CS145: INTRODUCTION TO DATA MINING

Set Data: Frequent Pattern Mining

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Methods to be Learnt

	Vector Data	Set Data	Sequence Data	Text Data
Classification	Logistic Regression; Decision Tree; KNN; SVM; NN			Naïve Bayes for Text
Clustering	K-means; hierarchical clustering; DBSCAN; Mixture Models			PLSA
Prediction	Linear Regression GLM*			
Frequent Pattern Mining		Apriori; FP growth	GSP; PrefixSpan	
Similarity Search			DTW	

Mining Frequent Patterns, Association and Correlations

Basic Concepts \longleftarrow



Frequent Itemset Mining Methods

Pattern Evaluation Methods

Summary

Set Data

- A data point corresponds to a set of items
 - Each data point is also called a transaction

Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

What Is Frequent Pattern Analysis?

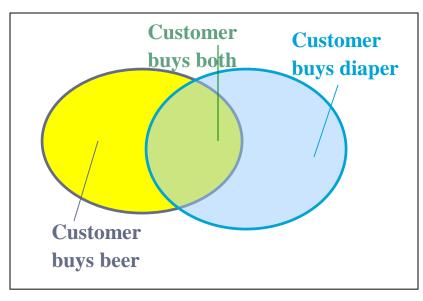
- Frequent pattern: a pattern (a set of items, subsequences, substructures, etc.) that occurs frequently in a data set
 - First proposed by Agrawal, Imielinski, and Swami [AIS93] in the context of frequent itemsets and association rule mining
- Motivation: Finding inherent regularities in data
 - What products were often purchased together?— Beer and diapers?!
 - What are the subsequent purchases after buying a PC?
 - What kinds of DNA are sensitive to this new drug?

Why Is Freq. Pattern Mining Important?

- Freq. pattern: An intrinsic and important property of datasets
- Foundation for many essential data mining tasks
 - Association, correlation, and causality analysis
 - Sequential, structural (e.g., sub-graph) patterns
 - Pattern analysis in spatiotemporal, multimedia, time-series, and stream data
 - Classification: discriminative, frequent pattern analysis
 - Cluster analysis: frequent pattern-based clustering
 - Broad applications

Basic Concepts: Frequent Patterns

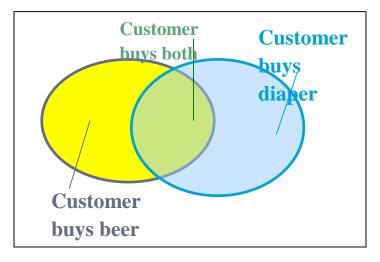
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50	Nuts, Coffee, Diaper, Eggs, Milk	



- itemset: A set of one or more items
- k-itemset X = {x₁, ..., x_k}: A set of kitems
- (absolute) support, or, support count of X: Frequency or occurrence of an itemset X
- (relative) support, s, is the fraction of transactions that contains X (i.e., the probability that a transaction contains X)
- An itemset X is *frequent* if X's support is no less than a *minsup* threshold

Basic Concepts: Association Rules

Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk



- Find all the rules X

 Y with minimum support and confidence
 - support, s, probability that a transaction contains $X \cup Y$
 - confidence, c, conditional probability that a transaction having X also contains Y

```
Let minsup = 50%, minconf = 50%

Freq. Pat.: {Beer}:3, {Nuts}:3, {Diaper}:4, {Eggs}:3, {Beer, Diaper}:3
```

- Strong Association rules
 - $\{Beer\} \rightarrow \{Diaper\} (60\%, 100\%)$
 - $\{Diaper\} \rightarrow \{Beer\} (60\%, 75\%)$

Closed Patterns and Max-Patterns

- A long pattern contains a combinatorial number of sub-patterns
 - e.g., $\{a_1, ..., a_{100}\}$ contains $2^{100} 1 = 1.27*10^{30}$ sub-patterns!
- •In general, {a₁, ..., a_n} contains 2ⁿ 1 subpatterns

$$\binom{n}{1} + \binom{n}{2} + \dots + \binom{n}{n} = 2^n - 1$$

Closed Patterns and Max-Patterns

- Solution: Mine closed patterns and max-patterns instead
- An itemset X is closed if X is frequent and there exists no superpattern Y > X, with the same support as X (proposed by Pasquier, et al. @ ICDT'99)
- An itemset X is a max-pattern if X is frequent and there exists no frequent super-pattern Y > X (proposed by Bayardo @ SIGMOD'98)
- Closed pattern is a lossless compression of freq. patterns
 - Reducing the # of patterns and rules

Closed Patterns and Max-Patterns

- Example. DB = $\{\{a_1, ..., a_{100}\}, \{a_1, ..., a_{50}\}\}$
 - Min_sup = 1.
- What is the set of closed pattern(s)?
 - {a₁, ..., a₁₀₀}: 1
 - {a₁, ..., a₅₀}: 2
 - Yes, it does have super-pattern, but not with the same support
- What is the set of max-pattern(s)?
 - {a₁, ..., a₁₀₀}: 1
- What is the set of all patterns?
 - !!

Computational Complexity of Frequent Itemset Mining

- How many itemsets are potentially to be generated in the worst case?
 - The number of frequent itemsets to be generated is sensitive to the minsup threshold
 - When minsup is low, there exist potentially an exponential number of frequent itemsets
 - The worst case: $\binom{M}{1} + \binom{M}{2} + \dots + \binom{M}{N}$
 - M: # distinct items, N: max length of transactions

•
$$\binom{M}{N} = M \times (M-1) \times \cdots \times (M-N+1)/N!$$

Mining Frequent Patterns, Association and Correlations

Basic Concepts

Frequent Itemset Mining Methods



Pattern Evaluation Methods

Summary

Scalable Frequent Itemset Mining Methods

Apriori: A Candidate Generation-and-Test Approach



- Improving the Efficiency of Apriori
- FPGrowth: A Frequent Pattern-Growth Approach
- *ECLAT: Frequent Pattern Mining with Vertical Data
 Format
- Generating Association Rules

The Apriori Property and Scalable Mining Methods

- The Apriori property of frequent patterns
 - Any nonempty subsets of a frequent itemset must be frequent
 - E.g., If {beer, diaper, nuts} is frequent, so is {beer, diaper}
 - i.e., every transaction having {beer, diaper, nuts} also contains {beer, diaper}
- Scalable mining methods: Three major approaches
 - Apriori (Agrawal & Srikant@VLDB'94)
 - Freq. pattern growth (FPgrowth—Han, Pei & Yin @SIGMOD'00)
 - *Vertical data format approach (Eclat)

Apriori: A Candidate Generation & Test Approach

- Apriori pruning principle: If there is any itemset which is infrequent, its superset should not be generated/tested! (Agrawal & Srikant @VLDB'94, Mannila, et al. @ KDD' 94)
- Method:
 - Initially, scan DB once to get frequent 1-itemset
 - Generate length k candidate itemsets from length k-1 frequent itemsets
 - Test the candidates against DB
 - Terminate when no frequent or candidate set can be generated

From Frequent k-1 Itemset To Frequent k-Itemset

 C_k : Candidate itemsets of size k

 L_k : frequent itemsets of size k

- From L_{k-1} to C_k (Candidates Generation)
 - The join step
 - The prune step
- From C_k to L_k
 - Test candidates by scanning database

Candidates Generation

Assume a pre-specified order for items, e.g., alphabetical order

- How to generate candidates C_k ?
 - Step 1: self-joining L_{k-1}
 - Two length k-1 itemsets l_1 and l_2 can join, only if the first k-2 items are the same, and for the last term, $l_1[k-1]$ $< l_2[k-1]$ (why?)
 - The joined length-k itemset is: $l_1 \cup l_2 = \{l_1[1], l_1[2], ..., l_1[k-1], l_2[k-1]\}$

- Step 2: pruning
 - Why we need pruning for candidates?
 - How?
 - Again, use Apriori property
 - A candidate itemset can be safely pruned, if it contains infrequent subset

Candidate-Generation Example

- Example of Candidate-generation from L_3 to C_4
 - L_3 ={abc, abd, acd, ace, bcd}
 - Self-joining: $L_3 * L_3$
 - abcd from abc and abd
 - acde from acd and ace
 - Pruning:
 - acde is removed because ade is not in L₃
 - $C_4 = \{abcd\}$

The Apriori Algorithm—Example



Tid	Items	
10	A, C, D	
20	B, C, E	
30	A, B, C, E	
40	B, E	

 $Sup_{min} = 2$

 C_1 1st scan

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

	Itemset	sup
L_{I}	{A}	2
	{B}	3
	{C}	3
	{E}	3

_			
L_2	Itemset	sup	
	{A, C}	2	
	{B, C}	2	•
	{B, E}	3	
	{C, E}	2	
ı			

2	Itemset	sup
	{A, B}	1
	{A, C}	2
	{A, E}	1
	{B, C}	2
	{B, E}	3
	{C, E}	2

 C_2 $2^{\text{nd}} \text{ scan}$

Itemset
{A, B}
{A, C}
{A, E}
{B, C}
{B, E}
{C, E}

C_3	Itemset	
3	{B, C, E}	

3 rd	scan	L_3

Itemset	sup
{B, C, E}	2

The Apriori Algorithm (Pseudo-Code)

```
C_k: Candidate itemsets of size k
L_k: frequent itemsets of size k
L_1 = \{ \text{frequent items} \};
for (k = 2; L_{k-1} != \varnothing; k++) do begin
  C_k = candidates generated from L_{k-1};
  for each transaction t in database do
     increment the count of all candidates in C_k that are
    contained in t
  L_k = candidates in C_k with min_support
end
return \bigcup_k L_k;
```

Questions

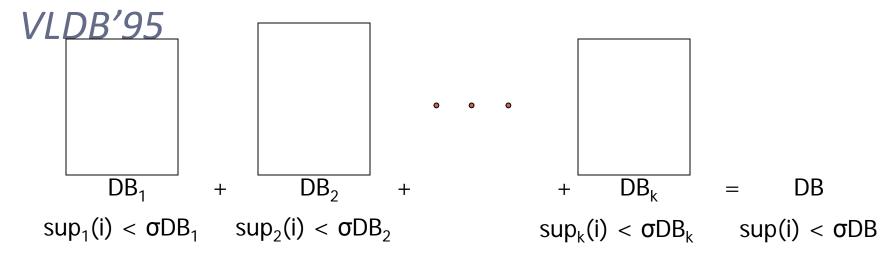
- How many scans on DB are needed for Apriori algorithm?
- When (k = ?) does Apriori algorithm generate the biggest number of candidate itemsets?
- Is support counting for candidates expensive?

Further Improvement of the Apriori Method

- Major computational challenges
 - Multiple scans of transaction database
 - Huge number of candidates
 - Tedious workload of support counting for candidates
- Improving Apriori: general ideas
 - Reduce passes of transaction database scans
 - Shrink number of candidates
 - Facilitate support counting of candidates

*Partition: Scan Database Only Twice

- Any itemset that is potentially frequent in DB must be frequent in at least one of the partitions of DB
 - Scan 1: partition database and find local frequent patterns
 - Scan 2: consolidate global frequent patterns
- A. Savasere, E. Omiecinski and S. Navathe,



*Hash-based Technique: Reduce the Number of Candidates

- A k-itemset whose corresponding hashing bucket count is below the threshold cannot be frequent
 - Candidates: a, b, c, d, e
 - Hash entries
 - {ab, ad, ae}
 - {bd, be, de}
 - ...
 - Frequent 1-itemset: a, b, d, e

count	itemsets
35	{ab, ad, ae}
88	{bd, be, de}
102	{yz, qs, wt}

Hash Table

- ab is not a candidate 2-itemset if the sum of count of {ab, ad, ae} is below support threshold
- J. Park, M. Chen, and P. Yu. An effective hash-based algorithm for mining association rules. SIGMOD'95

*Sampling for Frequent Patterns

- Select a sample of original database, mine frequent patterns within sample using Apriori
- Scan database once to verify frequent itemsets found in sample, only borders of closure of frequent patterns are checked
 - Example: check abcd instead of ab, ac, ..., etc.
- Scan database again to find missed frequent patterns
- H. Toivonen. Sampling large databases for association rules. In VLDB'96

Scalable Frequent Itemset Mining Methods

- Apriori: A Candidate Generation-and-Test Approach
 - Improving the Efficiency of Apriori
- FPGrowth: A Frequent Pattern-Growth Approach



- *ECLAT: Frequent Pattern Mining with Vertical Data
 Format
- Generating Association Rules

Pattern-Growth Approach: Mining Frequent Patterns Without Candidate Generation

- Bottlenecks of the Apriori approach
 - Breadth-first (i.e., level-wise) search
 - Scan DB multiple times
 - Candidate generation and test
 - Often generates a huge number of candidates
- The FPGrowth Approach (J. Han, J. Pei, and Y. Yin, SIGMOD' 00)
 - Depth-first search
 - Avoid explicit candidate generation

Major philosophy

- Grow long patterns from short ones using local frequent items only
 - "abc" is a frequent pattern
 - Get all transactions having "abc", i.e., project DB on abc: DB | abc
 - "d" is a local frequent item in DB | abc → abcd is a frequent pattern

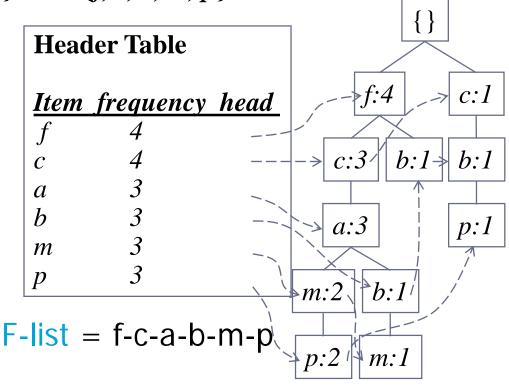
FP-Growth Algorithm Sketch

- Construct FP-tree (frequent pattern-tree)
 - Compress the DB into a tree
- Recursively mine FP-tree by FP-Growth
 - Construct conditional pattern base from FPtree
 - Construct conditional FP-tree from conditional pattern base
 - Until the tree has a single path or empty

Construct FP-tree from a Transaction Database

<u>TID</u>	Items bought	(ordered) frequent items	
100	$\{f, a, c, d, g, i, m, p\}$	$\{f, c, a, m, p\}$	
200	$\{a, b, c, f, l, m, o\}$	$\{f, c, a, b, m\}$	
300	$\{b, f, h, j, o, w\}$	{ <i>f</i> , <i>b</i> }	
400	$\{b, c, k, s, p\}$	$\{c, b, p\}$	min_support = 3
500	$\{a, f, c, e, \overline{l}, p, m, n\}$	$\{f, c, a, m, p\}$	

- Scan DB once, find frequent 1-itemset (single item pattern)
- Sort frequent items in frequency descending order, f-list
- 3. Scan DB again, construct FP-tree

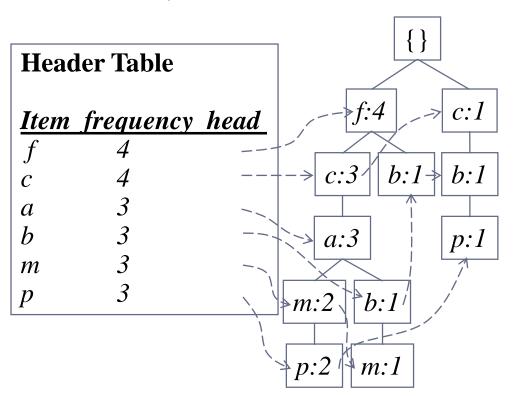


Partition Patterns and Databases

- Frequent patterns can be partitioned into subsets according to f-list
 - F-list = f-c-a-b-m-p
 - Patterns containing p
 - Patterns having m but no p
 - •
 - Patterns having c but no a nor b, m, p
 - Pattern f
- Completeness and non-redundency

Find Patterns Having P From P-conditional Database

- Starting at the frequent item header table in the FP-tree
- Traverse the FP-tree by following the link of each frequent item p
- Accumulate all of transformed prefix paths of item p to form p's conditional pattern base

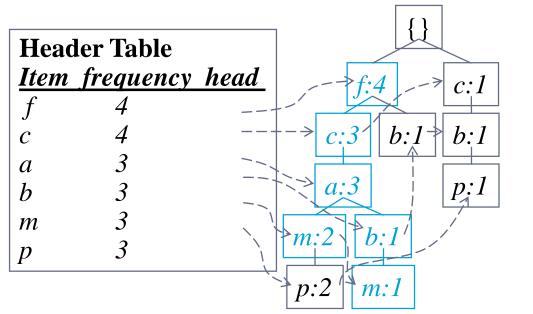


Conditional pattern bases

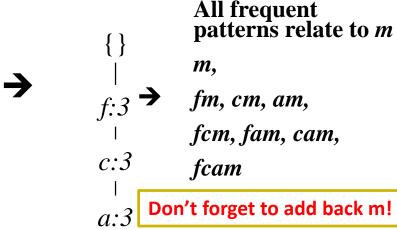
<u>item</u>	cond. pattern base
\overline{c}	f:3
a	fc:3
b	fca:1, f:1, c:1
m	fca:2, fcab:1
p	fcam:2, cb:1

From Conditional Pattern-bases to Conditional FP-trees

- For each pattern-base
 - Accumulate the count for each item in the base
 - Construct the FP-tree for the frequent items of the pattern base

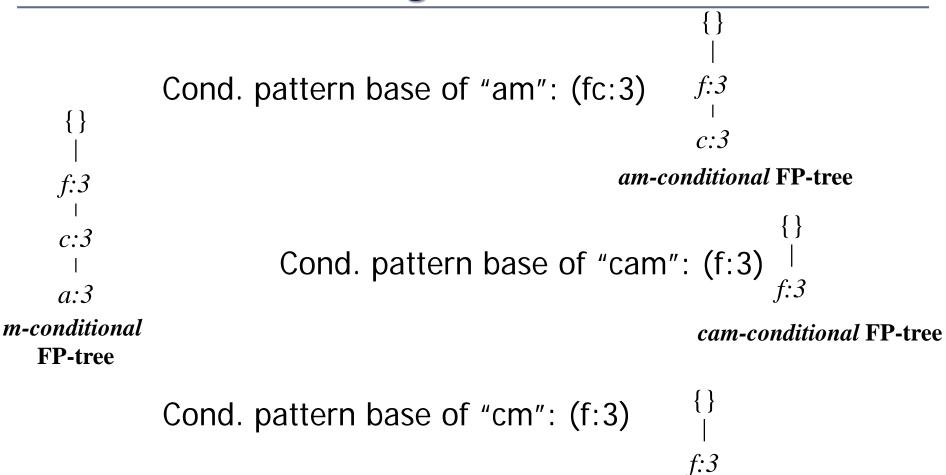


m-conditional pattern base (DB|m): fca:2, fcab:1



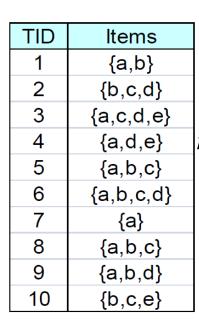
m-conditional FP-tree

Recursion: Mining Each Conditional FP-tree

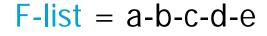


cm-conditional FP-tree

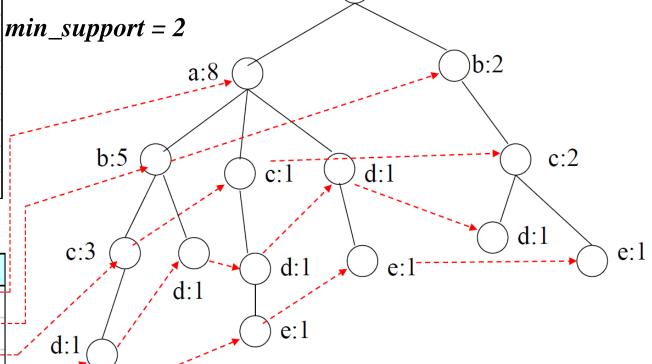
Another Example: FP-Tree Construction



Transaction Database



null



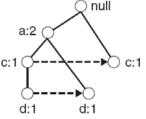
Header table

Item	Pointer
а	
b	
С	
d	
е	

Pointers are used to assist frequent itemset generation

Mining Sub-tree Ending with e

- Conditional pattern base for e: {acd:1; ad:1; bc:1}
- Conditional FP-tree for e:



- Conditional pattern base for de: {ac:1; a:1} null
- Conditional FP-tree for de:
- Frequent patterns for de: {ade:2, de:2}
- Conditional pattern base for ce: {a:1}
- Conditional FP-tree for ce: empty
- Frequent patterns for ce: {ce:2}
- Conditional pattern base for ae: {Ø}
- Conditional FP-tree for ae: empty
- Frequent patterns for ae: {ae:2}
- Therefore, all frequent patterns with e are: {ade:2, de:2, ce:2, ae:2, e:3}

Benefits of the FP-tree Structure

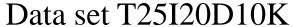
Completeness

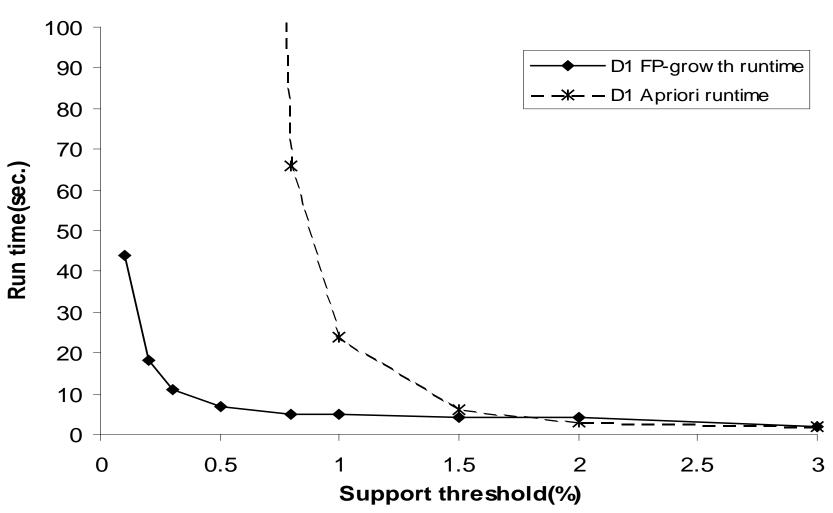
- Preserve complete information for frequent pattern mining
- Never break a long pattern of any transaction

Compactness

- Reduce irrelevant info—infrequent items are gone
- Items in frequency descending order: the more frequently occurring, the more likely to be shared
- Never be larger than the original database (not count node-links and the *count* field)

FP-Growth vs. Apriori: Scalability With the Support Threshold





Advantages of the Pattern Growth Approach

- Divide-and-conquer:
 - Decompose both the mining task and DB according to the frequent patterns obtained so far
 - Lead to focused search of smaller databases
- Other factors
 - No candidate generation, no candidate test
 - Compressed database: FP-tree structure
 - No repeated scan of entire database
 - Basic ops: counting local freq items and building sub FP-tree, no pattern search and matching

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Generating Association Rules

ECLAT: Mining by Exploring Vertical Data Format

Similar idea for inverted index in storing text

- Vertical format: t(AB) = {T₁₁, T₂₅, ...}
 - tid-list: list of trans.-ids containing an itemset
- Deriving frequent patterns based on vertical intersections
 - t(X) = t(Y): X and Y always happen together
 - $t(X) \subset t(Y)$: transaction having X always has Y
- Using diffset to accelerate mining
 - Only keep track of differences of tids
 - $t(X) = \{T_1, T_2, T_3\}, t(XY) = \{T_1, T_3\}$
 - Diffset (XY, X) = $\{T_9\}$
- Eclat (Zaki et al. @KDD'97)

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Generating Association Rules

- Strong association rules
 - Satisfying minimum support and minimum confidence
 - Recall: $Confidence(A \Rightarrow B) = P(B|A) = \frac{support(A \cup B)}{support(A)}$
- Steps of generating association rules from frequent pattern l:
 - Step 1: generate all nonempty subsets of *l*
 - Step 2: for every nonempty subset s, calculate the confidence for rule $s \Rightarrow (l s)$

Example

- $\bullet X = \{I1, I2, I5\}:2$
 - Nonempty subsets of X are: {*I*1, *I*2}: 4, {*I*1, *I*5}: 2, {*I*2, *I*5}: 2, {*I*1}: 6, {*I*2}: 7, and {*I*5}: 2
 - Association rules are:

$$\{I1, I2\} \Rightarrow I5,$$
 $confidence = 2/4 = 50\%$
 $\{I1, I5\} \Rightarrow I2,$ $confidence = 2/2 = 100\%$
 $\{I2, I5\} \Rightarrow I1,$ $confidence = 2/2 = 100\%$
 $I1 \Rightarrow \{I2, I5\},$ $confidence = 2/6 = 33\%$
 $I2 \Rightarrow \{I1, I5\},$ $confidence = 2/7 = 29\%$
 $I5 \Rightarrow \{I1, I2\},$ $confidence = 2/2 = 100\%$

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Frequent Itemset Mining Methods

Pattern Evaluation Methods 💝



Summary

Misleading Strong Association Rules

Not all strong association rules are interesting

	Basketball	Not basketball	Sum (row)
Cereal	2000	1750	3750
Not cereal	1000	250	1250
Sum(col.)	3000	2000	5000

- Shall we target people who play basketball for cereal ads? play basketball \Rightarrow eat cereal [40%, 66.7%]
- Hint: What is the overall probability of people who eat cereal?
 - 3750/5000 = 75% > 66.7%!
- Confidence measure of a rule could be misleading

Other Measures

- From association to correlation
 - Lift
 - $\cdot \chi^2$
 - All_confidence
 - Max_confidence
 - Kulczynski
 - Cosine

Interestingness Measure: Correlations (Lift)

- play basketball \Rightarrow eat cereal [40%, 66.7%] is misleading
 - The overall % of people eating cereal is 75% > 66.7%.
- play basketball \Rightarrow not eat cereal [20%, 33.3%] is more accurate, although with lower support and confidence
- Measure of dependent/correlated events: lift

$$lift = \frac{support(A \cup B)}{support(A)support(B)}$$

	Basketball	Not basketball	Sum (row)
Cereal	2000	1750	3750
Not cereal	1000	250	1250
Sum(col.)	3000	2000	5000

$$lift(B,C) = \frac{2000/5000}{3000/5000*3750/5000} = 0.89$$

$$lift(B, \neg C) = \frac{1000/5000}{3000/5000*1250/5000} = 1.33$$

1: independent

>1: positively correlated

<1: negatively correlated

Correlation Analysis (Nominal Data)

• χ^2 (chi-square) test

$$\chi^2 = \sum \frac{(Observed - Expected)^2}{Expected}$$

- Independency test between two attributes
 - The larger the χ^2 value, the more likely the variables are related
- The cells that contribute the most to the χ^2 value are those whose actual count is very different from the expected count under independence assumption
- Correlation does not imply causality
 - # of hospitals and # of car-theft in a city are correlated
 - Both are causally linked to the third variable: population

When Do We Need Chi-Square Test?

- Considering two attributes A and B
 - A: a nominal attribute with c distinct values,

$$a_1, \ldots, a_c$$

- E.g., Grades of Math
- B: a nominal attribute with r distinct values, $b_1, ..., b_r$
 - E.g., Grades of Science
- Question: Are A and B related?

How Can We Run Chi-Square Test?

- Constructing contingency table
 - Observed frequency o_{ij} : number of data objects taking value b_i for attribute B and taking value a_j for attribute A

	a_1	a_2		a_c
b_1	011	012		o_{1c}
b_2	021	022	•••	02c
b_r	o_{r1}	o_{r2}	•••	o_{rc}

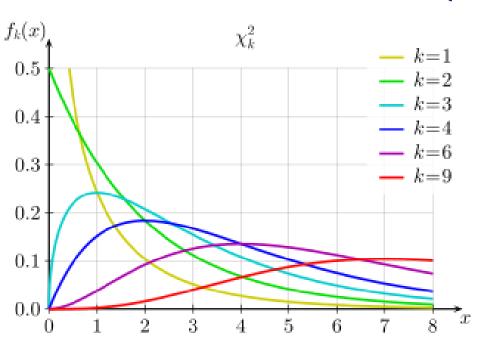
• Calculate expected frequency
$$e_{ij} = \frac{count(B=b_i) \times count(A=a_j)}{n}$$

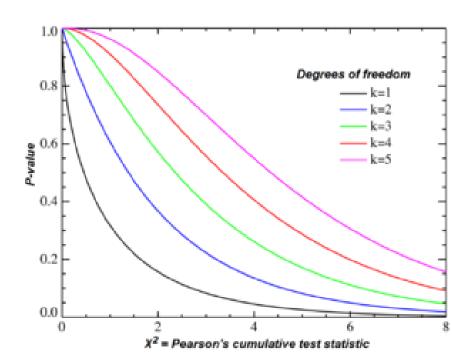
Null hypothesis: A and B are independent

• The Pearson χ^2 statistic is computed as:

•
$$X^2 = \sum_{i=1}^r \sum_{j=1}^c \frac{(o_{ij} - e_{ij})^2}{e_{ij}}$$

• Follows Chi-squared distribution with degree of freedom as $(r-1) \times (c-1)$





Chi-Square Calculation: An Example

	Play chess	Not play chess	Sum (row)
Like science fiction	250(90)	200(360)	450
Not like science fiction	50(210)	1000(840)	1050
Sum(col.)	300	1200	1500

• χ^2 (chi-square) calculation (numbers in parenthesis are expected counts calculated based on the data distribution in the two categories)

$$\chi^2 = \frac{(250 - 90)^2}{90} + \frac{(50 - 210)^2}{210} + \frac{(200 - 360)^2}{360} + \frac{(1000 - 840)^2}{840} = 507.93$$

- It shows that like_science_fiction and play_chess are correlated in the group
 - Degree of freedom = (2-1)(2-1) = 1
 - P-value = $P(X^2 > 507.93) = 0.0$
 - Reject the null hypothesis => A and B are dependent

Are *lift* and χ² Good Measures of Correlation?

- Lift and χ^2 are affected by null-transaction
 - E.g., number of transactions that do not contain milk nor coffee
- All_confidence
 - all_conf(A,B)= $min{P(A | B),P(B | A)}$
- Max_confidence
 - $\max_conf(A, B) = \max\{P(A \mid B), P(B \mid A)\}$
- Kulczynski
 - $Kulc(A, B) = \frac{1}{2}(P(A|B) + P(B|A))$
- Cosine
 - $cosine(A, B) = \sqrt{P(A|B) \times P(B|A)}$

Comparison of Interestingness Measures

- Null-(transaction) invariance is crucial for correlation analysis
- Lift and χ^2 are not null-invariant
- 5 null-invariant measures

	Milk	No Milk	Sum (row)
Coffee	m, c	~m, c	С
No Coffee	m, ~c	~m, ~c	~C
Sum(col.)	m	~m	Σ

Measure	Definition	Range	Null-Invariant
$\chi^2(a,b)$	$\sum_{i,j=0,1} \frac{(e(a_i,b_j) - o(a_i,b_j))^2}{e(a_i,b_j)}$	$[0,\infty]$	No
Lift(a, b)	$\frac{P(ab)}{P(a)P(b)}$	$[0,\infty]$	No
AllConf(a, b)	$\frac{sup(ab)}{max\{sup(a), sup(b)\}}$	[0, 1]	Yes
Coherence(a,b)	$\frac{sup(ab)}{sup(a)+sup(b)-sup(ab)}$	[0, 1]	Yes
Cosine(a,b)	$\frac{sup(ab)}{\sqrt{sup(a)sup(b)}}$	[0, 1]	Yes
Kulc(a,b)	$\frac{sup(ab)}{2}(\frac{1}{sup(a)} + \frac{1}{sup(b)})$	[0, 1]	Yes
MaxConf(a,b)	$max\{\frac{sup(ab)}{sup(a)}, \frac{sup(ab)}{sup(b)}\}$	[0, 1]	Yes
Table 3	. Interestingness measur	re defi	nitions.

Null-transactions w.r.t. m and c

Kulczynski measure (1927)

Null-invariant

Data set	mc	\overline{m}_C	$m\overline{s}$	\overline{mc}	χ^2	Lift	AllConf	Coherence	e Cesine	Kulc	MaxConf
D_1	10,000	1,000	1,000	200,000	90557	9.26	0.91	0.83	0.91	0.91	0.91
D_2	10,000	1,000	1,000	100	0	1	0.91	0.83	0.91	0.91	0.91
D_3	100	1,000	1,000	100,000	670	8.44	0.09	0.05	0.09	0.09	0.09
D_4	1,000	1,000	1,000	100,000	24740	25.75	0.5	0.33	0.5	0.5	0.5
D_5	1,000	100	10,000	100,000	8173	9.18	0.09	0.09	0.29	0.5	0.91
D_{6}	1,000	10	100,000	100,000	965	1.97	0.01	0.01	0.10	0.5	0.99

Table 2. Example data sets. Subtle: They disagree

*Analysis of DBLP Coauthor Relationships

Recent DB conferences, removing balanced associations, low sup, etc.

ID	Author a	Author b	sup(ab)	sup(a)	sup(b)	Coherence	Cosine	Kulc
1	Hans-Peter Kriegel	Martin Ester	28	146	54	0.163(2)	0.315(7)	0.355(9)
2	Michael Carey	Miron Livny	26	104	58	0.191(1)	0.335(4)	0.349 (10)
3	Hans-Peter Kriegel	Joerg Sander	24	146	36	0.152(3)	0.331(5)	0.416(8)
4	Christos Faloutsos	Spiros Papadimitriou	20	162	26	0.119(7)	0.308(10)	0.446(7)
5	Hans-Peter Kriegel	Martin Pfeifle	18	146	18	0.123(6)	0.351(2)	0.562(2)
6	Hector Garcia-Molina	Wilburt Labio	16	144	18	0.110(9)	0.314(8)	0.500(4)
7	Divyakant Agrawal	Wang Hsiung	16	120	16	0.133(5)	0.365(1)	0.567(1)
8	Elke Rundensteiner	Murali Mani	16	104	20	0.148(4)	0.351(3)	0.477(6)
9	Divyakant Agrawal	Oliver Po	\bigcirc 12	120	12	0.100(10)	0.316(6)	0.550(3)
10	Gerhard Weikum	Martin Theobald	12	106	14	0.111 (8)	0.312(9)	0485(5)

Table 5. Experiment on DBLP data set.

Advisor-advisee relation: Kulc: high, coherence: low, cosine: middle

Tianyi Wu, Yuguo Chen and Jiawei Han, "<u>Association Mining in Large Databases:</u>
 <u>A Re-Examination of Its Measures</u>", Proc. 2007 Int. Conf. Principles and Practice
 of Knowledge Discovery in Databases (PKDD'07), Sept. 2007

*Which Null-Invariant Measure Is Better?

 IR (Imbalance Ratio): measure the imbalance of two itemsets A and B in rule implications

$$IR(A,B) = \frac{|sup(A) - sup(B)|}{sup(A) + sup(B) - sup(A \cup B)}$$

- Kulczynski and Imbalance Ratio (IR) together present a clear picture for all the three datasets D₄ through D₆
 - D₄ is balanced & neutral
 - D₅ is imbalanced & neutral
 - D₆ is very imbalanced & neutral

Data	mc	$\overline{m}c$	$m\overline{c}$	\overline{mc}	$all_conf.$	$max_conf.$	Kulc.	cosine	$_{ m IR}$
D_1	10,000	1,000	1,000	100,000	0.91	0.91	0.91	0.91	0.0
D_2	10,000	1,000	1,000	100	0.91	0.91	0.91	0.91	0.0
D_3	100	1,000	1,000	100,000	0.09	0.09	0.09	0.09	0.0
D_4	1,000	1,000	1,000	100,000	0.5	0.5	0.5	0.5	0.0
D_5	1,000	100	10,000	100,000	0.09	0.91	0.5	0.29	0.89
D_6	1,000	10	100,000	100,000	0.01	0.99	0.5	0.10	0.99

Mining Frequent Patterns, Association and Correlations

Basic Concepts

Frequent Itemset Mining Methods

Pattern Fyaluation Methods

Summary



Summary

- Basic concepts
 - Frequent pattern, association rules, supportconfident framework, closed and max-patterns
- Scalable frequent pattern mining methods
 - Apriori
 - FPgrowth
 - *Vertical format approach (ECLAT)
 - Which patterns are interesting?
 - Pattern evaluation methods

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