



# EBU5302 A

Complete the information below about yourself very carefully.

QM student number

BUPT student number

Class number


Joint Programme Examinations 2015/16

EBU5302 Telecommunications Systems

Paper A

Answer ALL questions

For examiners' use only

1	
2	
3	
4	
Total	

Only regular scientific calculator allowed. No SMART PHONE calculator is ALLOWED.  
Make and type of any electronic calculator you are using \_\_\_\_\_

**INSTRUCTIONS**

- 1. You must not take answer books, used or unused, from the examination room.
- 2. Write only in black or blue pen and in English.
- 3. Do all rough work in the answer book – do not tear out any pages.
- 4. If you use Supplementary Answer Books, tie them to the end of this book.
- 5. Write clearly and legibly.
- 6. Read the instructions on the inside cover.

Examiners

Dr Yue Gao, Dr Yan Sun

### Question 1

Let  $x(t)$  be a band-limited signal to  $W = 2$  kHz, amplitude  $0 \leq x(t) \leq 2$  and power  $P = 1$ . Signal  $x(t)$  is sampled at a rate 20% higher than the Nyquist rate to provide a guard band. The maximum acceptable error in the sample amplitude (the maximum quantization error) is 0.5% of the peak amplitude. The quantized samples are binary coded.

Assume “Sr” is an  $M=8$  symbol source. Symbol A.... H represent each of the symbol amplitude values generated by the quantiser. The probability  $p_m$  of each symbol is shown in the following table:

**Table 1**

m	A	B	C	D	E	F	G	H
P(m)	0.3	0.1	0.06	0.25	0.04	0.05	0.18	0.02

- a) Using diagrams to explain why in general sampling has to meet the Nyquist sampling theorem. [4 marks]
- b) Illustrate what the sample rate for  $x(t)$  is. [1 mark]
- c) Find the minimum bandwidth of a channel required to transmit the encoded binary signal. [6 marks]
- d) If 24 such signals are time-division-multiplexed, determine the minimum transmission bandwidth required to transmit the multiplexed signal. [1 mark]
- e) What is the information content for each symbol of Sr? [9 marks]
- f) What are the source entropy and source efficiency for Sr? [4 marks]

## Question 2

A digital information source produces binary sequences at a rate of 5 kbps. The probability of producing the value 0 is  $p_0 = 0.2$ . A Hamming code with the following parity check matrix  $H$  is employed to protect information against errors:

$$H = \begin{bmatrix} 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

The resulting binary sequences are transmitted through a wireless channel where power falloff with distance follows the formula  $P_r(d) = P_t(d_0/d)^3$  for  $d_0=10\text{m}$ . Assume the channel has bandwidth  $B=30\text{ kHz}$  and AWGN with noise PSD (power spectral density)  $N_0/2$ , where  $N_0 = 10^{-9}\text{ W/Hz}$ .

a) For a transmit power of 1 W, find the capacity of this channel for a transmit-receive distance of 100m and 1km.

[6 marks]

b) Based on the parity check matrix  $H$ , determine the length of the input information sequences and the length of the code words. Calculate the code rate of this Hamming code and the resulting transmission rate.

[4 marks]

c) How can the systematic linear block code words of this Hamming code be obtained? Calculate the code words corresponding to the information sequences 0110 and 1010.

[5 marks]

d) Determine the number of errors can be detected and corrected in this Hamming code.

[5 marks]

e) Decode the following received sequence  $r = 1111010$ .

[5 marks]

### Question 3

a) A multilevel digital communication system sends one of 16 possible levels over the channel every 0.8 ms.

- i) What is the number of bits corresponding to each level?
- ii) What is the baud (Symbol) rate?
- iii) What is the bit rate?

[6 marks]

b) Multilevel data with an equivalent bit rate of 2,400 bits/s is sent over a channel using a four level line code that has a rectangular pulse shape at the output of the transmitter. The overall transmission system (i.e. the transmitter, channel and receiver) has an  $r=0.5$  raised cosine roll-off Nyquist filter characteristic.

- i) Find the baud (symbol) rate of the received signal.
- ii) Find the 6-dB bandwidth for this transmission system.
- iii) Find the absolute bandwidth for the system.

[8 marks]

c) The following table illustrates the operation of an FHSS system for one complete period of the PN sequence.

Time	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Input data	0	1	1	1	1	1	1	0	0	0	1	0	0	1	1	1	1	0	1	0
Frequency	$f_{11}$	$f_2$	$f_{11}$	$f_3$	$f_3$	$f_3$	$f_{22}$	$f_{10}$	$f_0$	$f_0$	$f_1$	$f_{22}$	$f_9$	$f_1$	$f_{23}$	$f_3$	$f_{22}$	$f_{11}$	$f_3$	$f_{31}$
PN Sequence	001	110	011	001	001	001	110	011	001	001	001	110	011	001	001	001	110	011	001	001

To determine:

- i) What is the period of the PN sequence?
- ii) The system makes use of a form of FSK. What form of FSK is it?
- iii) What is the number of bits per symbol?
- iv) What is the number of FSK frequencies?
- v) What is the length of a PN sequence per hop?
- vi) Is this a slow or fast FH system?
- vii) What is the total number of possible hops?
- viii) Show the variation of the dehopped frequency with time.

[11 marks]

Use this section for rough work

#### Question 4

a) If the received signal level for a particular digital system is -151dBW and the receiver system effective noise temperature is 1500 K, what is  $E_b/N_0$  for a link transmitting 2400bps?

[2 marks]

b) Using diagrams and engineering terms to compare for same data rate transmission by using single carrier, multi-carrier and OFDM modulations, respectively.

[11 marks]

c) Derive the power spectral density (PSD) equation for the polar NRZ signalling.

[12 marks]

**Rough Working**

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