

401

> solve(exp(2 x) = 3, x)

$$\frac{1}{2} \ln(3)$$

(1)

> fsolve(exp(2 x) = 3, x)

$$0.5493061443$$

(2)

> solve(exp(-x) = 4 exp(x) + 1, x)

$$\ln\left(-\frac{1}{8} - \frac{1}{8} \sqrt{17}\right), \ln\left(-\frac{1}{8} + \frac{1}{8} \sqrt{17}\right)$$

(3)

> fsolve(exp(-x) = 4 exp(x) + 1, x)

$$-0.9406136421$$

(4)

402

> solve(sqrt(x - 8) + sqrt(x) = 2, x)

> fsolve(sqrt(x - 8) + sqrt(x) = 2, x)

$$fsolve(\sqrt{x-8} + \sqrt{x} = 2, x)$$

(5)

> solve(sqrt(x - 8) + sqrt(x) = 12, x)

$$\frac{361}{9}$$

(6)

> fsolve(sqrt(x - 8) + sqrt(x) = 12, x)

$$40.11111111$$

(7)

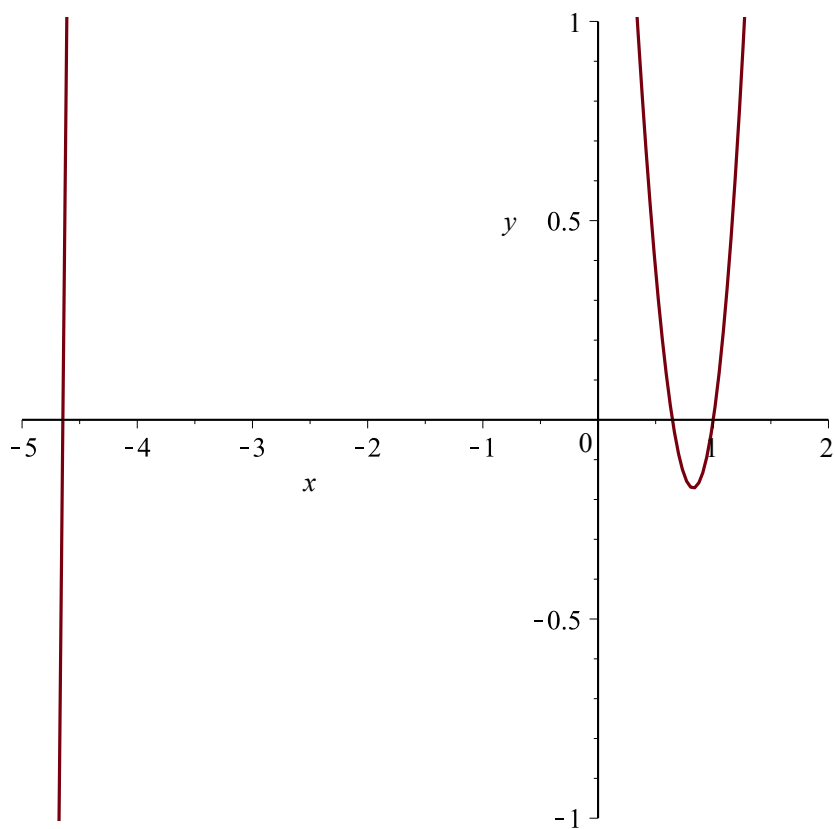
403

> f403 := x → x³ + 3 x² - 7 x + 3

$$f403 := x \rightarrow x^3 + 3 x^2 - 7 x + 3$$

(8)

> plot(f403(x), x = -5 .. 2, y = -1 .. 1)



```
> fsolve(f403(x) = 0, x, x = -5 .. 0)
```

-4.645751311

(9)

```
> fsolve(f403(x) = 0, x, x = 0 .. 0.9)
```

0.6457513111

(10)

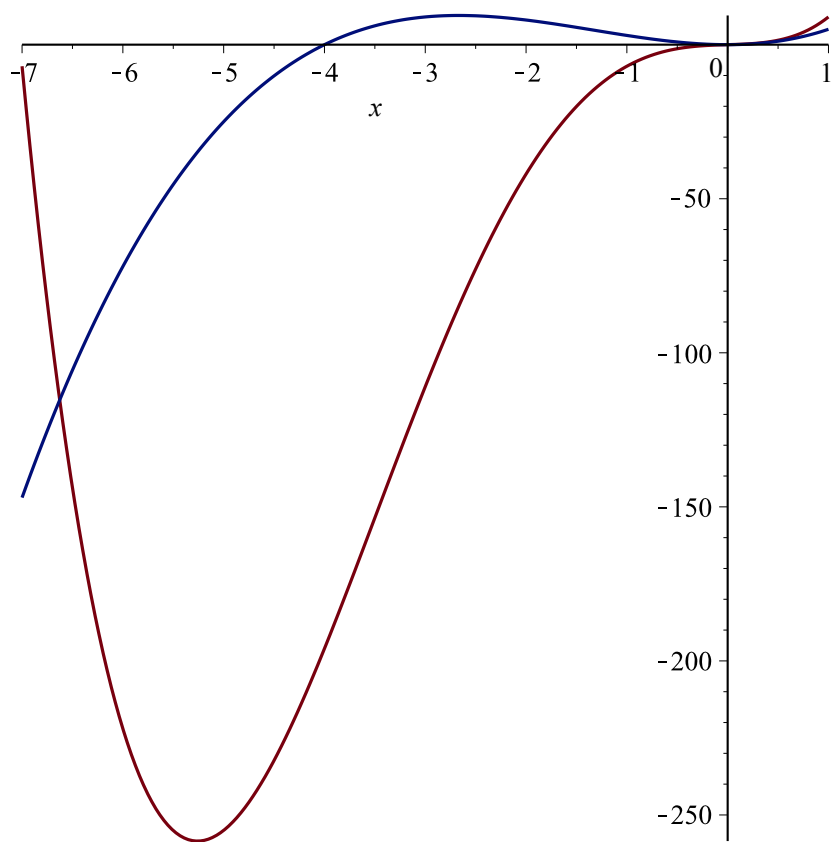
```
> fsolve(f403(x) = 0, x, x = 0.9 .. 2)
```

1.

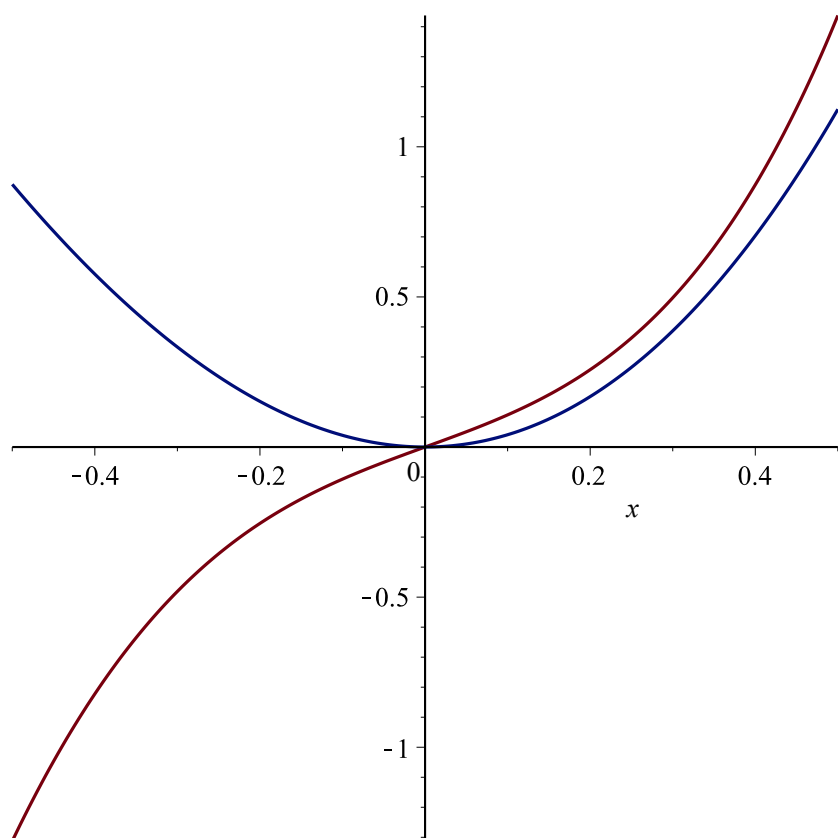
(11)

```
404
```

```
> plot([x^4 + 7 x^3 + x, x^3 + 4 x^2], x = -7 .. 1)
```



```
> plot([x^4 + 7 x^3 + x, x^3 + 4 x^2], x=-0.5..0.5)
```



```
> Digits := 3
```

```
Digits := 3
```

(12)

```
> fsolve( $x^4 + 7x^3 + x = x^3 + 4x^2$ , x, x = -7 .. -6)
```

```
-6.63
```

(13)

```
> fsolve( $x^4 + 7x^3 + x = x^3 + 4x^2$ , x, x = -6 .. 5)
```

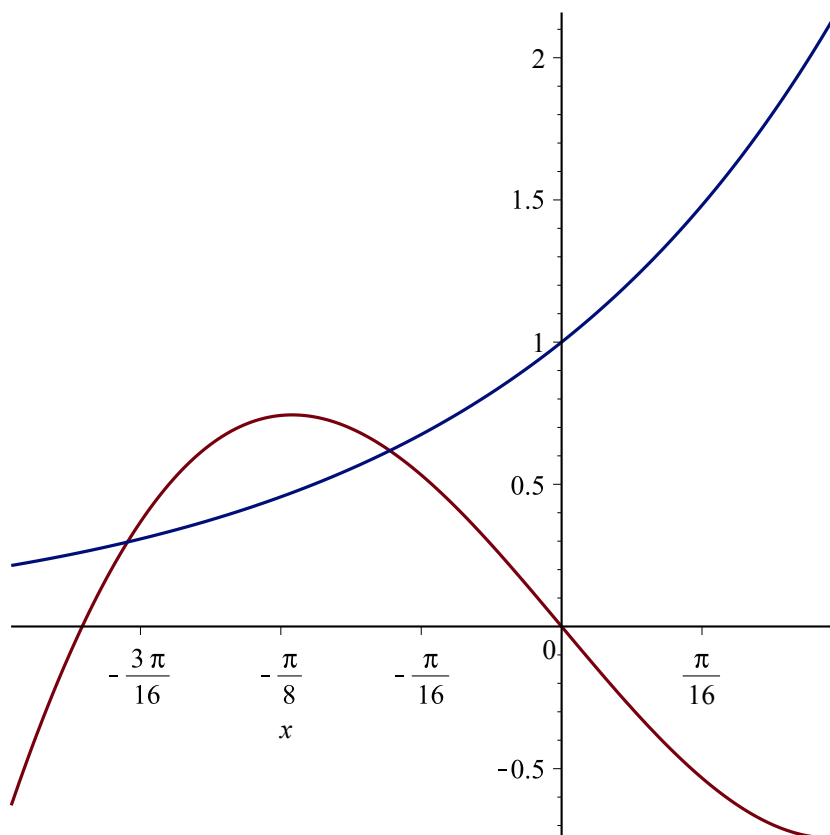
```
0.
```

(14)

Two more solutions must be complex

405

```
> plot( $[3x^3 - \sin(3x), \exp(2x)]$ , x = - $\frac{\text{Pi}}{4}$  ..  $\frac{\text{Pi}}{8}$ )
```



```
> fsolve(3 x^3 - sin(3 x) = exp(2 x), x, x = - Pi/4 .. - Pi/8 )
-0.607
```

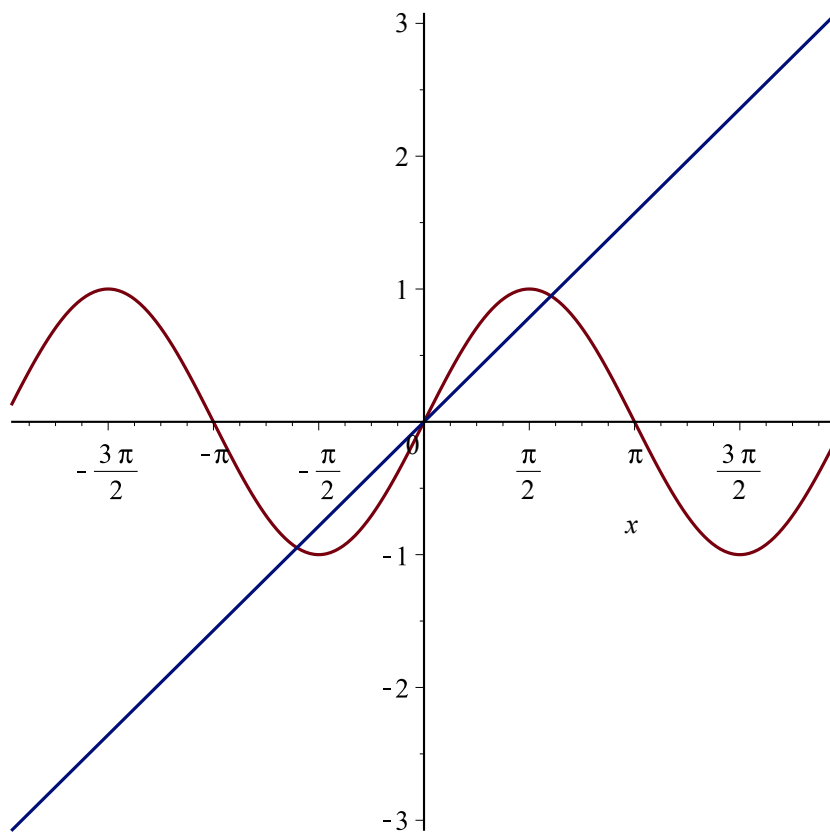
(15)

```
> fsolve(3 x^3 - sin(3 x) = exp(2 x), x, x = - Pi/8 .. 0 )
-0.240
```

(16)

```
406
```

```
> plot([ sin(x), x/2 ])
```



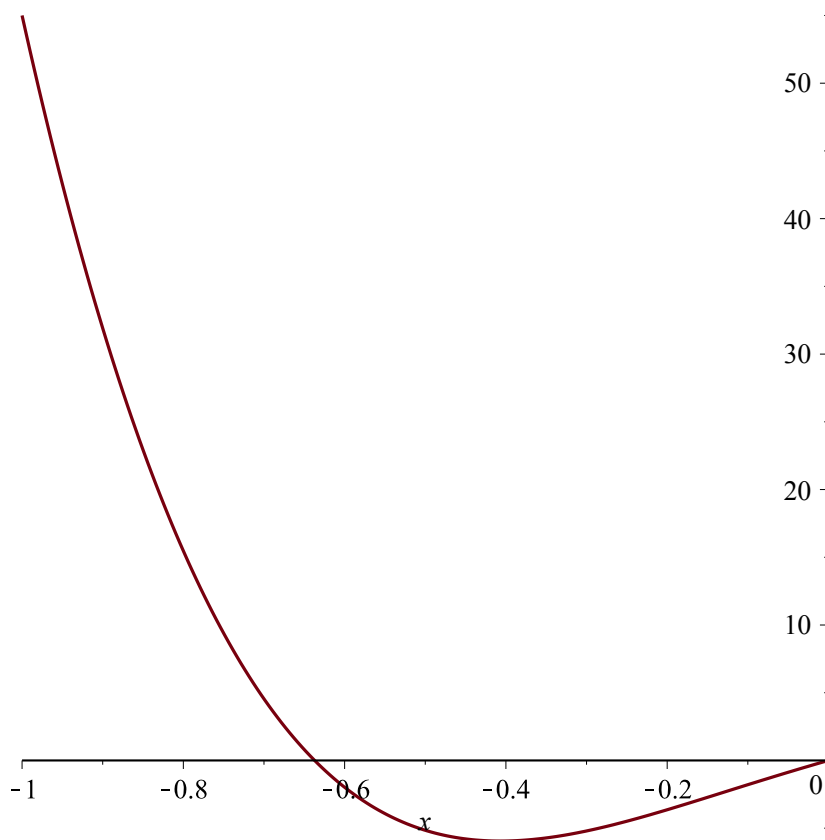
```
> fsolve(sin(x) = x/2, x, x=-Pi..-Pi/2)
```

-1.90

(17)

```
407
```

```
> plot(23 x^5 + 105 x^4 - 10 x^2 + 17 x, x=-1..0)
```



```
> fsolve(23 x^5 + 105 x^4 - 10 x^2 + 17 x = 0, x, x = -1 .. -0.5)
-0.637 (18)
```

```
> fsolve(23 x^5 + 105 x^4 - 10 x^2 + 17 x = 0, x, x = -0.5 .. 0)
0. (19)
```

```
408
> f408 := x -> exp(0.2 x) * (a * x^2 + b * x + c)
f408 := x -> e^{0.2 x} (a x^2 + b x + c) (20)
```

```
> gl408 := {f408(0) = 2, f408(1) = 3, f408(2) = 5}
gl408 := {1. c = 2, 1.22 a + 1.22 b + 1.22 c = 3, 5.96 a + 2.98 b + 1.49 c = 5} (21)
```

```
> solve(gl408, {a, b, c})
{a = 0.219, b = 0.240, c = 2.} (22)
```

```
> assign(%)
> f408(x)
e^{0.2 x} (0.219 x^2 + 0.240 x + 2.) (23)
```

```
> f408(-2)
1.61 (24)
```

```
409
```

```
> solve( {x + a·y=2, x - y=0}, {x, y})
{x=1.64, y=1.64} (25)
```

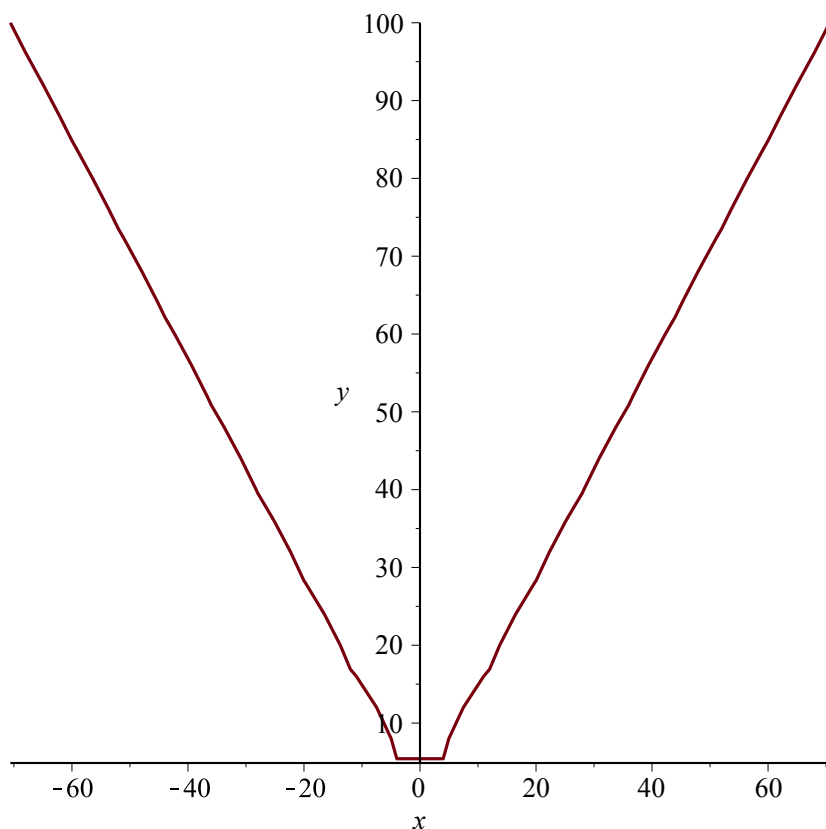
```
410
```

```
> solve( { (x - 2)2 + (y - 3)2 = 16, 3 x - 2 y = 3 }, {x, y})
{x=RootOf(13 _Z2 - 70 _Z + 33), y= 3/2 RootOf(13 _Z2 - 70 _Z + 33) - 3/2 } (26)
```

```
> allvalues(%)
{x= 35/13 - 2/13 √199, y= 33/13 - 3/13 √199}, {x= 35/13 + 2/13 √199, y= 33/13
+ 3/13 √199} (27)
```

```
411
```

```
> with(plots) :
pl4111 := implicitplot(2 x2 - y2 = -1, x=-100..100, y=0..100) :
pl4112 := implicitplot(x4 + y4 = 2, x=-100..100, y=0..100) :
display(pl4111, pl4112)
```



```
> , solve( {2 x2 - y2 = -1, x4 + y4 = 2, y > 0}, {x, y})
```


$$\left\{ x = \frac{1}{5} \sqrt{5}, y = \frac{1}{5} \sqrt{35} \right\}, \left\{ x = -\frac{1}{5} \sqrt{5}, y = \frac{1}{5} \sqrt{35} \right\} \quad (28)$$

$$\begin{aligned} & \text{fsolve}(\{2x^2 - y^2 = -1, x^4 + y^4 = 2\}, \{x, y\}) \\ & \{x = 0.447, y = -1.18\} \end{aligned} \quad (29)$$