Cryptography: Introduction

Myrto Arapinis School of Informatics University of Edinburgh

What is cryptography?

"The practice of creating and understanding codes that keep information secret."

Cambridge dictionary

What is cryptography?

"The practice of creating and understanding codes that keep information secret."

Cambridge dictionary

But nowadays cryptography encompasses many more things than just secret communications.

"Cryptography is the scientific study of techniques for securing [against internal or external attacks] digital information, transactions, and distributed computations."

Jonathan Katz and Yehuda Lindell in Introduction to Modern Cryptography

Cryptography is everywhere!

Cryptographic methods are powerful tools at the core of many security mechanisms used:

- to securely and confidentially access a website such as an online banking website;
- to attest the identity of the organization operating a web server;
- when talking over a mobile phone;
- to enforce access control in a multi-user operating system;
- to prevent thieves extracting trade secrets from stolen laptops;
- to prevent software copying;
- etc

Cryptography (and security more broadly) is becoming a more and more central topic within computer science

Important remark

Cryptography is not:

- ► The solution to all security problems (see other sections of the course)
- ► Secure if not implemented and/or deployed correctly
- ▶ Something you will be able to invent at the end of this course

Learning objectives for the Cryptography section

- ► Appreciate the variety of applications that use cryptography with different purposes
- ▶ Introduce the basic concepts of cryptography
- ▶ Understand the type of problems cryptography can address
- Understand the types of problems that need to be addressed when using cryptography

Topics in the Cryptography section

We will discuss constructions for:

- Symmetric Encryption
- Asymmetric (public-key) Encryption
- ► Hash functions and Message Authentication Codes (MACs)
- Digital Signatures
- ► Public Key Infrastructure (PKI)

We present only the rudiments of the topic:

- What cryptography can achieve
- ► That cryptography can go wrong
- What is good practice when using cryptography

Cryptography: Symmetric encryption

Goal: confidentiality

Secure communications



► File protection

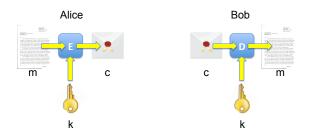


Symmetric encryption schemes

A symmetric cipher consists of two algorithms

- encryption algorithm $E: \mathcal{K} \times \mathcal{M} \to \mathcal{C}$
- ightharpoonup decryption algorithm $D: \mathcal{K} \times \mathcal{C} \to \mathcal{M}$

st. $\forall k \in \mathcal{K}$, and $\forall m \in \mathcal{M}$, D(k, E(k, m)) = m



- same key k to encrypt and decrypt
- ▶ the key *k* is secret: only known to Alice and Bob

What is a good encryption scheme?

An encryption scheme is secure against a given adversary, if this adversary cannot

- recover the secret key *k*
- recover the plaintext m underlying a ciphertext c
- recover any bits of the plaintext *m* underlying a ciphertext *c*

Kerckhoff's principle

The architecture and design of a security system/mechanism should be made public

No security through obscurity!

- ▶ The encryption (E) and decryption (D) algorithms are public
- ► The security relies entirely on the secrecy of the key

Open design allows for a system to be scrutinised by many users, white hat hackers, academics, etc.

→ early discovery and corrections of flaws/vulnerabilities

Adversary's capabilities

- A cryptographic scheme is secure under some assumptions, that is against a certain type of attacker
- A cryptographic scheme may be vulnerable to certain types of attacks but not others

Adversary's capabilities

- A cryptographic scheme is secure under some assumptions, that is against a certain type of attacker
- A cryptographic scheme may be vulnerable to certain types of attacks but not others

The attacker know the encryption/decryption algorithms but may have access to :

- ightharpoonup Ciphertext only attack some ciphertexts c_1, \ldots, c_n
- Nown plaintext attack some plaintext/ciphertext pairs (m_1, c_1) , ..., (m_n, c_n) st. $c_i = E(k, m_i)$
- ▶ Chosen plaintext attack he has access to an encryption oracle can maybe trick a user to encrypt messages m_1, \ldots, m_n of his choice
- ▶ Chosen ciphertext attack he has access to a decryption oracle can maybe trick a user to decrypt ciphertexts c_1, \ldots, c_n of his choice
- ightharpoonup unlimited, or polynomial, or realistic ($\leq 2^{80}$) computational power

Brute-force attack - attack on all schemes

▶ Try all possible keys $k \in \mathcal{K}$ - requires some knowledge about the structure of plaintext



- Making exhaustive search unfeasible:
 - $ightharpoonup \mathcal{K}$ should be sufficiently large, *i.e.* keys should be sufficiently long
 - lacktriangleright Keys should be sampled uniformly at random from ${\cal K}$

A simple scheme: the substitution cipher

> shared secret: a permutation π of the set of characters

$$\pi = a \mapsto q \ b \mapsto w \ c \mapsto e \ d \mapsto r \ e \mapsto t \ f \mapsto y \ g \mapsto u \ h \mapsto i \ i \mapsto o$$

$$j \mapsto m \ k \mapsto a \ l \mapsto s \ m \mapsto d \ n \mapsto f \ o \mapsto g \ p \mapsto h \ q \mapsto j \ r \mapsto k$$

$$s \mapsto l \ t \mapsto z \ u \mapsto x \ v \mapsto c \ w \mapsto v \ x \mapsto b \ y \mapsto n \ z \mapsto p$$

Encryption: apply π to each character of the plaintext

$$E(\pi, p_1 \dots p_n) = \pi(p_1) \dots \pi(p_n)$$

ightharpoonup Decryption: apply π^{-1} to each character of the plaintext

$$D(\pi, c_1 \dots c_n) = \pi^{-1}(c_1) \dots \pi^{-1}(c_n)$$

Substitution cipher: example

- $\pi = a \mapsto q \ b \mapsto w \ c \mapsto e \ d \mapsto r \ e \mapsto t \ f \mapsto y \ g \mapsto u \ h \mapsto i \ i \mapsto o \ j \mapsto m \ k \mapsto a \ l \mapsto s$ $m \mapsto d \ n \mapsto f \ o \mapsto g \ p \mapsto h \ q \mapsto j \ r \mapsto k \ s \mapsto l \ t \mapsto z \ u \mapsto x \ v \mapsto c \ w \mapsto v \ x \mapsto b$ $y \mapsto n \ z \mapsto p$
- m = THIS COURSE AIMS TO INTRODUCE YOU TO THE PRINCIPLES AND TECHNIQUES OF SECURING COMPUTERS AND COMPUTER NETWORKS WITH FOCUS ON INTERNET SECURITY. THE COURSE IS EFFECTIVELY SPLIT INTO TWO PARTS. FIRST INTRODUCING THE THEORY OF CRYPTOGRAPHY INCLUDING HOW MANY CLASSICAL AND POPULAR ALGORITHMS WORK E.G. DES, RSA, DIGITAL SIGNATURES, AND SECOND PROVIDING DETAILS OF REAL INTERNET SECURITY PROTOCOLS, ALGORITHMS, AND THREATS, E.G. IPSEC, VIRUSES, FIREWALLS. HENCE, YOU WILL LEARN BOTH THEORETICAL ASPECTS OF COMPUTER AND NETWORK SECURITY AS WELL AS HOW THAT THEORY IS APPLIED IN THE INTERNET. THIS KNOWLEDGE WILL HELP YOU IN DESIGNING AND DEVELOPING SECURE APPLICATIONS AND NETWORK PROTOCOLS AS WELL AS BUILDING SECURE NETWORKS.
- C = ZIOL EGXKLT QODL ZG OFZKGRXET NGX ZG ZIT HKOFEOHSTL QFR
 ZTEIFOJXTL GY LTEXKOFU EGDHXZTKL QFR EGDHXZTK FTZVGKAL VOZI
 YGEXL GF OFZTKFTZ LTEXKOZN. ZIT EGXKLT OL TYYTEZOCTSN LHSOZ
 OFZG ZVG HQKZL. YOKLZ OFZKGRXEOFU ZIT ZITGKN GY EKNHZGUKQHIN
 OFESXROFU IGV DQFN ESQLLOEQS QFR HGHXSQK QSUGKOZIDL VGKA T.U.
 RTL, KLQ, ROUOZQS LOUFQZXKTL, QFR LTEGFR HKGCOROFU RTZQOSL GY
 KTQS OFZTKFTZ LTEXKOZN HKGZGEGSL, QSUGKOZIDL, QFR ZIKTQZL, T.U.
 OHLTE, COKXLTL, YOKTVQSSL. ITFET, NGX VOSS STQKF WGZI ZITGKTZOEQS
 QLHTEZL GY EGDHXZTK QFR FTZVGKA LTEXKOZN QL VTSS QL IGV ZIQZ
 ZITGKN OL QHHSOTR OF ZIT OFZTKFTZ. ZIOL AFGVSTRUT VOSS ITSH NGX OF
 RTLOUFOFU QFR RTCTSGHOFU LTEXKT QHHSOEQZOGFL QFR FTZVGKA
 HKGZGEGSL QL VTSS QL WXOSROFU LTEXKT FTZVGKAL.

Quiz

Breaking the substitution cipher

Breaking the substitution cipher

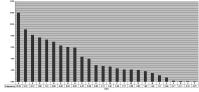
• Key space size: $|\mathcal{K}| = 26! \ (\approx 2^{88})$

⇒ brute force infeasible!

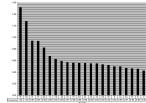
Breaking the substitution cipher

• Key space size: $|\mathcal{K}| = 26! \ (\approx 2^{88})$

- \Rightarrow brute force infeasible!
- Frequency analysis: exploit regularities of the language
 - Use frequency of letters in English text



Use frequency of digrams in English text



- ► Use frequency of trigrams in English text the > and > ing
- Use expected words

 $\pi =$

C = ZIOL EGXKLT QODL ZG OFZKGRXET NGX ZG ZIT HKOFEOHSTL QFR ZTEJFOJXTL GY
LTEXKOFU EGDHXZTKL QFR EGDHXZTK FTZVGKAL VOZI YGEXL GF OFZTKFTZ
LTEXKOZN. ZIT EGXKLT OL TYYTEZOCTSN LHSOZ OFZG ZVG HQKZL. YOKLZ
OFZKGRXEOFU ZIT ZITGKN GY EKNHZGUKQHIN OFESXROFU IGV DQFN ESQLLOEQS
QFR HGHXSQK QSUGKOZIOL VGKA T.U. RTL., KLQ, ROUOZQS LOUFQZXKTL, QFR
LTEGFR HKGCOROFU RTZQOSL GY KTQS OFZTKFTZ LTEXKOZN HKGZGEGSL,
QSUGKOZIDL, QFR ZIKTQZL, T.U. OHLTE, COKXLTL, YOKTVQSSL. ITFET, NGX
VOSS STQKF WGZI ZITGKTZOEQS QLHTEZL GY EGDHXZTK QFR FTZVGKA
LTEXKOZN QL VTSS QL IGV ZIQZ ZITGKN OL QHHSOTR OF ZIT OFZTKFTZ. ZIOL
AFGVSTRUT VOSS ITSH NGX OF RTLOUFOFU QFR RTCTSGHOFU LTEXKT
QHHSOEQZOGFL QFR FTZVGKA HKGZGEGSL QL VTSS QL WXOSROFU LTEXKT
FTZVGKAL.

C = ZIOL EGXKLT QODL ZG OFZKGRXET NGX ZG ZIT HKOFEOHSTL QFR ZTEIFOJXTL GY LTEXKOFU EGDHXZTKL QFR EGDHXZTK FTZVGKAL VOZI YGEXL GF OFZTKFTZ LTEXKOZN. ZIT EGXKLT OL TYYTEZOCTSN LHSOZ OFZG ZVG HQKZL. YOKLZ OFZKGRXEOFU ZIT ZITCKN GY EKNHZGUKQHIN OFESXROFU IGV DQFN ESQLLOEQS QFR HGXSQK QSIOL VGKA T.U. RTI. KLQ, ROUOZQS LOUPGZXKTL, QFR LTEGFR HKGCOROFU RTZQOSL GY KTQS OFZTKFTZ LTEXKOZN HKGZGEGSL, QSUGKOZIDL YGR ZIKTQZL, T.U. OHLTE, COKXLTL, YOKTYQSSL. ITFET, NGX VOSS STQKF WGZI ZITGKTZOEQS QLHTEZL GY EGDHXTTK QFR FTZVGKA LTEXKOZN QL VTSS QL IGV ZIQZ ZITGKN OL QHHSOTR OF ZIT OFZTKFTZ. ZIOL AFGVSTRUT YOSS ITSH NGX OF RTLOUFOPU OFR RTCTSGHOFU LTEXKT

QHHSOEQZOGFL QFR FTZVGKA HKGZGEGSL QL VTSS QL WXOSROFU LTEXKT

Most common letters in c: t > z > o > 1

 $\pi =$

FT7VGKAI

- $\pi = t \mapsto z e \mapsto t$
- C = TIOL EGXKLE QODL TG OFTKGRXEE NGX TG TIE HKOFEOHSEL QFR TEEIFOJXEL GY LEEXKOFU EGDHXTEKL QFR EGDHXTEK FETVGKAL VOTI YGEXL, GF OFTEKFET LEEXKOTN. TIE EGXKLE OL EYYEETOCESN LHSOT OFTG TVG HQKTL. YOKLT OFTKGRXEOFU TIE TIEGKN GY EKNHTGUKGHIN OFESXROFU IGV DQFN ESQLLOEQS QFR HGHXSQK QSUGKOTIDL VGKA E.U. REL, KLQ, ROUOTQS LOUFQTXKEL, QFR LEEGFR HKGCOROFU RETQOSL GY KEQS OFTEKFET LEEXKOTN HKGTGEGSL, QSUGKOTIDL, QFR TIKEQTI, E.U. OHLEE, COKXLEL, YOKEVQSSL. IEFEE, NGX VOSS SEQKF WGTI TIEGKETOEQS QLHEETL GY EGDHXTEK QFR FETVGKA LEEXKOTN QL VESS QL IGV TIQT TIEGKN OL QHHSOER OF TIE OFTEKFET. TIOL AFGYSERUE VOSS IESH NGX OF RELOUFOFU QFR RECESGHOFU LEEXKE QHHSOEQTOGFL QFR FETVGKA HKGTGEGSL QL VESS QL WXOSROFU LEEXKE FETVGKAL.

Most common letters in c: $t > z > \dots$

$\pi = t \mapsto z e \mapsto t$

C = TIOL EGXKLE QODL TG OFTKGRXEE NGX TG TIE HKOFEOHSEL QFR TEEIFOJXEL GY LEEXKOFU EGDHXTEKL OFR EGDHXTEK FETVGKAL VOTI YGEXL GF OFTEKFET LEEXKOTN. TIE EGXKLE OL EYYEETOCESN LHSOT OFTG TVG HQKTL. YOKLT OFTKGRXEOFU TIE TIEGKN GY EKNHTGUKQHIN OFESXROFU IGV DQFN ESQLLOEQS QFR HCHXSQK QSUGKOTIDL VGKA EU. REL, KLQ, ROUOTQS LOUFQTXKEL, GFR LEEGFR HKGCOROFU RETQOSL GY KEQS OFTEKFET LEEXKOTN HKGTGEGSL. QSUGKOTIDL, OFF TIKEOTL, EU. OHLEE, COKXLEL, YOKEVGSSL. IEFEE, NCX VOSS SEQKF WGTI TIEGKETOEQS QLHEETL GY EGDHXTEK QFR FETVGKA LEEXKOTN QL VESS QL IGV TIQT TIEGKN OL QHHSOER OF TIE OFTEKFET. TIOL AFGVSERUE VOSS IESH NGX OF RELOUDFOFU QFR RECESGHOFU LEEXKE QHHSOEQTOGFL QFR FETVGKA HKGTGEGSL QL VESS QL WXOSROFU LEEXKE FETVGKAL.

Most common digrams in c: of > zi > ...

$\pi = t \mapsto z e \mapsto t$

C = TIOL EGXKLE QODL TG OFTKGRXEE NGX TG TIE HKOFEOHSEL QFR TEEIFOJXEL GY LEEXKOFU EGDHXTEKL QFR EEGDHXTEK FETVCKAL VOTI YGEXL GF OFTEKFET LEEXKOTN. TIE EGXKLE OL EYYEETOCESN LHSOT OFTG TVG HQKTL. YOKLT OFTKGRXEOFU TIE TIEGKN GY EKNHTGUKQHIN OFESXROFU IGV DQFN ESQLLOEQS QFR HGHXSQK QSUGKOTIDL VGKA E.U. REL, KLQ, ROUOTQS LOUFQTXKEL, QFR LEEGFR HKGCOROFU RETQOSL GY KEQS OFTEKFET LEEXKOTN HKGTGEGSL, QSUGKOTIDL, OFR TIKEQTL, E.U. OHLEE, COKXLEL, YOKEVQSSL. IEFEE, NGX VOSS SEQKF WGTI TIEGKETOEQS QLHEETL GY EGDHXTEK QFR FETVGKA LEEXKOTN QL VESS QL IGV TIQT TIEGKN OL QHHSOER OF TIE OFTEKFET. TIOL AFGVSERUE VOSS IESH NGX OF RELOUFOFU QFR RECESSCHOFU LEEXKE QHHSOEQTOGFL QFR FETVGKA HKGTGEGSL QL VESS QL WXOSROFU LEEXKE FETVGKAL.

Most common digrams in c: of > zi > . . . $t{\mapsto}z$ suggests $h{\mapsto}i$

$\pi = t \mapsto z e \mapsto t h \mapsto i$

C = THOL EGXKLE QODL TG OFTKGRXEE NGX TG THE HKOFEOHSEL QPR TEEHFOJXEL GY LEEXKOFU EGDHXTEK EGDHXTEK FETVGKAL VOTH YGEXL GF OFTEKFET LEEXKOTN. THE EGXKLE OL EYYEETOCESN LHSOT OFTG TVG HQKTL. YOKLT OFTKGRXEOFU THE THEGKIN GY EKNHTGUKQHHIN OFESXROFU HGV DAPN ESQLLOEQS QPR HGMXSQK QSUGKOTHDL VGKA EU. REL, KLQ, ROUOTQS LOUPQTXKEL, QPR LEEGFR HKGCOROFU RETQOSL GY KEQS OFTEKFET LEEXKOTN HKGTGEGSL, QSUGKOTHDL, QFR THKEQTI, EU. OHLEE, COKXLEL, YOKEVQSSL. HEFEE, NGX VOSS SEQKF WGTH THEGKETOEQS QLHEETL GY EGDHXTEK QPR FETVGKA LEEXKOTN QL VESS QL HGV THQT THEGKN OL QHHSOER OF THE OFTEKFET. THOL AFGVSERUE VOSS HESH NGX OF RELOUPOFU QFR RECESGHOFU LEEXKE QHHSOEQTOGFL QPR FETVGKA HKGTGEGSL QL VESS QL WXOSROFU LEEXKE FETVGKAL.

Most common digrams in c: of > zi > ...

$\pi = t \mapsto z e \mapsto t h \mapsto i$

C = THOL EGKKLE QODL TG OFTKGRXEE NGX TG THE HKOFEOHSEL QPR TEEHFOJKEL GY LEEXKOFU EGDHATTEKL QPR EGDHATKER FETVGKAL VOTH YGEXL GF OFTEKFET LEEXKOTN. THE EGXKLE OL EYYEETOCESN LHSOT OFTG TVG HQKTL. YOKLT OFTKGRXEOFU THE THEGKN GY EKNHTGUKQHHN OFESXROFU HGV DAPN ESQLLOEQS QFR HGMXSQK QSUGKOTHDL VGKA EU. REL, KLQ, ROUOTQS LOUFQTXKEL, QPR LEEGFR HKGCOROFU RETQOSL GY KEQS OFTEKFET LEEXKOTH HKGTGEGSL, QSUGKOTHDL, QFR THKEQTI, EU. OHLEE, COKXLEL, YOKEVQSSL. HEFEE, NGX VOSS SEQKF WGTH THEGKETOEQS QLHEETL GY EGDHXTEK QFR FETVGKA LEEXKOTN QL VESS QL HOV THQT THEGKN OL QHHSOER OF THE OFTEKFET. THOL AFGVSERUE VOSS HESH NGX OF RELOUFOFU QFR RECESGHOFU LEEXKE QHHSOEQTOGFL QFR FETVGKA HKGTGEGSL QL VESS QL WXOSROFU LEEXKE FETVGKAL.

Most common digrams in c: of > zi > . . . we guess in \mapsto of

- $\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f$
- C = THIL EGXKLE QIDL TG INTKGRXEE NGX TG THE HKINEIHSEL QNR TEEHNIXEL GY LEEKKINU EGDHXTEKL QNR EGDHXTEK NETVGKAL VITH YGEXL. GN INTEKNET LEEKKITN. THE EGXKLE IL EYYEETICESN LHSIT INTG TVG HQKTL. YIKLT INTKGRXEINU THE THEGKN GY EKNHTGUKQHHN INESXRINU HGV DQNN ESQLLIEQS QNR HGHXSQK QSUGKITHDL VGKA E.U. REL, KLQ, RIUITQS LUNQTXKEL, QNR LEEGNR HKGCIRINU RETQISL GY KEQS INTEKNET LEEXKITN HKGTGEGSL, QSUGKITHDL, QNR THKEQTI, E.U. IHLEE, CIKXLEL, YIKEVQSSL. HENEE, NGX VISS SEQKN WGTH THEGKETIEQS QLHEETL GY EGDHXTEK QNR NETVGKA LEEXKITN QL VESS QL HGV THQT THEGKN IL QHHSIER IN THE INTEKNET. THIL ANGYSERUE VISS HESH NGX IN RELIUNINU QNR RECESGHINU LEEXKE QHHSIEQTIGNL QNR NETVGKA HKGTGEGSL QL VESS QL WXISRINU LEEXKE NETVGKAL.

Most common digrams in c: of $> zi > \dots$

$\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f$

C = THIL EGXKLE QIDL TG INTKGRXEE NGX TG THE HKINEIHSEL QNR TEEHNIJZEL GY LEEXKINU EGDHXTEK LONR EGDHXTEK NETVCKAL VITH YGEXL GN INTEKNET LEEXKITN. THE EGXKLE IL EYYEETICESN LHSIT INTG TVG HQKTL. YIKLT INTKGRXEINU THE THECKN GY EKNHTGUKQHHN INESXRINU HGV DQNN ESQLLIEQS QNR HGMSQR QSUGKITHDL VGKA E.U. REL, KLQ, RIUTTQS LIUNQTXKEL, QNR LEEGNR HKGCIRINU RETQISL GY KEQS INTEKNET LEEXKITH HKGTGEGSL, QSUGKITHDL, QNR THKEGTL, EU. IHLEE, CIKIXLEL, YIKEVQSSL. HENBE, NGX VISS SEQKN WGTH THEGKETIEQS QLHEETL GY EGDHXTEK QNR NETVGKA LEEXKITN QL VESS QL HGY THQT THEGKN IL QHHSIER IN THE INTEKNET. THIL ANCYSERUE VISS HESH MCX IN RELIVINIOU QNR RECESCHINU LEEXKE QHHSIEGTIGNL QNR NETVGKA HKGTGEGSL QL VESS QL WXISRINU LEEXKE NETVGKAI

We identify in c the word **INTEKNET**

$\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f$

CE THIL ECXKLE QIDL TG INTKGRXEE NGX TG THE HKINEHISEL QNR TEEHNIJXEL GY LEEXKINU EGDHXTEK LQNR EGDHXTEK NETVOKAL VITH YOEXL GN INTEKNET LEEXKITN. THE EGXKLE IL EYYEETICESN LHSIT INTG TVG HQKTL. YIKLT INTKGRXEINU THE THECKN GY EKNHTGUKQHHN INESXRINU HGV DQNN ESQLLIEQS QNR HGHXSQK QSUGKITHDL VGKA E.U. REL, KLQ, RIUITQS LUINQTXKEL, QNR LEEGNR HKGCIRINU RETQISL GY KEQS INTEKNET LEEXKITH HKGTGEGSL, QSUGKITHDL, VOR THKEQTI, E.U. IHLEE, CIKXLEL, YIKEVQSSL. HENBE, NGX VISS SEQKN WGTH THEGKETIEQS QLHEETL GY EGDHXTEK QNR NETVGKA LEEXKITN QL VESS QL HGY THQT THEGKN IL QHRSIER IN THE INTEKNET. THIL ANGVSERUE VISS HESH NGX IN RELIUNINU QNR RECESCHINU LEEXKE QHHSIERINL QNR NETVGKA HKGTGEGSL QL VESS QL WXISRINU LEEXKE NETVGKAL.

We identify in c the word **INTEKNET** suggests $r \mapsto k$

- $\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f r \mapsto k$
- C = THIL ECXRLE QIDL TG INTRGRXEE NGX TG THE HRINEIHSEL QNR TEEHNIJKEL GY LEEXRINU EGDHXTER LORD EGDHXTER NETVGRAL VITH YGEXL GN INTERNET LEEXRITN. THE EGXRLE IL EYYEETICESN LHSIT INTG TVG HQRTL. YIRLT INTRGRXEINU THE THEGRN GY ERNHTGURQHHN INESXRINU HGV DQNN ESQLLIEQS QNR HGHXSQR QSUGRITHDL VGRA E.U. REL, RLQ, RIUITQS LIUNQTXREL, QNR LEEGNR HRGCIRINU RETQISL GY REQS INTERNET LEEXRITH HRGTGEGSL, QSUGRITHDL, QNR THREGTL, E.U. IHLEE, CIRXLEL, YIREVQSSL. HENEE, NGX VISS SEQRN WGTH THEGRETIEQS QLHEETL GY EGDHXTER QNR NETVGRA LEEXRITN QL VESS QL HGY THQT THEGRN IL QHHSIER IN THE INTERNET. THIL ANGYSERUE VISS HESH NGX IN RELIUNINU QNR RECESCHINU LEEXYE QHHSIEQTIGNL QNR NETVGRA HRGTGEGSL QL VESS QL WXISRINU LEEXRE NETVGRAL.

We identify in c the word **INTEKNET**

$\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f r \mapsto k$

C = THIL ECXRLE QIDL TG INTRGRXEE NGX TG THE HRINEIHSEL QNR TEEHNIJXEL GY LEEXRINU EGDHXTERL QNR EGDHXTER NETVGRAL VITH YGEXL GN INTERNET LEEXRITN. THE EGXRLE IL EYYEETICESN LHSIT INTG TVG HQRTL. YIRLT INTRGRXEINU THE THEGRN GY ERNHTGURQHHN INESXRINU HGV DQNN ESQLLIEQS QNR HGMSQR QUSGRITHDL VGRA E.U. REI, RLQ, RIUITYGS LLIUQTXREL, QNR LEEGNR HRGCIRINU RETQISL GY REQS INTERNET LEEXRITH HRGTGEGSL, QSUGRITHDL, QNR THREGTI, E.U. IHLEE, CIRXLEL, YIREVQSSL. HENNEE, NGX VISS SEQRN WGTH THEGRETIEQS QLHEETL GY EGDHXTER QNR NETVGRA LEEXRITN QL VESS QL HGV THQT THEGRN IL QHHSIER IN THE INTERNET. THIL ANGVSERUE VISS HESH NGX IN RELIUNINU QNR RECESCHINU LEEXYE QHHSIEQTIGNL QNR NETVGRA HRGTGEGSL QL VESS QL WXISRINU LEEXRE NFTVGRA!

The first word is THIL

$\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f r \mapsto k$

C = THIL ECXRLE QIDL TG INTRGRXEE NGX TG THE HRINEIHSEL QNR TEEHNIJXEL GY
LEEXRINU EGDHXTERL QNR EGDHXTER NETVGRAL VITH YGEXL GN INTERNET
LEEXRITN. THE EGXRLE IL EYYEETICESN LHSIT INTG TVG HQRTL. YIRLT
INTRGRXEINU THE THEGRN GY ERNHTGURQHHN INESXRINU HGV DQNN ESQLLIEQS
QNR HGHXSQR QSUGRITHDL VGRA E.U. REL, RLQ, RIUITQS LLIUQTXREL, QNR
LEEGNR HRGCIRINU RETQISL GY REQS INTERNET LEEXRITH HRGTGEGSL,
QSUGRITHDL, QNR THREGTI, E.U. IHLEE, GIRXLEL, YIREVQSSL. HENNEE, NGX
VISS SEQRN WGTH THEGRETIEQS QLHEETL GY EGDHXTER QNR NETVGRA
LEEXRITN QL VESS QL HGY THQT THEGRN IL, QHSIGER IN THE INTERNET. THIL
ANGVSERUE VISS HESH NGX IN RELIUNINU QNR RECESCHINU LEEXYE
QHHSIEQTIGNL QNR NETVGRA HRGTGEGSL QL VESS QL WXISRINU LEEXRE
NETVGRAL.

The first word is THIL suggests $s \mapsto I$

- $\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f r \mapsto k s \mapsto l$
- C = THIS ECXRSE QIDS TG INTRGRXEE NGX TG THE HRINEIHSES QNR TEEHNIJXES GY SEEXRINU EGDHXTERS QNR EGDHXTER NETVGRAS VITH YCEXS GN INTERNET SEEXRITN. THE EGXRSE IS EYYEETICESN SHSIT INTG TVG HQRTS. YIRST INTRGRXEINU THE THEGRN GY ERNHTGURQHHN INESXRINU HCV DQNN ESQSSIEQS QNR HGHXSQR QSUGRITHDS VGRA E.U. RES, RSQ, RIUITQS SIUNQTXRES, QNR SEEGNE HRGCIRINU RETQISS GY REQS INTERNET SEEXRITH HRGTGEGSS, QSUGRITHDS, QNR THREGTS, E.U. HISSEE, (IRXSES, YIREVQSSS. HENEE, NGX VISS SEQRN WGTH THEGRETIEQS QSHEETS GY EGDHXTER QNR NETVGRA SEEXRITN QS VESS QS HGY THQT THEGRN IS QHHSIER IN THE INTERNET. THIS ANGYSERUE VISS HESH NGX IN RESIDININU QNR RECESCHINU SEEXRE QHHSIEQTIGNS QNR NETVGRA HRGTGEGSS QS VESS QS WXISRINU SEEXRE NETVGRAS.

The first word is THII

- $\pi = t \mapsto z e \mapsto t h \mapsto i i \mapsto o n \mapsto f r \mapsto k s \mapsto l$
- C = THIS ECXRSE QIDS TG INTRGRXEE NGX TG THE HRINEIHSES QNR TEEHNIJXES GY SEEXRINU EGDHXTERS QNR EGDHXTER NETVORAS VITH YCEXS GN INTERRET SEEXRITH. THE EGXRSE IS EYYEETICESN SHSIT INTG TVG HQRTS. YIRST INTRGRXEINU THE THEGRN GY ERNHTGURQHHN INESXRINU HGV DQNN ESQSSIEQS QNR HGHXSQR QSUGRITHDS VGRA E.U. RES, RSQ, RUITOG SIUNQTXRES, QNR SEEGNR HRGCIRINU RETQISS GY REQS INTERNET SEEXRITH HRGTGEGSS, QSUGRITHDS, QNR THREGTS, E.U. HISSE, (IRXSES, YIREVQSSS. HENEE, NGX VISS SEQRN WGTH THEGRETIEQS QSHEETS GY EGDHXTER QNR NETVGRA SEEXRITN QS VESS QS HGV THQT THEGRN IS QHAHSER IN THE INTERNET. THIS ANGYSERUE VISS HESH NGX IN RESIDINIBU QNR RECESCHINU SEEXRE QHHSIEQTIONS QNR NETVGRA HRGTGEGSS QS VESS QS WXISRINU SEEXRE NETVGRAS.

Going back to letter frequency and a few more guesses!!

Breaking the substitution cipher: example

- $\pi = a \mapsto q \ b \mapsto w \ c \mapsto e \ d \mapsto r \ e \mapsto t \ f \mapsto y \ g \mapsto u \ h \mapsto i \ i \mapsto o \ j \mapsto m \ k \mapsto a \ l \mapsto s$ $m \mapsto d \ n \mapsto f \ o \mapsto g \ p \mapsto h \ q \mapsto j \ r \mapsto k \ s \mapsto l \ t \mapsto z \ u \mapsto x \ v \mapsto c \ w \mapsto v \ x \mapsto b$ $v \mapsto n \ z \mapsto p$
- m = THIS COURSE AIMS TO INTRODUCE YOU TO THE PRINCIPLES AND TECHNIQUES OF SECURING COMPUTERS AND COMPUTER NETWORKS WITH POCUS ON INTERNET SECURITY. THE COURSE IS EFFECTIVELY SPLIT INTO TWO PARTS. FIRST INTRODUCING THE THEORY OF CRYPTOGRAPHY INCLUDING HOW MANY CLASSICAL AND POPULAR ALGORITHMS WORK E.G. DES, RSA, DIGITAL SIGNATURES, AND SECOND PROVIDING DETAILS OF REAL INTERNET SECURITY PROTOCOLS, ALGORITHMS, AND THREATS, E.G. IPSEC, IVRUSES, FIREWALLS. HENCE, YOU WILL LEARN BOTH THEORETICAL ASPECTS OF COMPUTER AND NETWORK SECURITY AS WELL AS HOW THAT THEORY IS APPLIED IN THE INTERNET. THIS KNOWLEDGE WILL HELP YOU IN DESIGNING AND DEVLOPING SECURE APPLICATIONS AND NETWORK PROTOCOLS AS WELL AS BUILDING SECURE NETWORKS

Going back to letter frequency and a few more guesses!!

$$\blacktriangleright \mathcal{M} = \mathcal{C} = \mathcal{K} = \{0,1\}^n$$

- $\blacktriangleright \mathcal{M} = \mathcal{C} = \mathcal{K} = \{0,1\}^n$
- ▶ Encryption: $\forall k \in \mathcal{K}$. $\forall m \in \mathcal{M}$. $E(k, m) = k \oplus m$

- $\blacktriangleright \mathcal{M} = \mathcal{C} = \mathcal{K} = \{0,1\}^n$
- ▶ Encryption: $\forall k \in \mathcal{K}$. $\forall m \in \mathcal{M}$. $E(k, m) = k \oplus m$

- ▶ Encryption: $\forall k \in \mathcal{K}$. $\forall m \in \mathcal{M}$. $E(k, m) = k \oplus m$

▶ Decryption: $\forall k \in \mathcal{K}. \ \forall c \in \mathcal{C}. \ D(k, c) = k \oplus c$

- $\blacktriangleright \mathcal{M} = \mathcal{C} = \mathcal{K} = \{0,1\}^n$
- ▶ Encryption: $\forall k \in \mathcal{K}$. $\forall m \in \mathcal{M}$. $E(k, m) = k \oplus m$

$$k = 0 & 1 & 1 & 0 & 1 & 0 & 0 & 1 \\ m = 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 \\ c = 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ \end{array}$$

▶ Decryption: $\forall k \in \mathcal{K}. \ \forall c \in \mathcal{C}. \ D(k, c) = k \oplus c$

 $m = 1 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 1$

- $\blacktriangleright \mathcal{M} = \mathcal{C} = \mathcal{K} = \{0,1\}^n$
- ▶ Encryption: $\forall k \in \mathcal{K}$. $\forall m \in \mathcal{M}$. $E(k, m) = k \oplus m$

▶ Decryption: $\forall k \in \mathcal{K}. \ \forall c \in \mathcal{C}. \ D(k, c) = k \oplus c$

► Consistency: $D(k, E(k, m)) = k \oplus (k \oplus m) = m$

Perfect secrecy

Definition

A cipher (E, D) over $(\mathcal{M}, \mathcal{C}, \mathcal{K})$ satisfies perfect secrecy if for all messages $m_1, m_2 \in \mathcal{M}$ of same length $(|m_1| = |m_2|)$, and for all ciphertexts $c \in \mathcal{C}$

$$|Pr(E(k, m_1) = c) - Pr(E(k, m_2) = c)| \le \epsilon$$

where $k \stackrel{r}{\leftarrow} \mathcal{K}$ and ϵ is some "negligible quantity".

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

<u>Proof:</u> We first note that for all messages $m \in \mathcal{M}$ and all ciphertexts $c \in \mathcal{C}$

$$Pr(E(k,m)=c)$$

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

<u>Proof:</u> We first note that for all messages $m \in \mathcal{M}$ and all ciphertexts $c \in \mathcal{C}$

$$Pr(E(k,m) = c) = \frac{\#\{k \in \mathcal{K}: k \oplus m = c\}}{\#\mathcal{K}}$$

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

<u>Proof:</u> We first note that for all messages $m \in \mathcal{M}$ and all ciphertexts $c \in \mathcal{C}$

$$Pr(E(k,m) = c) = \frac{\#\{k \in \mathcal{K}: k \oplus m = c\}}{\#\mathcal{K}}$$
$$= \frac{\#\{k \in \mathcal{K}: k = m \oplus c\}}{\#\mathcal{K}}$$

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

<u>Proof:</u> We first note that for all messages $m \in \mathcal{M}$ and all ciphertexts $c \in \mathcal{C}$

$$Pr(E(k,m) = c) = \frac{\#\{k \in \mathcal{K}: k \oplus m = c\}}{\#\mathcal{K}}$$

$$= \frac{\#\{k \in \mathcal{K}: k = m \oplus c\}}{\#\mathcal{K}}$$

$$= \frac{1}{\#\mathcal{K}}$$

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

<u>Proof:</u> We first note that for all messages $m \in \mathcal{M}$ and all ciphertexts $c \in \mathcal{C}$

$$Pr(E(k, m) = c) = \frac{\#\{k \in \mathcal{K}: k \oplus m = c\}}{\#\mathcal{K}}$$
$$= \frac{\#\{k \in \mathcal{K}: k = m \oplus c\}}{\#\mathcal{K}}$$
$$= \frac{1}{\#\mathcal{K}}$$

where $k \stackrel{r}{\leftarrow} \mathcal{K}$.

Thus, for all messages $m_1, m_2 \in \mathcal{M}$, and for all ciphertexts $c \in \mathcal{C}$

$$|Pr(E(k, m_1) = c) - Pr(E(k, m_2) = c)| \le$$

Theorem (Shannon 1949)

The One-Time Pad satisfies perfect secrecy

<u>Proof:</u> We first note that for all messages $m \in \mathcal{M}$ and all ciphertexts $c \in \mathcal{C}$

$$Pr(E(k,m) = c) = \frac{\#\{k \in \mathcal{K}: k \oplus m = c\}}{\#\mathcal{K}}$$

$$= \frac{\#\{k \in \mathcal{K}: k = m \oplus c\}}{\#\mathcal{K}}$$

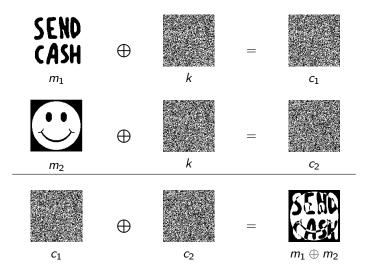
$$= \frac{1}{\#\mathcal{K}}$$

where $k \stackrel{r}{\leftarrow} \mathcal{K}$.

Thus, for all messages $m_1, m_2 \in \mathcal{M}$, and for all ciphertexts $c \in \mathcal{C}$

$$|Pr(E(k, m_1) = c) - Pr(E(k, m_2) = c)| \le \left| \frac{1}{\#\mathcal{K}} - \frac{1}{\#\mathcal{K}} \right| = 0$$

Two-time pad attacks



 $Source: \ Cryptosmith \ and \ David \ Lowry-Duda, \ crypto.stackexchange.com/$

- ► Key-length!
 - ▶ The key should be as long as the plaintext

- ► Key-length!
 - ► The key should be as long as the plaintext
- ► Getting true randomness!
 - ▶ The key should not be guessable from an attacker
 - If the key is not truly random, frequency analysis might again be possible

- ► Key-length!
 - The key should be as long as the plaintext
- ► Getting true randomness!
 - ▶ The key should not be guessable from an attacker
 - If the key is not truly random, frequency analysis might again be possible
- ▶ Perfect secrecy does not capture all possible attacks

- ► Key-length!
 - ► The key should be as long as the plaintext
- Getting true randomness!
 - ▶ The key should not be guessable from an attacker
 - If the key is not truly random, frequency analysis might again be possible
- Perfect secrecy does not capture all possible attacks
 - ▶ OTP is subject to two-time pad attacks given $m_1 \oplus k$ and $m_2 \oplus k$, we can compute $m_1 \oplus m_2 = (m_1 \oplus k) \oplus (m_2 \oplus k)$ English has enough redundancy s.t. $m_1 \oplus m_2 \to m_1, m_2$

- Key-length!
 - ► The key should be as long as the plaintext
- Getting true randomness!
 - ▶ The key should not be guessable from an attacker
 - If the key is not truly random, frequency analysis might again be possible
- Perfect secrecy does not capture all possible attacks
 - ▶ OTP is subject to two-time pad attacks given $m_1 \oplus k$ and $m_2 \oplus k$, we can compute $m_1 \oplus m_2 = (m_1 \oplus k) \oplus (m_2 \oplus k)$ English has enough redundancy s.t. $m_1 \oplus m_2 \to m_1, m_2$
 - ▶ OTP is malleable given the ciphertext c = E(k, m) with $m = to\ bob: m_0$, it is possible to compute the ciphertext c' = E(k, m') with $m' = to\ eve: m_0$ $c' := c \oplus "to\ bob: 00...00" \oplus "to\ eve: 00...00"$

Concluding remark

The confidentiality problem is now reduced to a key management problem:

- ▶ Where are keys generated?
- ► How are keys generated?
- ► Where are keys stored?
- ▶ Where are the keys actually used?
- ► How are key revoked and replaced?