

ImagesToLARModel, a tool for creation of three-dimensional models from a stack of images

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Abstract

Here we will present a software for creating a three-dimensional model from a stack of images. This can be useful because of the simplicity of these type of representations. In particular a scope of use can be offered by medicine, where there is an enormous number of images but with very complex two-dimensional representations.

This work will use the LAR representation ([[CL13](#)]) with the Julia language, because of its simplicity, showing how it can be used for quickly process image data.

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1 Introduction

This work has the aim to transform a two-dimensional representation of a model (based on a stack of images) into a three-dimensional representation based on the LAR schema. In particular, it will produce a single obj model which can be viewed with standard graphics softwares.

In the past were developed other softwares using same principles (see [PDFJ15]). However, they were optimized for speed and cannot be able to accept huge amounts of data. With the rise of the big data era, we now have more and more data available for research purposes, so softwares must be able to deal with them. A typical hardware environment is based on a cluster of computers where computation can be distributed among a lot of different processes. However, as stated by *Amdahl's law*, the speedup of a program using multiple processors is limited by the time needed for the sequential fraction of the program. So use of parallel techniques for dealing with big data is not important for time performance gain but for memory space gain. In fact, our biggest problem is lack of memory, due to model sizes. As a consequence, every parts of this software is written with the clear objective of minimizing memory usage at the cost of losing something in terms of time performance. So, for example, images will be converted in blocks determined by a grid size (see section 5) among different processes and different machines of the cluster

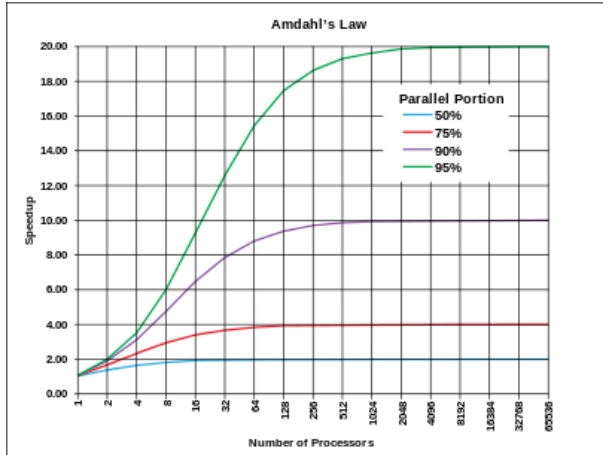


Figure 1: Amdahl's law

1.1 Why Julia

Ricordare che precedenti versioni erano in python

Semplicità

Efficienza

Capacità di realizzare programmi paralleli con poco sforzo

2 Software structure

2.1 Julia packages

This software will be distributed as a Julia Package. For the actual release (Julia 0.4) a package is a simple git project with the structure showed in figure 2



Figure 2: Julia module structure

Source code must be in folder `src`, while in `test` folder there are module tests with a `runtests.jl` for executing them and with a `REQUIRE` file for specifying tests dependencies. For listing dependencies for the entire project, there is another `REQUIRE` file in main folder. As an example in figure 3 there is the `REQUIRE` file for `ImagesToLARMModel.jl`.

After creating this structure for a project it can be pushed on a git repository and installed on Julia systems. The usual installation procedure use this syntax:

```
Pkg.add("Package-name")
```

This will check for that package in METADATA.jl repository on github where there are all official Julia package. However it is also possible to install an unofficial package (on a public git repository) using this syntax:

```
julia 0.3
JSON
Logging
PyCall
Images
Colors
```

Figure 3: REQUIRE contents for `ImagesToLARModel.jl`

```
Pkg.clone("git://repository-address.git")
```

This will install the package on your system with all the dependencies listed in REQUIRE file.

2.2 Architecture of ImagesToLARModel

In previous section we have seen how to create a Julia package for distribute our application. Now we focus on the structure of our application. In `src` folder we can find the following modules:

ImagesToLARModel.jl: main module for the software, it takes input parameters and start images conversion

ImagesConversion.jl: it is called by `ImagesToLARModel.jl` module and controls the entire conversion process calling all other modules

GenerateBorderMatrix.jl: it generates the boundary operator for grid specified in input, saving it in a JSON file

PngStack2Array3dJulia.jl: it is responsible of images loading and conversion into computable data

Lar2Julia.jl: it contains a small subset of LAR functions written in Julia language

LARUtils.jl: it contains utility functions for manipulation of LAR models

Model2Obj.jl: it contains function that manipulates obj files

larcc.py: python larcc module for boundary computation. In next releases of the software it will be rewritten in Julia language

In figure 4 there is a simple schema of dependencies between modules.

Next sections of this document will explain in details all these modules showing also the code involved in conversion

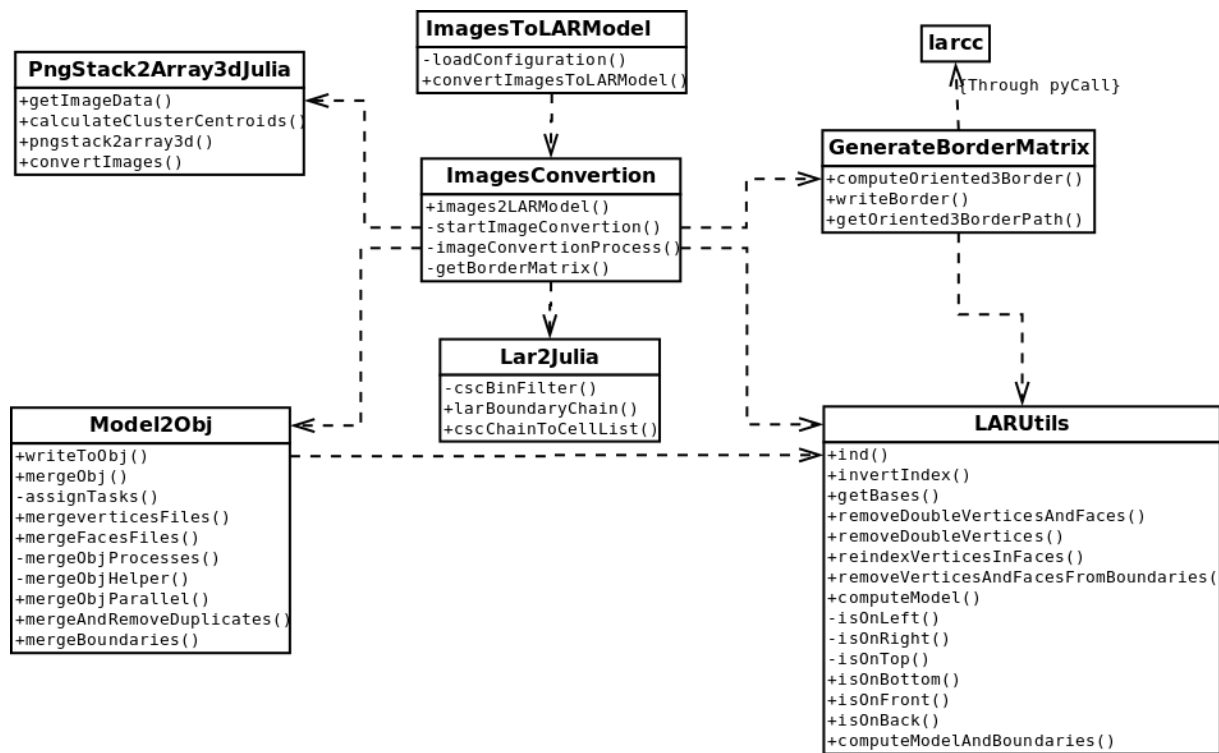


Figure 4: Schema of module dependencies of ImagesToLARModel

3 ImagesToLARModel

This is the main module for the application; it takes the input data and start conversion calling `ImagesConversion.jl`.

3.1 Calling modules

As we have already said, this first module has the responsibility of starting the conversion calling all other modules in the package. In Julia calling modules requires that they are in a path specified by `LOAD_PATH` array. So at the beginning of this module we need to add this line:

```

< update load path 6 > ≡
    push!(LOAD_PATH, Pkg.dir("ImagesToLARModel/src"))
    ◇

```

Fragment referenced in 56a.

`Pkg.dir()` function gives us the path of the Julia installation, so `Pkg.dir("ImagesToLARModel/src")` returns “ $\langle Julia - path \rangle / ImagesToLARModel / src$ ”

After this line we can now import all modules defined here and export public functions:

```
 $\langle modules\ import\ ImagesToLARModel\ 7a \rangle \equiv$   
    import JSON  
    import ImagesConversion  
  
    using Logging  
  
    export convertImagesToLARModel  
  
     $\diamond$ 
```

Fragment referenced in 56a.

3.2 Input loading

Images conversion takes several parameters:

- `inputDirectory`: The path of the directory containing the stack of images
- `outputDirectory`: The path of the directory containing the output
- `bestImage`: Image chosen for centroid computation (see section 4)
- `nx`, `ny`, `nz`: Sizes of the grid chosen for image segmentation (see section 4)
- `DEBUG.LEVEL`: Debug level for Julia logger
- `parallelMerge` (experimental): Choose between sequential or parallel merge of files (see section 9)

Because of their number it has been realized a function for simply loading them from a JSON configuration file; this is the code:

```
 $\langle load\ JSON\ configuration\ 7b \rangle \equiv$   
function loadConfiguration(configurationFile)  
    """  
        load parameters from JSON file  
  
        configurationFile: Path of the configuration file  
    """
```



```

configuration = JSON.parse(configurationFile)

DEBUG_LEVELS = [DEBUG, INFO, WARNING, ERROR, CRITICAL]

parallelMerge = false
try
    if configuration["parallelMerge"] == "true"
        parallelMerge = true
    else
        parallelMerge = false
    end
catch
end

return configuration["inputDirectory"], configuration["outputDirectory"],
        configuration["bestImage"],
        configuration["nx"], configuration["ny"], configuration["nz"],
        DEBUG_LEVELS[configuration["DEBUG_LEVEL"]],
        parallelMerge

end
◇

```

Fragment referenced in 56a.

A valid JSON file has the following structure:

```

{
  "inputDirectory": "Path of the input directory",
  "outputDirectory": "Path of the output directory",
  "bestImage": "Name of the best image (with extension) ",
  "nx": x grid size,
  "ny": y grid size,
  "nz": border z,
  "DEBUG_LEVEL": julia Logging level (can be a number from 1 to 5)
  "parallelMerge": "true" or "false"
}

```

For example, we can write:

```

{
  "inputDirectory": "/home/juser/IMAGES/"
}

```

```

    "outputDirectory": "/home/juser/OUTPUT/",
    "bestImage": "0009.tiff",
    "nx": 2,
    "ny": 2,
    "nz": 2,
    "DEBUG_LEVEL": 2
}

```

As we can see, in a valid JSON configuration file `DEBUG_LEVEL` can be a number from 1 to 5. Instead, when we explicitly define parameters, `DEBUG_LEVEL` can only be one of the following Julia constants:

- `DEBUG`
- `INFO`
- `WARNING`
- `ERROR`
- `CRITICAL`

3.3 Starting conversion

As we have already said, this module has the only responsibility to collect data input and starts other modules. These are the functions that start the process and the only exposed to the application users:

```

⟨ Start conversion from JSON file 9 ⟩ ≡
function convertImagesToLARModel(configurationFile)
    """
        Start conversion of a stack of images into a 3D model
        loading parameters from a JSON configuration file

        configurationFile: Path of the configuration file
    """
    inputDirectory, outputDirectory, bestImage, nx, ny, nz,
        DEBUG_LEVEL, parallelMerge = loadConfiguration(open(configurationFile))
    convertImagesToLARModel(inputDirectory, outputDirectory, bestImage,
        nx, ny, nz, DEBUG_LEVEL, parallelMerge)
end
◇

```

Fragment referenced in 56a.

$\langle \textit{Start manual conversion 10} \rangle \equiv$

```
function convertImagesToLARModel(inputDirectory, outputDirectory, bestImage,
                                nx, ny, nz, DEBUG_LEVEL = INFO, parallelMerge = false)
    """
    Start conversion of a stack of images into a 3D model

    inputDirectory: Directory containing the stack of images
    outputDirectory: Directory containing the output
    bestImage: Image chosen for centroids computation
    nx, ny, nz: Border dimensions (Possibly the biggest power of two of images dimensions)
    DEBUG_LEVEL: Debug level for Julia logger. It can be one of the following:
        - DEBUG
        - INFO
        - WARNING
        - ERROR
        - CRITICAL
    """
    # Create output directory
    try
        mkpath(outputDirectory)
    catch
    end

    Logging.configure(level=DEBUG_LEVEL)
    ImagesConversion.images2LARModel(nx, ny, nz, bestImage,
                                     inputDirectory, outputDirectory, parallelMerge)
end
◇
```

Fragment referenced in 56a.

4 PngStack2Array3dJulia

This module has the responsibility of convert a png image into an array of values that will be passed to other modules

4.1 Module imports

These are modules needed for this part of the package and the public functions exported

```

⟨ modules import PngStack2Array3dJulia 11a ⟩ ≡
    using Images # For loading png images
    using Colors # For grayscale images
    using PyCall # For including python clustering
    using Logging
    @pyimport scipy.ndimage as ndimage
    @pyimport scipy.cluster.vq as cluster

    NOISE_SHAPE_DETECT=10

    export calculateClusterCentroids, pngstack2array3d, getImageData, convertImages
    ◇

```

Fragment referenced in 78a.

We need `Images` and `Colors` packages for manipulating png images and `PyCall` for using Python functions for clustering and filtering images. As a consequence, we need a python environment with `scipy` to be able to run the package

4.2 Convert input to png

First thing to do in our program is getting our input folder and convert the stack of images into png format. This process lets us to avoid managing an enormous variety of formats during computation, simplifying code used for transformation.

Conversion needs the following parameters:

- `inputPath`: path of the folder containing the original images
- `outputPath`: path where we will save png images
- `bestImage`: name of the image chosen for centroids computing (see section 4.4)

After conversion `outputPath` will contain our png images and the function will return the new name chosen for the best image.

Now we can examine single parts of conversion process. First of all we need to specify a new name for images, keeping the right order between them; so we need to define a prefix based on number of images:

```

⟨ Define string prefix 11b ⟩ ≡

```

```

imageFiles = readdir(inputPath)
numberOfImages = length(imageFiles)
outputPrefix = ""
for i in 1: length(string(numberOfImages)) - 1
    outputPrefix = string(outputPrefix,"0")
end ◇

```

Fragment referenced in 14.

Next we need to open the single image doing the following operations:

1. Open images using `Images` library (which relies on `ImageMagick`) and save them in greyscale png format
2. if one or both dimensions of the image are odd we need to remove one row (or column) of pixels to make it even. This will be more clear when we will introduce the grid for parallel computation (see section 5)

⟨ Greyscale conversion 12a ⟩ ≡

```

rgb_img = convert(Image{ColorTypes.RGB}, img)
gray_img = convert(Image{ColorTypes.Gray}, rgb_img) ◇

```

Fragment referenced in 14.

As we can see, we first need to convert image to RGB and then reconvert to greyscale. Without the RGB conversion these rows will return a stackoverflow error due to the presence of alpha channel

⟨ Image resizing 12b ⟩ ≡

```

# resizing images if they do not have even dimensions
dim = size(img)
if(dim[1] % 2 != 0)
    debug("Image has odd x; resizing")
    xrange = 1: dim[1] - 1
else
    xrange = 1: dim[1]
end

if(dim[2] % 2 != 0)
    debug("Image has odd y; resizing")
    yrange = 1: dim[2] - 1
end

```

```

else
    yrange = 1: dim[2]
end

img = subim(gray_img, xrange, yrange) ◇

```

Fragment referenced in 14.

Next we just have to search for the best image and add one image if they are odd (for same reasons we need even image dimensions)

```

⟨ Search for best image 13a ⟩ ≡
# Searching the best image
if(imageFile == bestImage)
    newBestImage = string(outputPrefix[length(string(imageNumber)):end],
                           imageNumber, ".png")
end
imageNumber += 1 ◇

```

Fragment referenced in 14.

```

⟨ Add one image 13b ⟩ ≡
# Adding another image if they are odd
if(numberOfImages % 2 != 0)
    debug("Odd images, adding one")
    imageWidth, imageHeight = getImageData(string(outputPath, "/", newBestImage))

    if(imageWidth % 2 != 0)
        imageWidth -= 1
    end

    if(imageHeight % 2 != 0)
        imageHeight -= 1
    end

    imArray = zeros(UInt8, imageWidth, imageHeight)
    img = grayim(imArray)
    outputFilename = string(outputPath, "/",
                             outputPrefix[length(string(imageNumber)):end], imageNumber, ".png")
    imwrite(img, outputFilename)
end ◇

```

Fragment referenced in 14.

Finally this is the code for the entire function:

```
< Convert to png 14 > ≡
function convertImages(inputPath, outputPath, bestImage)
    """
    Get all images contained in inputPath directory
    saving them in outputPath directory in png format.
    If images have one of two odd dimensions, they will be resized
    and if folder contains an odd number of images another one will be
    added

    inputPath: Directory containing input images
    outputPath: Temporary directory containing png images
    bestImage: Image chosen for centroids computation

    Returns the new name for the best image
    """

< Define string prefix 11b >

    newBestImage = ""
    imageNumber = 0
    for imageFile in imageFiles
        img = imread(string(inputPath, imageFile))
        < Greyscale conversion 12a >
        < Image resizing 12b >
        outputFilename = string(outputPath, outputPrefix[length(string(imageNumber)):end],
                                imageNumber, ".png")
        imwrite(img, outputFilename)

        < Search for best image 13a >

    end

    < Add one image 13b >

    return newBestImage
end
◇
```

Fragment referenced in 78a.

4.3 Getting data from a png

Now we need to load information data from png images. In particular we are interested in getting width and height of an image. As stated in [W3C] document, a standard PNG file contains a *signature* followed by a sequence of *chunks* (each one with a specific type).

The signature always contain the following values:

137 80 78 71 13 10 26 10

This signature indicates that the remainder of the datastream contains a single PNG image, consisting of a series of chunks beginning with an IHDR chunk and ending with an IEND chunk. Every chunk is preceded by four bytes indicating its length.

As we are interested in width and height we need to parse the IHDR chunk. It is the first chunk in PNG datastream and its type field contains the decimal values:

73 72 68 82

The header also contains:

Width	4 bytes
Height	4 bytes
Bit depth	1 bytes
Color type	1 byte
Compression method	1 byte
Filter method	1 byte
Interlace method	1 byte

So for reading width and height we need first 24 bytes; the first eight contain the signature, then we have four bytes for length, four bytes for the type field and eight bytes for information we are interested in. This is the code:

```
< Get image data 15 > ≡  
function getImageData(imageFile)  
    ""  
    Get width and height from a png image  
    ""  
  
    input = open(imageFile, "r")  
    data = readbytes(input, 24)  
  
    if (convert(Array{Int},data[1:8]) != reshape([137 80 78 71 13 10 26 10],8))  
        error("This is not a valid png image")  
    end
```



```

w = data[17:20]
h = data[21:24]

width = reinterpret{Int32, reverse(w)}[1]
height = reinterpret{Int32, reverse(h)}[1]

close(input)

return width, height
end
◇

```

Fragment referenced in 78a.

4.4 Centroids computation

As we have seen above, this package uses greyscale images for conversion into three-dimensional models and for next steps we need binary images so we can distinguish between the background and the model we want to represent. We can use clustering techniques for obtaining this result. First step is centroids calculation from a chosen image (this choice must be made from the user, because we cannot know in advance what is the best image for finding clusters). Moreover we compute these centroids only for an image and then reuse them when we want to cluster all other images, saving processing time. Actually we need only two centroids, because next steps should only recognize between background and foreground pixels. This is the code used for centroid computation:

```

⟨ Centroid computation 16 ⟩ ≡
function calculateClusterCentroids(path, image, numberOfClusters = 2)
    """
    Loads an image and calculate cluster centroids for segmentation

    path: Path of the image folder
    image: name of the image
    numberOfClusters: number of desired clusters
    """
    imageFilename = string(path, image)

    img = imread(imageFilename) # Open png image with Julia Package

    imArray = raw(img)

    imageWidth = size(imArray)[1]

```

```

imageHeight = size(imArray)[2]

# Getting pixel values and saving them with another shape
image3d = Array{Array{UInt8,2}, 0}

# Inserting page on another list and reshaping
push!(image3d, imArray)
pixel = reshape(image3d[1], (imageWidth * imageHeight), 1)

centroids,_ = cluster.kmeans(pixel, numberOfClusters)

return centroids

end
◇

```

Fragment referenced in 78a.

4.5 Transform pixels to three-dimensional array

Now we can study the most important part of this module, where images are converted into data usable by other modules for the creation of the three-dimensional model. The basic concept consists in transforming every single pixel in an integer value representing color, and then clustering them all using centroids computed earlier. So, we can obtain a matrix containing only two values (the two centroids) representing background and foreground of the image.

Now we will follow the code. This function uses four parameters

- path: Path of the images directory
- minSlice: First image to read
- maxSlice: Last image to read
- centroids: Array containing centroids for clustering

For every image we want to transform in the interval [minSlice, maxSlice) we have to read it from disk and save pixel informations into a multidimensional Array:

```

⟨ Read raw data 17 ⟩ ≡
    img = imread(imageFilename) # Open png image with Julia Package
    imArray = raw(img) # Putting pixel values into RAW 3d array ◇

```

Fragment referenced in 20.

The `Images.jl raw` function, get all pixel values saving them in an Array. In Figure 7 we can see how the array will be like for a sample greyscale image.

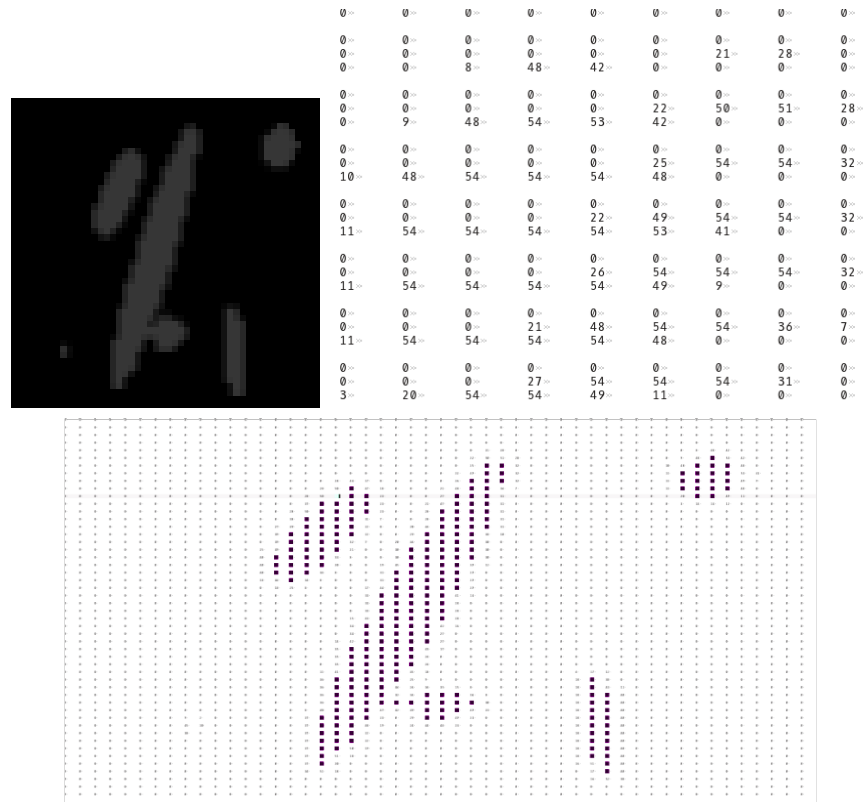


Figure 5: Reading raw data from image. (a) Original greyscale image (b) A view of raw data array (c) The entire raw data array with main color highlighted

Next we have to reduce noise on the image. The better choice is using a *median filter* from package `scipy.ndimage` because it preserves better the edges of the image:

```
⟨ Reduce noise 18 ⟩ ≡
    # Denoising
    image3d[page] = ndimage.median_filter(image3d[page], NOISE_SHAPE_DETECT) ◇
```

Fragment referenced in 20.

Where image3d is an array containing all raw data from images

Finally we have to compute clusters (using `scipy`) obtaining images with only two values:

```

< Clustering images 19 > ≡
# Image Quantization
debug("page = ", page)
debug("image3d[page] dimensions: ", size(image3d[page])[1], "\t", size(image3d[page])[2])
pixel = reshape(image3d[page], size(image3d[page])[1] * size(image3d[page])[2] , 1)
qnt,_ = cluster.vq(pixel,centroids)

# Reshaping quantization result
centers_idx = reshape(qnt, size(image3d[page],1), size(image3d[page],2))
#centers_idx = reshape(qnt, size(image3d[page]))

# Inserting quantized values into 3d image array
tmp = Array{UInt8, size(image3d[page],1), size(image3d[page],2))

for j in 1:size(image3d[1],2)
    for i in 1:size(image3d[1],1)
        tmp[i,j] = centroids[centers_idx[i,j] + 1]
    end
end

image3d[page] = tmp ◊

```

Fragment referenced in 20.



Figure 6: Image transformation. (a) Original greyscale image (b) Denoised image (c) Two-colors image

This is the complete code:

$\langle \text{Pixel transformation 20} \rangle \equiv$

```
function pngstack2array3d(path, minSlice, maxSlice, centroids)
    """
    Import a stack of PNG images into a 3d array

    path: path of images directory
    minSlice and maxSlice: number of first and last slice
    centroids: centroids for image segmentation
    """

    # image3d contains all images values
    image3d = Array{Array{UInt8,2}, 0}

    debug("maxSlice = ", maxSlice, " minSlice = ", minSlice)
    files = readdir(path)

    for slice in minSlice : (maxSlice - 1)
        debug("slice = ", slice)
        imageFilename = string(path, files[slice + 1])
        debug("image name: ", imageFilename)
         $\langle \text{Read raw data 17} \rangle$ 
        debug("imArray size: ", size(imArray))

        # Inserting page on another list and reshaping
        push!(image3d, imArray)

    end

    # Removing noise using a median filter and quantization
    for page in 1:length(image3d)

         $\langle \text{Reduce noise 18} \rangle$ 

         $\langle \text{Clustering images 19} \rangle$ 

    end

    return image3d
end
 $\diamond$ 
```

Fragment referenced in 78a.

5 ImagesConversion

Now we will study the most important module for this package: `ImagesConversion`. It has the responsibility of doing the entire conversion process delegating tasks to the other modules.

5.1 General algorithm

Now we will examine, in a general way, the algorithm used for conversion from a two-dimensional to a three-dimensional representation of our biomedical models.

We have already seen in section 4 how to get information from a png image, obtaining arrays with only two values; one for the **background** color and one for **foreground** color. This is only the first step of the complete conversion process.

Now we focus only on a single image of the stack. Our two-dimensional representation, consists of pixels of two different colors (where only the one associated with foreground is significant); so we can obtain a three-dimensional representation simply replacing every foreground pixel with a small cube. Focusing on the entire stack of images, the full three-dimensional representation can be obtained simply overlapping all the image representations

This algorithm is very simple, however we does not considered problems concerning lack of memory. In fact, we could have images so big that we cannot build these models entirely in memory; moreover they would require a lot of CPU time for computation. A good solution to these problems consists in taking our representation based on images and divide according to a **grid**.

So, instead of converting the entire model with a unique process, we can subdivide the input among a lot of processes, where every process will execute the conversion process on a small number of **blocks** according to the grid subdivision.

Summing up we can define the following terms, which will be used in next parts of this documentation:

- **Grid:** It is the subdivision of the entire stack of images, with sizes defined by the user. They should be powers of two (for increasing performance during border matrix computation which we will see in section 6)
- **Block:** It is a single cell of the grid
- **xBlock:** It is the x-coordinate of a block
- **yBlock:** It is the y-coordinate of a block



Figure 7: The grid used for parallel computation (a) 2D grid on a single image (b) 3D grid for the stack of images

- **zBlock:** It is the z-coordinate of a block

$xBlock$ and $yBlock$ are defined on a single image, while $zBlock$ is defined on different images; in the code it will often be replaced by terms **StartImage** and **EndImage**, which indicate the first image and the last image of that block respectively.

In next subsections we will examine the conversion algorithm in detail, showing what happens for every block of the grid.

5.2 Module imports

These are modules needed for this part of the package and the public functions exported.

```

⟨ modules import ImagesConversion 22 ⟩ ≡
    import GenerateBorderMatrix
    import PngStack2Array3dJulia
    import Lar2Julia
    import Model2Obj
    import LARUtils

    using Logging

    export images2LARModel
    ◇

```

Fragment referenced in 56b.

5.3 Data preparation

As a first thing, we will see how to prepare our data for conversion process. Firstly we need to convert input images to greyscale png; so we need to create a temporary directory for saving them.

Later, we need to compute the LAR boundary operator for finding boundaries of our cells (for the generation see section 6) getting width and height from our images.

Finally we can start conversion with all these parameters calling `startImageConversion` function, which will be explained in next subsection.

⟨main function for ImagesConversion 23⟩ \equiv

```
function images2LARModel(nx, ny, nz, bestImage,
                        inputDirectory, outputDirectory, parallelMerge)
    """
    Convert a stack of images into a 3d model
    """

    info("Starting model creation")

    numberOfClusters = 2 # Number of clusters for
                        # images segmentation

    info("Moving images into temp directory")
    try
        mkdir(string(outputDirectory, "TEMP"))
    catch
    end

    tempDirectory = string(outputDirectory, "TEMP/")

    newBestImage = PngStack2Array3dJulia.convertImages(inputDirectory, tempDirectory,
                                                         bestImage)

    imageWidth, imageHeight = PngStack2Array3dJulia.getImageData(
                                string(tempDirectory, newBestImage))
    imageDepth = length(readdir(tempDirectory))

    # Computing border matrix
    info("Computing border matrix")
    try
```



```

        mkdir(string(outputDirectory, "BORDERS"))
    catch
    end
    borderFilename = GenerateBorderMatrix.getOriented3BorderPath(
        string(outputDirectory, "BORDERS"), nx, ny, nz)

    # Starting images conversion and border computation
    info("Starting images conversion")
    startImageConversion(tempDirectory, newBestImage, outputDirectory, borderFilename,
        imageHeight, imageWidth, imageDepth,
        nx, ny, nz,
        numberOfClusters, parallelMerge)

end
◇

```

Fragment referenced in 56b.

5.4 Images conversion

Now we can see how conversion of images works. First of all we compute the centroids from the best image using module `PngStack2Array3dJulia` and then get the previously computed border matrix in csc sparse array format

```

⟨ compute centroids and get border matrix 24 ⟩ ≡
    # Create clusters for image segmentation
    info("Computing image centroids")
    debug("Best image = ", bestImage)
    centroidsCalc = PngStack2Array3dJulia.calculateClusterCentroids(sliceDirectory,
        bestImage, numberOfClusters)
    debug(string("centroids = ", centroidsCalc))

    try
        mkdir(string(outputDirectory, "BORDERS"))
    catch
    end
    debug("Opening border file: border_", imageDx, "-", imageDy, "-", imageDz, ".json")
    boundaryMat = GenerateBorderMatrix.getBorderMatrix(
        string(outputDirectory, "BORDERS/", "border_",
            imageDx, "-", imageDy, "-", imageDz, ".json"))
◇

```

Fragment referenced in 26.

Now we can start the conversion process.

First of all we need to iterate on the grid finding the zBlock coordinate; we saw earlier that the *imageDz* parameter must be a divisor of the image depth, so we will have exactly *imageDepth/imageDz* blocks on the z coordinate. Moreover, at every zBlock correspond a startImage and an endImage where *endImage - startImage = imageDz*.

Now we can simply parallelize the conversion process spawning a new process for every zBlock, so we open at most *imageDz* images for process.

This is the code for the first part of conversion.

```
< conversion parallelization 25a > ≡  
    beginImageStack = 0  
    endImage = beginImageStack  
  
    info("Converting images into a 3d model")  
    tasks = Array(RemoteRef, 0)  
    for zBlock in 0:(imageDepth / imageDz - 1)  
        startImage = endImage  
        endImage = startImage + imageDz  
        info("StartImage = ", startImage)  
        info("endImage = ", endImage)  
  
        task = @spawn imageConversionProcess(sliceDirectory, outputDirectory,  
                                              beginImageStack, startImage, endImage,  
                                              imageDx, imageDy, imageDz,  
                                              imageHeight, imageWidth,  
                                              centroidsCalc, boundaryMat)  
  
        push!(tasks, task)  
    end  
    ◇
```

Fragment referenced in 26.

All processes produce a lot of files containing three-dimensional models of a block, so after their termination, we should merge the boundaries between blocks (see later for a better explanation), the remaining boundaries with their block and all resulting model files as we can see in this piece of code:

```
< final file merge 25b > ≡  
    info("Merging boundaries")  
    # Merge Boundaries files  
    Model2Obj.mergeBoundaries(string(outputDirectory, "MODELS"),
```

```

        imageHeight, imageWidth, imageDepth,
        imageDx, imageDy, imageDz)

info("Merging blocks")
Model2Obj.mergeBlocks(string(outputDirectory, "MODELS"),
        imageHeight, imageWidth, imageDepth,
        imageDx, imageDy, imageDz)

info("Merging obj models")
if parallelMerge
    Model2Obj.mergeObjParallel(string(outputDirectory, "MODELS"))
else
    Model2Obj.mergeObj(string(outputDirectory, "MODELS"))
end
◇

```

Fragment referenced in 26.

This is the final code for this function:

$\langle \text{start conversion of images 26} \rangle \equiv$

```

function startImageConversion(sliceDirectory, bestImage, outputDirectory, borderFilename,
        imageHeight, imageWidth, imageDepth,
        imageDx, imageDy, imageDz,
        numberOfClusters, parallelMerge)

    """
    Support function for converting a stack of images into a model

    sliceDirectory: directory containing the image stack
    imageForCentroids: image chosen for centroid computation
    """

     $\langle \text{compute centroids and get border matrix 24} \rangle$ 
     $\langle \text{conversion parallelization 25a} \rangle$ 
    # Waiting for tasks completion
    for task in tasks
        wait(task)
    end
     $\langle \text{final file merge 25b} \rangle$ 
    end
    ◇

```

Fragment referenced in 56b.

5.4.1 Images conversion (for single process)

After we have sketchily studied images conversion, now we will see in details what happens for every process. First thing to do is read an image calling the `PngStack2Array3dJulia`, after that is necessary to sort the centroid array for choosing correct background and foreground pixels.

```
< image read and centroids sort 27a > ≡
    info("Transforming png data into 3d array")
    theImage = PngStack2Array3dJulia.pngstack2array3d(sliceDirectory,
                                                    startImage, endImage, centroids)

    centroidsSorted = sort(vec(reshape(centroids, 1, 2)))
    background = centroidsSorted[1]
    foreground = centroidsSorted[2]
    debug(string("background = ", background, " foreground = ", foreground))
    ◇
```

Fragment referenced in 30b.

Now we can start iterating on other blocks of the grid getting the corresponding slice of the image:

```
< get image slice 27b > ≡
    # Getting a slice of theImage array

    image = Array{UInt8, (convert{Int, length(theImage)},
                          convert{Int, xEnd - xStart}, convert{Int, yEnd - yStart}))
    debug("image size: ", size(image))
    for z in 1:length(theImage)
        for x in 1 : (xEnd - xStart)
            for y in 1 : (yEnd - yStart)
                image[z, x, y] = theImage[z][x + xStart, y + yStart]
            end
        end
    end
    ◇
```

Fragment referenced in 30b.

Here $xStart$ and $yStart$ are the absolute coordinates of the model and are calculated from the block coordinates. At the end of this process, we have an array called `image` with size $(imageDz, imageDx, imageDy)$.

Now we can get the value of the single pixel into this array and, if it represents a foreground point, put it into an array called `chain3D`. This structure contains indexes of the linearized array created from the matrix. In Figure 8 there is a sample conversion from the matrix to the array

$$\begin{pmatrix} 0^0 & 0^2 \\ 0^1 & 0^3 \end{pmatrix} \begin{pmatrix} 46^4 & 0^6 \\ 46^5 & 46^7 \end{pmatrix} \rightarrow 0^0 \ 0^1 \ 0^2 \ 0^3 \ 46^4 \ 46^5 \ 0^6 \ 46^7$$

$$\begin{pmatrix} 0^0 & 0^2 \\ 0^1 & 0^3 \end{pmatrix} \begin{pmatrix} 0^4 & 46^6 \\ 46^5 & 46^7 \end{pmatrix} \rightarrow 0^0 \ 0^1 \ 0^2 \ 0^3 \ 0^4 \ 46^5 \ 46^6 \ 46^7$$

Figure 8: Transformation of a matrix resulting from a 2x2x2 grid into a linearized array (with cells indexes) (a) First example (b) Second example

As we can see from that figure, from a 2x2x2 grid we can obtain eight values for the single block (or **cell**), where the indexes for the foreground pixels represent indexes of non-empty cells in a 2x2x2 cuboidal geometry

This is the code for getting foreground pixels:

```

⟨ get foreground pixels 28 ⟩ ≡
  nz, nx, ny = size(image)
  chains3D = Array(UInt8, 0)
  zStart = startImage - beginImageStack
  for y in 0:(ny - 1)
    for x in 0:(nx - 1)
      for z in 0:(nz - 1)
        if(image[z + 1, x + 1, y + 1] == foreground)
          push!(chains3D, y + ny * (x + nx * z))
        end
      end
    end
  end
  ◇

```

Fragment referenced in 30b.

Now we have full cells for the geometry, we can convert it into a full *LAR model*. In particular, we are interested in cell boundaries for every block (as we want to obtain only the boundaries for the final model) so we can call function `larBoundaryChain` from

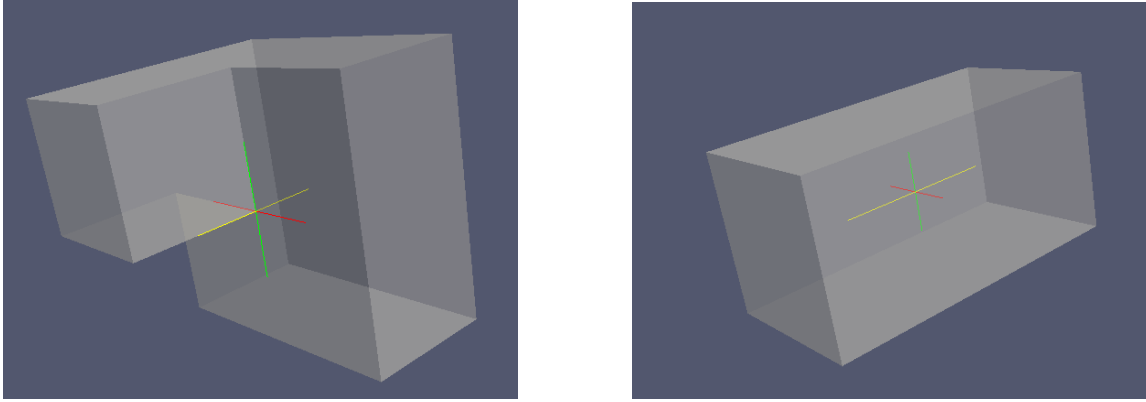


Figure 9: Sample models of 2x2x2 blocks

`Lar2Julia` module (which will be explained in section 7). In Figure 9 there are some examples of models extracted from a single $2 \times 2 \times 2$ block.

After model computation, next step is getting vertices and faces from model cells writing results to file. However, as we have already said, we are only interested in boundaries of the final model while now we have only boundaries of a single block. Consequently, we have to separate boundaries from the inner faces of the block on different files (boundaries separation will be explained in section 8). As we can see later, we will merge boundaries together deleting common faces on both block borders, obtaining a model without internal faces. These are pieces of code for getting the inner block model and the boundaries and for file writing:

⟨get inner model and boundaries 29⟩ \equiv

```
# IMPORTANT: inverting xStart and yStart for obtaining correct rotation of the model
models = LARUtils.computeModelAndBoundaries(imageDx, imageDy, imageDz,
                                              yStart, xStart, zStart, objectBoundaryChain)

V, FV = models[1][1] # inside model
V_left, FV_left = models[2][1]
V_right, FV_right = models[3][1] # right boundary
V_top, FV_top = models[4][1] # top boundary
V_bottom, FV_bottom = models[5][1] # bottom boundary
V_front, FV_front = models[6][1] # front boundary
V_back, FV_back = models[7][1] # back boundary
◇
```

Fragment referenced in 30b.

< write block models to file 30a > ≡

```
# Writing all models on disk
model_outputFilename = string(outputDirectory, "MODELS/model_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V, FV, model_outputFilename)

left_outputFilename = string(outputDirectory, "MODELS/left_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V_left, FV_left, left_outputFilename)

right_outputFilename = string(outputDirectory, "MODELS/right_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V_right, FV_right, right_outputFilename)

top_outputFilename = string(outputDirectory, "MODELS/top_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V_top, FV_top, top_outputFilename)

bottom_outputFilename = string(outputDirectory, "MODELS/bottom_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V_bottom, FV_bottom, bottom_outputFilename)

front_outputFilename = string(outputDirectory, "MODELS/front_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V_front, FV_front, front_outputFilename)

back_outputFilename = string(outputDirectory, "MODELS/back_output_", xBlock,
                              "-", yBlock, "_", startImage, "_", endImage)
Model2Obj.writeToObj(V_back, FV_back, back_outputFilename)
```

◇

Fragment referenced in 30b.

< image conversion process 30b > ≡

```
function imageConversionProcess(sliceDirectory, outputDirectory,
                               beginImageStack, startImage, endImage,
                               imageDx, imageDy, imageDz,
                               imageHeight, imageWidth,
                               centroids, boundaryMat)

    ""
    Support function for converting a stack of image on a single
    independent process
    ""
```

⟨ image read and centroids sort 27a ⟩

```
for xBlock in 0:(imageHeight / imageDx - 1)
  for yBlock in 0:(imageWidth / imageDy - 1)
    yStart = xBlock * imageDx
    xStart = yBlock * imageDy
    xEnd = xStart + imageDx
    yEnd = yStart + imageDy
    debug("*****")
    debug(string("xStart = ", xStart, " xEnd = ", xEnd))
    debug(string("yStart = ", yStart, " yEnd = ", yEnd))
    debug("theImage dimensions: ", size(theImage)[1], " ",
          size(theImage[1])[1], " ", size(theImage[1])[2])
```

⟨ get image slice 27b ⟩

⟨ get foreground pixels 28 ⟩

```
if(length(chains3D) != 0)
  # Computing boundary chain
  debug("chains3d = ", chains3D)
  debug("Computing boundary chain")
  objectBoundaryChain = Lar2Julia.larBoundaryChain(boundaryMat, chains3D)
  debug("Converting models into obj")
  try
    mkdir(string(outputDirectory, "MODELS"))
  catch
  end
  ⟨ get inner model and boundaries 29 ⟩
```

⟨ write block models to file 30a ⟩

```
else
  debug("Model is empty")
end
end
end
end ◇
```

Fragment referenced in 56b.

6 GenerateBorderMatrix

This module has the responsibility of generating the border matrix operator for models boundary computation.

6.1 Module imports

These are modules needed for this part of the package and the public functions exported

```
< modules import GenerateBorderMatrix 32a > ≡
import LARUtils
using PyCall

import JSON

export computeOriented3Border, writeBorder, getOriented3BorderPath

@pyimport sys
# Search for python modules in package folder
unshift!(PyVector(pyimport("sys")["path"]), Pkg.dir("ImagesToLARModel/src"))
@pyimport larcc # Importing larcc from local folder
@pyimport scipy.sparse as Pysparse ◇
```

Fragment referenced in 57a.

We can notice some lines for importing `larcc` python library, which will be used in subsection [6.5](#)

6.2 Get border matrix from file

As we have already seen in previous sections, we need to compute boundaries for every block of the model grid. This can be done using the topological boundary operator from LAR package. However, the resulting matrix depends only on grid sizes; so it could be reused for other models. Consequently first time we need a border operator we compute it and then save it on disk for next conversions. This function does that work searching for a file containing the border and, if it does not exist, calculate and save it:

```
< get Border matrix 32b > ≡
function getOriented3BorderPath(borderPath, nx, ny, nz)
    """
    Try reading 3-border matrix from file. If it fails matrix
    is computed and saved on disk in JSON format
```

```

borderPath: path of border directory
nx, ny, nz: image dimensions
"""

filename = string(borderPath, "/border_", nx, "-", ny, "-", nz, ".json")
if !isfile(filename)
    border = computeOriented3Border(nx, ny, nz)
    writeBorder(border, filename)
end
return filename

end ◇

```

Fragment referenced in 57a.

6.3 Write border matrix on file

We have already seen that for performance reasons border operator matrix is saved on file; here we will see code used for this scope. Firstly, we have defined a function `writeBorder`, which takes as parameters a `PyObject` containing a matrix (computed in subsection 6.4) and the output file path.

```

⟨ write Border matrix 33 ⟩ ≡
function writeBorder(boundaryMatrix, outputFile)
    """
    Write 3-border matrix on json file

    boundaryMatrix: matrix to write on file
    outputFile: path of the outputFile
    """

    rowcount = boundaryMatrix[:shape][1]
    colcount = boundaryMatrix[:shape][2]

    row = boundaryMatrix[:indptr]
    col = boundaryMatrix[:indices]
    data = boundaryMatrix[:data]

    # Writing informations on file
    outfile = open(outputFile, "w")

    matrixObj = MatrixObject(rowcount, colcount, row, col, data)

```

```

JSON.print(outfile, matrixObj)
close(outfile)

```

end ◇

Fragment referenced in 57a.

We can see that, in final JSON file, we write an object called `MatrixObject` which has the following definition:

```

⟨ Matrix object for JSON file 34a ⟩ ≡
    type MatrixObject
        ROWCOUNT
        COLCOUNT
        ROW
        COL
        DATA
    end ◇

```

Fragment referenced in 57a.

6.4 Compute border matrix

Here we can see code used for computation of the border operator. As we can see, we call the python `larcc` module, from the `LAR` module, which returns a `PyObject` containing a *sparse csr matrix*. In next versions this function will be probably changed and the code for boundary computation will be moved in `LAR2Julia` module (also transforming all `csr` matrix in `csc` matrix) avoiding python calls.

```

⟨ compute border matrix 34b ⟩ ≡
    # Compute the 3-border operator
    function computeOriented3Border(nx, ny, nz)
        """
        Compute the 3-border matrix using a modified
        version of larcc
        """
        V, bases = LARUtils.getBases(nx, ny, nz)
        boundaryMat = larcc.signedCellularBoundary(V, bases)
        return boundaryMat
    end ◇

```

Fragment referenced in 57a.

6.5 Transform border matrix

We have seen that matrix stored in JSON file was in csr matrix as it was returned from `larcc` module of LAR library. However, Julia has only sparse matrices in csc format, so we need a function for loading the contents of JSON file converting the output for next uses with Julia libraries. When porting of `larcc` in Julia will be complete, we can safely remove this function

```
< transform border matrix in csc format 35 > ≡  
function getBorderMatrix(borderFilename)  
    """  
    TO REMOVE WHEN PORTING OF LARCC IN JULIA IS COMPLETED  
  
    Get the border matrix from json file and convert it in  
    CSC format  
    """  
    # Loading borderMatrix from json file  
    borderData = JSON.parsefile(borderFilename)  
    row = Array{Int64, length(borderData["ROW"])}  
    col = Array{Int64, length(borderData["COL"])}  
    data = Array{Int64, length(borderData["DATA"])}  
  
    for i in 1: length(borderData["ROW"])  
        row[i] = borderData["ROW"][i]  
    end  
  
    for i in 1: length(borderData["COL"])  
        col[i] = borderData["COL"][i]  
    end  
  
    for i in 1: length(borderData["DATA"])  
        data[i] = borderData["DATA"][i]  
    end  
  
    # Converting csr matrix to csc  
    csrBorderMatrix = Pysparse.csr_matrix((data,col,row),  
        shape=(borderData["ROWCOUNT"],borderData["COLCOUNT"]))  
    denseMatrix = pycall(csrBorderMatrix["toarray"],PyAny)  
  
    cscBoundaryMat = sparse(denseMatrix)
```

```

        return cscBoundaryMat

    end ◇

```

Fragment referenced in 57a.

7 Lar2Julia

This module contains functions used in LAR library which are converted using Julia syntax. Next versions of the software will contain more and more functions from the original LAR library (which is written in python)

7.1 Module imports

These are modules used for `Lar2Julia` and the public functions

```

⟨ modules import Lar2Julia 36a ⟩ ≡
    import JSON

    using Logging

    export larBoundaryChain, cscChainToCellList ◇

```

Fragment referenced in 57b.

7.2 Get boundary chain from a model

Now we will observe how to compute the boundary chain of a LAR model given the list of non-empty cells and the boundary operator stored as a csc sparse matrix. This algorithm is very simply: firstly we need to convert the list of cells into a sparse array containing the LAR model. So, the resulting array (which will be called `cscChain`) will contain a one for every `cscChain[i][1] $\forall i \in \text{brcCellList}$` . Next, we just have to compute the product between the two sparse matrices and convert all values of the result into one of these: $\{-1; +1; 0\}$ using function `cscBinFilter`.

```

⟨ get boundary chain 36b ⟩ ≡

```

```

function larBoundaryChain(cscBoundaryMat, brcCellList)
    """
    Compute boundary chains
    """

    # Computing boundary chains
    n = size(cscBoundaryMat)[1]
    m = size(cscBoundaryMat)[2]

    debug("Boundary matrix size: ", n, "\t", m)

    data = ones(Int64, length(brcCellList))

    i = Array{Int64, length(brcCellList)}
    for k in 1:length(brcCellList)
        i[k] = brcCellList[k] + 1
    end

    j = ones{Int64, length(brcCellList)}

    debug("cscChain rows length: ", length(i))
    debug("cscChain columns length: ", length(j))
    debug("cscChain data length: ", length(brcCellList))

    debug("rows ", i)
    debug("columns ", j)
    debug("data ", data)

    cscChain = sparse(i, j, data, m, 1)
    cscmat = cscBoundaryMat * cscChain
    out = cscBinFilter(cscmat)
    return out
end

function cscBinFilter(CSCm)
    k = 1
    data = nonzeros(CSCm)
    sgArray = copysign(1, data)

    while k <= nnz(CSCm)
        if data[k] % 2 == 1 || data[k] % 2 == -1
            data[k] = 1 * sgArray[k]
        else
            data[k] = 0
        end
        k += 1
    end
end

```

```

        end

        return CSCm
    end
    ◇

```

Fragment referenced in 57b.

7.3 Get oriented cells from a chain

Another operation that could be useful (even if it is not actually used in the package) consists in getting of “+1” oriented cells from a chain. For obtaining this result, it is necessary to get all non-zeros element from the sparse Julia array (remembering that if the user manually write a zero into the array it will be returned from `nonzeros` function anyway) and then returning only indices of cells that have a “+1” in nonzero element array.

(get oriented cells from a chain 38) ≡

```

function cscChainToCellList(CSCm)
    """
    Get a csc containing a chain and returns
    the cell list of the "+1" oriented faces
    """
    data = nonzeros(CSCm)
    # Now I need to remove zero element (problem with Julia nonzeros)
    nonzeroData = Array{Int64, 0}
    for n in data
        if n != 0
            push!(nonzeroData, n)
        end
    end

    cellList = Array{Int64, 0}
    for (k, theRow) in enumerate(findn(CSCm)[1])
        if nonzeroData[k] == 1
            push!(cellList, theRow)
        end
    end
    return cellList
end ◇

```

Fragment referenced in 57b.

7.4 Transform relationships from arrays of arrays to a sparse matrix

```
< transform relationships to csc 39a > ≡
function relationshipListToCSC(larRelation)
    """
    Get a LAR relationship
    and convert it into a CSC matrix
    """

    # Build I and J arrays for creation of
    # sparse matrix
    data = Array{Int, 0}
    I = Array{Int, 0}
    J = Array{Int, 0}
    for (k,row) in enumerate(larRelation)
        for col in row
            push!(I, k)
            push!(J, col)
            push!(data, 1)
        end
    end

    return sparse(I, J, data)
end ◇
```

Fragment referenced in 57b.

8 LARUtils

This module contains functions used for manipulation of LAR models

8.1 Module imports

These are modules used in LARUtils and the functions exported

```
< modules import LARUtils 39b > ≡
using Logging

export ind, invertIndex, getBases, removeDoubleVerticesAndFaces,
       computeModel, computeModelAndBoundaries
◇
```

Fragment referenced in 58.

8.2 Transformation from matrix to array

First utility functions we will see, transform a matrix into an array and vice versa. We have already seen in section 5.4.1 uses of this linearized matrices; now we can focus on code for transformation.

```
< conversion from matrix to array 40a > ≡
function ind(x, y, z, nx, ny)
    """
    Transform coordinates into linearized matrix indexes
    """
    return x + (nx + 1) * (y + (ny + 1) * (z))
end ◇
```

Fragment referenced in 58.

Here we have defined also the inverse transformation from the array to the matrix, which is useful for obtaining vertices coordinates from a cell

```
< conversion from array to matrix 40b > ≡
function invertIndex(nx,ny,nz)
    """
    Invert indexes
    """
    nx, ny, nz = nx + 1, ny + 1, nz + 1
    function invertIndex0(offset)
        a0, b0 = trunc(offset / nx), offset % nx
        a1, b1 = trunc(a0 / ny), a0 % ny
        a2, b2 = trunc(a1 / nz), a1 % nz
        return b0, b1, b2
    end
    return invertIndex0
end ◇
```

Fragment referenced in 58.

8.3 Get bases of a LAR model

For generation of LAR models from an array of non-empty cells, we need to define a function for obtaining a base for every model, which will contain all LAR relationships:

- **V**: the array of vertices of a LAR model

- **VV**: the relationship between a vertex and itself
- **EV**: the relationship between an edge and its vertices
- **FV**: the relationship between a face and its vertices
- **CV**: the relationship between a cell and its vertices

From a geometrical point of view these bases create a chain composed from $nx \times ny \times nz$ square cells (where nx ny and nz are the grid size).

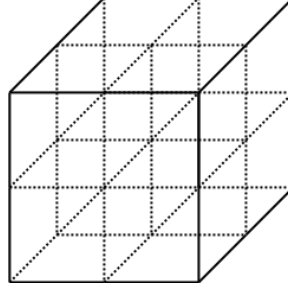


Figure 10: LAR bases geometry for a $2 \times 2 \times 2$ grid

Now we will see in details how to obtain all LAR relationships. First of all we need to compute vertices for the geometry:

```

⟨ compute vertices 41a ⟩ ≡
  # Calculating vertex coordinates (nx * ny * nz)
  V = Array{Int64}[]
  for z in 0:nz
    for y in 0:ny
      for x in 0:nx
        push!(V, [x,y,z])
      end
    end
  end
end ◇

```

Fragment referenced in 44.

So we assume that our cube geometry has only integers coordinates that can vary from (0,0,0) to (nx,ny,nz)

Next we have to compute the CV relationship:

```

⟨ compute CV 41b ⟩ ≡

```

```

# Building CV relationship
CV = Array{Int64}[]
for z in 0:nz-1
  for y in 0:ny-1
    for x in 0:nx-1
      push!(CV,the3Dcell([x,y,z]))
    end
  end
end ◇

```

Fragment referenced in 44.

For every coordinate in the space delimited by the grid size, it is called function `the3Dcell`, which get the coordinate values returning a cell in the three-dimensional space:

```

⟨ compute three-dimensional cells 42a ⟩ ≡
function the3Dcell(coords)
  x,y,z = coords
  return [ind(x,y,z,nx,ny), ind(x+1,y,z,nx,ny), ind(x,y+1,z,nx,ny),
          ind(x,y,z+1,nx,ny), ind(x+1,y+1,z,nx,ny), ind(x+1,y,z+1,nx,ny),
          ind(x,y+1,z+1,nx,ny), ind(x+1,y+1,z+1,nx,ny)]
end
◇

```

Fragment referenced in 44.

Now we have to compute the FV relationship, which will be widely used in this package:

```

⟨ compute FV 42b ⟩ ≡
# Building FV relationship
FV = Array{Int64}[]
v2coords = invertIndex(nx,ny,nz)

for h in 0:(length(V)-1)
  x,y,z = v2coords(h)

  if (x < nx) && (y < ny)
    push!(FV, [h,ind(x+1,y,z,nx,ny),ind(x,y+1,z,nx,ny),ind(x+1,y+1,z,nx,ny)])
  end

  if (x < nx) && (z < nz)

```

```

    push!(FV, [h, ind(x+1,y,z,nx,ny), ind(x,y,z+1,nx,ny), ind(x+1,y,z+1,nx,ny)])
end

if (y < ny) && (z < nz)
    push!(FV, [h, ind(x,y+1,z,nx,ny), ind(x,y,z+1,nx,ny), ind(x,y+1,z+1,nx,ny)])
end

end ◇

```

Fragment referenced in 44.

Finally we have the VV relationship (which is trivial)

```

⟨ compute VV 43a ⟩ ≡
    # Building VV relationship
    VV = map((x)->[x], 0:length(V)-1) ◇

```

Fragment referenced in 44.

and the EV relationship

```

⟨ compute EV 43b ⟩ ≡
    # Building EV relationship
    EV = Array{Int64}[]
    for h in 0:length(V)-1
        x,y,z = v2coords(h)
        if (x < nx)
            push!(EV, [h, ind(x+1,y,z,nx,ny)])
        end
        if (y < ny)
            push!(EV, [h, ind(x,y+1,z,nx,ny)])
        end
        if (z < nz)
            push!(EV, [h, ind(x,y,z+1,nx,ny)])
        end
    end ◇

```

Fragment referenced in 44.

This is the complete code for the function `getBases`

```

⟨ get LAR bases 44 ⟩ ≡
function getBases(nx, ny, nz)
    """
    Compute all LAR relations
    """

    ⟨ compute three-dimensional cells 42a ⟩

    ⟨ compute vertices 41a ⟩

    ⟨ compute CV 41b ⟩

    ⟨ compute FV 42b ⟩

    ⟨ compute VV 43a ⟩

    ⟨ compute EV 43b ⟩

    # return all basis
    return V, (VV, EV, FV, CV)
end ◇

```

Fragment referenced in 58.

8.4 Double vertices and faces removal

Another useful function for our models is *removal of double vertices and faces*. In fact, when we produce a LAR model getting only full cell from the geometry in Figure 10 we could obtain double vertices (and consequently double faces). Figure 11 shows an example of a model with these vertices:

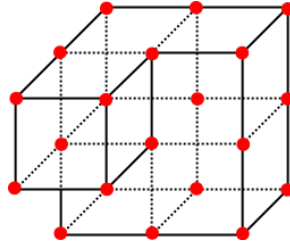


Figure 11: A sample model taken from a $2 \times 2 \times 2$ grid with double vertices between faces in red (remember that we have only the boundaries faces for the model as we have seen in section 5.4.1)

As we can see, for every model there are a lot of double vertices, so we need to remove them for obtaining a compact representation and for next smoothing of the objects. First of all we have to identify double vertices, so it can be useful to define an order between them. Unfortunately Julia does not define a function for order array containing coordinates (which is format used in V array); so we have to define first a custom ordering function:

```

< vertices comparator function 45a > ≡
function lessThanVertices(v1, v2)
    """
    Utility function for comparing vertices coordinates
    """

    if v1[1] == v2[1]
        if v1[2] == v2[2]
            return v1[3] < v2[3]
        end
        return v1[2] < v2[2]
    end
    return v1[1] < v2[1]
end ◇

```

Fragment referenced in 47.

Now we can remove double vertices from the V array simply ordering them and removing all consecutive equal vertices. This procedure is more complex than a simple call to Julia `unique` function for removal of double elements because we need the new vertices indices for renaming faces (as we can see later)

```

< removal of double vertices 45b > ≡
function removeDoubleVertices(V)
    """
    Remove double vertices from a LAR model

    V: Array containing all vertices of the model
    """

    # Sort the vertices list and returns the ordered indices
    orderedIndices = sortperm(V, lt = lessThanVertices, alg=MergeSort)

    orderedVerticesAndIndices = collect(zip(sort(V, lt = lessThanVertices),
                                             orderedIndices))

    newVertices = Array{Array{Int}, 0}()
    indices = zeros{Int, length(V)}

```

```

prevv = Nothing
i = 1
for (v, ind) in orderedVerticesAndIndices
  if v == prevv
    indices[ind] = i - 1
  else
    push!(newVertices, v)
    indices[ind] = i
    i += 1
    prevv = v
  end
end
return newVertices, indices
end ◇

```

Fragment referenced in 47.

As we can see the algorithm does the following steps:

1. Sort of vertices list
2. Set the current vertex index counter to 1
3. For every couple (*vertex*, *index* into V array) do:
 - (a) If the current *vertex* is equal to the previous one put into the indices array at position *index* the value for the current vertex index count
 - (b) If the current *vertex* is not equal to the previous one save it into a new V array, insert the indices array at position *index* the current index count and increment it by one

So at the end of this function the array *newVertices* will contain all unique vertices, while the *indices* array will contain the correct index for every vertex into *newVertices* and the index corresponding to the saved vertex for every deleted vertex.

Now we can use these informations for renaming all faces.

$\langle \text{renaming of faces 46} \rangle \equiv$

```

function reindexVerticesInFaces(FV, indices, offset)
  """
  Reindex vertices indices in faces array

  FV: Faces array of the LAR model

```

```

indices: new Indices for faces
offset: offset for faces indices
"""

for f in FV
    for i in 1: length(f)
        f[i] = indices[f[i] - offset] + offset
    end
end
return FV
end ◇

```

Fragment referenced in 47.

Here we can observe a *offset* parameter, which is necessary only if we are renaming faces whose indices doesn't start from zero; actually in `ImagesToLARModel` it is always equal to zero.

Finally for removing double faces, we only have to call `unique` function on renamed faces. This is the final code

⟨ removal of double vertices and faces 47 ⟩ \equiv
⟨ vertices comparator function 45a ⟩

```

function removeDoubleVerticesAndFaces(V, FV, facesOffset)
    """
    Removes double vertices and faces from a LAR model

    V: Array containing all vertices
    FV: Array containing all faces
    facesOffset: offset for faces indices
    """

    newV, indices = removeDoubleVertices(V)
    reindexedFaces = reindexVerticesInFaces(FV, indices, facesOffset)
    newFV = unique(FV)

    return newV, newFV
end

```

⟨ removal of double vertices 45b ⟩

⟨ renaming of faces 46 ⟩ ◇

Fragment never referenced.

8.5 Creation of a LAR model

Now we can see code used for creation of a LAR model given the sparse array containing full cells of our block (**objectBoundaryChain** as we had seen in Section 7.2). We also need the following parameters:

- **imageDx, imageDy, imageDz**: The grid size
- **xStart, yStart, zStart**: The coordinate offsets for the current block vertices
- **facesOffset**: The offset for faces of this block

First thing to do is define models that will be returned from the function:

```
< models definition 48 > ≡  
  V_model = Array(Array{Int}, 0)  
  FV_model = Array(Array{Int}, 0)  
  
  V_left = Array(Array{Int},0)  
  FV_left = Array(Array{Int},0)  
  
  V_right = Array(Array{Int},0)  
  FV_right = Array(Array{Int},0)  
  
  V_top = Array(Array{Int},0)  
  FV_top = Array(Array{Int},0)  
  
  V_bottom = Array(Array{Int},0)  
  FV_bottom = Array(Array{Int},0)  
  
  V_front = Array(Array{Int},0)  
  FV_front = Array(Array{Int},0)  
  
  V_back = Array(Array{Int},0)  
  FV_back = Array(Array{Int},0) ◇
```

Fragment referenced in 52.

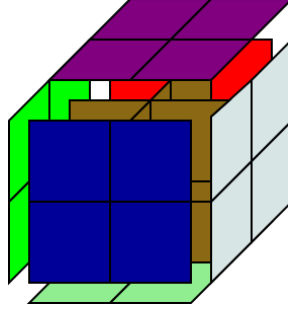


Figure 12: Decomposition of a LAR model into seven parts: the inside model (brown), the left boundary (green), the right boundary (light blue), the top boundary (purple), the bottom boundary (light green), the front boundary (blue), the back boundary (red)

We can see from Figure 12 that our grid is divided into seven parts.

We need this decomposition because we are interested in boundaries of the entire model, while we currently have boundaries only for blocks. So we need to split the inner parts of a single block model, as we need to freely merge boundaries between adjacent blocks removing the common faces. Function for boundaries merging are shown in subsection 8.6.

After model definition we have to get the cells indices from the block boundary chain and for every non-empty cell we have found, choose the correct model for it. We can observe that every boundary face has a fixed coordinate; for example all faces on the top boundary have the maximum z-coordinate, or faces on right boundary have the maximum y-coordinate (as shown in Figure 13)

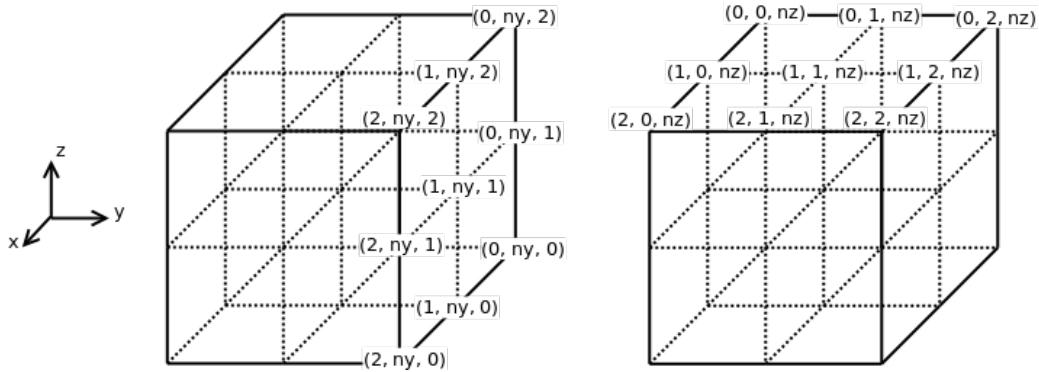


Figure 13: Boundaries coordinates for top and right boundaries of a $2 \times 2 \times 2$ grid. We can observe that every boundary has a fixed coordinate

So we can define a series of functions for checking the membership of a given face to a

boundary exploiting these fixed coordinates:

```
< check membership of a face to a boundary 50 > ≡
function isOnLeft(face, V, nx, ny, nz)
    ""
    Check if face is on left boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][2] != 0)
            return false
        end
    end
    return true

end

function isOnRight(face, V, nx, ny, nz)
    ""
    Check if face is on right boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][2] != ny)
            return false
        end
    end
    return true

end

function isOnTop(face, V, nx, ny, nz)
    ""
    Check if face is on top boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][3] != nz)
            return false
        end
    end
    return true
end

function isOnBottom(face, V, nx, ny, nz)
    ""
```

```

    Check if face is on bottom boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][3] != 0)
            return false
        end
    end
    return true
end

function isOnFront(face, V, nx, ny, nz)
    ""
    Check if face is on front boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][1] != nx)
            return false
        end
    end
    return true
end

function isOnBack(face, V, nx, ny, nz)
    ""
    Check if face is on back boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][1] != 0)
            return false
        end
    end
    return true
end
end

```

Fragment referenced in 52.

After choosing of the right model, we have to insert our face into it. We can do it with the following function, which takes vertices and faces of the base and the model, the face, and the offset of the current face for the model chosen:

$\langle \text{add a face to a model } 51 \rangle \equiv$

```

function addFaceToModel(V_base, FV_base, V, FV, face, vertex_count)
    """
    Insert a face into a LAR model

    V_base, FV_base: LAR model of the base
    V, FV: LAR model
    face: Face that will be added to the model
    vertex_count: Indices for faces vertices
    """
    new_vertex_count = vertex_count
    for vtx in FV_base[face]
        push!(V, [convert{Int, V_base[vtx + 1][1] + xStart},
                  convert{Int, V_base[vtx + 1][2] + yStart},
                  convert{Int, V_base[vtx + 1][3] + zStart}])
        new_vertex_count += 1
    end
    push!(FV, [vertex_count, vertex_count + 1, vertex_count + 3])
    push!(FV, [vertex_count, vertex_count + 3, vertex_count + 2])

    return new_vertex_count
end ◇

```

Fragment referenced in 52.

As we can see, for every face we put into the model FV array two faces, in fact our final representation is not based on square faces but on triangular faces.

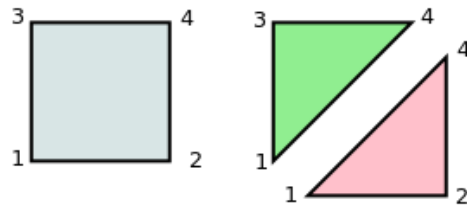


Figure 14: Triangulation of a single face

This is the complete code for creation of a model

$\langle \text{LAR model creation } 52 \rangle \equiv$

$\langle \text{check membership of a face to a boundary } 50 \rangle$

```

function computeModelAndBoundaries(imageDx, imageDy, imageDz,
                                    xStart, yStart, zStart,

```

```

                                objectBoundaryChain)
"""
Takes the boundary chain of a part of the entire model
and returns a LAR model splitting the boundaries

imageDx, imageDy, imageDz: Boundary dimensions
xStart, yStart, zStart: Offset of this part of the model
objectBoundaryChain: Sparse csc matrix containing the cells
"""

< add a face to a model 51 >

< models definition 48 >

V, bases = getBases(imageDx, imageDy, imageDz)
FV = bases[3]

vertex_count_model = 1
vertex_count_left = 1
vertex_count_right = 1
vertex_count_top = 1
vertex_count_bottom = 1
vertex_count_front = 1
vertex_count_back = 1

#b2cells = Lar2Julia.cscChainToCellList(objectBoundaryChain)
# Get all cells (independently from orientation)
b2cells = findn(objectBoundaryChain)[1]

debug("b2cells = ", b2cells)

for f in b2cells
    old_vertex_count_model = vertex_count_model
    old_vertex_count_left = vertex_count_left
    old_vertex_count_right = vertex_count_right
    old_vertex_count_top = vertex_count_top
    old_vertex_count_bottom = vertex_count_bottom
    old_vertex_count_front = vertex_count_front
    old_vertex_count_back = vertex_count_back

    # Choosing the right model for vertex
    if(isOnLeft(FV[f], V, imageDx, imageDy, imageDz))
        vertex_count_left = addFaceToModel(V, FV, V_left, FV_left,
                                            f, old_vertex_count_left)
    elseif(isOnRight(FV[f], V, imageDx, imageDy, imageDz))
        vertex_count_right = addFaceToModel(V, FV, V_right, FV_right,

```

```

                                f, old_vertex_count_right)
elseif(isOnTop(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_top = addFaceToModel(V, FV, V_top, FV_top,
                                f, old_vertex_count_top)
elseif(isOnBottom(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_bottom = addFaceToModel(V, FV, V_bottom, FV_bottom,
                                f, old_vertex_count_bottom)
elseif(isOnFront(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_front = addFaceToModel(V, FV, V_front, FV_front,
                                f, old_vertex_count_front)
elseif(isOnBack(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_back = addFaceToModel(V, FV, V_back, FV_back,
                                f, old_vertex_count_back)
else
    vertex_count_model = addFaceToModel(V, FV, V_model, FV_model,
                                f, old_vertex_count_model)
end

end

# Removing double vertices
return [removeDoubleVerticesAndFaces(V_model, FV_model, 0)],
[removeDoubleVerticesAndFaces(V_left, FV_left, 0)],
[removeDoubleVerticesAndFaces(V_right, FV_right, 0)],
[removeDoubleVerticesAndFaces(V_top, FV_top, 0)],
[removeDoubleVerticesAndFaces(V_bottom, FV_bottom, 0)],
[removeDoubleVerticesAndFaces(V_front, FV_front, 0)],
[removeDoubleVerticesAndFaces(V_back, FV_back, 0)]
end ◇

```

Fragment never referenced.

8.6 Removing double faces and vertices from boundaries

8.7 Smoothing models

$\langle \textit{Smoothing of a LAR model 54} \rangle \equiv$

```

function adjacencyQuery(FV)
    """
    Takes the faces of a LAR model and returns
    a sparse matrix containing the adjacent vertices
    """
    cscFV = relationshipListToCSC(FV)

```

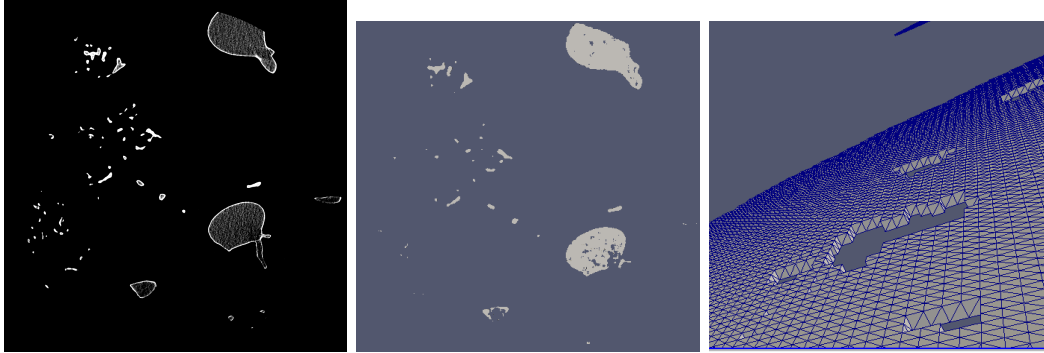


Figure 15: Creation of a sample model. (a) The original image (b) The three-dimensional model (c) The three-dimensional model (detail with triangular faces)

```

    cscAdj = transpose(cscFV) * cscFV
    return cscAdj
end

function adjVerts(V, FV)
    """
    Compute the adjacency graph of vertices
    of a LAR model

    V, FV: LAR model

    Returns the list of indices of vertices adjacent
    to a vertex
    """
    VV = Array{Int}[]
    V2V = adjacencyQuery(FV)

    for i in 1:length(V)
        dataBuffer = nonzeros(V2V[i, :])
        colBuffer = findn(V2V[i, :])[2]
        row = Array{Int, 0}
        for (val, j) in zip(dataBuffer, colBuffer)
            if val == 2
                push!(row, j)
            end
        end
        push!(VV, [row])
    end
    return VV
end

```



```

function makeSmoothing(V)
    """
    Execute a Laplacian smoothing on a LAR model returning
    the new smoothed model

    V, FV: LAR model
    """
    VV = adjVerts(V, FV)

    # TODO: Convert these statements from python to Julia
    V1 = AA(CCOMB)([[V[v] for v in adj] for adj in VV])
    V2 = AA(CCOMB)([[V1[v] for v in adj] for adj in VV])
end
◇

```

Fragment never referenced.

9 Model2Obj

10 Exporting the library

ImagesToLARModel

```

"src/ImagesToLARModel.jl" 56a≡
    module ImagesToLARModel

        < update load path 6 >

        < modules import ImagesToLARModel 7a >
        < load JSON configuration 7b >
        < Start conversion from JSON file 9 >
        < Start manual conversion 10 >
    end
◇

```

ImagesConversion

```

"src/ImagesConversion.jl" 56b≡

```

```

module ImagesConversion

  < modules import ImagesConversion 22 >

  < main function for ImagesConversion 23 >

  < start conversion of images 26 >

  < image conversion process 30b >
end
◇

```

GenerateBorderMatrix

```

"src/GenerateBorderMatrix.jl" 57a≡
  module GenerateBorderMatrix

    < Matrix object for JSON file 34a >

    < modules import GenerateBorderMatrix 32a >

    < compute border matrix 34b >

    < write Border matrix 33 >

    < get Border matrix 32b >

    < transform border matrix in csc format 35 >
  end
  ◇

```

Lar2Julia

```

"src/Lar2Julia.jl" 57b≡
  module Lar2Julia

    < modules import Lar2Julia 36a >

    < get boundary chain 36b >

```

```

    < get oriented cells from a chain 38 >

    < transform relationships to csc 39a >
end
◇

```

LARUtils

```

"src/LARUtils.jl" 58≡
module LARUtils

    < modules import LARUtils 39b >

    < conversion from matrix to array 40a >

    < conversion from array to matrix 40b >

    < get LAR bases 44 >

function lessThanVertices(v1, v2)
    """
        Utility function for comparing vertices coordinates
    """

    if v1[1] == v2[1]
        if v1[2] == v2[2]
            return v1[3] < v2[3]
        end
        return v1[2] < v2[2]
    end
    return v1[1] < v2[1]
end

function removeDoubleVerticesAndFaces(V, FV, facesOffset)
    """
        Removes double vertices and faces from a LAR model

        V: Array containing all vertices
        FV: Array containing all faces
        facesOffset: offset for faces indices
    """

```

```

    newV, indices = removeDoubleVertices(V)
    reindexedFaces = reindexVerticesInFaces(FV, indices, facesOffset)
    newFV = unique(FV)

    return newV, newFV
end

function removeDoubleVertices(V)
    """
    Remove double vertices from a LAR model

    V: Array containing all vertices of the model
    """

    # Sort the vertices list and returns the ordered indices
    orderedIndices = sortperm(V, lt = lessThanVertices, alg=MergeSort)

    orderedVerticesAndIndices = collect(zip(sort(V, lt = lessThanVertices),
                                             orderedIndices))

    newVertices = Array{Array{Int}, 0}()
    indices = zeros{Int, length(V)}
    prevv = Nothing
    i = 1
    for (v, ind) in orderedVerticesAndIndices
        if v == prevv
            indices[ind] = i - 1
        else
            push!(newVertices, v)
            indices[ind] = i
            i += 1
            prevv = v
        end
    end
    return newVertices, indices
end

function reindexVerticesInFaces(FV, indices, offset)
    """
    Reindex vertices indices in faces array

    FV: Faces array of the LAR model
    indices: new Indices for faces
    offset: offset for faces indices
    """

```

```

    for f in FV
        for i in 1: length(f)
            f[i] = indices[f[i] - offset] + offset
        end
    end
    return FV
end

function removeVerticesAndFacesFromBoundaries(V, FV)
    """
    Remove vertices and faces duplicates on
    boundaries models

    V,FV: lar model of two merged boundaries
    """

    newV, indices = removeDoubleVertices(V)
    uniqueIndices = unique(indices)

    # Removing double faces on both boundaries
    FV_reindexed = reindexVerticesInFaces(FV, indices, 0)
    FV_unique = unique(FV_reindexed)

    FV_cleaned = Array{Array{Int}, 0}
    for f in FV_unique
        if(count((x) -> x == f, FV_reindexed) == 1)
            push!(FV_cleaned, f)
        end
    end

    # Creating an array of faces with explicit vertices
    FV_vertices = Array{Array{Array{Int}}, 0}

    for i in 1 : length(FV_cleaned)
        push!(FV_vertices, Array{Array{Int}, 0})
        for vtx in FV_cleaned[i]
            push!(FV_vertices[i], newV[vtx])
        end
    end

    V_final = Array{Array{Int}, 0}
    FV_final = Array{Array{Int}, 0}

    # Saving only used vertices
    for face in FV_vertices
        for vtx in face

```

```

        push!(V_final, vtx)
    end
end

V_final = unique(V_final)

# Renumbering FV
for face in FV_vertices
    tmp = Array{Int, 0}
    for vtx in face
        ind = findfirst(V_final, vtx)
        push!(tmp, ind)
    end
    push!(FV_final, tmp)
end

return V_final, FV_final
end

function computeModel(imageDx, imageDy, imageDz,
                      xStart, yStart, zStart,
                      facesOffset, objectBoundaryChain)
    """
    Takes the boundary chain of a part of the entire model
    and returns a LAR model

    imageDx, imageDy, imageDz: Boundary dimensions
    xStart, yStart, zStart: Offset of this part of the model
    facesOffset: Offset for the faces
    objectBoundaryChain: Sparse csc matrix containing the cells
    """

    V, bases = getBases(imageDx, imageDy, imageDz)
    FV = bases[3]

    V_model = Array{Array{Int}, 0}
    FV_model = Array{Array{Int}, 0}

    vertex_count = 1

    #b2cells = Lar2Julia.cscChainToCellList(objectBoundaryChain)
    # Get all cells (independently from orientation)
    b2cells = findn(objectBoundaryChain)[1]

    debug("b2cells = ", b2cells)
end

```

```

for f in b2cells
  old_vertex_count = vertex_count
  for vtx in FV[f]
    push!(V_model, [convert{Int, V[vtx + 1][1] + xStart},
                    convert{Int, V[vtx + 1][2] + yStart},
                    convert{Int, V[vtx + 1][3] + zStart}])
    vertex_count += 1
  end

  push!(FV_model, [old_vertex_count + facesOffset, old_vertex_count + 1 + facesOffset, old_v
  push!(FV_model, [old_vertex_count + facesOffset, old_vertex_count + 3 + facesOffset, old_v
end

# Removing double vertices
return removeDoubleVerticesAndFaces(V_model, FV_model, facesOffset)

end

function isOnLeft(face, V, nx, ny, nz)
  """
  Check if face is on left boundary
  """

  for(vtx in face)
    if(V[vtx + 1][2] != 0)
      return false
    end
  end
  return true
end

function isOnRight(face, V, nx, ny, nz)
  """
  Check if face is on right boundary
  """

  for(vtx in face)
    if(V[vtx + 1][2] != ny)
      return false
    end
  end
  return true
end

```

```

function isOnTop(face, V, nx, ny, nz)
    ""
    Check if face is on top boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][3] != nz)
            return false
        end
    end
    return true
end

function isOnBottom(face, V, nx, ny, nz)
    ""
    Check if face is on bottom boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][3] != 0)
            return false
        end
    end
    return true
end

function isOnFront(face, V, nx, ny, nz)
    ""
    Check if face is on front boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][1] != nx)
            return false
        end
    end
    return true
end

function isOnBack(face, V, nx, ny, nz)
    ""
    Check if face is on back boundary
    ""

    for(vtx in face)
        if(V[vtx + 1][1] != 0)

```



```

        return false
    end
end
return true
end

function computeModelAndBoundaries(imageDx, imageDy, imageDz,
                                   xStart, yStart, zStart,
                                   objectBoundaryChain)
    """
    Takes the boundary chain of a part of the entire model
    and returns a LAR model splitting the boundaries

    imageDx, imageDy, imageDz: Boundary dimensions
    xStart, yStart, zStart: Offset of this part of the model
    objectBoundaryChain: Sparse csc matrix containing the cells
    """

    function addFaceToModel(V_base, FV_base, V, FV, face, vertex_count)
        """
        Insert a face into a LAR model

        V_base, FV_base: LAR model of the base
        V, FV: LAR model
        face: Face that will be added to the model
        vertex_count: Indices for faces vertices
        """
        new_vertex_count = vertex_count
        for vtx in FV_base[face]
            push!(V, [convert{Int}(V_base[vtx + 1][1] + xStart),
                     convert{Int}(V_base[vtx + 1][2] + yStart),
                     convert{Int}(V_base[vtx + 1][3] + zStart)])
            new_vertex_count += 1
        end
        push!(FV, [vertex_count, vertex_count + 1, vertex_count + 3])
        push!(FV, [vertex_count, vertex_count + 3, vertex_count + 2])

        return new_vertex_count
    end

    V, bases = getBases(imageDx, imageDy, imageDz)
    FV = bases[3]

    V_model = Array{Array{Int}, 0}()
    FV_model = Array{Array{Int}, 0}()

```

```

V_left = Array(Array{Int},0)
FV_left = Array(Array{Int},0)

V_right = Array(Array{Int},0)
FV_right = Array(Array{Int},0)

V_top = Array(Array{Int},0)
FV_top = Array(Array{Int},0)

V_bottom = Array(Array{Int},0)
FV_bottom = Array(Array{Int},0)

V_front = Array(Array{Int},0)
FV_front = Array(Array{Int},0)

V_back = Array(Array{Int},0)
FV_back = Array(Array{Int},0)

vertex_count_model = 1
vertex_count_left = 1
vertex_count_right = 1
vertex_count_top = 1
vertex_count_bottom = 1
vertex_count_front = 1
vertex_count_back = 1

#b2cells = Lar2Julia.cscChainToCellList(objectBoundaryChain)
# Get all cells (independently from orientation)
b2cells = findn(objectBoundaryChain)[1]

debug("b2cells = ", b2cells)

for f in b2cells
    old_vertex_count_model = vertex_count_model
    old_vertex_count_left = vertex_count_left
    old_vertex_count_right = vertex_count_right
    old_vertex_count_top = vertex_count_top
    old_vertex_count_bottom = vertex_count_bottom
    old_vertex_count_front = vertex_count_front
    old_vertex_count_back = vertex_count_back

    # Choosing the right model for vertex
    if(isOnLeft(FV[f], V, imageDx, imageDy, imageDz))
        vertex_count_left = addFaceToModel(V, FV, V_left, FV_left, f, old_vertex_count_left)
    elseif(isOnRight(FV[f], V, imageDx, imageDy, imageDz))
        vertex_count_right = addFaceToModel(V, FV, V_right, FV_right, f, old_vertex_count_right)
    end
end

```

```

elseif(isOnTop(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_top = addFaceToModel(V, FV, V_top, FV_top, f, old_vertex_count_top)
elseif(isOnBottom(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_bottom = addFaceToModel(V, FV, V_bottom, FV_bottom, f, old_vertex_count_bot)
elseif(isOnFront(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_front = addFaceToModel(V, FV, V_front, FV_front, f, old_vertex_count_front)
elseif(isOnBack(FV[f], V, imageDx, imageDy, imageDz))
    vertex_count_back = addFaceToModel(V, FV, V_back, FV_back, f, old_vertex_count_back)
else
    vertex_count_model = addFaceToModel(V, FV, V_model, FV_model, f, old_vertex_count_model)
end

end

# Removing double vertices
return [removeDoubleVerticesAndFaces(V_model, FV_model, 0)],
[removeDoubleVerticesAndFaces(V_left, FV_left, 0)],
[removeDoubleVerticesAndFaces(V_right, FV_right, 0)],
[removeDoubleVerticesAndFaces(V_top, FV_top, 0)],
[removeDoubleVerticesAndFaces(V_bottom, FV_bottom, 0)],
[removeDoubleVerticesAndFaces(V_front, FV_front, 0)],
[removeDoubleVerticesAndFaces(V_back, FV_back, 0)]
end
end
◇

```

Model2Obj

```

"src/Model2Obj.jl" 66≡
module Model2Obj

import LARUtils

using Logging

export writeToObj, mergeObj, mergeObjParallel

function writeToObj(V, FV, outputFilename)
    """
    Take a LAR model and write it on obj file

    V: array containing vertices coordinates
    FV: array containing faces
    """

```

```

outputFilename: prefix for the output files
"""

if (length(V) != 0)
  outputVtx = string(outputFilename, "_vtx.stl")
  outputFaces = string(outputFilename, "_faces.stl")

  fileVertex = open(outputVtx, "w")
  fileFaces = open(outputFaces, "w")

  for v in V
    write(fileVertex, "v ")
    write(fileVertex, string(v[1], " "))
    write(fileVertex, string(v[2], " "))
    write(fileVertex, string(v[3], "\n"))
  end

  for f in FV

    write(fileFaces, "f ")
    write(fileFaces, string(f[1], " "))
    write(fileFaces, string(f[2], " "))
    write(fileFaces, string(f[3], "\n"))
  end

  close(fileVertex)
  close(fileFaces)

end

end

function mergeObj(modelDirectory)
  """
  Merge stl files in a single obj file

  modelDirectory: directory containing models
  """

  files = readdir(modelDirectory)
  vertices_files = files[find(s -> contains(s, string("_vtx.stl")), files)]
  faces_files = files[find(s -> contains(s, string("_faces.stl")), files)]
  obj_file = open(string(modelDirectory, "/", "model.obj"), "w") # Output file

  vertices_counts = Array{Int64, length(vertices_files)}
  number_of_vertices = 0

```

```

for i in 1:length(vertices_files)
    vtx_file = vertices_files[i]
    f = open(string(modelDirectory, "/", vtx_file))

    # Writing vertices on the obj file
    for ln in eachline(f)
        write(obj_file, ln)
        number_of_vertices += 1
    end
    # Saving number of vertices
    vertices_counts[i] = number_of_vertices
    close(f)
end

for i in 1 : length(faces_files)
    faces_file = faces_files[i]
    f = open(string(modelDirectory, "/", faces_file))
    for ln in eachline(f)
        splitted = split(ln)
        write(obj_file, "f ")
        if i > 1
            write(obj_file, string(parse(splitted[2]) + vertices_counts[i - 1], " "))
            write(obj_file, string(parse(splitted[3]) + vertices_counts[i - 1], " "))
            write(obj_file, string(parse(splitted[4]) + vertices_counts[i - 1]))
        else
            write(obj_file, string(splitted[2], " "))
            write(obj_file, string(splitted[3], " "))
            write(obj_file, splitted[4])
        end
        write(obj_file, "\n")
    end
    close(f)
end
close(obj_file)

# Removing all tmp files
for vtx_file in vertices_files
    rm(string(modelDirectory, "/", vtx_file))
end

for fcs_file in faces_files
    rm(string(modelDirectory, "/", fcs_file))
end
end

```

```

function assignTasks(startInd, endInd, taskArray)
    """
    This function choose the first files to merge
    creating a tree where number of processes is maximized

    startInd: starting index for array subdivision
    endInd: end index for array subdivision
    taskArray: array containing indices of files to merge for first
    """
    if (endInd - startInd == 2)
        push!(taskArray, startInd)
    elseif (endInd - startInd < 2)
        if (endInd % 4 != 0 && startInd != endInd)
            # Stop recursion on this branch
            push!(taskArray, startInd)
        end
        # Stop recursion doing nothing
    else
        assignTasks(startInd, startInd + trunc((endInd - startInd) / 2), taskArray)
        assignTasks(startInd + trunc((endInd - startInd) / 2) + 1, endInd, taskArray)
    end
end

function mergeVerticesFiles(file1, file2, startOffset)
    """
    Support function for merging two vertices files.
    Returns the number of vertices of the merged file

    file1: path of the first file
    file2: path of the second file
    startOffset: starting face offset for second file
    """

    f1 = open(file1, "a")

    f2 = open(file2)
    debug("Merging ", file2)
    number_of_vertices = startOffset
    for ln in eachline(f2)
        write(f1, ln)
        number_of_vertices += 1
    end
    close(f2)

    close(f1)

```

```

    return number_of_vertices
end

function mergeFacesFiles(file1, file2, facesOffset)
    """
    Support function for merging two faces files

    file1: path of the first file
    file2: path of the second file
    facesOffset: offset for faces
    """

    f1 = open(file1, "a")

    f2 = open(file2)
    for ln in eachline(f2)
        splitted = split(ln)
        write(f1, "f ")
        write(f1, string(parse(splitted[2]) + facesOffset, " "))
        write(f1, string(parse(splitted[3]) + facesOffset, " "))
        write(f1, string(parse(splitted[4]) + facesOffset, "\n"))
    end
    close(f2)

    close(f1)
end

function mergeObjProcesses(fileArray, facesOffset = Nothing)
    """
    Merge files on a single process

    fileArray: Array containing files that will be merged
    facesOffset (optional): if merging faces files, this array contains
        offsets for every file
    """

    if(contains(fileArray[1], string("_vtx.stl")))
        # Merging vertices files
        offsets = Array{Int, 0}
        push!(offsets, countlines(fileArray[1]))
        vertices_count = mergeVerticesFiles(fileArray[1], fileArray[2], countlines(fileArray[1]))
        rm(fileArray[2]) # Removing merged file
        push!(offsets, vertices_count)
        for i in 3: length(fileArray)
            vertices_count = mergeVerticesFiles(fileArray[1], fileArray[i], vertices_count)
        end
    end
end

```

```

        rm(fileArray[i]) # Removing merged file
        push!(offsets, vertices_count)
    end
    return offsets
else
    # Merging faces files
    mergeFacesFiles(fileArray[1], fileArray[2], facesOffset[1])
    rm(fileArray[2]) # Removing merged file
    for i in 3 : length(fileArray)
        mergeFacesFiles(fileArray[1], fileArray[i], facesOffset[i - 1])
        rm(fileArray[i]) # Removing merged file
    end
end
end
end

function mergeObjHelper(vertices_files, faces_files)
    """
    Support function for mergeObj. It takes vertices and faces files
    and execute a single merging step

    vertices_files: Array containing vertices files
    faces_files: Array containing faces files
    """
    numberOfImages = length(vertices_files)
    taskArray = Array{Int, 0}
    assignTasks(1, numberOfImages, taskArray)

    # Now taskArray contains first files to merge
    numberOfVertices = Array{Int, 0}
    tasks = Array{RemoteRef, 0}
    for i in 1 : length(taskArray) - 1
        task = @spawn mergeObjProcesses(vertices_files[taskArray[i] : (taskArray[i + 1] - 1)])
        push!(tasks, task)
        #append!(numberOfVertices, mergeObjProcesses(vertices_files[taskArray[i] : (taskArray[i + 1] - 1)])
    end

    # Merging last vertices files
    task = @spawn mergeObjProcesses(vertices_files[taskArray[length(taskArray)] : end])
    push!(tasks, task)
    #append!(numberOfVertices, mergeObjProcesses(vertices_files[taskArray[length(taskArray)] : end])

    for task in tasks
        append!(numberOfVertices, fetch(task))
    end
end

```



```

debug("NumberOfVertices = ", numberOfVertices)

# Merging faces files
tasks = Array(RemoteRef, 0)
for i in 1 : length(taskArray) - 1

    task = @spawn mergeObjProcesses(faces_files[taskArray[i] : (taskArray[i + 1] - 1)],
                                    numberOfVertices[taskArray[i] : (taskArray[i + 1] - 1)])
    push!(tasks, task)

    #mergeObjProcesses(faces_files[taskArray[i] : (taskArray[i + 1] - 1)],
    #                  numberOfVertices[taskArray[i] : (taskArray[i + 1] - 1)])
end

#Merging last faces files
task = @spawn mergeObjProcesses(faces_files[taskArray[length(taskArray)] : end],
                                numberOfVertices[taskArray[length(taskArray)] : end])

push!(tasks, task)
#mergeObjProcesses(faces_files[taskArray[length(taskArray)] : end],
#                  numberOfVertices[taskArray[length(taskArray)] : end])

for task in tasks
    wait(task)
end

end

function mergeObjParallel(modelDirectory)
    """
    Merge stl files in a single obj file using a parallel
    approach. Files will be recursively merged two by two
    generating a tree where number of processes for every
    step is maximized
    Actually use of this function is discouraged. In fact
    speedup is influenced by disk speed. It could work on
    particular systems with parallel accesses on disks

    modelDirectory: directory containing models
    """

    files = readdir(modelDirectory)

    # Appending directory path to every file
    files = map((s) -> string(modelDirectory, "/", s), files)

```

```

# While we have more than one vtx file and one faces file
while(length(files) != 2)
  vertices_files = files[find(s -> contains(s,string("_vtx.stl")), files)]
  faces_files = files[find(s -> contains(s,string("_faces.stl")), files)]

  # Merging files
  mergeObjHelper(vertices_files, faces_files)

  files = readdir(modelDirectory)
  files = map((s) -> string(modelDirectory, "/", s), files)
end

mergeVerticesFiles(files[2], files[1], 0)
mv(files[2], string(modelDirectory, "/model.obj"))
rm(files[1])

end

function getModelsFromFiles(arrayV, arrayFV)
  ""
  Get a LAR models for two arrays of vertices
  and faces files

  arrayV: Array containing all vertices files
  arrayFV: Array containing all faces files
  ""

  V = Array(Array{Int}, 0)
  FV = Array(Array{Int}, 0)
  offset = 0

  for i in 1:length(arrayV)
    if isfile(arrayFV[i])
      f_FV = open(arrayFV[i])

      for ln in eachline(f_FV)
        splitted = split(ln)
        push!(FV, [parse(splitted[2]) + offset, parse(splitted[3]) + offset, parse(splitted[4])])
      end
      close(f_FV)

      f_V = open(arrayV[i])
      for ln in eachline(f_V)
        splitted = split(ln)
        push!(V, [parse(splitted[2]), parse(splitted[3]), parse(splitted[4])])
        offset += 1
      end
    end
  end
end

```

```

        end
        close(f_V)
    end
end
return LARUtils.removeVerticesAndFacesFromBoundaries(V, FV)
end

function mergeBoundariesAndRemoveDuplicates(firstPath, secondPath)
    """
    Merge two boundary files removing common faces between
    them

    firstPath, secondPath: Prefix of paths to merge
    """

    firstPathV = string(firstPath, "_vtx.stl")
    firstPathFV = string(firstPath, "_faces.stl")

    secondPathV = string(secondPath, "_vtx.stl")
    secondPathFV = string(secondPath, "_faces.stl")

    if(isfile(firstPathV) && isfile(secondPathV))

        V, FV = getModelsFromFiles([firstPathV, secondPathV], [firstPathFV, secondPathFV])

        # Writing model to file
        rm(firstPathV)
        rm(firstPathFV)
        rm(secondPathV)
        rm(secondPathFV)
        writeToObj(V, FV, firstPath)
    end
end

function mergeBlocksProcess(modelDirectory, startImage, endImage,
                             imageDx, imageDy,
                             imageWidth, imageHeight)
    """
    Helper function for mergeBlocks.
    It is executed on different processes

    modelDirectory: Directory containing model files
    startImage: Block start image
    endImage: Block end image
    imageDx, imageDy: x and y sizes of the grid
    imageWidth, imageHeight: Width and Height of the image
    """

```

```

""
for xBlock in 0:(imageHeight / imageDx - 1)
    for yBlock in 0:(imageWidth / imageDy - 1)

        blockCoordsV = string(xBlock, "-", yBlock, "_", startImage, "_", endImage, "_vtx.stl")
        blockCoordsFV = string(xBlock, "-", yBlock, "_", startImage, "_", endImage, "_faces.stl")

        arrayV = [string(modelDirectory, "/left_output_", blockCoordsV),
                  string(modelDirectory, "/right_output_", blockCoordsV),
                  string(modelDirectory, "/top_output_", blockCoordsV),
                  string(modelDirectory, "/bottom_output_", blockCoordsV),
                  string(modelDirectory, "/front_output_", blockCoordsV),
                  string(modelDirectory, "/back_output_", blockCoordsV),
                  string(modelDirectory, "/model_output_", blockCoordsV)]

        arrayFV = [string(modelDirectory, "/left_output_", blockCoordsFV),
                   string(modelDirectory, "/right_output_", blockCoordsFV),
                   string(modelDirectory, "/top_output_", blockCoordsFV),
                   string(modelDirectory, "/bottom_output_", blockCoordsFV),
                   string(modelDirectory, "/front_output_", blockCoordsFV),
                   string(modelDirectory, "/back_output_", blockCoordsFV),
                   string(modelDirectory, "/model_output_", blockCoordsFV)]

        V, FV = getModelsFromFiles(arrayV, arrayFV)
        for i in 1:length(arrayV)
            if(isfile(arrayV[i]))
                rm(arrayV[i])
                rm(arrayFV[i])
            end
        end
        end
        writeToObj(V, FV, string(modelDirectory, "/model_output_",
                                xBlock, "-", yBlock, "_", startImage, "_", endImage))

    end
end
end

function mergeBoundariesProcess(modelDirectory, startImage, endImage,
                                imageDx, imageDy,
                                imageWidth, imageHeight)

""
Helper function for mergeBoundaries.
It is executed on different processes

modelDirectory: Directory containing model files
startImage: Block start image

```

```

endImage: Block end image
imageDx, imageDy: x and y sizes of the grid
imageWidth, imageHeight: Width and Height of the image
"""
for xBlock in 0:(imageHeight / imageDx - 1)
    for yBlock in 0:(imageWidth / imageDy - 1)

        # Merging right Boundary
        firstPath = string(modelDirectory, "/right_output_", xBlock, "-", yBlock, "_", startImage)
        secondPath = string(modelDirectory, "/left_output_", xBlock, "-", yBlock + 1, "_", startImage)
        mergeBoundariesAndRemoveDuplicates(firstPath, secondPath)

        # Merging top boundary
        firstPath = string(modelDirectory, "/top_output_", xBlock, "-", yBlock, "_", startImage)
        secondPath = string(modelDirectory, "/bottom_output_", xBlock, "-", yBlock, "_", endImage)
        mergeBoundariesAndRemoveDuplicates(firstPath, secondPath)

        # Merging front boundary
        firstPath = string(modelDirectory, "/front_output_", xBlock, "-", yBlock, "_", startImage)
        secondPath = string(modelDirectory, "/back_output_", xBlock + 1, "-", yBlock, "_", startImage)
        mergeBoundariesAndRemoveDuplicates(firstPath, secondPath)
    end
end
end

function mergeBoundaries(modelDirectory,
                        imageHeight, imageWidth, imageDepth,
                        imageDx, imageDy, imageDz)
    """
    Merge boundaries files. For every cell of size
    (imageDx, imageDy, imageDz) in the model grid,
    it merges right faces with next left faces, top faces
    with the next cell bottom faces, and front faces
    with the next cell back faces

    modelDirectory: directory containing models
    imageHeight, imageWidth, imageDepth: images sizes
    imageDx, imageDy, imageDz: sizes of cells grid
    """

    beginImageStack = 0
    endImage = beginImageStack

    tasks = Array{RemoteRef, 0}
    for zBlock in 0:(imageDepth / imageDz - 1)
        startImage = endImage

```

```

    endImage = startImage + imageDz
    task = @spawn mergeBoundariesProcess(modelDirectory, startImage, endImage,
                                         imageDx, imageDy,
                                         imageWidth, imageHeight)

    push!(tasks, task)
end

# Waiting for tasks
for task in tasks
    wait(task)
end
end

function mergeBlocks(modelDirectory,
                    imageHeight, imageWidth, imageDepth,
                    imageDx, imageDy, imageDz)
    """
    Merge block taking the models and the corresponding boundaries.
    For every merged block double faces and vertices are removed.

    modelDirectory: directory containing models
    imageHeight, imageWidth, imageDepth: images sizes
    imageDx, imageDy, imageDz: sizes of cells grid
    """

    beginImageStack = 0
    endImage = beginImageStack

    tasks = Array{RemoteRef, 0}
    for zBlock in 0:(imageDepth / imageDz - 1)
        startImage = endImage
        endImage = startImage + imageDz
        task = @spawn mergeBlocksProcess(modelDirectory, startImage, endImage,
                                         imageDx, imageDy,
                                         imageWidth, imageHeight)

        push!(tasks, task)
    end

    # Waiting for tasks
    for task in tasks
        wait(task)
    end
end
end
◇

```

PngStack2Array3dJulia

```
"src/PngStack2Array3dJulia.jl" 78a≡  
    module PngStack2Array3dJulia  
  
        ⟨ modules import PngStack2Array3dJulia 11a ⟩  
        ⟨ Convert to png 14 ⟩  
        ⟨ Get image data 15 ⟩  
        ⟨ Centroid computation 16 ⟩  
        ⟨ Pixel transformation 20 ⟩  
    end  
    ◇
```

10.1 Installing the library

11 Conclusions

11.1 Results

11.2 Further improvements

References

- [CL13] CVD-Lab, *Linear Algebraic Representation*, Tech. Report 13-00, Roma Tre University, October 2013.
- [PDFJ15] Alberto Paoluzzi, Antonio DiCarlo, Francesco Furiani, and Miroslav Jirik, *CAD models from medical images using LAR*, Computer-Aided Design and Applications **13** (2015), To appear.
- [W3C] W3C, *Portable Network Graphics (PNG) Specification (Second Edition)*, Tech. report.

A Utility functions

B Tests

Generation of the border matrix

```
"test/generateBorderMatrix.jl" 78b≡
```

[illegible]


```

end

function executeAllTests()
    @time testComputeOriented3Border()
    @time testWriteBorder()
    println("Tests completed.")
end

executeAllTests()

◇

```

Conversion of a png stack to a 3D array

```

"test/pngStack2Array3dJulia.jl" 80≡
push!(LOAD_PATH, "../..")
import PngStack2Array3dJulia
using Base.Test

function testGetImageData()
    """
    Test function for getImageData
    """

    width, height = PngStack2Array3dJulia.getImageData("images/0.png")

    @test width == 50
    @test height == 50

end

function testCalculateClusterCentroids()
    """
    Test function for calculateClusterCentroids
    """

    path = "images/"
    image = 0
    centroids = PngStack2Array3dJulia.calculateClusterCentroids(path, image, 2)

    expected = [0, 253]
    centroids = vec(reshape(centroids, 1, 2))

    @test sort(centroids) == expected

```

```

end

function testPngstack2array3d()
    """
    Test function for pngstack2array3d
    """
    path = "images/"
    minSlice = 0
    maxSlice = 4
    centroids = PngStack2Array3dJulia.calculateClusterCentroids(path, 0, 2)
    image3d = PngStack2Array3dJulia.pngstack2array3d(path, minSlice, maxSlice, centroids)

    @test size(image3d)[1] == 5
    @test size(image3d[1])[1] == 50
    @test size(image3d[1])[2] == 200

end

function executeAllTests()
    @time testCalculateClusterCentroids()
    @time testPngstack2array3d()
    @time testGetImageData()
    println("Tests completed.")
end

executeAllTests()

◇

```

Test for LAR utilities

```

"test/LARUtils.jl" 81≡
push!(LOAD_PATH, "../..")
import LARUtils
using Base.Test

function testInd()
    """
    Test function for ind
    """

    nx = 2
    ny = 2

```

```

    @test LARUtils.ind(0, 0, 0, nx, ny) == 0
    @test LARUtils.ind(1, 1, 1, nx, ny) == 13
    @test LARUtils.ind(2, 5, 4, nx, ny) == 53
    @test LARUtils.ind(1, 1, 1, nx, ny) == 13
    @test LARUtils.ind(2, 7, 1, nx, ny) == 32
    @test LARUtils.ind(1, 0, 3, nx, ny) == 28
end

function executeAllTests()
    @time testInd()
    println("Tests completed.")
end

executeAllTests()

◇

```