
                                                                   4.5183
## methodIV
                    -0.0682
                              2.1758 -0.0314 0.9754
                                                         -4.6588
                                                                   4.5223
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

For the meta-regressions of Expenditure Per Capita, we find no significant moderator. We also run the meta-regressions adding all coefficients in the papers. The results follow below:

```
##
## Multivariate Meta-Analysis Model (k = 74; method: REML)
##
     logLik Deviance
                             AIC
                                        BIC
                                                  AICc
## -189.3432 378.6864 396.6864 416.5287 399.8443
##
## Variance Components:
                       sqrt nlvls fixed
                                                       factor
              estim
## sigma^2.1 0.3126 0.5591
                                9
                                      no
                                                    id_level1
## sigma^2.2 3.6076 1.8994
                                74
                                      no id_level1/id_level2
## Test for Residual Heterogeneity:
## QE(df = 67) = 568.5327, p-val < .0001
```

```
## Test of Moderators (coefficients 2:7):
## F(df1 = 6, df2 = 67) = 4.3658, p-val = 0.0009
## Model Results:
##
                    estimate
                                                           ci.lb
                                                                     ci.ub
                                          tval
                                                  pval
## intrcpt
                   -297.3475 134.2323 -2.2152 0.0302 -565.2764 -29.4187
## indepvar2N
                     -3.7603
                               0.7996 -4.7025 <.0001
                                                          -5.3564
                                                                   -2.1642 ***
## year
                      0.1483
                               0.0671
                                       2.2105 0.0305
                                                          0.0144
                                                                    0.2823
## publishedYes
                      2.3076
                               1.5956 1.4462 0.1528
                                                          -0.8773
                                                                    5.4925
## elecsys2Non-Maj
                      0.9664
                               0.9837 0.9824 0.3294
                                                          -0.9971
                                                                    2.9300
## methodPANEL
                      0.5848
                               1.0259 0.5701 0.5705
                                                          -1.4629
                                                                    2.6325
## methodIV
                     -0.0778
                               0.9670 -0.0804 0.9361
                                                          -2.0080
                                                                    1.8524
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

With all coefficients, the results of the effect sizes on the Expenditure Per Capita regressions are the following:

- 1. Compared with K, models with N tend to detect significantly smaller effects.
- 2. Year has now a positive effect on coefficient sizes.
- 3. All other coefficents were not significant.

## I.2 Meta-Regressions for Log of Expenditure Per Capita

```
##
## Multivariate Meta-Analysis Model (k = 9; method: REML)
##
    logLik Deviance
                          AIC
                                    BIC
                                             ATCc
    3.7595 -7.5189
                     8.4811 1.2700 152.4811
##
## Variance Components:
##
                      sqrt nlvls fixed
                                                      factor
              estim
## sigma^2.1 0.0055 0.0740
                                7
                                                    id_level1
                                      no
## sigma^2.2 0.0000 0.0000
                                     no id_level1/id_level2
                                9
## Test for Residual Heterogeneity:
```

```
## QE(df = 3) = 29.9437, p-val < .0001
##
## Test of Moderators (coefficients 2:6):
## F(df1 = 5, df2 = 3) = 5.9158, p-val = 0.0871
## Model Results:
##
                estimate
                                                     ci.lb
                                                            ci.ub
                                     tval
                                            pval
## intrcpt
                  4.0894 21.1208 0.1936 0.8588 -63.1264 71.3052
## indepvar2logN
                 0.0733 0.1397 0.5243 0.6364
                                                   -0.3714 0.5179
## year
                 -0.0019 0.0105 -0.1839 0.8658
                                                   -0.0354 0.0315
## publishedYes
                 -0.1625 0.0502 -3.2399 0.0479
                                                   -0.3221 -0.0029 *
## methodPANEL
                  0.0453 0.0737 0.6139 0.5827
                                                   -0.1893
## methodRDD
                 -0.1615 0.1164 -1.3870 0.2595
                                                   -0.5320 0.2090
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The only significant result points that published papers tend to report a smaller coefficient than unpublished papers.

Below we also run the meta-regressions adding all coefficients in the papers. The results follow below:

```
##
## Multivariate Meta-Analysis Model (k = 33; method: REML)
##
    logLik Deviance
                          AIC
                                    BIC
                                             AICc
   30.8904 -61.7808 -45.7808 -35.4141 -37.7808
## Variance Components:
##
              estim
                     sgrt nlvls fixed
                                                       factor
## sigma^2.1 0.0023 0.0483
                                7
                                                   id level1
                                      no
## sigma^2.2 0.0038 0.0619
                             33
                                   no id_level1/id_level2
## Test for Residual Heterogeneity:
## QE(df = 27) = 125.5351, p-val < .0001
## Test of Moderators (coefficients 2:6):
## F(df1 = 5, df2 = 27) = 9.7639, p-val < .0001
## Model Results:
```

```
##
                estimate
                                                    ci.lb
                                                            ci.ub
##
                              se
                                     tval
                                            pval
## intrcpt
                -19.1652 14.7647 -1.2980 0.2053 -49.4598 11.1294
                 0.2082 0.0883 2.3566 0.0260
## indepvar2logN
                                                    0.0269
                                                           0.3895
                  0.0096 0.0073 1.3097 0.2013
                                                   -0.0054
                                                           0.0247
## year
## publishedYes
                 -0.0724 0.0457 -1.5846 0.1247
                                                   -0.1661
                                                           0.0213
## methodPANEL
                 -0.1464 0.0450 -3.2527 0.0031
                                                   -0.2388 -0.0541
## methodRDD
                 -0.2192 0.0512 -4.2844 0.0002
                                                  -0.3242 -0.1142 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

With all coefficients, the results of the effect sizes on the Log of Expenditure Per Capita Regressions are the following:

- 1. In terms of the modeling, passing from OLS to PANEL or RDD decreases the detected effects.
- 2. Having the log of lower house seats (logN) as the main independent variable increases the detected effect.

All other results are insignificant.

##

# I.3 Meta-Regressions for Expenditure as a Percentage of the GDP

```
## Multivariate Meta-Analysis Model (k = 11; method: REML)
##
                          AIC
    logLik Deviance
                                    BTC
    8.3335 -16.6669 -0.6669 -3.7914 143.3331
##
## Variance Components:
                      sgrt nlvls fixed
                                                      factor
              estim
## sigma^2.1 0.0004 0.0212
                                8
                                                   id_level1
                                     no
## sigma^2.2 0.0000 0.0000
                               11
                                   no id_level1/id_level2
## Test for Residual Heterogeneity:
## QE(df = 5) = 23.7235, p-val = 0.0002
## Test of Moderators (coefficients 2:6):
## F(df1 = 5, df2 = 5) = 11.0772, p-val = 0.0098
## Model Results:
```

```
##
                  estimate
                                                     ci.lb
                                                             ci.ub
##
                                      tval
                                             pval
## intrcpt
                    8.1390 4.3347
                                   1.8777 0.1192 -3.0036 19.2816
## indepvar2logN
                   -0.0081 0.0378 -0.2148 0.8384 -0.1053
                                                            0.0891
## indepvar2N
                   -0.0094 0.0055 -1.7249 0.1451 -0.0235
                                                            0.0046
                   -0.0030 0.0022 -1.4098 0.2177 -0.0086
                                                             0.0025
## elecsys2Non-Maj -2.0586 0.2964 -6.9446 0.0010 -2.8205 -1.2966 ***
## methodPANEL
                    0.0124 0.0228 0.5440 0.6098 -0.0462
                                                             0.0709
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

We have the following results for the meta-regressions of Expenditure as a Percentage of GDP:

- 1. Passing from Majoritarian to Non-Majoritarian, decreases significantly the effects found in our models.
- 2. All other moderators remain insignificant.

Below we also run the meta-regressions adding all coefficients in the papers. The results follow below:

```
##
## Multivariate Meta-Analysis Model (k = 41; method: REML)
##
     logLik Deviance
                              AIC
                                                  AICc
     89.3969 -178.7939 -162.7939 -150.3511 -157.2554
##
## Variance Components:
##
              estim
                       sqrt nlvls fixed
                                                       factor
## sigma^2.1 0.0004 0.0203
                                                    id_level1
## sigma^2.2 0.0001 0.0102
                                      no id_level1/id_level2
                                41
## Test for Residual Heterogeneity:
## QE(df = 35) = 1217.8992, p-val < .0001
##
## Test of Moderators (coefficients 2:6):
## F(df1 = 5, df2 = 35) = 32.4229, p-val < .0001
##
## Model Results:
                                                      ci.lb ci.ub
                   estimate
##
                                        tval
                                                pval
## intrcpt
                     8.2197 4.0107
                                      2.0495 0.0480
                                                       0.0776 16.3618
```

For all the coefficients, we have the following results:

- 1. Passing from Majoritarian to Non-Majoritarian, decreases significantly the effects found in our models.
- 2. All other moderators remain insignificant.

# J Robustness: Meta-Regressions (All Coefficients)

In this section, we aggregate all the coefficients and run a multivariate meta-regression, controlling for:

- 1. The type of the dependent variable in the study (expenditure per capita, log of the expenditure per capita, and share of government expenditure in the GDP).
- 2. The type of the independent variable in the study (lower house size, upper house size, or log of lower house size).
- 3. The electoral system (Majoritarian versus Non-Majoritarian).
- 4. The year when the study was published.
- 5. Whether the study is a working paper or published work.
- 6. The estimation method used in the paper (OLS, PANEL, IV, or RDD).

The results follow below, and show null effects for all variables, including the intercept.

```
##
## Multivariate Meta-Analysis Model (k = 44; method: REML)
##
## logLik Deviance AIC BIC AICC
## -67.0973 134.1947 160.1947 179.6493 179.3526
##
## Variance Components:
##
```

```
estim
                       sqrt nlvls fixed
                                                        factor
## sigma^2.1 0.0000 0.0001
                                                     id level1
                                21
                                       no
## sigma^2.2 0.1953 0.4420
                                       no id_level1/id_level2
## Test for Residual Heterogeneity:
## QE(df = 33) = 255.2630, p-val < .0001
## Test of Moderators (coefficients 2:11):
## F(df1 = 10, df2 = 33) = 0.6096, p-val = 0.7943
## Model Results:
                                                           ci.lb
                   estimate
                                         tval
                                                 pval
                                                                    ci.ub
## intrcpt
                    -23.1869 38.1315 -0.6081 0.5473 -100.7660 54.3921
## depvar2logExpPC
                    -0.2960
                              0.4029 -0.7346 0.4678
                                                         -1.1157
                                                                   0.5238
## depvar2PCTGDP
                    -0.0108
                              0.3254 -0.0333 0.9736
                                                         -0.6728
                                                                   0.6511
## indepvar2logN
                     0.2944
                              0.4646
                                      0.6336 0.5307
                                                         -0.6508
                                                                   1.2395
## indepvar2N
                    -0.1580
                              0.2597 -0.6083 0.5472
                                                         -0.6863
                                                                   0.3704
                     0.0118
                                       0.6193 0.5400
                                                         -0.0269
                                                                   0.0505
## publishedYes
                    -0.2413
                              0.3184 -0.7578 0.4539
                                                         -0.8890
                                                                   0.4064
## elecsys2Non-Maj
                    -0.0691
                              0.2800 -0.2469 0.8065
                                                         -0.6388
                                                                   0.5005
## methodPANEL
                    -0.0194
                              0.2525 -0.0769 0.9392
                                                         -0.5332
                                                                   0.4944
## methodIV
                    -0.2113
                              0.4310 -0.4902 0.6273
                                                         -1.0881
                                                                   0.6656
                     0.0380
## methodRDD
                              0.4853 0.0782 0.9381
                                                         -0.9495
                                                                   1.0254
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

In the restricted model, with only the main coefficients in the selected papers, no moderator has a significant effect. We also run the meta-regressions adding all coefficients in the papers. The results follow below:

```
## Multivariate Meta-Analysis Model (k = 148; method: REML)
##
##
     logLik Deviance
                              AIC
                                         BIC
                                                   AICc
## -153.0761
              306.1523 332.1523
                                  370.1120
##
## Variance Components:
##
                       sart nlvls fixed
                                                        factor
              estim
## sigma^2.1 0.4606 0.6786
                                                     id_level1
                                21
## sigma^2.2 0.0015 0.0386
                               148
                                       no id_level1/id_level2
```

```
## Test for Residual Heterogeneity:
## QE(df = 137) = 2279.7730, p-val < .0001
## Test of Moderators (coefficients 2:11):
## F(df1 = 10, df2 = 137) = 15.3559, p-val < .0001
## Model Results:
##
                    estimate
                                  se
                                         tval
                                                 pval
                                                          ci.lb
                                                                     ci.ub
## intrcpt
                   -157.2949 28.3337 -5.5515 <.0001 -213.3227 -101.2670 ***
## depvar2logExpPC
                    -1.5450
                              0.1594 -9.6897 <.0001
                                                         -1.8602
                                                                   -1.2297 ***
## depvar2PCTGDP
                      0.0076
                              0.0415 0.1840 0.8543
                                                         -0.0744
                                                                    0.0897
## indepvar2logN
                     1.7495
                              0.1823 9.5985 <.0001
                                                         1.3891
                                                                    2.1099 ***
## indepvar2N
                     -0.0202
                              0.0157 -1.2865 0.2005
                                                         -0.0512
                                                                    0.0108
                      0.0786
                              0.0141 5.5579 <.0001
                                                         0.0506
                                                                    0.1066 ***
## publishedYes
                     -0.2803
                              0.0586 -4.7812 <.0001
                                                         -0.3962
                                                                   -0.1643 ***
## elecsys2Non-Maj
                      0.1601
                              0.3619 0.4423 0.6590
                                                         -0.5556
                                                                    0.8757
## methodPANEL
                     -0.2105
                              0.0337 -6.2531 <.0001
                                                         -0.2771
                                                                   -0.1439 ***
## methodIV
                     -0.0608
                              0.0495 -1.2275 0.2217
                                                         -0.1587
                                                                    0.0371
                     -0.2252 0.0387 -5.8161 <.0001
                                                                   -0.1487 ***
## methodRDD
                                                         -0.3018
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

In the full model, we can see that:

- 1. For the dependent variable, models with Log of Per Capita Expenditure tend to report significantly smaller effects than models with Per Capita Expenditure.
- 2. For the independent variable, models with Log of Lower House Size tend to report significantly larger effects than models with Upper House Size.
- 3. Over time, the reported coefficients have been increasing in size.
- 4. Compared with OLS, Panel and RDD report significantly smaller coefficients.
- 5. All other moderators are insignificant.

## **K** Session Information

```
## R version 4.0.3 (2020-10-10)
```

```
## Platform: x86_64-apple-darwin17.0 (64-bit)
## Running under: macOS Catalina 10.15.7
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/4.0/Resources/lib/libRblas.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/4.0/Resources/lib/libRlapack.dylib
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8
## attached base packages:
## [1] grid
                stats
                          graphics grDevices utils
                                                       datasets methods
## [8] base
##
## other attached packages:
## [1] dmetar_0.0.9000
                           compareGroups_4.5.0 broom_0.7.5
## [4] pander_0.6.3
                           stargazer_5.2.2
                                              magick_2.5.2
## [7] kableExtra_1.3.4
                           ggpubr_0.4.0
                                              gridExtra_2.3
## [10] gridGraphics_0.5-0 knitr_1.31
                                              data.table_1.14.0
## [13] devtools_2.3.2
                           usethis_1.6.3
                                              readxl_1.3.1
## [16] metafor_2.4-0
                           Matrix_1.2-18
                                              meta_4.18-0
## [19] forcats_0.5.0
                           stringr_1.4.0
                                              dplyr_1.0.5
## [22] purrr_0.3.4
                           readr_1.4.0
                                              tidyr_1.1.3
## [25] tibble_3.1.0
                           ggplot2_3.3.3
                                              tidyverse_1.3.0
##
## loaded via a namespace (and not attached):
    [1] uuid_0.1-4
                            backports_1.2.1
                                               systemfonts_1.0.1
##
    [4] splines_4.0.3
                            digest_0.6.27
                                               htmltools_0.5.1.1
##
    [7] fansi_0.4.2
                            magrittr_2.0.1
                                               Rsolnp_1.16
## [10] memoise_1.1.0
                            cluster_2.1.0
                                               openxlsx_4.2.3
  [13] remotes_2.2.0
                            modelr_0.1.8
                                               officer_0.3.17
  [16] svglite_2.0.0
                            prettyunits_1.1.1
                                               colorspace_2.0-0
## [19] rvest_1.0.0
                            ggrepel_0.9.1
                                               haven_2.3.1
  [22] xfun_0.22
                            callr_3.5.1
                                               crayon_1.4.1
## [25] jsonlite_1.7.2
                            lme4_1.1-26
                                               survival_3.2-7
## [28] glue_1.4.2
                            gtable_0.3.0
                                               webshot_0.5.2
## [31] kernlab_0.9-29
                            car_3.0-10
                                               pkgbuild_1.1.0
  [34] DEoptimR_1.0-8
                                               abind_1.4-5
                            prabclus_2.3-2
## [37] scales_1.1.1
                            DBI_1.1.0
                                               rstatix_0.6.0
## [40] Rcpp_1.0.6
                            viridisLite_0.3.0
                                               magic_1.5-9
## [43] foreign_0.8-80
                            mclust_5.4.7
                                               stats4_4.0.3
```

```
[46] netmeta_1.3-0
                             truncnorm_1.0-8
                                                httr_1.4.2
  [49] fpc_2.2-9
                            ellipsis_0.3.1
                                                modeltools_0.2-23
   [52] mice_3.13.0
                             farver_2.1.0
                                                pkgconfig_2.0.3
   [55] flexmix_2.3-17
                            nnet_7.3-14
                                                dbplyr_2.0.0
   [58] utf8_1.2.1
                            labeling_0.4.2
                                                tidyselect_1.1.0
   [61] rlang_0.4.10
                             munsell_0.5.0
                                                 cellranger_1.1.0
   [64] tools_4.0.3
                            cli_2.3.1
                                                generics_0.1.0
   [67] evaluate_0.14
                            yaml_2.2.1
                                                processx_3.4.5
  [70] fs_1.5.0
                             robustbase_0.93-7
                                                zip_2.1.1
   [73] nlme_3.1-149
                            xml2_1.3.2
                                                compiler_4.0.3
   [76] rstudioapi_0.13
                            curl_4.3
                                                 testthat_3.0.0
   [79] ggsignif_0.6.0
                             reprex_0.3.0
                                                 statmod_1.4.35
   [82] stringi_1.5.3
                            HardyWeinberg_1.7.1 highr_0.8
  [85] ps_1.6.0
                            desc_1.2.0
                                                 gdtools_0.2.3
  [88] lattice_0.20-41
                             poibin_1.5
                                                nloptr_1.2.2.2
  [91] vctrs_0.3.6
                            CompQuadForm_1.4.3 pillar_1.5.1
  [94] lifecycle_1.0.0
                            flextable_0.6.4
                                                R6 2.5.0
## [97] MuMIn_1.43.17
                             rio_0.5.16
                                                writexl_1.3.1
## [100] codetools_0.2-16
                             sessioninfo_1.1.1
                                                boot_1.3-25
                             assertthat_0.2.1
## [103] MASS_7.3-53
                                                pkgload_1.1.0
## [106] chron_2.3-56
                             rprojroot_2.0.2
                                                withr_2.4.1
## [109] diptest_0.75-7
                            parallel_4.0.3
                                                hms_0.5.3
## [112] class_7.3-17
                            minqa_1.2.4
                                                rmarkdown_2.7.3
## [115] carData_3.0-4
                            lubridate_1.7.9.2 base64enc_0.1-3
## [118] tinytex_0.30
```

#### References

Borenstein, M., Hedges, L. V., Higgins, J. P., and Rothstein, H. R. (2011). *Introduction to meta-analysis*. John Wiley & Sons. Cited on page 13.

Cheung, M. W.-L. (2014). Modeling dependent effect sizes with three-level meta-analyses: a structural equation modeling approach. *Psychological Methods*, 19(2):211. Cited on page 13.

Cheung, M. W.-L. (2019). A guide to conducting a meta-analysis with non-independent effect sizes. *Neuropsychology review*, 29(4):387–396. Cited on page 13.

Egger, M., Smith, G. D., Schneider, M., and Minder, C. (1997). Bias in meta-analysis detected by a simple, graphical test. *Bmj*, 315(7109):629–634. Cited on pages 14, 16, 19, 21, 22, 24, 26, 27, 29, 31, 35, 39, 41, 43, 45, 46, 49, 50 and 52.

Harrer, M., Cuijpers, P., Furukawa, T., and Ebert, D. (2019). Doing meta-analysis in r: A hands-on guide. *PROTECT Lab Erlangen*. Cited on pages 13 and 14.

Veroniki, A. A., Jackson, D., Viechtbauer, W., Bender, R., Bowden, J., Knapp, G., Kuss, O., Higgins, J. P., Langan, D., and Salanti, G. (2016). Methods to estimate the between-study variance and its uncertainty in meta-analysis. *Research synthesis methods*, 7(1):55–79. Cited on pages 13 and 14.