$$\int x(x+1)(x-2)dx = \int x(x^2-x-2)dx = \int (x^3-x^2-2x)dx = \frac{x^4}{4} - \frac{x^3}{3} - x^2 + C$$

$$\int \frac{x^2 - x + 1}{\sqrt{x}} dx = \int \frac{x^2}{\sqrt{x}} dx - \int \frac{x}{\sqrt{x}} dx + \int \frac{dx}{\sqrt{x}} = \int x^{\frac{3}{2}} dx - \int x^{\frac{1}{2}} dx + \int x^{-\frac{1}{2}} dx =$$

$$= \frac{2x^2 \sqrt{x}}{5} - \frac{2x \sqrt{x}}{3} + 2\sqrt{x} + C$$

$$\int \sqrt{x\sqrt{x\sqrt{x}}} dx = \int x^{\frac{7}{8}} dx = \frac{8}{15} x^{\frac{15}{8}} + C$$

$$\int \frac{dx}{7+x^2} = \frac{1}{\sqrt{7}} \arctan \frac{x}{\sqrt{7}} + C$$

$$\int \frac{dx}{2x^2 + 3} = \frac{1}{2} \int \frac{dx}{x^2 + \frac{3}{2}} = \frac{1}{2} \sqrt{\frac{2}{3}} \arctan\left(\sqrt{\frac{2}{3}}x\right) + C$$

$$\int \frac{dx}{3x^2 - 7} = -\frac{1}{3} \int \frac{dx}{\frac{7}{3} - x^2} = -\frac{1}{3} \frac{1}{2\sqrt{\frac{7}{3}}} \ln \left| \frac{\sqrt{\frac{7}{3}} + x}{\sqrt{\frac{7}{3}} - x} \right| + C$$

$$\int \frac{x^2}{1 - x^2} dx = \int \left(\frac{1}{1 - x^2} - 1\right) dx = \int \frac{dx}{1 - x^2} - \int dx = \frac{1}{2} \ln \left| \frac{1 + x}{1 - x} \right| - x + C$$

$$\int \frac{dx}{x^4 - 1} = \int \left(\frac{1}{2x^2 - 2} - \frac{1}{2x^2 + 2}\right) dx = -\frac{1}{2} \int \frac{dx}{1 - x^2} - \frac{1}{2} \int \frac{dx}{x^2 + 1} =$$

$$= -\frac{1}{4} \ln \left|\frac{1 + x}{1 - x}\right| - \frac{1}{2} \arctan x + C$$

$$\begin{split} &\int \frac{(1+x)^2}{x(1+x^2)} dx = \int \frac{x^2+2x+1}{x(1+x^2)} dx = \int \frac{x}{1+x^2} dx + 2 \int \frac{dx}{1+x^2} + \int \frac{dx}{x(1+x^2)} = \\ &= \left| \frac{1}{x(1+x^2)} = \frac{1}{x} - \frac{x}{1+x^2} \right| = \int \frac{x}{1+x^2} dx + 2 \int \frac{dx}{1+x^2} + \int \frac{dx}{x} - \int \frac{x}{1+x^2} dx = \\ &= \frac{1}{2} \ln|1+x^2| + 2 \arctan x + \ln|x| - \frac{1}{2} \ln|1+x^2| + C = 2 \arctan x + \ln|x| + C \end{split}$$

$$\int \frac{dx}{\sqrt{2-x^2}} = \arcsin\frac{x}{\sqrt{2}} + C$$

#### 

$$\int (5^x - 2^x)^2 dx = \int (5^{2x} - 2 * 10^x + 4^x) dx = \int 25^x dx - 2 \int 10^x dx + \int 4^x dx =$$

$$= \frac{25^x}{\ln 25} - \frac{2 * 10^x}{\ln 10} + \frac{4^x}{\ln 4} + C$$

## 

$$\int \frac{2^x 3^{2x} 4^{3x}}{5^x 6^{2x}} dx = \int \left(\frac{32}{5}\right)^x dx = \left(\frac{32}{5}\right)^x \frac{1}{\ln\left(\frac{32}{5}\right)} + C$$

$$\int \frac{e^{3x} - 1}{e^x - 1} dx = \int \frac{(e^x - 1)(e^{2x} + e^x + 1)}{e^x - 1} dx = \int e^{2x} dx + \int e^x dx + \int dx = \frac{1}{2}e^{2x} + e^x + x + C$$

$$\int \left(\sin\frac{x}{2}\right)^2 dx = \int \frac{1 - \cos x}{2} dx = \frac{1}{2} \int dx - \frac{1}{2} \int \cos x dx = \frac{x - \sin x}{2} + C$$

$$\int \left(\cos\frac{x}{2}\right)^2 dx = \int \frac{1 + \cos x}{2} dx = \frac{1}{2} \int dx + \frac{1}{2} \int \cos x dx = \frac{x}{2} + \frac{\sin x}{2} + C$$

# 

$$\int \frac{dx}{(\sin x)^2 (\cos x)^2} = 4 \int \frac{dx}{(\sin 2x)^2} = |t - 2xdt - 2dx| = 2 \int \frac{dt}{(\sin t)^2} = -2 \operatorname{ctg} t + C = -2 \operatorname{ctg} 2x + C$$

#### 

$$\int (\operatorname{tg} x)^2 dx = \left| (\operatorname{tg} x)^2 = \frac{(\sin x)^2}{(\cos x)^2} = \frac{1 - (\cos x)^2}{(\cos x)^2} = \frac{1}{(\cos x)^2} - 1 \right| =$$

$$= \int \frac{dx}{(\cos x)^2} - \int dx = \operatorname{tg} x - x + C$$

#### 

$$\int (\operatorname{ctg} x)^2 dx = \left| (\operatorname{ctg} x)^2 = \frac{(\cos x)^2}{(\sin x)^2} = \frac{1 - (\sin x)^2}{(\sin x)^2} = \frac{1}{(\sin x)^2} - 1 \right| =$$

$$= \int \frac{dx}{(\sin x)^2} - \int dx = -\operatorname{ctg} x - x + C$$

$$\int \frac{dx}{2x+3} = |2x+3=t, \quad dt = 2dx| = \frac{1}{2} \int \frac{dt}{t} = \frac{1}{2} \ln|t| + C = \frac{1}{2} \ln|2x+3| + C$$

$$\int \frac{x+3}{(x+2)(x-1)} dx = |t = x - 1, \quad dt = dx| = \int \frac{t+4}{t(t+3)} dt = dt$$

$$= \int \frac{dt}{t+3} + 4 \int \frac{dt}{t(t+3)} = \int \frac{dt}{t+3} + \frac{4}{3} \left( \int \frac{dt}{t} - \int \frac{dt}{t+3} \right) = dt$$

$$= |t+3 = q, \quad dq = dt| = \int \frac{dq}{q} + \frac{4}{3} \int \frac{dt}{t} - \frac{4}{3} \int \frac{dq}{q} = dt$$

$$= -\frac{1}{3} \ln|q| + \frac{4}{3} \ln|t| + C = -\frac{1}{3} \ln|x+2| + \frac{4}{3} \ln|x-1| + C$$

$$\int \frac{2+x}{1+x} dx = \int (\frac{1}{1+x} + 1) dx = \int \frac{dx}{1+x} + \int dx = |1+x=t|, \quad dt = dx| =$$

$$= \int \frac{dt}{t} + \int dx = \ln|t| + x + C = \ln|1+x| + x + C$$

#### 

$$\int (2x+5)^{15} dx = |t = 2x+5, \quad dt = 2dx| = \frac{1}{2} \int t^{15} dt = \frac{t^{16}}{32} + C =$$
$$= \frac{(2x+5)^{16}}{32} + C$$

#### 

$$\int x(x-2)^5 dx = |t = x - 2, \quad x = t + 2, \quad dt = dx| = \int (t+2)t^5 dt = \int (t^6 + 2t^5) dt =$$

$$= \int t^6 dt + 2 \int t^5 dt = \frac{t^7}{7} + \frac{t^6}{3} + C = \frac{(x-2)^7}{7} + \frac{(x-2)^6}{3} + C$$

$$\int (x+2)\sqrt{x-2}dx \, |t=x-2, \quad x+2=t+4, \quad dt=dx | = \int (t+4)\sqrt{t}dt =$$

$$= \int t^{\frac{3}{2}}dt + 4 \int t^{\frac{1}{2}}dt = \frac{2}{5}t^{\frac{5}{2}} + \frac{8}{3}t^{\frac{3}{2}} + C = \frac{2(x-2)^{\frac{5}{2}}}{5} + \frac{8(x-2)^{\frac{3}{2}}}{2} + C$$

$$\int \frac{2x-7}{\sqrt{1+3x}} dx = \left| t = 1+3x, \quad dt = 3dx, \quad 2x-7 = \frac{2t-23}{3}, \quad x = \frac{t-1}{3} \right| =$$

$$= \frac{1}{9} \int \frac{2t-23}{\sqrt{t}} dt = \frac{2}{9} \int t^{\frac{1}{2}} dt - \frac{23}{9} \int t^{-\frac{1}{2}} dt = \frac{4}{27} (1+3x)^{\frac{3}{2}} - \frac{46}{9} \sqrt{1+3x} + C$$

$$\int \frac{x^2 + 1}{2x - 1} dx = \left| t = 2x - 1, \quad dt = 2dx, \quad x = \frac{t + 1}{2} \right| = \frac{1}{4} \left( \int t dt + 2 \int dt + 5 \int dt \right) = \frac{1}{4} \left( \frac{t^2}{2} + 2t + 5t \right) + C = \frac{t^2}{8} + \frac{t}{2} + \frac{5t}{4} + C = \frac{(2x - 1)^2}{8} + \frac{2x - 1}{2} + \frac{2(2x - 1)}{4} + C$$

## 

$$\int (2x+3)^2 (1-x)^8 dx = |t = 1 - x, \quad dt = -dx, \quad x = 1 - t, \quad 2x + 3 = -2t + 5| = -\int (-2t+5)^2 t^8 dt = -\int (4t^2 - 20t + 25) t^8 dt = -4 \int t^{10} dt + 20 \int t^9 dt - 25 \int t^8 dt = -\frac{4t^{11}}{11} + 2t^{10} - \frac{25t^9}{9} + C = -\frac{4(1-x)^{11}}{11} + 2(1-x)^{10} - \frac{25(1-x)^9}{9} + C$$

$$\int \frac{x-4}{\sqrt{x^2-2}} dx = \int \frac{x}{\sqrt{x^2-2}} dx - 4 \int \frac{dx}{\sqrt{x^2-2}} =$$

$$= |t = x^2 - 2, \quad dt = 2x dx| = \frac{1}{2} \int \frac{dt}{\sqrt{t}} - 4 \int \frac{dx}{\sqrt{x^2-2}} = \sqrt{t} - 4 \ln|x + \sqrt{x^2-2}| + C =$$

$$= \sqrt{x^2-2} - 4 \ln|x + \sqrt{x^2-2}| + C$$