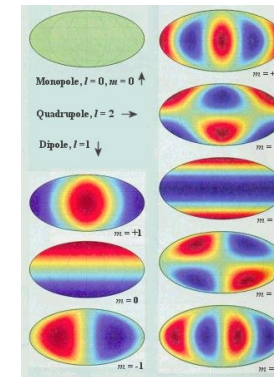
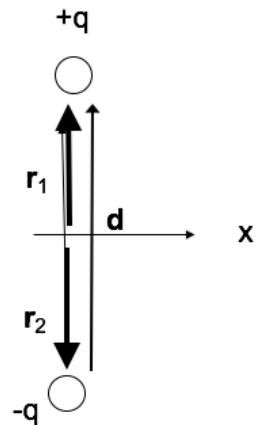


MULTIPOLE EXPANSION

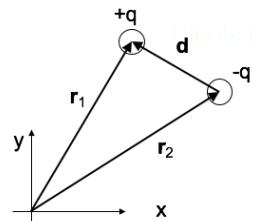


Multipole Expansion of the Power Spectrum of CMBR



Two charges are positioned as shown to the left. The relative position vector between them is \mathbf{d} . What is the value of the dipole moment? $\sum_i q_i \mathbf{r}_i$

- A. $+q\mathbf{d}$
- B. $-q\mathbf{d}$
- C. Zero
- D. None of these



Two charges are positioned as shown to the left. The relative position vector between them is \mathbf{d} . What is the dipole moment of this configuration?

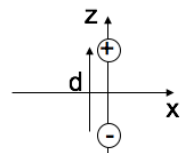
$$\sum_i q_i \mathbf{r}_i$$

- A. $+q\mathbf{d}$
- B. $-q\mathbf{d}$
- C. Zero
- D. None of these; it's more complicated than before!

For a dipole at the origin pointing in the z-direction, we have derived:

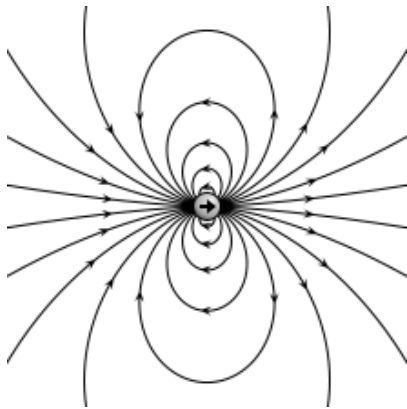
$$\mathbf{E}_{dip}(\mathbf{r}) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

For the dipole $\mathbf{p} = q\mathbf{d}$ shown, what does the formula predict for the direction of $\mathbf{E}(\mathbf{r} = 0)$?



- A. Down
- B. Up
- C. Some other direction
- D. The formula doesn't apply

IDEAL VS. REAL DIPOLE



Griffiths argues that the force on a dipole in an E field is:

$$\mathbf{F} = (\mathbf{p} \cdot \nabla) \mathbf{E}$$

If the dipole \mathbf{p} points in the z direction, what direction is the force?

- A. Also in the z direction
- B. perpendicular to z
- C. it could point in any direction

Griffiths argues that the force on a dipole in an E field is:

$$\mathbf{F} = (\mathbf{p} \cdot \nabla) \mathbf{E}$$

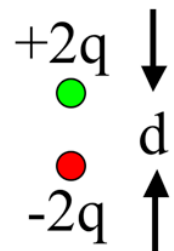
If the dipole \mathbf{p} points in the z direction, what can you say about \mathbf{E} if I tell you the force is in the x direction?

- A. \mathbf{E} simply points in the x direction
- B. E_z must depend on x
- C. E_z must depend on z
- D. E_x must depend on x
- E. E_x must depend on z

$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the magnitude of the dipole moment of this charge distribution?

- A. qd
- B. $2qd$
- C. $3qd$
- D. $4qd$
- E. It's not determined

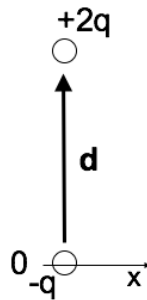


$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the dipole moment of this system?

(BTW, it is NOT overall neutral!)

- A. $q\mathbf{d}$
- B. $2q\mathbf{d}$
- C. $\frac{3}{2}q\mathbf{d}$
- D. $3q\mathbf{d}$
- E. Something else (or not defined)

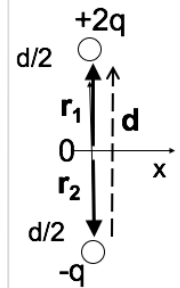


$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the dipole moment of this system?

(Same as last question, just shifted in z .)

- A. $q\mathbf{d}$
- B. $2q\mathbf{d}$
- C. $\frac{3}{2}q\mathbf{d}$
- D. $3q\mathbf{d}$
- E. Something else (or not defined)



You have a physical dipole, $+q$ and $-q$ a finite distance d apart. When can you use the expression:

$$V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \frac{\mathbf{p} \cdot \hat{\mathbf{r}}}{r^2}$$

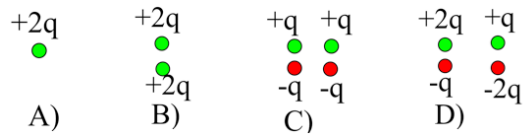
- A. This is an exact expression everywhere.
- B. It's valid for large r
- C. It's valid for small r
- D. No idea...

You have a physical dipole, $+q$ and $-q$ a finite distance d apart. When can you use the expression:

$$V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{\mathfrak{R}_i}$$

- A. This is an exact expression everywhere.
- B. It's valid for large r
- C. It's valid for small r
- D. No idea...

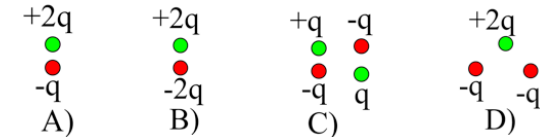
Which charge distributions below produce a potential that looks like $\frac{C}{r^2}$ when you are far away?



E) None of these, or more than one of these!

(For any which you did not select, how DO they behave at large r ?)

Which charge distributions below produce a potential that looks like $\frac{C}{r^2}$ when you are far away?



E) None of these, or more than one of these!

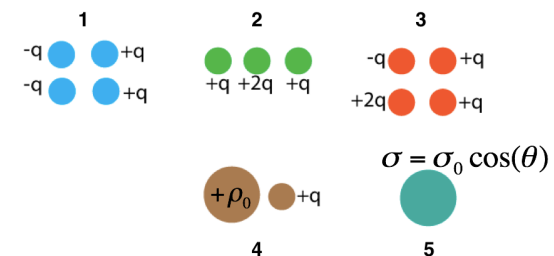
(For any which you did not select, how DO they behave at large r ?)

In terms of the multipole expansion $V(r) = V(\text{mono}) + V(\text{dip}) + V(\text{quad}) + \dots$, the following charge distribution has the form:



- A. $V(r) = V(\text{mono}) + V(\text{dip}) + \text{higher order terms}$
- B. $V(r) = V(\text{dip}) + \text{higher order terms}$
- C. $V(r) = V(\text{dip})$
- D. $V(r) = \text{only higher order terms than dipole}$
- E. No higher terms, $V(r) = 0$ for this one.

In which situation is the dipole term the leading non-zero contribution to the potential?



- A. 1 and 3
- B. 2 and 4
- C. only 5
- D. 1 and 5
- E. Some other combo