

ALL ABOUT NUMBER SYSTEMS

PRESENTED BY: GESITE, DAN JOSEPH

TODAY'S AGENDA

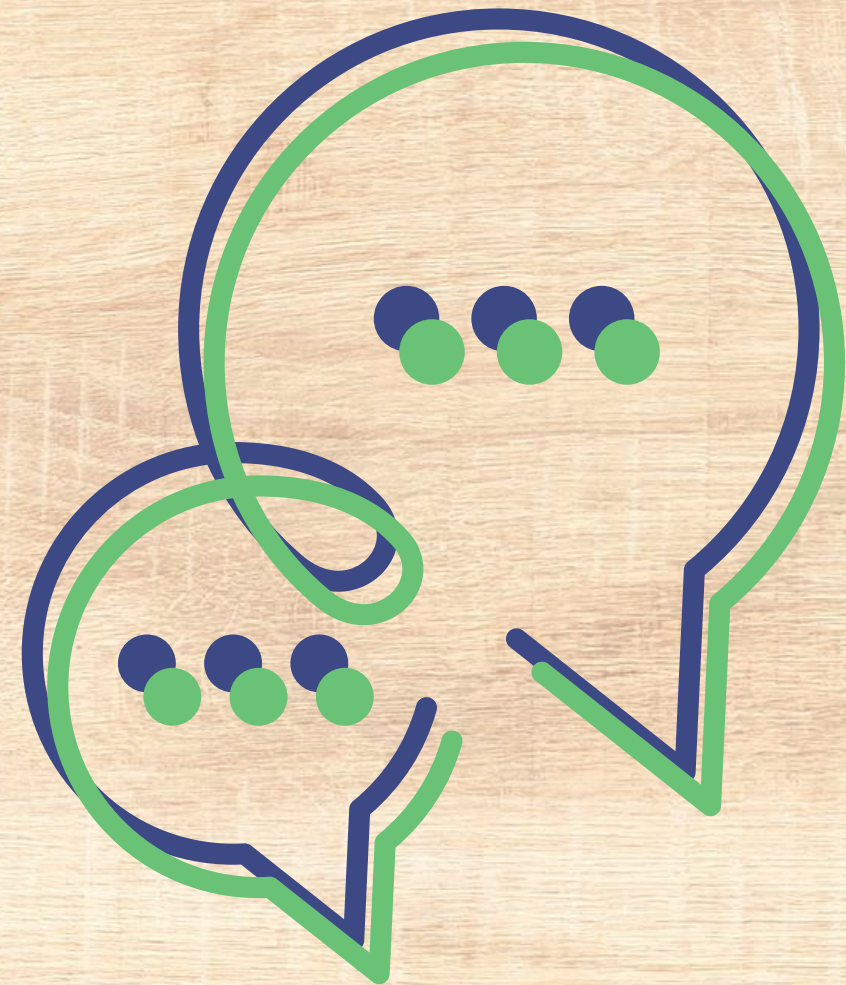
**What are
Number
Systems?**

**Types of
Number
Systems**

**What are the
uses/significance
of each number
system?**

WHAT ARE NUMBER SYSTEMS

A number system is a mathematical method for representing numbers, allowing arithmetic operations like addition, subtraction, multiplication, and division. It includes binary, octal, decimal, and hexadecimal number systems with distinct attributes.



INTRODUCTION TO COMPUTING

WHAT ARE NUMBER SYSTEMS

➤ The decimal number system

➤ The octal number system

➤ The binary number system

➤ The hexadecimal number system

DECIMAL NUMBER SYSTEM

The base 10 number system, also known as the decimal number system, uses digits 0-9 to represent numbers. Each digit has a place value, which increases by 10 times as we move from right to left. The decimal number system uses ten digits (0,1,2,3,4,5,6,7,8,9) with a base of 10. Any number without a base is represented as 10.

Position weights $\rightarrow 10^2 \ 10^1 \ 10^0$
Number digits \rightarrow

3	7	5
---	---	---

The diagram shows three arrows originating from the digits in the table and pointing to the following calculations:

- From the digit 5: $5 \times 10^0 = 5 +$
- From the digit 7: $7 \times 10^1 = 70 +$
- From the digit 3: $3 \times 10^2 = 300$

The final result is shown as a sum:

$$\begin{array}{r} 5 + \\ 70 + \\ 300 \\ \hline 375 \end{array}$$

BINARY NUMBER SYSTEM

A computer understands only the "on" and "off" states of a switch, represented by 1 and 0. The binary number system uses positional notation, with each digit multiplied by a power of two. A bit is the smallest unit of memory or instruction on a computer, either a 0 or 1. Combinations of bytes, known as kilobytes, form collections of 1000 bytes, with kilobytes containing approximately one thousand letters.

Position weights	→	2^2	2^1	2^0	
Number digits	→	1	1	0	
					$0 \times 2^0 = 0 +$
					$1 \times 2^1 = 2 +$
					$1 \times 2^2 = 4$
					<hr/>
					6

OCTAL NUMBER SYSTEM

The octal number system, used in minicomputers, uses eight digits (0 to 7), with a base of 8, and is similar to binary but excludes 8 and 9 digits. It represents numbers with a base of 8.

Positional powers of 8:	8^2	8^1	8^0
Decimal positional value:	64	8	1
Octal number:	3	5	7

$$\begin{array}{r} (3 \times 64) + (5 \times 8) + (7 \times 1) \\ 192 + 40 + 7 \\ 357_8 = \underline{239}_{10} \end{array}$$

HEXADECIMAL NUMBER SYSTEM

The hexadecimal number system uses sixteen digits/alphabets, with the base number being 16. A-F represents numbers 10-15 in the decimal number system.

Hexadecimal	0	1	2	3	4	5	6	7	8
Decimal	0	1	2	3	4	5	6	7	8
Hexadecimal	9	A	B	C	D	E	F		
Decimal	9	10	11	12	13	14	15		

Positional powers of 16: 16^3 16^2 16^1 16^0
Decimal positional value: 4096 256 16 1
Hexadecimal number: 1 F 4

$$\begin{aligned} & (1 \times 256) + (F \times 16) + (4 \times 1) \\ &= (1 \times 256) + (15 \times 16) + (4 \times 1) \\ &= 256 + 240 + 4 = 500_{10} \end{aligned}$$

CONVERSION

BINARY TO DECIMAL

$$\begin{array}{r} 01101_2 \\ \begin{array}{l} 1 \times 2^0 = 1 \\ 0 \times 2^1 = 0 \\ 1 \times 2^2 = 4 \\ 1 \times 2^3 = 8 \\ 0 \times 2^4 = 0 \\ 1 \times 2^5 = 32 \end{array} \\ 32 + 8 + 4 + 1 = 45_{10} \end{array}$$

DECIMAL TO BINARY

$$\begin{array}{r} 45_{10} \\ 2 \overline{)45} \\ 2 \overline{)22} \\ 2 \overline{)11} \\ 2 \overline{)5} \\ 2 \overline{)2} \\ 2 \overline{)1} \\ 1 \end{array} \begin{array}{l} 1 \uparrow \\ 0 \\ 1 \\ 1 \\ 1 \\ 0 \\ 1 \end{array} = 101101_2$$

OCTAL TO DECIMAL

$$\begin{array}{r} 140_8 \\ \begin{array}{ccc} 8^2 & 8^1 & 8^0 \\ \downarrow & \downarrow & \downarrow \\ 64 & 8 & 1 \end{array} \\ (1 \times 64) + (4 \times 8) + (0 \times 1) \\ 64 + 32 \\ = 96_{10} \end{array}$$

DECIMAL TO OCTAL

$$\begin{array}{r} 96_{10} \\ 8 \overline{)96} \\ 8 \overline{)12} \\ 8 \overline{)1} \\ 0 \uparrow \\ 1 \uparrow \\ 1 \end{array} = 140_8$$

HEXADECIMAL TO DECIMAL

$$\begin{array}{r} 23E_{16} \\ \begin{array}{ccc} 16^2 & 16^1 & 16^0 \\ \downarrow & \downarrow & \downarrow \\ 256 & 16 & 1 \end{array} \\ (2 \times 256) + (3 \times 16) + (14 \times 1) \\ 512 + 48 + 14 \\ = 574_{10} \end{array}$$

DECIMAL TO HEXADECIMAL

$$\begin{array}{r} 574_{10} \\ 16 \overline{)574} \\ 16 \overline{)35} \\ 16 \overline{)2} \\ 14 = E \\ 3 \\ 2 \\ = 23E_{16} \end{array}$$

CONVERSION

BINARY TO OCTAL

110101_2
 $101 = 5$
 $110 = 6$
 $= 65_8$

OCTAL TO DECIMAL

65_8
 $6 = 110$
 $5 = 101$
 $= 110101_2$

BINARY TO HEXADECIMAL

1011011_2
 $0111 = 7$
 $1011 = 11 \text{ or } B$
 $= B7_{16}$

HEXADECIMAL TO DECIMAL

$B7$
 $B = 1011$
 $7 = 0111$
 $= 1011011_2$

OCTAL TO HEXADECIMAL

213_8
 $3 = 011$ 0100 01011
 4 B
 $1 = 001$
 $2 = 010$
 $= 8B_{16}$

HEXADECIMAL TO OCTAL

$8B_{16}$
 $8 = 1000$ 10001011
 4 2 1 3
 $B = 1011$
 $= 213_8$



THANK YOU

PRESENTED BY: GESITE, DAN JOSEPH C.