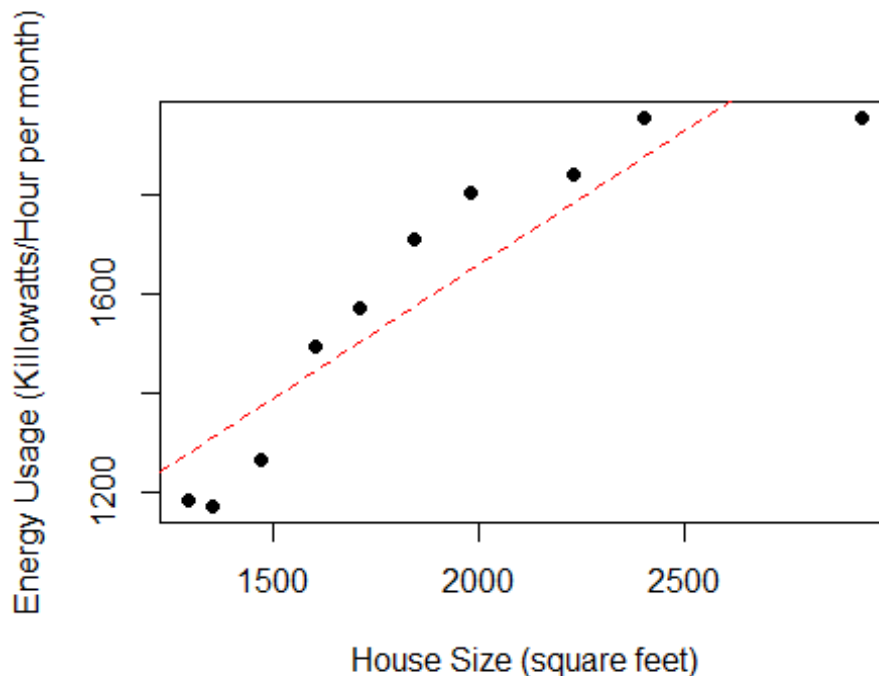


Regression_3_Extensions.R

Curvilinear Section

```
# A real estate agency collects data concerning energy usage (kilowatt/hour per month) and house sizes (square feet).  
#install readxl package first  
library(readxl)  
energy <- read_excel("energy.xlsx", na="NA", col_names = TRUE)  
attach(energy)
```

```
# scatter plot  
plot(Size, Usage, pch = 16, xlab = "House Size (square feet)", ylab = "Energy Usage (Kilowatts/Hour per month)")  
abline(lm(Usage ~ Size), lty=2, col="red")
```



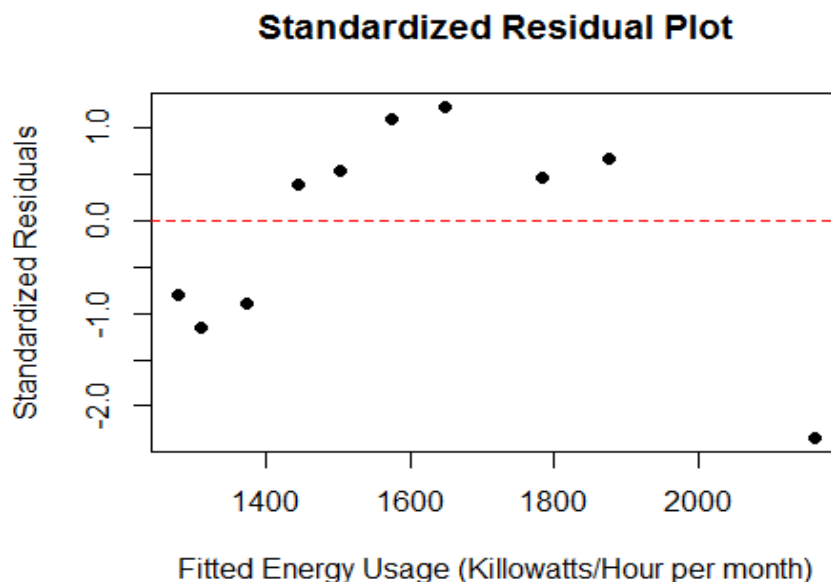
```

# fit the linear model
linefit <- lm(Usage ~ Size)
summary(linefit)

##
## Call:
## lm(formula = Usage ~ Size)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -208.02 -105.36   52.89   77.29  155.27
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  578.92775   166.96806    3.467  0.008476 **
## Size          0.54030    0.08593    6.288  0.000236 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 133.4 on 8 degrees of freedom
## Multiple R-squared:  0.8317, Adjusted R-squared:  0.8107
## F-statistic: 39.54 on 1 and 8 DF,  p-value: 0.0002359

# standardized residual plot - on fitted values
linefit.stres <- rstandard(linefit)
plot(linefit$fitted.values, linefit.stres, pch = 16, main = "Standardized Residual Plot", xlab = "Fitted Energy Usage (Kilowatts/Hour per month)", ylab = "Standardized Residuals")
abline(0,0, lty=2, col="red")

```



```

# fit the quadratic model
energy$SizeSqd <- Size^2
attach(energy)

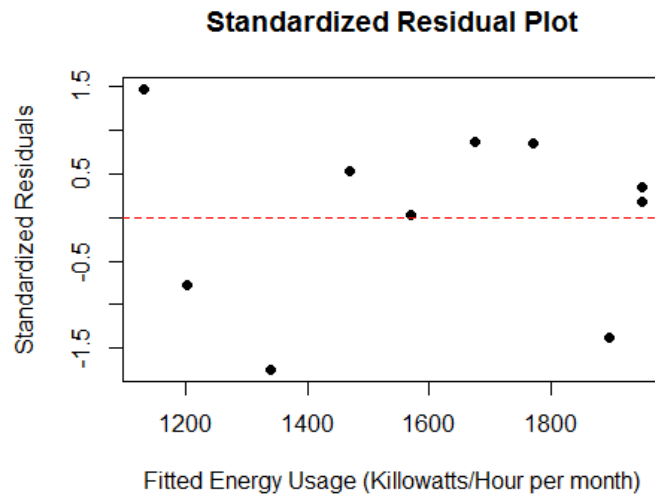
## The following objects are masked from energy (pos = 3):
##
##      Size, Usage

linefitQ <- lm(Usage ~ Size + SizeSqd)
summary(linefitQ)

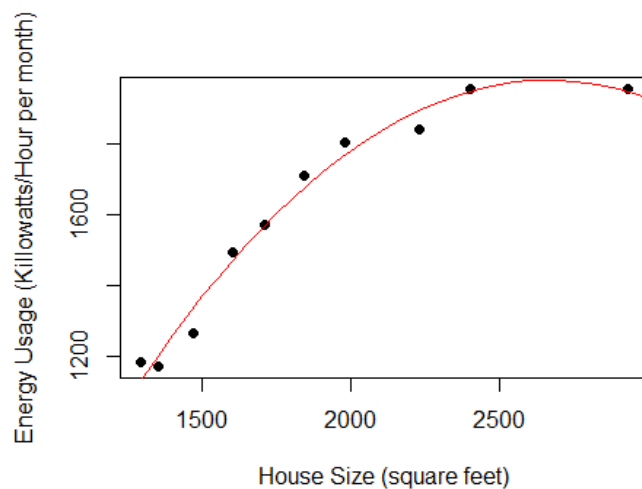
##
## Call:
## lm(formula = Usage ~ Size + SizeSqd)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -73.792 -22.426   5.886  31.689  52.436
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.216e+03  2.428e+02  -5.009 0.001550 **
## Size         2.399e+00  2.458e-01   9.758 2.51e-05 ***
## SizeSqd      -4.500e-04  5.908e-05  -7.618 0.000124 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 46.8 on 7 degrees of freedom
## Multiple R-squared:  0.9819, Adjusted R-squared:  0.9767
## F-statistic: 189.7 on 2 and 7 DF,  p-value: 8.001e-07

```

```
# standardized residual plot - on fitted values
linefitQ.stres <- rstandard(linefitQ)
plot(linefitQ$fitted.values, linefitQ.stres, pch = 16, main = "Standardized Residual Plot", xlab = "Fitted Energy Usage (Kilowatts/Hour per month)", ylab = "Standardized Residuals")
abline(0,0, lty=2, col="red")
```



```
# scatter plot with fitted quadratic model curve
XvaluesQ <- seq(1000, 3000, 50)
YpredictedQ <- linefitQ$coefficients[3]*XvaluesQ^2 + linefitQ$coefficients[2]*XvaluesQ + linefitQ$coefficients[1]
plot(Size, Usage, pch = 16, xlab = "House Size (square feet)", ylab = "Energy Usage (Kilowatts/Hour per month)")
lines(XvaluesQ, YpredictedQ, type = "l", col = "red")
```



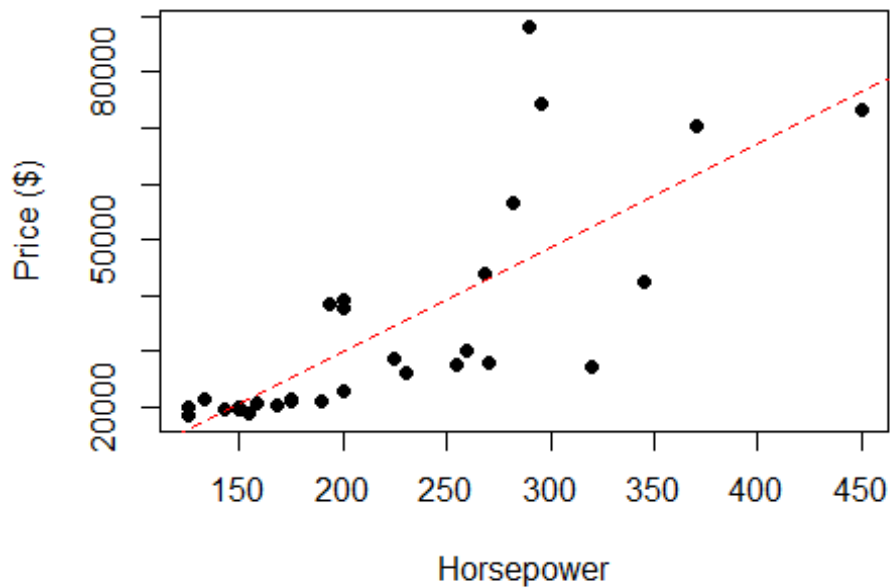
```
detach(energy)
```

Categorical Section

```
# A company is interested in the relationship between sales price ($) and horsepower and type of car
#install readxl package first
library(readxl)
cars <- read_excel("cars.xlsx", na="NA", col_names = TRUE)

# convert Type to a factor variable TypeF, i.e., nominal
cars$TypeF<-factor(cars$Type)
attach(cars)

# scatter plot with Horsepower
plot(Horsepower, Price, pch = 16, xlab = "Horsepower", ylab = "Price ($)")
abline(lm(Price ~ Horsepower), lty=2, col="red")
```



```

# fit the simple linear regression model
linefitH <- lm(Price ~ Horsepower)
summary(linefitH)

##
## Call:
## lm(formula = Price ~ Horsepower)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -24972  -6649  -1218    3845   41584
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -7203.81    6923.91  -1.040    0.307
## Horsepower   185.36     29.42    6.301 8.18e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12730 on 28 degrees of freedom
## Multiple R-squared:  0.5864, Adjusted R-squared:  0.5716
## F-statistic: 39.7 on 1 and 28 DF, p-value: 8.182e-07

```

```

# fit the ANOVA
fitT <- aov(Price ~ TypeF)
summary(fitT)
##              Df      Sum Sq   Mean Sq F value    Pr(>F)
## TypeF          4  8.160e+09  2.040e+09   18.19 4.07e-07 ***
## Residuals     25  2.803e+09  1.121e+08
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

print(model.tables(fitT, "means"))

## Tables of means
## Grand mean
## 33891.6
## TypeF
##          1      2      3      4      5
##      20162 37554 20790 27981 61663
## rep      9      5      5      4      7

# to check all the pairwise contrasts
TukeyHSD(fitT, conf.level = .90)

## Tukey multiple comparisons of means
## 90% family-wise confidence level
## Fit: aov(formula = Price ~ TypeF)
## $TypeF
##          diff          lwr          upr      p adj
## 2-1  17392.5111    2010.283 32774.7394 0.0491675
## 3-1   628.3111  -14753.917 16010.5394 0.9999689
## 4-1   7819.3611  -8752.906 24391.6280 0.7350784
## 5-1  41501.3968   27603.432 55399.3617 0.0000004
## 3-2 -16764.2000  -34206.007   677.6074 0.1219798
## 4-2  -9573.1500  -28072.980   8926.6805 0.6651140
## 5-2  24108.8857   7960.910 40256.8616 0.0054346
## 4-3   7191.0500  -11308.780 25690.8805 0.8472906
## 5-3  40873.0857   24725.110 57021.0616 0.0000062
## 5-4  33682.0357   16396.660 50967.4112 0.0002746

# SSTreatment
anova(fitT)[["Sum Sq"]][1]
## [1] 8160453274
# SSEerror
anova(fitT)[["Sum Sq"]][2]
## [1] 2803444345
# R^2
(anova(fitT)[["Sum Sq"]][1])/((anova(fitT)[["Sum Sq"]][1])+(anova(fitT)[["Sum
Sq"]][2]))
## [1] 0.7443022
# sqrt(MSE)
sqrt(anova(fitT)[["Sum Sq"]][2]/fitT$df.residual)
## [1] 10589.51

```

```
# collinearity check between 2 predictors
fitM <- aov(Horsepower ~ TypeF)
summary(fitM)

##              Df Sum Sq Mean Sq F value    Pr(>F)
## TypeF          4 155613   38903   30.88 2.42e-09 ***
## Residuals     25  31499    1260
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# R^2
(anova(fitM)[["Sum Sq"]][1])/((anova(fitM)[["Sum Sq"]][1])+(anova(fitM)[["Sum
Sq"]][2]))

## [1] 0.8316561
```

```
# fit the first-order multiple regression model (TypeF=1 as base category)
linefitHT <- lm(Price ~ Horsepower + TypeF)
summary(linefitHT)

## Call:
## lm(formula = Price ~ Horsepower + TypeF)
## Residuals:
##      Min       1Q   Median       3Q      Max
## -34013   -605     -15    1740   27929
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 15406.19    9801.66   1.572  0.12909
## Horsepower    31.56      60.55   0.521  0.60697
## TypeF2       15292.43    7222.61   2.117  0.04479 *
## TypeF3         74.88    6087.81   0.012  0.99029
## TypeF4        4565.60    8981.86   0.508  0.61587
## TypeF5       35646.96   12469.10   2.859  0.00866 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10750 on 24 degrees of freedom
## Multiple R-squared:  0.7472, Adjusted R-squared:  0.6945
## F-statistic: 14.18 on 5 and 24 DF, p-value: 1.662e-06
```



```

# fit the first-order model (TypeF=2 as base category)
# reorder the data frame with TypeF = 2 as reference
cars <- within(cars, TypeF <- relevel(TypeF, ref = 2))
linefitHTalt <- lm(cars$Price ~ cars$Horsepower + cars$TypeF)
summary(linefitHTalt)
## Call:
## lm(formula = cars$Price ~ cars$Horsepower + cars$TypeF)
## Residuals:
##      Min       1Q   Median       3Q      Max
## -34013   -605     -15    1740   27929
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    30698.62   14003.10   2.192   0.0383 *
## cars$Horsepower     31.56     60.55   0.521   0.6070
## cars$TypeF1    -15292.43    7222.61  -2.117   0.0448 *
## cars$TypeF3    -15217.55    7416.54  -2.052   0.0512 .
## cars$TypeF4    -10726.83    7541.53  -1.422   0.1678
## cars$TypeF5     20354.53    9564.37   2.128   0.0438 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10750 on 24 degrees of freedom
## Multiple R-squared:  0.7472, Adjusted R-squared:  0.6945
## F-statistic: 14.18 on 5 and 24 DF,  p-value: 1.662e-06

# return dataframe to original order with TypeF = 1 as reference
cars <- within(cars, TypeF <- relevel(TypeF, ref = 2))

```

```

# fit the first-order model (TypeF=3 as base category)
# reorder the data frame with TypeF = 3 as reference
cars <- within(cars, TypeF <- relevel(TypeF, ref = 3))
linefitHTalt <- lm(cars$Price ~ cars$Horsepower + cars$TypeF)
summary(linefitHTalt)

##
## Call:
## lm(formula = cars$Price ~ cars$Horsepower + cars$TypeF)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -34013   -605    -15    1740   27929
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   15481.07   11262.33   1.375   0.18196
## cars$Horsepower    31.56     60.55   0.521   0.60697
## cars$TypeF1     -74.88    6087.81  -0.012   0.99029
## cars$TypeF2    15217.55    7416.54   2.052   0.05125 .
## cars$TypeF4     4490.72    8877.67   0.506   0.61758
## cars$TypeF5    35572.07   11959.24   2.974   0.00659 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10750 on 24 degrees of freedom
## Multiple R-squared:  0.7472, Adjusted R-squared:  0.6945
## F-statistic: 14.18 on 5 and 24 DF,  p-value: 1.662e-06

# return dataframe to original order with TypeF = 1 as reference
# for switch to Type = k as reference, run the re-sort (k-1) times to undo
# You can check the order of the values for TypeF under the Cars dataframe
in the Environment window at right to see what is happening
cars <- within(cars, TypeF <- relevel(TypeF, ref = 3))
cars <- within(cars, TypeF <- relevel(TypeF, ref = 3))

# This process can be repeated for using the other types as the base

```

```

# fit the second-order multiple regression model with interaction term (TypeF
# =1 as base category)
linefitHT2 <- lm(Price ~ Horsepower * TypeF)
summary(linefitHT2)

##
## Call:
## lm(formula = Price ~ Horsepower * TypeF)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -34112   -589    -16    1845   27644
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    14297.93    27059.84   0.528   0.603
## Horsepower         38.92     177.70   0.219   0.829
## TypeF2         12524.07    49700.81   0.252   0.804
## TypeF3         1049.22    61294.99   0.017   0.987
## TypeF4        -2814.08   105012.83  -0.027   0.979
## TypeF5         38832.25    38634.75   1.005   0.327
## Horsepower:TypeF2     10.49     260.44   0.040   0.968
## Horsepower:TypeF3     -6.56     370.83  -0.018   0.986
## Horsepower:TypeF4     26.09     436.96   0.060   0.953
## Horsepower:TypeF5    -13.54     195.28  -0.069   0.945
##
## Residual standard error: 11770 on 20 degrees of freedom
## Multiple R-squared:  0.7475, Adjusted R-squared:  0.6338
## F-statistic: 6.577 on 9 and 20 DF,  p-value: 0.0002325

```

```

# fit the second-order model with interaction term (TypeF=5 as base category)
# reorder the data frame with TypeF = 5 as reference
cars <- within(cars, TypeF <- relevel(TypeF, ref = 5))
linefitHTalt <- lm(cars$Price ~ cars$Horsepower * cars$TypeF)
summary(linefitHTalt)

##
## Call:
## lm(formula = cars$Price ~ cars$Horsepower * cars$TypeF)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -34112   -589    -16    1845   27644
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      53130.176   27575.515    1.927  0.0683 .
## cars$Horsepower       25.385     80.961    0.314  0.7571
## cars$TypeF1      -38832.247  38634.751   -1.005  0.3268
## cars$TypeF2      -26308.179  49983.438   -0.526  0.6044
## cars$TypeF3      -37783.025  61524.387   -0.614  0.5461
## cars$TypeF4      -41646.327 105146.893   -0.396  0.6962
## cars$Horsepower:cars$TypeF1      13.535    195.278    0.069  0.9454
## cars$Horsepower:cars$TypeF2      24.027    206.899    0.116  0.9087
## cars$Horsepower:cars$TypeF3       6.975    335.401    0.021  0.9836
## cars$Horsepower:cars$TypeF4      39.629    407.323    0.097  0.9235
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11770 on 20 degrees of freedom
## Multiple R-squared:  0.7475, Adjusted R-squared:  0.6338
## F-statistic: 6.577 on 9 and 20 DF,  p-value: 0.0002325

# return dataframe to original order with TypeF = 1 as reference
cars <- within(cars, TypeF <- relevel(TypeF, ref = 5))
cars <- within(cars, TypeF <- relevel(TypeF, ref = 5))
cars <- within(cars, TypeF <- relevel(TypeF, ref = 5))
cars <- within(cars, TypeF <- relevel(TypeF, ref = 5))

# clean up
detach(cars)

```