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Ordering in bidirectional pedestrian flows and its influence on the fundamental diagram

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Abstract. Experiments under laboratory conditions were carried out to study the ordering in bidirectional pedestrian streams and its influence on the fundamental diagram (density–speed–flow relation). The Voronoi method is used to resolve the fine structure of the resulting velocity–density relations and spatial dependence of the measurements. The data show that the specific flow concept is applicable also for bidirectional streams. For various forms of ordering in bidirectional streams, no large differences among density–flow relationships are found in the observed density range. The fundamental diagrams of bidirectional streams with different forms of ordering are compared with those of unidirectional streams. The result shows differences in the shape of the relation for $\rho > 1.0 \text{ m}^{-2}$. The maximum of the specific flow in unidirectional streams is significantly larger than that in all bidirectional streams examined.

Keywords: traffic and crowd dynamics

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1. Introduction

In the last few decades, problems related to bidirectional flow and its effects on pedestrian dynamics have gained increasing attention. A large number of models [1]–[6] have been developed to understand the basic characteristics related to bidirectional flow including lane formation [5, 7, 8], jamming transition [2, 6, 9, 10] and fundamental diagram [11]. Computer simulations of various models have found a jamming transition from a free flow state to a jammed state. However, this phenomenon has never been observed in experimental as well as field studies.

Furthermore, a large number of empirical studies have been conducted to investigate the characteristics of bidirectional flow. Pedestrian flow characteristics at crosswalks [12]–[16] and shopping streets [17] were studied in different countries. Some of the studies compare mean walking speed and maximum flow rate among different regions. The influence of facility width on the pedestrian characteristics is studied in [15, 17]. Figure 1 assembles the fundamental diagrams of bidirectional flow from these empirical studies. From the density–velocity relationship in figure 1(a) it can be seen that they follow nearly the same trend. Further, we compare the relationship between density and specific flow J_s , as shown in figure 1(b), using the hydrodynamic relation $J_s = \rho \cdot v$. In this graph, differences can be observed especially for densities $\rho > 2.0 \text{ m}^{-2}$. The density values where the specific flow reaches the maximum range from about 1.3 to 2.3 m^{-2} . Also the maximum specific flows from different studies range from about 1.0 to 2.0 $\text{m}^{-1} \text{ s}^{-1}$. But from these studies no conclusion could be drawn at which density the flow reaches zero due to congestion.

On the other hand, there is still no consensus whether the fundamental diagrams of uni- and multi-directional flows are different or not. Predtechenskii and Milinskii [19] and Weidmann [18] neglected the differences in accordance with Fruin, who states that the fundamental diagrams of multi- and unidirectional flow differ only slightly [20]. This disagrees with results of Navin and Wheeler [16] who found a reduction of the flow

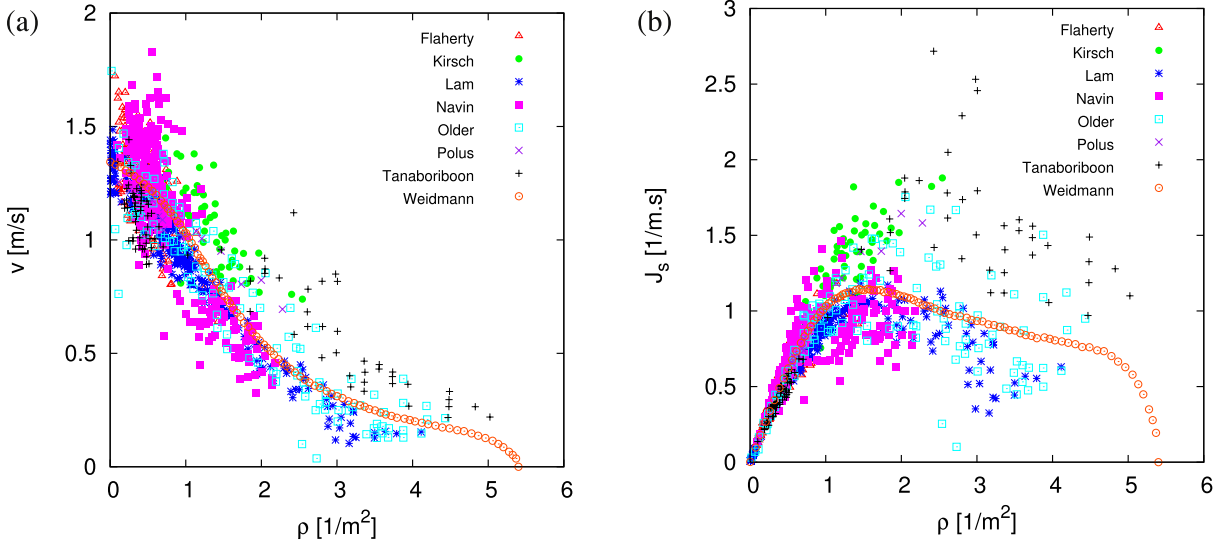


Figure 1. Comparison of fundamental diagrams of bidirectional pedestrian flow from various studies. Note that the data given by Weidmann [18], who performed a metastudy, is an idealized fundamental diagram obtained by collecting and fitting 25 other experiments. (a) Density–velocity and (b) density–specific flow.

dependent on directional imbalances. Further, Pushkarev *et al* [21] and Lam *et al* [12, 22] assume that bidirectional flow is not substantially different from unidirectional flow as long as the densities of the opposite streams are not too different. However, Older *et al* state that different ratios of flow in the bidirectional stream do not show any consistent effect on the walking speed [17]. Besides, Helbing *et al* [23] concluded that counterflows are significantly more efficient than unidirectional flows. However, they compare average flow values without considering the influence of the density. Kretz *et al* [7] have reported similar findings, but the influence of density and variations in time on the flow are not considered in this study. Facing these disagreements, we collect the fundamental diagrams of unidirectional [24]–[27] and bidirectional flow in figure 2. It seems that the fundamental diagrams of unidirectional flow lie above those of bidirectional flow, especially for $\rho > 1.0 \text{ m}^{-2}$. Since the data compared are obtained under different experimental situations and different measurement methods, thus we could not conclude whether and how the type of flow (uni- or bidirectional) influences the fundamental diagram.

The above discussion shows that up to now there is no consensus about the origin of the discrepancies between different types of pedestrian flow. In our study, we carry out a series of laboratory experiments of bidirectional and unidirectional pedestrian streams. The formation of lanes in bidirectional streams depends on time as well as space and could be stable or unstable. Moreover the opposing flows in bidirectional streams could be balanced or unbalanced. To categorize these types, we classify the bidirectional streams into *stable separated lanes (SSL)* and *dynamical multi-lanes (DML) flow*. According to the typical densities in the opposing streams we introduce the types *balanced flow ratio (BFR)* and *unbalanced flow ratio (UFR)*. The aim of our study is to obtain the fundamental diagrams and calibrate the previous research results. We will study the effects of different corridor widths and different flow types on the fundamental diagrams of bidirectional

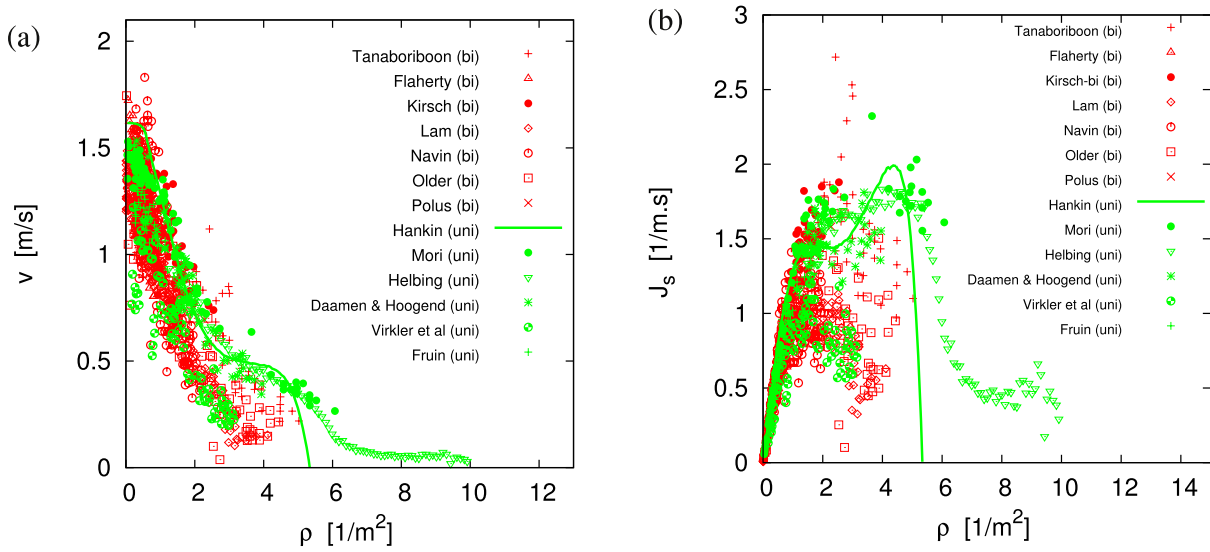


Figure 2. The fundamental diagram of uni- and bidirectional pedestrian flow from different previous studies. (a) Density–velocity and (b) density–specific flow.

streams. We also compare the fundamental diagram of unidirectional and bidirectional streams.

The structure of this paper is as follows. In section 2 we describe the set-up of the experiment. The identification of lanes is studied by means of the Voronoi diagram in section 3. Section 4 compares the fundamental diagrams for different stream types. Finally, the conclusions from our investigations will be discussed.

2. Experiment set-up

The experiments were performed in Hall 2 of the Fairground Düsseldorf (Germany) in May 2009. Up to 350 participants, mostly students, participated in the experiments. Each of them was paid 50 €/day. The mean age and height of the participants was 25 ± 5.7 years and 1.76 ± 0.09 m, respectively. The average free velocity $v_0 = 1.55 \pm 0.18$ m s⁻¹ was obtained by measuring the free movement of 42 participants.

Figure 3 shows a sketch of the experimental set-up. 22 runs of bidirectional pedestrian streams (see tables 1–3) were performed in straight corridors with widths of 3.0 m and 3.6 m, respectively. To control the density inside the corridor and the ratio of the opposing streams, the widths b_l of the left entrance and b_r of the right entrance were changed in each run (for details, see figure 3 and tables 1–3). Before the start of an experiment, the participants were arranged within the waiting area at the left and right side of the corridor. At the beginning of each run, the pedestrians pass through a 4 m passage into the corridor. The passage was used as a buffer to minimize the effect of the entrance. In this way, the flow in the corridor was nearly homogeneous over the entire width of the corridor. When a pedestrian arrived at the other side of the corridor, he or she left the corridor from the passage and returned to the waiting area for the next run. To vary the form of the ordering the test persons get different instructions and the width of the entrances is changed. These variations result in different types of bidirectional flow.

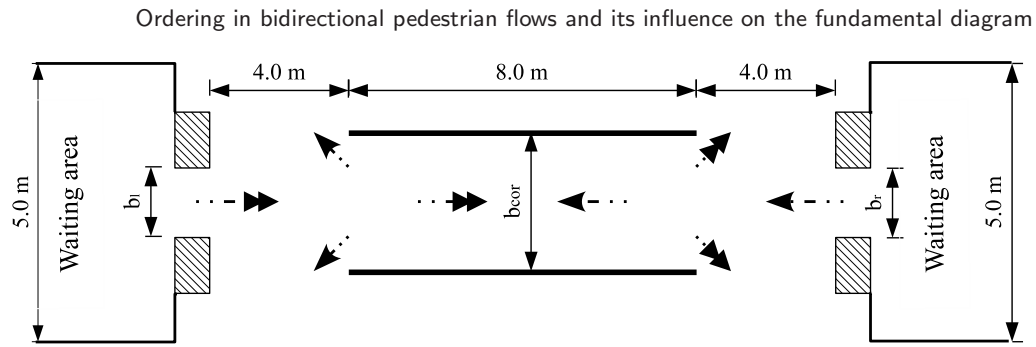


Figure 3. Schematic illustration of the bidirectional pedestrian experiment in a corridor.

Table 1. The related parameters in BFR-SSL experiments.

Index	Name	b_{cor} (m)	b_l (m)	b_r (m)	N_l	N_r
1	BFR-SSL-360-050-050	3.60	0.50	0.50	57	61
2	BFR-SSL-360-075-075	3.60	0.75	0.75	56	80
3	BFR-SSL-360-090-090	3.60	0.90	0.90	109	105
4	BFR-SSL-360-120-120	3.60	1.20	1.20	143	164
5	BFR-SSL-360-160-160	3.60	1.60	1.60	143	166

Table 2. The related parameters in BFR-DML experiments.

Index	Name	b_{cor} (m)	b_l (m)	b_r (m)	N_l	N_r
1	BFR-DML-300-050-050	3.00	0.50	0.50	54	71
2	BFR-DML-300-065-065	3.00	0.65	0.65	64	83
3	BFR-DML-300-075-075	3.00	0.75	0.75	61	86
4	BFR-DML-300-085-085	3.00	0.85	0.85	119	97
5	BFR-DML-300-100-100	3.00	1.00	1.00	125	105
6	BFR-DML-360-050-050	3.60	0.50	0.50	56	74
7	BFR-DML-360-075-075	3.60	0.75	0.75	62	65
8	BFR-DML-360-090-090	3.60	0.90	0.90	110	102
9	BFR-DML-360-120-120	3.60	1.20	1.20	115	106
10	BFR-DML-360-160-160	3.60	1.60	1.60	140	166
11	BFR-DML-360-200-200	3.60	2.00	2.00	143	166
12	BFR-DML-360-250-250	3.60	2.50	2.50	141	163

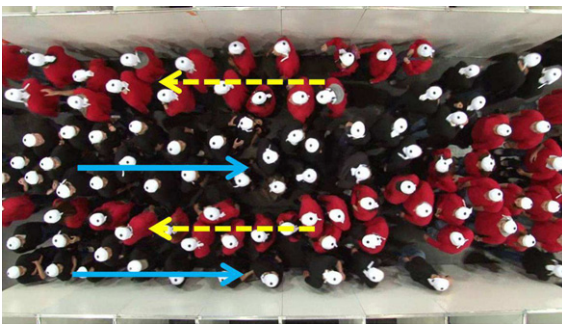
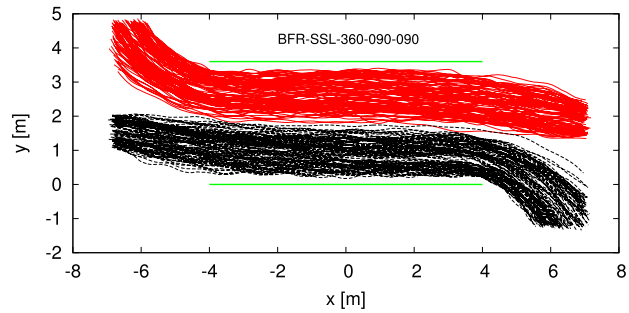
BFR-SSL flow (figure 4(a)): this type of flow was realized in our experiments by using the same entrance width for both directions ($b_l = b_r$) and giving no instruction to the test persons about which exit they have to choose. The opposing flows segregate and occupy proportional shares of the corridor. Stable lanes formed autonomously and immediately after the run starts.

BFR-DML flow (figure 4(b)): again identical widths b_l and b_r are chosen in the experiments, but the instruction to the test person at the beginning of the experiments changed. The participants were asked to choose an exit at the end of the corridor according to a number given to them in advance (odd numbers exit to the left, even numbers to the right). With this initial condition again lane formation is observable, but the lanes are

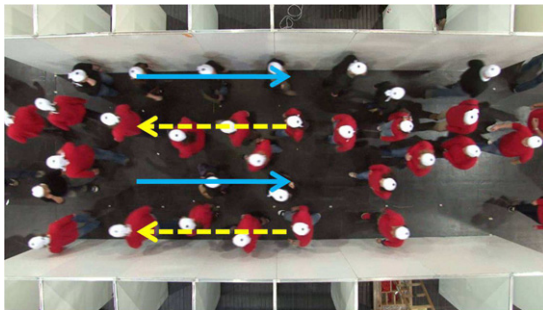
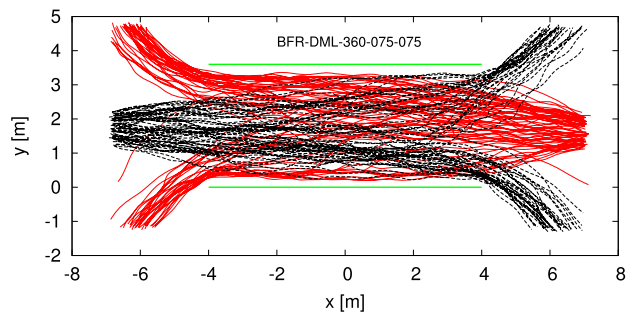
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(a)



(b)



(c)

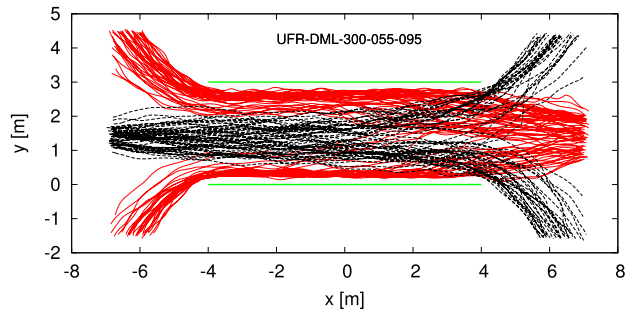


Figure 4. Snapshots from the experiments (left) and actual trajectories of pedestrians (right). In the plots, red solid lines represent the paths of left moving pedestrians, while the black dashed lines represent the paths of right moving pedestrians. (a) BFR-SSL, (b) BFR-DML and (c) UFR-DML.

Table 3. The related parameters in UFR-DML experiments.

Index	Name	b_{cor} (m)	b_l (m)	b_r (m)	N_l	N_r
1	UFR-DML-300-050-070	3.00	0.50	0.70	72	63
2	UFR-DML-300-050-085	3.00	0.50	0.85	61	64
3	UFR-DML-300-055-095	3.00	0.55	0.95	58	70
4	UFR-DML-300-065-105	3.00	0.65	1.05	117	112
5	UFR-DML-300-080-120	3.00	0.80	1.20	116	103

unstable and vary in time and space. This type of flow is comparable with two streams crossing at a small angle.

UFR-DML flow (figure 4(c)): in this case the widths of entrances b_l and b_r are different and the participants are instructed to choose an exit at the end of the corridor according to a number given at the beginning of the day (odd numbers left, even numbers to the right). Again lanes are unstable and vary in time and space. The cumulated trajectories indicate that the flow ratio of the opposing streams is unbalanced.

The experiments were recorded by two cameras mounted on a rack at the ceiling of the hall. To cover the complete region, the left and the right part of the corridor were recorded separately. The trajectories were automatically extracted from video recordings using the software PeTrack [28]. Finally, the trajectories from the two cameras were corrected and combined. All the analysis and the pedestrian characteristics below including flow, density and velocity are obtained from these trajectories.

3. Lane formation

Lane formation, as an important phenomenon in bidirectional flow, occurs because pedestrians follow closely behind some other person who moves in the same direction to minimize conflicts with persons moving in the opposite direction. Lanes that emerge in this way could be stable (SSL) and unstable (DML). The recognition and representation of the lanes has been investigated in different ways, e.g. the cluster analysis method introduced by Hoogendoorn [8], the bond index method of Yamori [29] *et al* as well as the laning order parameter used to detect lanes in driven colloidal systems [30]. In this study, using the Voronoi method introduced in [31, 32], we are able to calculate the integrated velocity over small (10 cm) measurement regions. In this way, the velocity distribution over the whole space can be easily obtained. Figure 5 shows the velocity and density profiles of BFR-DML-360-160-160 for two different times. We use different colors to present the value of the velocity and density. Then the number of lanes in the corridor can be easily determined from the velocity profiles. The velocity profiles seem to be a good way to display the lane formation in bidirectional streams. In comparison, density profiles do not have such an ability to show the lanes clearly. However, it is possible for density profiles to show some other information such as crowded and dangerous spots.

4. Fundamental diagram

In this study we use the Voronoi method [31, 32] to analyze the flows quantitatively. We have verified that alternative methods (see the discussion in [31]) do not lead to large changes in the fundamental diagrams. The advantage of the Voronoi method lies in its small scatter and high resolution in time and space.

For the analysis a rectangle with a length of 2 m from $x = -1$ to 1 m and the width of the corridor is chosen as the measurement area. We calculate the densities and velocities every frame (corresponding to 0.0625 s) with a frame rate of 16 fps. To determine the fundamental diagram only data from stationary flows are used, which are selected manually by analyzing the time series of density and velocity. Finally, we use one frame per second to limit the number of data points. The influences of corridor width and

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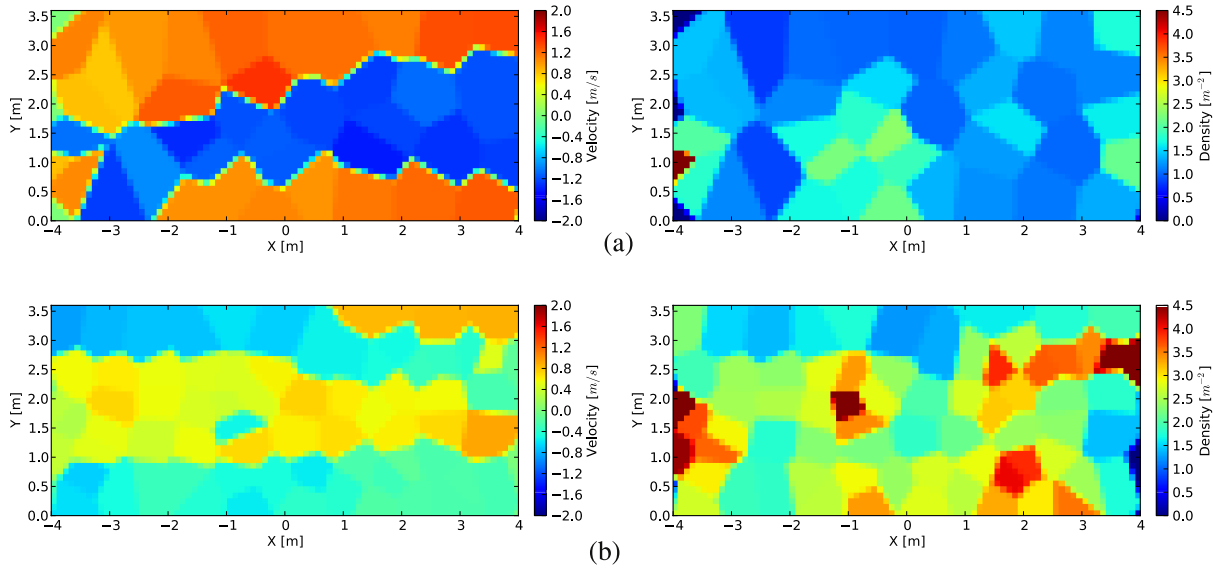


Figure 5. Velocity and density profiles of experiment BFR-DML-360-160-160 for different frames (times). (a) $t = 222$ frame = 13.875 s and (b) $t = 822$ frame = 51.375 s.

the type of flow on the fundamental diagram are studied and compared with the diagram of unidirectional flow.

4.1. Influence of corridor width

Firstly, we study the influence of the corridor width on the fundamental diagram. For BFR-DML flow, two widths $b_{\text{cor}} = 3.0$ and 3.6 m are chosen in the experiments and the fundamental diagrams are compared. Due to the limitation of the time resources for the experiment only densities $\rho < 2.0 \text{ m}^{-2}$ are realized for $b_{\text{cor}} = 3.0$ m. As shown in figure 6, the fundamental diagrams are in good agreement for different widths. Figure 6(b) shows the relationship between the Voronoi density and specific flow for these two widths. The specific flow reaches its maximum of $1.5 \text{ m}^{-1} \text{ s}^{-1}$ at a density of $\rho = 2.0 \text{ m}^{-2}$.

4.2. Comparison of SSL and DML flow

In bidirectional pedestrian flow, especially for DML type, head-on conflicts and cross-directional conflicts occur. To investigate their influence on the flow we compare in figure 7 the fundamental diagram of SSL and DML flow for $b_{\text{cor}} = 3.6$ m. It can be seen that the fundamental diagrams of these two types of bidirectional flow are consistent at least for the density $\rho < 2.0 \text{ m}^{-2}$. The lower degree of ordering in dynamical multi-lanes (DML) has no effect on the fundamental diagram which agrees with the findings of Older [17]. This might be taken as an indication that head-on conflicts in multi-lanes have the same influence as the conflicts at the borders in stable separated lane flow on the fundamental diagram. On the other hand, the self-organized lanes increase the order and make pedestrian movement smoother. Whether the degree of ordering has an influence on the fundamental diagram at higher densities cannot be decided from our data. In

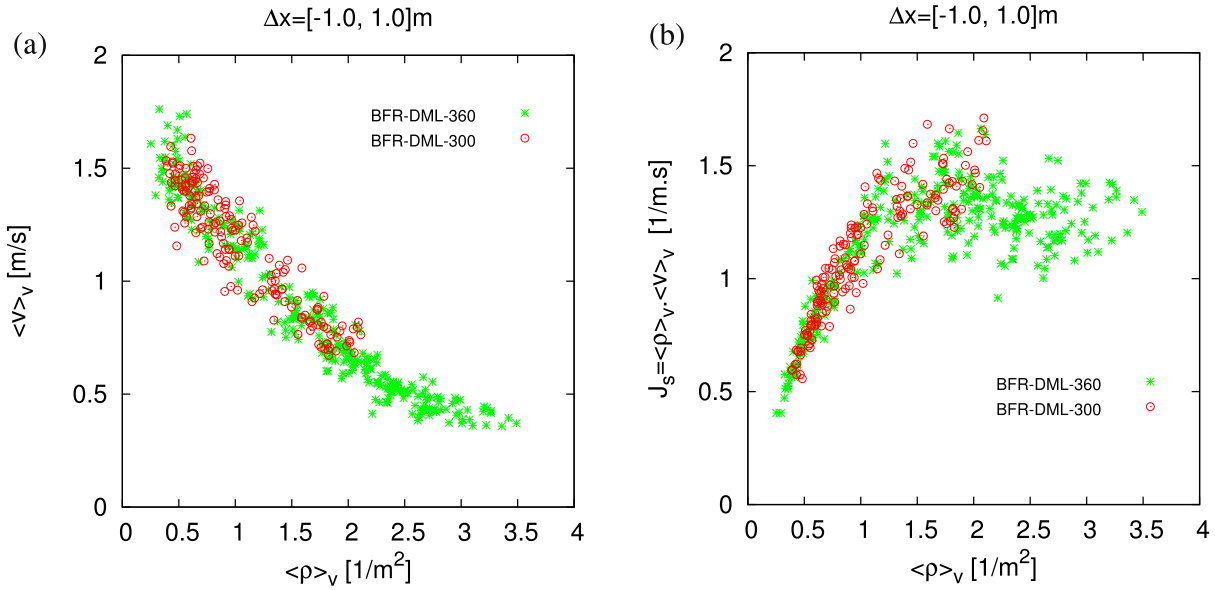


Figure 6. Comparison of fundamental diagrams of DML flow at different corridor widths. (a) Density-velocity and (b) density-specific flow.

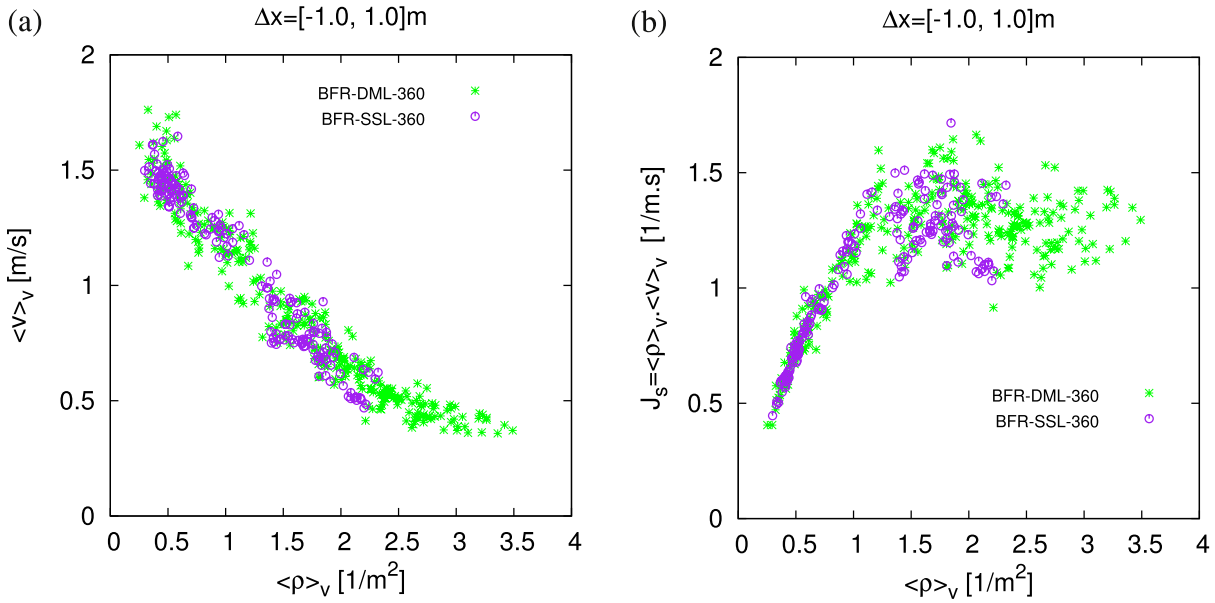


Figure 7. Comparison of the fundamental diagrams of SSL and DML flow. (a) Density-velocity and (b) density-specific flow.

particular, it would be interesting to find out whether the density where the velocity and specific flow becomes zero depends on the degree of order.

4.3. Comparison of BFR and UFR flow

The flow ratio of the opposing pedestrian streams is another important factor that is worth studying. Under unbalanced conditions, pedestrians from the direction with high

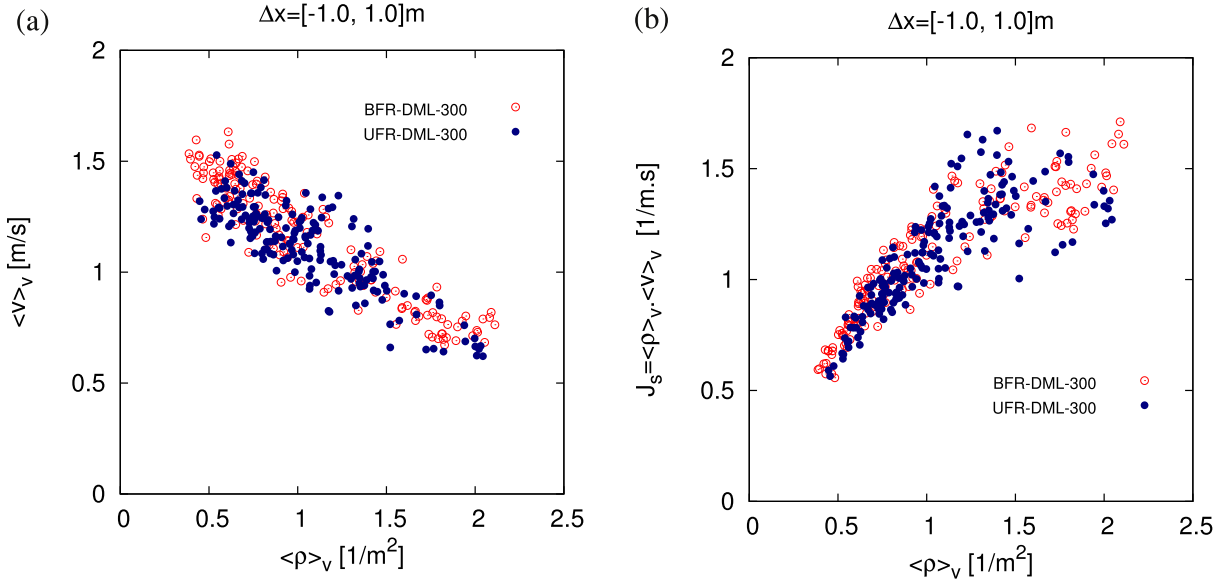


Figure 8. Comparison of the fundamental diagrams of BFR and UFR flow. (a) Density–velocity and (b) density–specific flow.

flow ratio may dominate and restrain the movement of pedestrians from the opposing direction. We compare the fundamental diagrams of BFR and UFR flow to study the influence of the ratio of opposing flows, as shown in figure 8. This comparison is performed for $b_{\text{cor}} = 3.0$ m of DML flow. Due to the limitation of the number of runs, only data for $\rho < 2.0 \text{ m}^{-2}$ have been obtained. It can be seen that the asymmetry in the flows does not affect the fundamental diagrams, at least for DML flows and densities $\rho < 2.0 \text{ m}^{-2}$.

4.4. Comparison between uni- and bidirectional flows

In this section we compare the fundamental diagram of uni- and bidirectional flows, see figure 9. Since both the width of the corridor and the forms of bidirectional flow have little influence on the fundamental diagram, the data for unidirectional flow (U-300) in [31] at $b_{\text{cor}} = 3.0$ m are used to compare with the fundamental diagram of BFR-DML flow at $b_{\text{cor}} = 3.6$ m. These experiments were carried out at the same day with the same participants. It is worth noting that the data of the unidirectional flow for $\rho > 2.0 \text{ m}^{-2}$ are obtained by slide change of the experiment set-up. To reach densities $\rho > 2.0 \text{ m}^{-2}$ for the unidirectional experiment, a bottleneck at the end of the corridor is introduced. We discussed in [31] that the decrease of the flow is induced by changing the boundary conditions. This limits the comparability of fundamental diagrams for $\rho > 2.0 \text{ m}^{-2}$.

Figure 9(a) shows the relationship between density and velocity for these two kinds of flow. For the free flow state at densities $\rho < 1.0 \text{ m}^{-2}$ no significant difference exists. For $\rho > 1.0 \text{ m}^{-2}$, however, the velocities for unidirectional flow are larger than that of bidirectional streams. The difference between the two cases becomes more pronounced in the flow–density diagram where a qualitative difference can be observed. In the bidirectional case a plateau is formed starting at a density $\rho \approx 1.0 \text{ m}^{-2}$ where the flow becomes almost independent of the density. Such plateaus are typical for systems

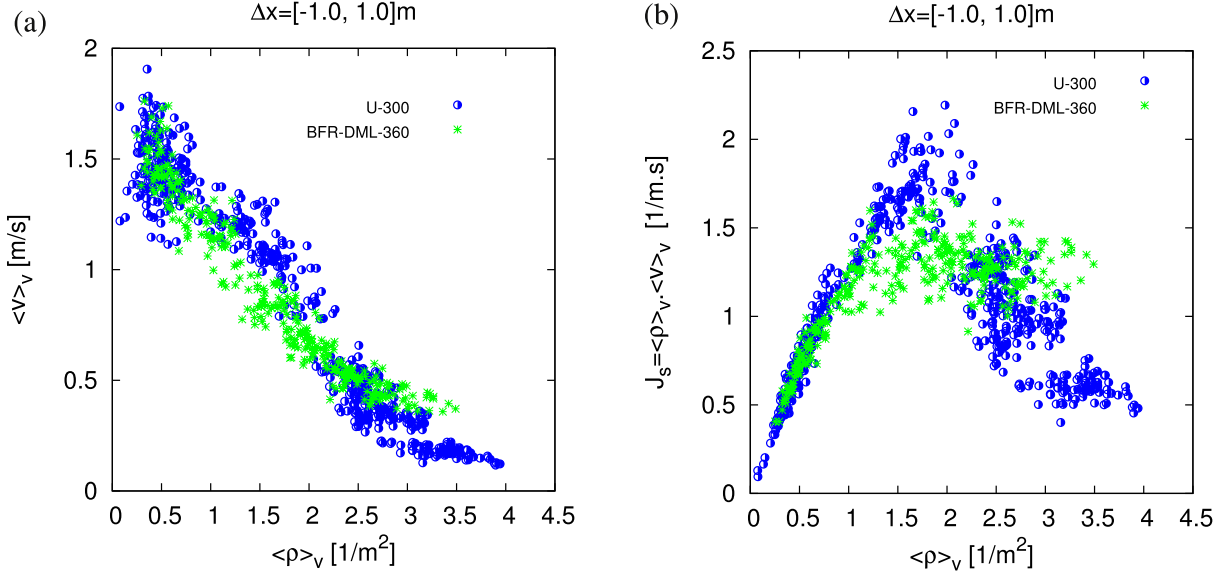


Figure 9. Comparison of the fundamental diagrams of unidirectional flow and bidirectional flow. (a) Density–velocity and (b) density–specific flow.

which contain ‘defects’ which limit the flow [33] and have been observed, for example, on bidirectional ant trails [34] where they are a consequence of the interaction of the ants. In our experiments the defects are persons moving in the opposite direction which leads to conflicts and a reduction of the velocity.

The observed difference in the fundamental diagrams implies that SSL flow should not be interpreted as two unidirectional flows. Although the self-organized lanes can decrease the head-on conflicts, interactions between the opposing streams are still relevant.

5. Conclusion

A series of well-controlled laboratory pedestrian experiments of bidirectional flow were performed in straight corridors. Up to 350 persons participated and the whole processes of the experiment were recorded using two video cameras. The trajectories of each pedestrian are extracted with high accuracy from the video recordings automatically using PeTrack. After comparing the fundamental diagrams from the four measurement methods introduced in [31], we do not find large differences among these results and adopt the Voronoi method in this study for its small fluctuation and high resolution in time and space. For different degrees of ordering in bidirectional pedestrian streams (DML, SSL, BFR and UFR), no significant differences are found in the fundamental diagrams for densities below 2.0 m^{-2} . Due to the limitation of the number of runs, the fundamental diagrams for different types of bidirectional flow are mainly compared for densities $\rho < 2.0 \text{ m}^{-2}$. Whether a jamming transition, which is due to overcrowding and lead to a total breakdown of flow, occurs in case the degree of ordering is lower. This needs to be studied by further experiments. The fundamental diagrams of bidirectional flow and unidirectional flow shows clear differences. The maximum flow value is about $2.0 \text{ m}^{-1} \text{ s}^{-1}$ for unidirectional flow while $1.5 \text{ m}^{-1} \text{ s}^{-1}$ for bidirectional flow. The self-organized lanes

can help to relief the head-on conflicts effectively and increase the ordering of the stream. However, these conflicts do have influence on the fundamental diagram of bidirectional flow. It is also demonstrated that the lanes could be determined easily by measuring the velocity profile of bidirectional streams using the Voronoi method.

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