Regression Models Project 1

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Executive Summary

There is a common believe that cars with a manual transmission are more fuel-efficient than automatics. Using 1974 data from *Motor Trends* we can analyze this claim using regression analysis. Based on the analysis presented below, although manual transmission cars get on average 7.24 more miles per gallon than automatic cars, we can confidently say that this is because automatic transmission vehicles weigh more, and therefore have lower gas mileage. We do not believe that manual transmission vehicles have a better gas mileage, once you account for the weight of the vehicle.

Research Question

We start our analysis by examining the claim that manual transmission cars have better gas mileage than automatic cars. We can load the data and do some basic analysis in R on this dataset.

```
data(mtcars)
str(mtcars)
```

```
'data.frame':
                    32 obs. of 11 variables:
                 21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
##
    $ mpg : num
                 6 6 4 6 8 6 8 4 4 6 ...
    $ disp: num
                 160 160 108 258 360 ...
##
            num
                 110 110 93 110 175 105 245 62 95 123 ...
##
                 3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
    $ drat: num
##
         : num
                 2.62 2.88 2.32 3.21 3.44 ...
##
    $ qsec: num
                 16.5 17 18.6 19.4 17 ...
##
    $ vs
         : num
                 0 0 1 1 0 1 0 1 1 1 ...
##
                 1 1 1 0 0 0 0 0 0 0 ...
    $ am
         : num
    $ gear: num
                 4 4 4 3 3 3 3 4 4 4 ...
    $ carb: num
                 4 4 1 1 2 1 4 2 2 4 ...
```

summary(mtcars)

```
##
                           cyl
                                            disp
                                                               hp
         mpg
##
           :10.40
                     Min.
                             :4.000
                                              : 71.1
                                                        Min.
                                                               : 52.0
                     1st Qu.:4.000
                                       1st Qu.:120.8
##
    1st Qu.:15.43
                                                        1st Qu.: 96.5
##
    Median :19.20
                     Median :6.000
                                       Median :196.3
                                                        Median :123.0
            :20.09
                                              :230.7
##
    Mean
                     Mean
                             :6.188
                                       Mean
                                                        Mean
                                                                :146.7
##
    3rd Qu.:22.80
                     3rd Qu.:8.000
                                       3rd Qu.:326.0
                                                        3rd Qu.:180.0
            :33.90
##
                             :8.000
                                              :472.0
                                                                :335.0
    Max.
                     Max.
                                       Max.
                                                        Max.
##
         drat
                            wt
                                            qsec
                                                               vs
                             :1.513
##
    Min.
            :2.760
                     Min.
                                      Min.
                                              :14.50
                                                        Min.
                                                                :0.0000
    1st Qu.:3.080
                     1st Qu.:2.581
                                       1st Qu.:16.89
                                                        1st Qu.:0.0000
##
##
    Median :3.695
                     Median :3.325
                                      Median :17.71
                                                        Median :0.0000
    Mean
           :3.597
                     Mean
                            :3.217
                                      Mean
                                              :17.85
                                                        Mean
                                                               :0.4375
    3rd Qu.:3.920
                     3rd Qu.:3.610
                                       3rd Qu.:18.90
                                                        3rd Qu.:1.0000
```

```
:4.930
                                                                 :1.0000
##
    Max.
                      Max.
                             :5.424
                                       Max.
                                               :22.90
                                                         Max.
##
                            gear
                                              carb
           am
            :0.0000
                               :3.000
##
    Min.
                      Min.
                                        Min.
                                                :1.000
    1st Qu.:0.0000
                       1st Qu.:3.000
                                        1st Qu.:2.000
##
##
    Median :0.0000
                       Median :4.000
                                        Median :2.000
            :0.4062
                               :3.688
                                                :2.812
##
    Mean
                       Mean
                                        Mean
##
    3rd Qu.:1.0000
                       3rd Qu.:4.000
                                        3rd Qu.:4.000
##
    Max.
            :1.0000
                       Max.
                               :5.000
                                        Max.
                                                :8.000
```

Specifically, our variables of interest are mpg and am, which is coded to 0 for automatic transmissions, and 1 for manual transmission. We can regress

```
Y_i = \beta_0 + \beta_1 X_i + \epsilon_i
```

where X_i is the as variable in the mtcars dataset. Simple Least Squares regression will give the average mpg for automatics (X = 0) and $beta_1$ will give the added average miles per gallon of a manual transmission. Looking at just the transmission, we can see that automatic transmission vehicles have an average of 17.15 miles per gallon, and manuals get an additional 7.24 miles per gallon on average (24.39 total).

```
model=lm(mpg ~ am, data=mtcars)
summary(model)$coef
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 17.147368 1.124603 15.247492 1.133983e-15
## am 7.244939 1.764422 4.106127 2.850207e-04
```

Correction for Car Weight

Before jumping to the conclusion that manual transmissions are more fuel efficient, we should try to control for other variables in the dataset. Specifically, let's look at the number of cylinders, horsepower, and vehicle weight.

```
Y_i = \beta_0 + \beta_1 X_i + \sum \beta_i X_i j + \epsilon_i
```

where β_1 is the coefficient for the dummy variable as and the sum of β_j and X_j includes the cyl, hp, and wt variables from the data frame.

```
model=lm(mpg ~ am + cyl + hp + wt, data=mtcars)
summary(model)$coef
```

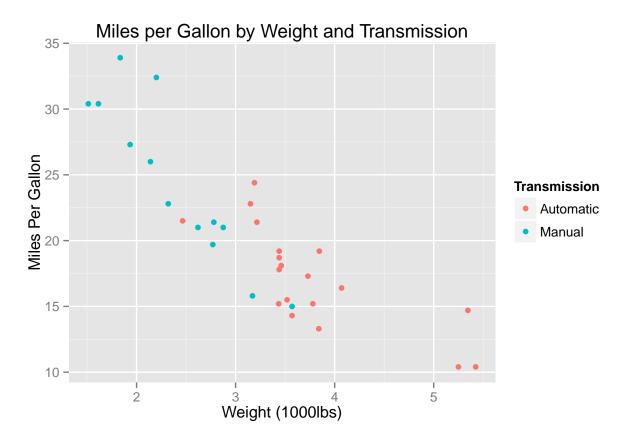
```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 36.14653575 3.10478079 11.642218 4.944804e-12
## am 1.47804771 1.44114927 1.025603 3.141799e-01
## cyl -0.74515702 0.58278741 -1.278609 2.119166e-01
## hp -0.02495106 0.01364614 -1.828433 7.855337e-02
## wt -2.60648071 0.91983749 -2.833632 8.603218e-03
```

Controlling for weight, manual vs. automatic ceases to be a statistically significant predictor of gas mileage

Conclusions

Despite the fact that manual transmission vehicles do, on average, have a better gas mileage, when controling for the number of cylinders, horsepower, and most importantly vehicle weight, this difference ceases to be substantive or significant. This spurious relationship between mpg, transmission, is very well illustrated by the following graph.

```
library(ggplot2)
q<-qplot(x=wt,y=mpg,data=mtcars,colour=as.factor(am))
q<-q + scale_color_discrete(name="Transmission",labels=c("Automatic","Manual"))
q<-q + ggtitle("Miles per Gallon by Weight and Transmission")
q<-q + xlab("Weight (1000lbs)") + ylab("Miles Per Gallon")
q</pre>
```



So we can see clearly that automatics tend to be both heavier and have a lower gas mileage, but comparibly weighted manual transmission vehicles tend to have comparible gas mileage.