



Aprendizado por Reforço

Programação dinâmica (Experimento 2 – iteração de política)

Implementação



Algoritmo de iteração de política

Policy Iteration (using iterative policy evaluation) for estimating $\pi \approx \pi_*$

1. Initialization

$$V(s) \in \mathbb{R}$$
 and $\pi(s) \in \mathcal{A}(s)$ arbitrarily for all $s \in S$

2. Policy Evaluation

Loop:

$$\Delta \leftarrow 0$$

Loop for each $s \in S$:

$$v \leftarrow V(s)$$

$$V(s) \leftarrow \sum_{s',r} p(s',r|s,\pi(s)) [r + \gamma V(s')]$$

$$\Delta \leftarrow \max(\Delta, |v - V(s)|)$$

until $\Delta < \theta$ (a small positive number determining the accuracy of estimation)

3. Policy Improvement

$$policy$$
-stable $\leftarrow true$

For each $s \in S$:

$$old\text{-}action \leftarrow \pi(s)$$

$$\pi(s) \leftarrow \operatorname{arg\,max}_a \sum_{s',r} p(s',r|s,a) [r + \gamma V(s')]$$

If $old\text{-}action \neq \pi(s)$, then $policy\text{-}stable \leftarrow false$

If policy-stable, then stop and return $V \approx v_*$ and $\pi \approx \pi_*$; else go to 2

Implementação



Algoritmo de iteração de política

Algorithm 4.2: Policy iteration algorithm

Initialization: The system model, p(r|s,a) and p(s'|s,a) for all (s,a), is known. Initial guess π_0 .

Goal: Search for the optimal state value and an optimal policy.

While v_{π_k} has not converged, for the kth iteration, do

Policy evaluation:

Initialization: an arbitrary initial guess $v_{\pi_k}^{(0)}$

While $v_{\pi_k}^{(j)}$ has not converged, for the jth iteration, do

For every state $s \in \mathcal{S}$, do

$$v_{\pi_k}^{(j+1)}(s) = \sum_a \pi_k(a|s) \left[\sum_r p(r|s,a)r + \gamma \sum_{s'} p(s'|s,a)v_{\pi_k}^{(j)}(s') \right]$$

Policy improvement:

For every state $s \in \mathcal{S}$, do

For every action $a \in \mathcal{A}$, do

$$q_{\pi_k}(s, a) = \sum_r p(r|s, a)r + \gamma \sum_{s'} p(s'|s, a)v_{\pi_k}(s')$$

$$a_k^*(s) = \arg\max_a q_{\pi_k}(s, a)$$

$$\pi_{k+1}(a|s) = 1 \text{ if } a = a_k^*, \text{ and } \pi_{k+1}(a|s) = 0 \text{ otherwise}$$