

Consumption Tax in HANK

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May 6, 2022

1 One-Asset HANK as in Auclert et al. (2021)

In this model, τ_t is a *tax*, proportional to households' labor productivity e_{it} : $\tau_t \bar{\tau}(e_{it})$.

Households Continuum of households i . Utility function

$$E_0 \sum_{t=0}^{\infty} \beta^t \left\{ \frac{c_{it}^{1-\sigma}}{1-\sigma} - \varphi \frac{n_{it}^{1+\nu}}{1+\nu} \right\}.$$

Budget constraint and borrowing constraint

$$c_{it} + b_{it} = w_t e_{it} n_{it} + (1 + r_t) b_{it-1} - \tau_t \bar{\tau}(e_{it}) + d_t \bar{d}(e_{it}),$$
$$b_{it} \geq \underline{b}.$$

Optimal labor supply and consumption-saving decisions for unconstrained households

$$n_{it} = \left(\frac{w_t e_{it}}{\varphi c_{it}^\sigma} \right)^{\frac{1}{\nu}}.$$
$$c_{it}^{-\sigma} = \beta E_t (1 + r_{t+1}) c_{it+1}^{-\sigma}.$$

When the borrowing constraint binds, $b_{it} = \underline{b}$, the budget constraint rewrites as

$$c_{it} + \underline{b} = w_t e_{it} n_{it} + (1 + r_t) b_{it-1} - \tau_t \bar{\tau}(e_{it}) + d_t \bar{d}(e_{it}).$$

Plug in the labor supply condition

$$c_{it} + \underline{b} = w_t e_{it} \left(\frac{w_t e_{it}}{\varphi c_{it}^\sigma} \right)^{\frac{1}{\nu}} + (1 + r_t) b_{it-1} - \tau_t \bar{\tau}(e_{it}) + d_t \bar{d}(e_{it}).$$

Firms Continuum of intermediate firms j . Production function

$$y_{jt} = Z_t n_{jt}.$$

Cost minimization $-w_t n_{jt} + m c_{jt} [Z_t n_{jt} - y_{jt}]$ yields labor demand

$$m c_{jt} = m c_t = \frac{w_t}{Z_t}.$$

Quadratic adjustment cost

$$\psi(p_{jt}, p_{jt-1}) = \frac{\mu}{\mu - 1} \frac{1}{2\kappa} \left[\log \left(\frac{p_{jt}}{p_{jt-1}} \right) \right]^2 Y_t.$$

Phillips curve

$$\log(1 + \pi_t) = \kappa \left(\frac{w_t}{Z_t} - \frac{1}{\mu} \right) + \frac{1}{1 + r_{t+1}} \frac{Y_{t+1}}{Y_t} \log(1 + \pi_{t+1}).$$

Aggregate dividends

$$d_t = Y_t - w_t N_t - \psi_t.$$

Government Government budget constraint: the tax finances interest payment on bonds

$$\tau_t = r_t B.$$

Monetary policy

$$i_t = r_t^* + \phi \pi_t.$$

Fisher equation

$$1 + r_t = \frac{1 + i_{t-1}}{1 + \pi_t}.$$

Market clearing Aggregate production function and resource constraint

$$Y_t = Z_t N_t; \quad Y_t = C_t + \psi_t \quad \text{where } C_t = \int_i c_{it} di.$$

Clearing in the bond and labor markets

$$B_t = \int_i b_{it} di; \quad N_t = \int_i e_{it} n_{it} di.$$

2 One-Asset HANK with Exogenous Uniform Cash Transfers

Same model as in Section 1, except that τ_t is no longer a proportional *tax* but instead becomes an exogenous, lump-sum *transfer*. Government debt B becomes a time-varying endogenous variable B_t .

Households Continuum of households i . Utility function

$$E_0 \sum_{t=0}^{\infty} \beta^t \left\{ \frac{c_{it}^{1-\sigma}}{1-\sigma} - \varphi \frac{n_{it}^{1+\nu}}{1+\nu} \right\}.$$

Budget constraint and borrowing constraint

$$c_{it} + b_{it} = w_t e_{it} n_{it} + (1 + r_t) b_{it-1} + \tau_t + d_t \bar{d}(e_{it}),$$

$$b_{it} \geq \underline{b}.$$

Same FOCs as before

$$n_{it} = \left(\frac{w_t e_{it}}{\varphi c_{it}^{\sigma}} \right)^{\frac{1}{\nu}}.$$

$$c_{it}^{-\sigma} = \beta E_t (1 + r_{t+1}) c_{it+1}^{-\sigma}.$$

Firms Same as before

Government Government budget constraint: τ_t is now a transfer

$$\tau_t + (1 + r_t) B_{t-1} = B_t.$$

In steady state, this implies $\tau = -rB$.

Market clearing Same as before

3 One-Asset HANK with Transfers and Taxes

Same model as in Section 2, but now we add exogenous consumption and labor taxes.

Households Continuum of households i . Utility function

$$E_0 \sum_{t=0}^{\infty} \beta^t \left\{ \frac{c_{it}^{1-\sigma}}{1-\sigma} - \varphi \frac{n_{it}^{1+\nu}}{1+\nu} \right\}.$$

Budget constraint and borrowing constraint

$$(1 + \tau_{ct})c_{it} + b_{it} = (1 - \tau_n)w_t e_{it} n_{it} + (1 + r_t)b_{it-1} + \tau_t + d_t \bar{d}(e_{it}),$$

$$b_{it} \geq \underline{b}.$$

Optimal labor supply and consumption-saving decisions

$$n_{it} = \left[\frac{(1 - \tau_n)w_t e_{it}}{(1 + \tau_{ct})\varphi c_{it}^\sigma} \right]^{\frac{1}{\nu}}.$$

$$c_{it}^{-\sigma} = \beta E_t \frac{1 + \tau_{ct}}{1 + \tau_{ct+1}} (1 + r_{t+1}) c_{it+1}^{-\sigma}.$$

Firms Same as before

Government Government budget constraint

$$\tau_t + (1 + r_t)B_{t-1} = \tau_{ct}C_t + \tau_n W_t N_t + B_t.$$

Same monetary policy and Fisher equation

$$i_t = r_t^* + \phi \pi_t; \quad 1 + r_t = \frac{1 + i_{t-1}}{1 + \pi_t}.$$

Market clearing Same as before