Analysis of ascorbic acid and tooth growth in hamsters

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Synopsis

A study was undertaken whereby 10 hamsters where given different dosages of ascorbic acid, delivered either through orange juice or a vitamin C supplement. This paper firstly does a brief graphical analysis of the data to determine possible hypotheses. Statistical inference methods are then used to either support or reject them.

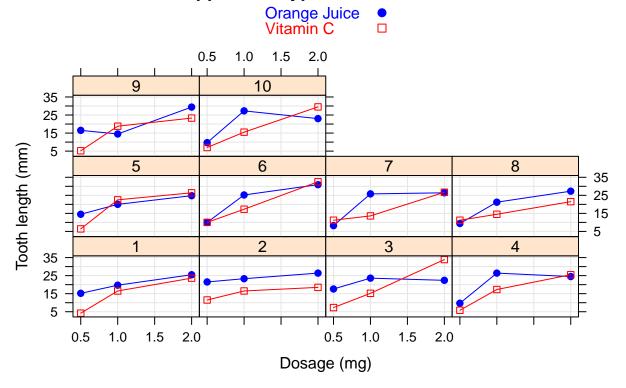
Data Exploration

The ToothGrowth data is a set of 6 trials on 10 hamsters, with 3 trials using ascorbic acid delivered in 3 different dosages (0.5mg, 1mg, 2mg) via orange juice and three with these same dosages but delivered through a vitamin C supplement. First, the data is loaded and an hamster id associated with each of the observations.

```
data("ToothGrowth")
ham_id = { id<- NULL; for (i in 1:6) { for (i in 1:10) { id <- c(id,i)}}; id}
tgi <- cbind(ham_id, ToothGrowth)</pre>
```

Now we can create a plot for each hamster, showing the toothgrowth for different dosages and different delivery methods.

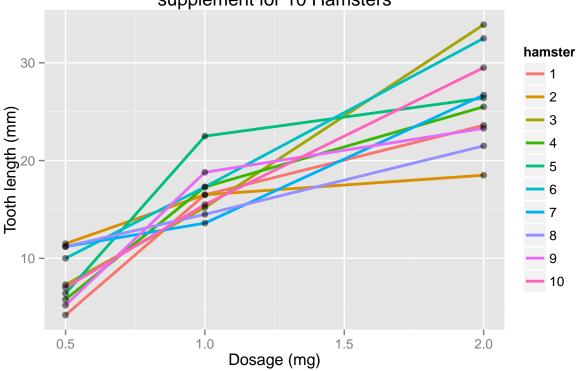
Hamster tooth length by Ascorbic Acid dosage and supplement type for 10 hamsters



As can be seen, for all hamsters there is a strong correlation between ascorbic acid dosage and tooth length, although the effect is less pronounced when incerasing the dosage from 1.0mg to 2.0mg delivered through orange juice.

This correlation is shown even clearer when all 10 hamsters are shown on the same graph for vitamin C supplements.





Does Ascorbic acid increase tooth growth in hamsters?

This is just one of the many questions about hamsters that you wanted to know but were afraid to ask.

The null hypothesis is that increasing the dosage of vitamin C doesn't increase tooth size, the alternate hypothesis is that it does.

From the graphs generated during the data exploration, it would appear that the largest tooth growth is when the dosage is administered through an orange juice supplement. As there is a low sample number (10), we will use the t-test interval to determined the probability of this alternate hypothesis.

```
tg_05_oj <- filter(tgi, supp=="0J" & dose==0.5)$len
tg_10_oj <- filter(tgi, supp=="0J" & dose==1)$len
tg_20_oj <- filter(tgi, supp=="0J" & dose==2)$len
t1<-t.test(tg_10_oj,tg_05_oj, paired=T)
t2<-t.test(tg_20_oj,tg_10_oj, paired=T)</pre>
```

The lattice graphs show a marked increase in tooth length between a dosage of 0.5mg and 1.0mg when supplied through orange juice, so we will consider the difference of these two trials first.

The 95% confidence interval of the difference in means of the alternate hypothesis is 4.3246159, 14.6153841, with a t-statistic of 4.1634653 and a p-value of 0.0024351 of the null hypothesis. This shows that there is a

high probability that a supplement of orange juice does increase tooth growth in hamsters. If we look at the effect of increasing the dose to 2mg from 1mg using orange juice, the effect is in-conclusive, with the 95% confidence interval including 0, i.e. -0.5509376, 7.2709376.

However, there may be factors other than the ascorbic acid in the orange juice that is having this effect on tooth length. So let's turn our attention to the pure vitamin C supplement.

```
tg_05_vc <- filter(tgi, supp=="VC" & dose==0.5)$len
tg_10_vc <- filter(tgi, supp=="VC" & dose==1)$len
tg_20_vc <- filter(tgi, supp=="VC" & dose==2)$len
t3<-t.test(tg_10_vc,tg_05_vc, paired=T)
t4<-t.test(tg_20_vc,tg_10_vc, paired=T)</pre>
```

The correlation between tooth growth and vitamin C dosage is even greater when the dosage is through a vitamin C supplement. Looking at the difference between 0.5mg and 1.0mg, the 95% confidence interval of the difference in means of the alternate hypothesis is 5.5496008, 12.0303992, with a t-statistic of 6.1363925 and a p-value of 0.0001715 of the null hypothesis. Increasing the dosage further from 1.0mg to 2.0mg further supports the alternate hypothesis, with a difference in mean confidence interval of 5.4050824, 13.3349176

Conclusion

There is strong statistical support of the hypothesis that ascorbic acid increases tooth growth in hamsters.

In addition, the lack of increase from 1.0mg to 2.0mg in tooth growth when delivered using orange juice but a strong increase when a pure vitamin C supplement was used, suggests that other factors come into play by increasing the dosage of through orange juice, e.g. increased tooth decay.

However, without a control trial, i.e. where no vitamin C supplement is given, these findings cannot be conclusive, as other factors cannot be ruled out, e.g. simply a more nutrious diet may increase tooth growth, rather then a particular vitamin.

Note that this analysis makes a number of assumptions about the data:

- 1. The same hamsters were used in each of the 6 trials and each of the results were in the same order
- 2. Each of the six trials were carried out over the same time period
- 3. An appropriate time gap between trials took place to ensure no carry over of effects
- 4. All other treatment of the hamsters in each of the trials was constant
- 5. Hamsters have consistent tooth growth throughout their lives, as the trials were conducted at different ages of the hamster