# Decision trees (recap), Nearest Neighbors

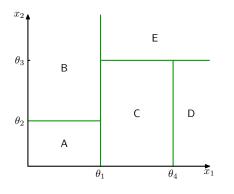
#### Sriram Sankararaman

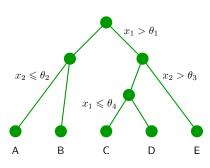
The instructor gratefully acknowledges Fei Sha, Ameet Talwalkar, Eric Eaton, and Jessica Wu whose slides are heavily used, and the many others who made their course material freely available online.

#### Outline

- Review of previous lecture
- 2 Hyperparameters
- 3 Nearest neighbor classifier
- What we have learned

# A tree partitions the feature space





# Decision tree learning

#### **Setup**

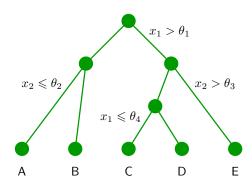
- Set of possible instances X
  - lacktriangle Each instance  $x\in\mathbb{X}$  is a feature vector
- Set of possible labels Y
  - Y is discrete valued
- Unknown target function  $f: \mathbb{X} \to \mathbb{Y}$
- Model/Hypotheses:  $H = \{h|h : \mathbb{X} \to \mathbb{Y}\}.$
- Each hypothesis h is a decision tree

Goal: Train/induce/learn a function h that maps instance to label.

### Learning a tree model

#### Three things to learn:

- The structure of the tree.
- ② The threshold values  $(\theta_i)$ .
- The values for the leaves  $(A, B, \ldots)$ .



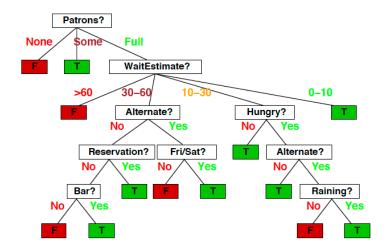
#### **Choosing a restaurant**

(Example from Russell & Norvig, AIMA)

Example	Attributes									Target	
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
$X_1$	T	F	F	T	Some	\$\$\$	F	T	French	0–10	T
$X_2$	T	F	F	T	Full	\$	F	F	Thai	30–60	F
$X_3$	F	<i>T</i>	F	F	Some	\$	F	F	Burger	0–10	T
$X_4$	T	F	T	T	Full	\$	F	F	Thai	10–30	T
$X_5$	<i>T</i>	F	T	F	Full	\$\$\$	F	T	French	>60	F
$X_6$	F	<i>T</i>	F	T	Some	<i>\$\$</i>	T	<i>T</i>	Italian	0–10	T
$X_7$	F	T	F	F	None	\$	T	F	Burger	0–10	F
$X_8$	F	F	F	T	Some	<i>\$\$</i>	T	T	Thai	0–10	T
$X_9$	F	T	T	F	Full	\$	T	F	Burger	>60	F
$X_{10}$	T	T	T	T	Full	\$\$\$	F	T	Italian	10–30	F
$X_{11}$	F	F	F	F	None	\$	F	F	Thai	0–10	F
$X_{12}$	T	T	T	T	Full	\$	F	F	Burger	30–60	T

Classification of examples is positive (T) or negative (F)

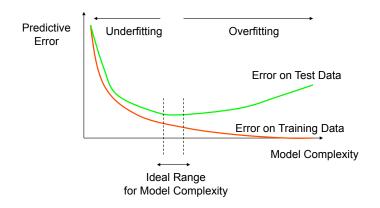
# Greedily we build the tree and get this



## What is the optimal Tree Depth?

- We need to be careful to pick an appropriate tree depth
- If the tree is too deep, we can overfit (memorize the training data).
- If the tree is too shallow, we underfit (not learn enough).
- Max depth is a hyperparameter that should be tuned by the data
  - ▶ A parameter that controls the other parameters of the tree.
  - Max depth of 0: underfitting
  - ▶ Max depth of  $\infty$ : overfitting.

# Overfitting



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# Hyperparameters in Decision tree

#### Max depth of the tree

- Critical to choose max depth carefully for good generalization.
- Choosing max depth (as well as any other hyperparameters) based on empirical studies.

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#### Max depth of the tree

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How do we choose max depth?

# Hyperparameter selection (tuning) by using a validation dataset

#### Training data (set)

- N samples/instances:  $\mathcal{D}^{ ext{TRAIN}} = \{(m{x}_1, y_1), (m{x}_2, y_2), \cdots, (m{x}_{\mathsf{N}}, y_{\mathsf{N}})\}$
- ullet They are used for learning  $h(\cdot)$

#### Test (evaluation) data

- ullet M samples/instances:  $\mathcal{D}^{ ext{TEST}} = \{(m{x}_1, y_1), (m{x}_2, y_2), \cdots, (m{x}_{\mathsf{M}}, y_{\mathsf{M}})\}$
- They are used for assessing how well  $h(\cdot)$  will do in predicting an unseen  ${\pmb x} \notin \mathcal{D}^{\text{\tiny TRAIN}}$

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#### Validation (or development) data

- L samples/instances:  $\mathcal{D}^{ ext{DEV}} = \{(m{x}_1, y_1), (m{x}_2, y_2), \cdots, (m{x}_{\mathsf{L}}, y_{\mathsf{L}})\}$
- They are used to optimize hyperparameter(s).

Training data, validation and test data should *not* overlap!

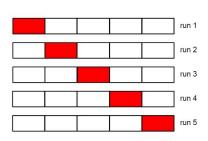
- For each possible value of the hyperparameter (say Max depth  $=1,3,\cdots$ )
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  - lacktriangle Evaluate the performance of the model on  $\mathcal{D}^{ ext{DEV}}$
- ullet Choose the model with the best performance on  $\mathcal{D}^{ ext{DEV}}$
- ullet Evaluate the model on  $\mathcal{D}^{ ext{TEST}}$

# Cross-validation (CV)

#### What if we do not have validation data?

- We split the training data into K equal parts (termed folds or splits).
- We use each part in turn as a validation dataset and use the others as a training dataset.
- We choose the hyperparameter such that on average, the model performing the best

 $\mathsf{K} = 5$ : 5-fold cross validation



Special case: when K = N, this will be leave-one-out (LOO).

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    - $\star$  Train a model using  $\mathcal{D}_{\backslash k}^{\scriptscriptstyle \mathrm{TRAIN}} = \mathcal{D}^{\scriptscriptstyle \mathrm{TRAIN}} \mathcal{D}_k^{\scriptscriptstyle \mathrm{TRAIN}}$
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## Summary

- Model/hypotheses: Trees
- Have parameters: Features at each internal node, values along edges and labels at leaves.
- Have hyperparameters: max depth

# Summary

#### Advantages of using trees

- Easily interpretable by humans (as long as the tree is not too big)
- Computationally efficient
- Handles both numerical and categorical data

#### **Disadvantages**

- Heuristic training techniques
  - Finding partition of space that minimizes empirical error is NP-hard
  - We resort to greedy approaches with limited theoretical underpinnings

# Summary

- You should now be able to use decision trees to do machine learning.
- Given data, use training, development and test splits (or cross-validation).
- Use training and development to tune for Max depth that trades off overfitting and underfitting.
- Use test to get an estimate of generalization or accuracy on unseen data.
- Read 1.3,1.4-1.10 of CIML

#### Outline

- Review of previous lecture
- 2 Hyperparameters
- Nearest neighbor classifier
  - Example
  - General setup for classification
  - Algorithm
  - Some practical sides of NNC
  - Preprocessing data
- 4 What we have learned

# Recognizing flowers

#### Types of Iris: setosa, versicolor, and virginica







# Measuring the properties of the flowers

### Features: the widths and lengths of sepal and petal



# Snapshot of Iris data

#### Iris data

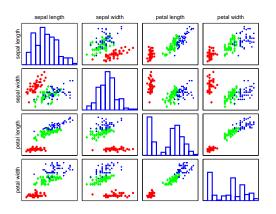
- 4 features
- 3 classes

#### Fisher's Iris Data

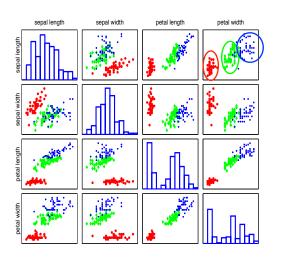
Sepal length +	Sepal width +	Petal length +	Petal width +	Species +
5.1	3.5	1.4	0.2	I. setosa
4.9	3.0	1.4	0.2	I. setosa
4.7	3.2	1.3	0.2	I. setosa
4.6	3.1	1.5	0.2	I. setosa
5.0	3.6	1.4	0.2	I. setosa
5.4	3.9	1.7	0.4	I. setosa
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4.4	2.9	1.4	0.2	I. setosa
4.9	3.1	1.5	0.1	I. setosa

# Pairwise scatter plots of 131 flower specimens Visualization helps to identify the right learning model to use

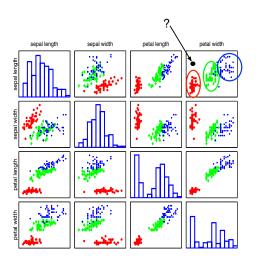
Each colored point is an instance ( flower specimen ): setosa, versicolor, virginica



# Different types seem well-clustered and separable Using two features: petal width and sepal length



# Labeling an unknown flower type



Closer to red cluster: so labeling it as setosa

#### Inductive bias

• Label of point (instance) is similar to the label of nearby points.

#### Multi-class classification

#### Classify data into one of the multiple categories

- ullet Instance (feature vectors):  $oldsymbol{x} \in \mathbb{R}^{\mathsf{D}}$
- Label:  $y \in [C] = \{1, 2, \cdots, C\}$
- Learning goal: y = h(x)

#### Special case: binary classification

- Number of classes: C=2
- Labels:  $\{0,1\}$  or  $\{-1,+1\}$

# **Terminology**

#### Training data (set)

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Training data and test data should *not* overlap:  $\mathcal{D}^{\text{TRAIN}} \cap \mathcal{D}^{\text{TEST}} = \emptyset$ 

# Nearest neighbor classification (NNC)

#### **Training**

• Store the entire training set.

# Nearest neighbor classification (NNC)

#### **Testing**

$$\boldsymbol{x}(1) = \boldsymbol{x}_{\mathsf{nn}(\boldsymbol{x})}$$

where  $\operatorname{nn}(\boldsymbol{x}) \in [\mathsf{N}] = \{1, 2, \cdots, \mathsf{N}\}$ , i.e., the index to one of the training instances

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$$nn(x) = \arg\min_{n \in [N]} \|x - x_n\|_2^2 = \arg\min_{n \in [N]} \sum_{d=1}^{D} (x_d - x_{nd})^2$$

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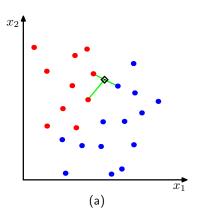
$$nn(x) = \arg\min_{n \in [N]} ||x - x_n||_2^2 = \arg\min_{n \in [N]} \sum_{d=1}^{D} (x_d - x_{nd})^2$$

#### Classification rule

$$y = h(\boldsymbol{x}) = y_{\mathsf{nn}(\boldsymbol{x})}$$

### Visual example

In this 2-dimensional example, the nearest point to  $\boldsymbol{x}$  is a red training instance, thus,  $\boldsymbol{x}$  will be labeled as red.



### Example: classify Iris with two features

#### **Training data**

ID (n)	petal width $(x_1)$	sepal length $(x_2)$	category $(y)$
1	0.2	5.1	setosa
2	1.4	7.0	versicolor
3	2.5	6.7	virginica

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Calculating distance = 
$$\sqrt{(x_1-x_{n1})^2+(x_2-x_{n2})^2}$$

ID	distance
1	1.75
2	0.72
3	0.76

Thus, the category is *versicolor* (the real category is *virginica*)

#### How to measure nearness with other distances?

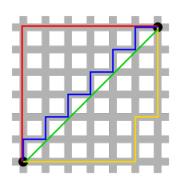
#### Previously, we use the Euclidean distance

$$\mathsf{nn}(\boldsymbol{x}) = \arg\min\nolimits_{n \in [\mathsf{N}]} \|\boldsymbol{x} - \boldsymbol{x}_n\|_2^2$$

### We can also use alternative distances E.g., the following $L_1$ distance (i.e., city

block distance, or Manhattan distance)

$$\operatorname{nn}(\boldsymbol{x}) = \operatorname{arg\,min}_{n \in [\mathbb{N}]} \|\boldsymbol{x} - \boldsymbol{x}_n\|_1$$
$$= \operatorname{arg\,min}_{n \in [\mathbb{N}]} \sum_{d=1}^{\mathsf{D}} |x_d - x_{nd}|$$



Green line is Euclidean distance. Red, Blue, and Yellow lines are  $L_1$  distance

• Real-valued features (discussion so far).

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- Binary features :

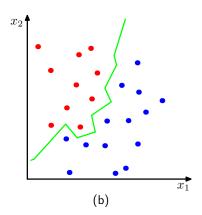
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- Binary features : map to 0 and 1.
  - Example: Is flower white or colored ?
- ullet Categorical features with V values: map to V-binary features.
  - Example: Color (white, blue, pink): map to three binary features IsltWhite?, IsltBlue? IsltPink?
  - Termed one-hot encoding.

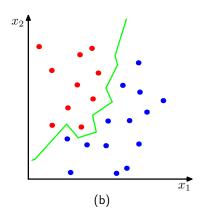
### **Decision boundary**

For every point in the space, determine its label using the NNC rule. Gives rise to a *decision boundary* that partitions the space into different regions.



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Compare to decision boundary of decision trees

# K-nearest neighbor (KNN) classification

#### Increase the number of nearest neighbors to use?

- ullet 1-nearest neighbor:  $\mathsf{nn}_1(oldsymbol{x}) = rg \min_{n \in [\mathsf{N}]} \|oldsymbol{x} oldsymbol{x}_n\|_2^2$
- ullet 2nd-nearest neighbor:  $\mathsf{nn}_2(oldsymbol{x}) = rg\min_{n \in [\mathsf{N}] \mathsf{nn}_1(oldsymbol{x})} \|oldsymbol{x} oldsymbol{x}_n\|_2^2$
- ullet 3rd-nearest neighbor:  $\operatorname{nn}_3(m{x}) = rg\min_{n \in [\mathbf{N}] \operatorname{nn}_1(m{x}) \operatorname{nn}_2(m{x})} \|m{x} m{x}_n\|_2^2$

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#### The set of K-nearest neighbors

$$\mathsf{knn}(\boldsymbol{x}) = \{\mathsf{nn}_1(\boldsymbol{x}), \mathsf{nn}_2(\boldsymbol{x}), \cdots, \mathsf{nn}_K(\boldsymbol{x})\}$$

Let 
$${\boldsymbol x}(k) = {\boldsymbol x}_{\operatorname{nn}_k({\boldsymbol x})}$$
, then

$$\|\boldsymbol{x} - \boldsymbol{x}(1)\|_2^2 \le \|\boldsymbol{x} - \boldsymbol{x}(2)\|_2^2 \dots \le \|\boldsymbol{x} - \boldsymbol{x}(K)\|_2^2$$

How to classify with K neighbors?

# How to classify with K neighbors?

#### Classification rule

- ullet Every neighbor votes: suppose  $y_n$  (the label) for  $oldsymbol{x}_n$  is c, then
  - ▶ vote for c is 1
  - vote for  $c' \neq c$  is 0

We use the *indicator function*  $\mathbb{I}(y_n == c)$  to represent.

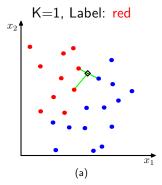
Aggregate everyone's vote

$$v_c = \sum_{n \in \mathsf{knn}(\boldsymbol{x})} \mathbb{I}(y_n == c), \quad \forall \quad c \in [\mathsf{C}]$$

Label with the majority

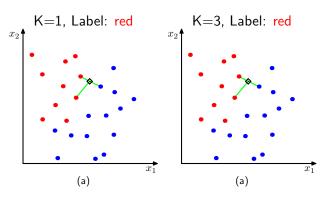
$$y = h(\boldsymbol{x}) = \arg\max_{c \in [\mathsf{C}]} v_c$$

# Example

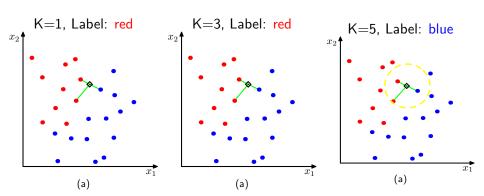




# Example

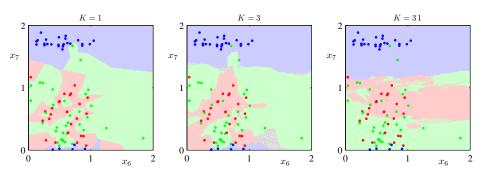


# Example



# Decision boundary as a function of K

### Decision boundary as a function of K



When K increases, the decision boundary becomes smooth.

# Mini-summary

#### **Advantages of NNC**

 Computationally, simple and easy to implement – just computing the distance

#### **Disadvantages of NNC**

- $\bullet$  Computationally intensive for large-scale problems:  $O({\rm N}D)$  for labeling a data point
- We need to "carry" the training data around. Without it, we cannot
  do classification. This type of method is called *nonparametric*.
- ullet Choosing the right distance measure and K can be involved.

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# Hypeparameters in NNC

#### Two practical issues about NNC

- Choosing K, i.e., the number of nearest neighbors (default is 1)
- Choosing the right distance measure (default is Euclidean distance), for example, from the following generalized distance measure

$$\|\boldsymbol{x} - \boldsymbol{x}_n\|_p = \left(\sum_d |x_d - x_{nd}|^p\right)^{1/p}$$

for  $p \geq 1$ .

Those are not specified by the algorithm itself — resolving them requires empirical studies and are task/dataset-specific.

# Tuning by using a validation dataset

#### Training data (set)

- ullet N samples/instances:  $\mathcal{D}^{ ext{TRAIN}} = \{(m{x}_1, y_1), (m{x}_2, y_2), \cdots, (m{x}_{\mathsf{N}}, y_{\mathsf{N}})\}$
- ullet They are used for learning  $h(\cdot)$

#### Test (evaluation) data

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#### **Development (or validation) data**

- ullet L samples/instances:  $\mathcal{D}^{ ext{DEV}} = \{(oldsymbol{x}_1, y_1), (oldsymbol{x}_2, y_2), \cdots, (oldsymbol{x}_{\mathsf{L}}, y_{\mathsf{L}})\}$
- They are used to optimize hyperparameter(s).

Training data, validation and test data should *not* overlap!

# Recipe

- For each possible value of the hyperparameter (say  $K=1,3,\cdots,100$ )
  - ightharpoonup Train a model using  $\mathcal{D}^{ ext{TRAIN}}$
  - lacktriangle Evaluate the performance of the model on  $\mathcal{D}^{ ext{DEV}}$
- ullet Choose the model with the best performance on  $\mathcal{D}^{ ext{DEV}}$
- ullet Evaluate the model on  $\mathcal{D}^{ ext{TEST}}$

What if we do not have validation data?

#### What if we do not have validation data?

• Use cross-validation.

### Yet, another practical issue with NNC

#### Assumes all features are equally important!

• Distances depend on units of the features.

#### Preprocess data

# Normalize data to have zero mean and unit standard deviation in each dimension

• Compute the means and standard deviations in each feature

$$\bar{x}_d = \frac{1}{N} \sum_n x_{nd}, \qquad s_d^2 = \frac{1}{N-1} \sum_n (x_{nd} - \bar{x}_d)^2$$

Scale the feature accordingly

$$x_{nd} \leftarrow \frac{x_{nd} - \bar{x}_d}{s_d}$$

Many other ways of normalizing data — you would need/want to try different ones and pick them using (cross)validation

#### Outline

- Review of previous lecture
- 2 Hyperparameters
- Nearest neighbor classifier
- What we have learned

# Summary so far

- Decision trees and Nearest Neighbor Classifier: two simple learning algorithm
  - Used intensively in practical applications.
- Discussed a few practical aspects, such as tuning hyperparameters, with (cross)validation

#### Summary

- You should now be able to use decision trees and nearest neighbors to do machine learning.
- Given data, use training, development and test splits (or cross-validation).
- Use training and development to tune hyperparameters that trades off overfitting and underfitting.
- Use test to get an estimate of generalization or accuracy on unseen data.
- Further reading
  - ► Read 1.3,1.4-1.10 of CIML for decision trees (v0.90).
  - ▶ Read 2-2.3 of CIML for nearest neighbors (v0.90).