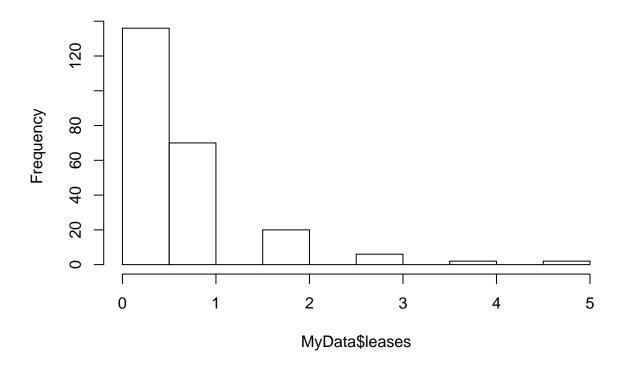
$MoviesDemand-Exp-Feb_18-1.R$

danny 2020-02-18

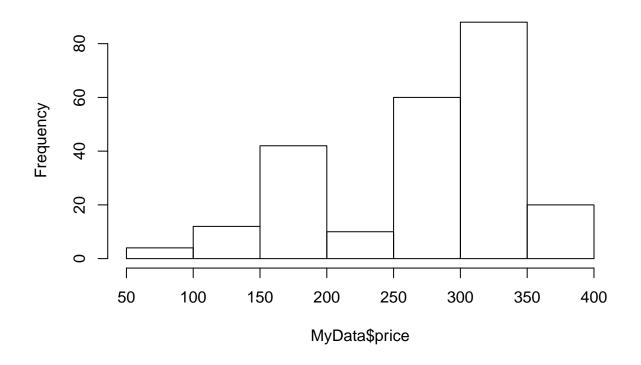
```
suppressWarnings(suppressPackageStartupMessages({
  library(data.table)
  library(stargazer)
 library(ggplot2)
 library(MESS)
}))
#*** MSBA 6440 ***#
#*** Gordon Burtch and Gautam Ray***#
#*** Updated Feb 2020 ***#
#*** Code for Lecture 3 ***#
# Analyzing Movie Rental Pricing Experiment Data
#*** Load Dataset ***#
MyData<- read.csv("MovieData-Exp.csv")</pre>
View(MyData)
# Descriptive statistics / plots...
hist(MyData$leases)
```

Histogram of MyData\$leases



hist(MyData\$price)

Histogram of MyData\$price



```
# Let's make a treatment dummy to keep things simple for now.
# This helps us do some easy randomization checks.
# Let's also construct the discount variable.
MyData$disc <- MyData$base_price - MyData$price</pre>
summary(MyData[MyData$disc>0,]$disc)
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                               Max.
     10.00
                     50.00
##
             30.00
                             52.88
                                     70.00 120.00
MyData$treated <- (MyData$disc > 0)
# Let's check randomization...
t.test(likes~treated,data=MyData)
##
##
   Welch Two Sample t-test
##
## data: likes by treated
## t = 0.060292, df = 233.42, p-value = 0.952
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -465366.0 494747.5
## sample estimates:
## mean in group FALSE mean in group TRUE
```

2328429

2343120

##

```
##
##
   Welch Two Sample t-test
##
## data: base_price by treated
## t = -0.30694, df = 233.79, p-value = 0.7592
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -20.11877 14.69504
## sample estimates:
## mean in group FALSE mean in group TRUE
##
              306.6271
                                  309.3390
# Let's evaluate statistical power now.
# Do we have enough data? Remember, we have 0.5 leases per movie-week on average prior
# to the experiment taking place, for this set of customers.
# Management wants to know about a 20% increase with 90% confidence.
# Thus, we need to detect an increase of 0.10 leases per movie in the week of the experiment.
# That is, 0.50 * 20\% = 0.10. This is our delta parameter.
# 90% confidence implies an alpha of 0.10 (1 - 0.9 = 0.1).
# We assume a power of 80% absent other information.
# The first power test tells us what sort of difference we can reliably detect with our current
# sample size... 118 movies per group.
power_t_test(n=118,type=c("two.sample"),alternative="two.sided",power=0.8,sig.level=0.1,delta=NULL)
##
##
        Two-sample t test power calculation
##
##
                 n = 118
##
             delta = 0.324651
                sd = 1
##
         sig.level = 0.1
##
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
# The second tells how big a sample we would need to detect the 20% change they hope to find.
power_t_test(n=NULL,type=c("two.sample"),alternative="two.sided",power=0.8,sig.level=0.1,delta=0.1)
##
##
        Two-sample t test power calculation
##
##
                 n = 1237.188
##
             delta = 0.1
##
                sd = 1
##
         sig.level = 0.1
##
             power = 0.8
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
```

t.test(base_price~treated,data=MyData)

```
# Note: we appear to be heavily underpowered to detect the effect management is looking for.
# I would thus caution management about reading too much into results from this experiment.
# I might even advise repeating it with the bigger, requisite sample.
# That said, moving on...
# Let's estimate the treatment effect.
#*** OLS of leases on price and log(price) ***#
ols <- lm(leases ~ price, data = MyData)</pre>
olslog <- lm(leases ~ log(price), data = MyData)</pre>
stargazer(ols,olslog,title="OLS leases on prices and log(price)",type="text",column.labels=c("price","l
##
## OLS leases on prices and log(price)
##
                                 Dependent variable:
##
##
                                       leases
                                 price log(price)
                                           (2)
## price
                                 -0.001
                                (0.001)
##
##
## log(price)
                                              -0.255
##
                                              (0.177)
##
                                0.973***
                                             2.043**
## Constant
##
                                (0.229)
                                             (0.994)
## Observations
                                  236
                                              236
## R2
                                             0.009
                                 0.011
## Adjusted R2
                                 0.007
                                             0.005
## Residual Std. Error (df = 234) 0.909 0.910
## F Statistic (df = 1; 234) 2.571 2.062
## Note:
                              *p<0.1; **p<0.05; ***p<0.01
#*** OLS of leases on price and log(price) with additional controls***#
olslogcontrols <- lm(leases ~ log(price) + log(likes), data = MyData)</pre>
stargazer(ols,olslog,olslogcontrols,title="OLS leases on prices, log(price) and controls",type="text",c
##
## OLS leases on prices, log(price) and controls
##
                                     Dependent variable:
##
##
                                           leases
                                    log(price)
(2)
##
                          price
                                                         with controls
                          (1)
```

```
## price
                         -0.001
##
                          (0.001)
##
                                           -0.255
## log(price)
                                                            -0.266
##
                                            (0.177)
                                                             (0.177)
##
## log(likes)
                                                              0.043
##
                                                             (0.031)
##
                        0.973***
                                           2.043**
                                                              1.506
## Constant
##
                         (0.229)
                                          (0.994)
                                                             (1.066)
##
                          236
                                            236
## Observations
                                                               236
## R2 0.011
## Adjusted R2 0.007
                                      0.009
0.005
                                                        0.017
0.008
## Residual Std. Error 0.909 (df = 234) 0.910 (df = 234) 0.909 (df = 233)
## F Statistic 2.571 (df = 1; 234) 2.062 (df = 1; 234) 1.978 (df = 2; 233)
*p<0.1; **p<0.05; ***p<0.01
# Hmmm... something is wrong!
# WAIT!!! We can't just look at price...
# Not all of the variation in price is from our experiment!
# The variation across movies in base-price is endogenous...
# We need to focus just on the price discount treatment itself...
t.test(leases~treated, data=MyData)
##
## Welch Two Sample t-test
##
## data: leases by treated
## t = -1.8645, df = 217.08, p-value = 0.0636
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.45326122 0.01258325
## sample estimates:
## mean in group FALSE mean in group TRUE
##
           0.5084746
                     0.7288136
ols_treat <- lm(leases ~ treated, data = MyData)</pre>
ols_log_discount <- lm(leases ~ log(disc+1), data = MyData)</pre>
# Does a positive coefficient make sense? Yes, discount is amount of money removed from price.
stargazer(ols_treat,ols_log_discount,type="text",column.labels=c("Binary","Log Discount"))
##
##
                                 Dependent variable:
##
##
                                        leases
```

```
##
                                                                                            (1)
                                                                                                                    (2)
                                                                                         0.220*
## treated
##
                                                                                        (0.118)
##
## log(disc + 1)
                                                                                                                           0.055*
##
                                                                                                                           (0.030)
##
                                                                                       0.508***
                                                                                                                        0.512***
## Constant
##
                                                                                        (0.084)
                                                                                                                          (0.083)
## Observations
                                                                                            236
                                                                                                                               236
                                                                                         0.015
                                                                                                                        0.014
## R2
## Adjusted R2
                                                                                         0.010
                                                                                                                           0.010
## Residual Std. Error (df = 234) 0.908
                                                                                                                          0.908
                                                                                    3.476*
## F Statistic (df = 1; 234)
*p<0.1; **p<0.05; ***p<0.01
# What sort of heterogeneity might we look at here? And how?
# Let's check out base price.
ols_moderated_base <- lm(leases ~ treated*base_price, data=MyData)</pre>
ols_log_disc_moderated_base <- lm(leases ~ log(disc+1)*base_price, data=MyData)
stargazer(ols_moderated_base,ols_log_disc_moderated_base, type="text",column.labels=c("Treated Moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_log_disc_moderated_base,ols_
##
      ______
                                                                                                                                 Dependent variable:
##
                                                                                                                                                leases
                                                                                Treated Moderatedy by Base Price Disc Moderated by Base Price
##
                                                                                                            (1)
## -----
## treated
                                                                                                              0.477
##
                                                                                                             (0.552)
## log(disc + 1)
                                                                                                                                                                                        0.071
##
                                                                                                                                                                                      (0.133)
##
## base_price
                                                                                                               -0.001
                                                                                                                                                                                       -0.001
                                                                                                             (0.001)
                                                                                                                                                                                       (0.001)
##
##
                                                                                                               -0.001
## treatedTRUE:base_price
##
                                                                                                             (0.002)
## log(disc + 1):base_price
                                                                                                                                                                                      -0.0001
##
                                                                                                                                                                                       (0.0004)
##
## Constant
                                                                                                              0.695*
                                                                                                                                                                                      0.782**
##
                                                                                                             (0.383)
                                                                                                                                                                                      (0.382)
##
```

Binary

Log Discount

##

```
## Observations
                                        236
                                                                 236
## R.2
                                       0.021
                                                                 0.020
                                       0.009
## Adjusted R2
                                                                 0.007
## Residual Std. Error (df = 232)
                                       0.909
                                                                 0.909
## F Statistic (df = 3; 232)
                                       1.673
                                                                 1.551
## Note:
                                                        *p<0.1; **p<0.05; ***p<0.01
# Why does the treatment effect disappear? Because it's the effect of treatment when
# base price = 0... this never actually occurs in the data!
# Let's shift the base price variable so it is mean 0.
# Then, the coefficient on treatment's main effect reflects treatment on the average movie.
MyData$log_base_price_demean <- log(MyData$base_price)-mean(log(MyData$base_price))
\verb|ols_moderated_dm| <- lm(leases - treated*log_base_price_demean, data=MyData)| \\
ols_log_disc_moderated_dm <- lm(leases ~ log(disc+1)*log_base_price_demean, data=MyData)
stargazer(ols_moderated_dm,ols_log_disc_moderated_dm, type="text",column.labels=c("Base Price Moderator
##
Dependent variable:
                                -----
##
##
                                             leases
##
                                Base Price Moderator De-Meaned
                                         (1)
## treated
                                          0.223*
##
                                         (0.118)
##
## log(disc + 1)
                                                           0.055*
##
                                                          (0.030)
##
                                          -0.141
                                                           -0.227
## log_base_price_demean
##
                                         (0.336)
                                                          (0.335)
                                          -0.289
## treatedTRUE:log_base_price_demean
##
                                         (0.475)
##
## log(disc + 1):log_base_price_demean
                                                           -0.024
                                                          (0.115)
##
##
## Constant
                                         0.508***
                                                          0.513***
##
                                         (0.084)
                                                          (0.083)
## Observations
                                           236
                                                           236
## R2
                                          0.022
                                                           0.020
## Adjusted R2
                                          0.010
                                                           0.008
## Residual Std. Error (df = 232)
                                          0.908
                                                           0.909
## F Statistic (df = 3; 232)
## Note:
                                          *p<0.1; **p<0.05; ***p<0.01
## Log Disc Base Price Moderated De-Meaned
```

```
# Nope, the effect doesn't seem to be moderated by baseline price.
# You can try it with a log transformation and you'll come to the same conclusion.
# What can we conclude?
# Nothing! Don't draw conclusions from null results...
# Try doing the same thing with likes...
MyData$likes_demean <- MyData$likes-mean(MyData$likes)</pre>
ols_moderated_likes_dm <- lm(leases ~ treated*likes_demean, data=MyData)
ols_log_disc_moderated__likes_dm <- lm(leases ~ log(disc+1)*likes_demean, data=MyData)
stargazer(ols_moderated_likes_dm,ols_log_disc_moderated__likes_dm, type="text",column.labels=c("Like Mo
##
                                                     Dependent variable:
##
##
##
                                  Like Moderator De-Meaned Log Price, Like Moderator De-Mean
## treated
                                           0.221*
##
                                          (0.117)
##
                                                                         0.055*
## log(disc + 1)
##
                                                                         (0.030)
## likes_demean
                                         0.00000**
                                                                       0.00000***
                                                                        (0.00000)
##
                                         (0.00000)
                                         -0.00000*
## treatedTRUE:likes_demean
                                         (0.00000)
##
##
## log(disc + 1):likes_demean
                                                                        -0.00000*
                                                                        (0.00000)
##
##
                                          0.508***
                                                                        0.512***
## Constant
##
                                          (0.083)
                                                                         (0.082)
## Observations
                                            236
                                                                           236
## R2
                                           0.042
                                                                          0.043
## Adjusted R2
                                           0.029
                                                                          0.030
```

```
# We do find that popular movies respond less strongly to the discount treatment.
# This makes some sense... if a movie is really good, "I don't care what it costs!"
# The strength of the moderation is pretty weak, however, in practical terms...
# We are going out to many significant digits... you can try the log transform here,
# But a better option might also be to just rescale the variable (e.g., 1,000's of likes)
```

0.899

3.356**

0.899

3.442**

*p<0.1; **p<0.05; ***p<0.01

Residual Std. Error (df = 232)

Note:

F Statistic (df = 3; 232)

```
MyData$likes_demean <- MyData$likes/1000000-mean(MyData$likes/1000000)
ols_moderated_likes_dm <- lm(leases ~ treated*likes_demean, data=MyData)
ols_log_disc_moderated__likes_dm <- lm(leases ~ log(disc+1)*likes_demean, data=MyData)
stargazer(ols_moderated_likes_dm,ols_log_disc_moderated__likes_dm, type="text",column.labels=c("Like Moderated_likes_dm,ols_log_disc_moderated_likes_dm, type="text",column.labels=c("Like Moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_disc_moderated_likes_dm,ols_log_d
```

	Dependent variable:	
	(1)	leases Log Disc, Like Moderator De-Mean (2)
treated	0.221*	
	(0.117)	
7 (1)		0.055
log(disc + 1)		0.055* (0.030)
		(0.030)
likes_demean	0.111**	0.112***
_	(0.043)	(0.043)
treatedTRUE:likes_demean	-0.106*	
	(0.063)	
log(disc + 1):likes_demean		-0.028*
108 (ulbo / 1) llinob_uomoun		(0.016)
Constant	0.508***	0.512***
	(0.083)	(0.082)
Observations	236	236
R2	0.042	0.043
Adjusted R2	0.029	0.030
Residual Std. Error (df = 232)		0.899
F Statistic (df = 3; 232)	3.356**	3.442**