

# 1 Function Design

## `resizeTasks`

params - `int newCapacity`

returns - `void`

Resizes the `tasks` array by `newCapacity` while preserving the elements. Assigns the value of `newCapacity` to `capacity`.

## `pushFront, pushBack`

params - `int taskId`

returns - `void`

Pushes a new `taskId` the front/back of the deque. If the deque is full after pushing, resize by `capacity * 2`.

## `popFront, popBack`

returns - `void`

Pops an existing `taskId` from the front/back of the deque. If `currSize` reaches  $\frac{1}{4}$  of `capacity` after popping, resize by `capacity / 2`.

## `findCoreIdWithLeastTasks, findCoreIdWithMostTasks`

returns - `int`

Returns the core id with the least/most amount of assigned tasks from the array of cores.

## `findCoreIdWithLeastTasksExcluding`

params - `int C_ID`

returns - `int`

Returns the core id with the least amount of assigned tasks from the array of cores, excluding the specified `C_ID`.

# 2 Runtime

The

`findCoreIdWithLeastTasks, findCoreIdWithLeastTasksExcluding, findCoreIdWithMostTasks`

methods each have a runtime of  $O(\text{numCores})$ , where `numCores` is the number of cores in the current CPU instance.

Each method has a loop that runs `numCores` times to do element comparison and return value update. The computation per iteration is done in  $O(1)$ . Thus, the total loop is done in  $O(\text{numCores})$ .

The `resizeTasks` method has a runtime of  $O(C)$  when the deque is full, where `C` is the capacity of the core's deque.

A `newTasks` array with `newCapacity` set to twice the original capacity is created (done in  $O(1)$  time).

Then it copies each element from the current `tasks` to `newTasks`, which executes a loop that runs `C` times to access each `tasks` element (done in  $O(C)$  time).

Then, it assigns the value of `newTasks` to `tasks`, and the value of `newCapacity` to `capacity` (done in  $O(1)$  time).

The dominant time complexity for this method is  $O(C)$ .

The `RUN` command has a runtime of  $O(1)$ , presuming no resizing occurs. The associated method is `runTask`.

**Out of range:** early return. Done in  $O(1)$  time.

**Core is empty:** find core id with most tasks (done in  $O(\text{numcores})$  time). Steal work from that core if it is not empty (done in  $O(1)$  time). Early return.

**Run next task:** get the front task id from the deque, and pop the task. Done in  $O(1)$  time.

**Core is empty after running task:** find core id with most tasks (done in  $O(\text{numcores})$  time). Steal work from that core if it is not empty (done in  $O(1)$  time).

**Runtime:**  $O(\text{numCores})$  is the dominant time complexity. By asymptotic analysis, this is considered  $O(1)$ , since `numCores` is a constant value after CPU initialization.

The `SPAWN` command has a worst-case runtime of  $O(C)$ , where `C` is the capacity of the core's deque. The associated method is `spawnTask`.

**Worst-case: find core id with least tasks, push to the back of the deque with resizing:**

Finding the core id with the least amount of tasks is done in  $O(\text{numCores})$  time.

Resizing the deque when full is done in  $O(C)$ .

$O(C)$  dominates  $O(\text{numCores})$  in asymptotic analysis, since  $O(\text{numCores})$  is considered  $O(1)$  here.