

Tutorials Electromagnetic Theory
(Term: Aug to Dec 2019)

1. Given $\vec{D} = (2y^2z - 8xy)\hat{i} + (4xyz - 4x^2)\hat{j} + (2xy^2 - 4z)\hat{k}$. Determine the total charge within a volume 10^{-14} m^3 at P (1,-2,3), if the divergence of \vec{D} gives the charge density ρ_v .
2. Given $\vec{D} = 9x^3\hat{i} + 5y^2\hat{j} + 2z\hat{k} \text{ Cm}^{-2}$. If the divergence of \vec{D} represents the charge density ρ_v , find ρ_v at the point (1,5,9) m.
3. Given $\vec{D} = 4x\hat{i} + 3y^2\hat{j} + 2z^3\hat{k} \text{ Cm}^{-3}$. If the divergence of \vec{D} represents the charge density ρ_v , then find the total charge in a volume defined by six planes for which $1 \leq x \leq 2, 2 \leq y \leq 3, 3 \leq z \leq 4$.
4. The magnetic field intensity is given in a certain region of space as

$$\vec{H} = \frac{x+2y}{z^2}\hat{j} + \frac{2}{z}\hat{k} \text{ Am}^{-1}.$$

Find the curl of the magnetic field.

5. A point charge, $Q = 30\text{nC}$ is located at the origin in Cartesian system. Find the electric flux density and the electric field intensity at (1, 3,-4).
6. Suppose $A = x^2z^2\hat{i} - 2y^2z^2\hat{j} + xy^2z\hat{k}$. Find $\nabla \cdot A$ at the point P (1,-1, 1).
7. A parallel plate capacitor consists of plates of area 10 cm^2 with separation 10mm and dielectric medium of permittivity $\epsilon = 4 \epsilon_0$. Calculate the displacement current, if the voltage applied is $15 \sin(1000t)$ and $\epsilon = 4 \epsilon_0$.
8. $\vec{A} = x^2yz\hat{i} + xy^2z\hat{j} + xyz^2\hat{k}$. Determine curl \vec{A} .
9. $\vec{A} = x\hat{i} + y\hat{j} + z\hat{k}$. Find div A and curl \vec{A} .

$$(\epsilon_0 = 8.854 \times 10^{-12} \text{ Fm}^{-1})$$