

We defined the volume current density in terms of the

$$\text{differential, } \mathbf{J} \equiv \frac{d\mathbf{I}}{da_{\perp}}.$$

When is ok to determine the volume current density by taking the ratio of current to cross-sectional area?

$$\mathbf{J} \stackrel{?}{=} \frac{\mathbf{I}}{A}$$

- A. Never
- B. Always
- C. I is uniform
- D. I is uniform and A is \perp to I
- E. None of these

A "ribbon" (width a) of surface current flows (with surface current density K). Right next to it is a second identical ribbon of current. Viewed collectively, what is the new total surface current density?

- A. K
- B. $2K$
- C. $K/2$
- D. Something else

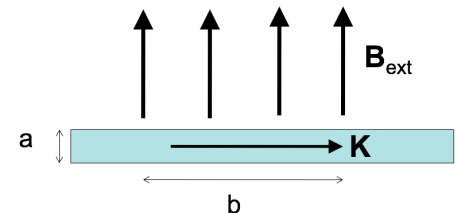


Current I flows down a wire (length L) with a square cross section (side a). If it is uniformly distributed over the outer surfaces only, what is the magnitude of the surface current density K ?

- A. $K = I/a^2$
- B. $K = I/a$
- C. $K = I/4a$
- D. $K = aI$
- E. None of the above

A "ribbon" (width a) with uniform surface current density K passes through a uniform magnetic field \mathbf{B}_{ext} . Only the length b along the ribbon is in the field. What is the magnitude of the force on the ribbon?

- A. KB
- B. aKB
- C. $abKB$
- D. bKB/a
- E. $KB/(ab)$



Which of the following is a statement of charge conservation?

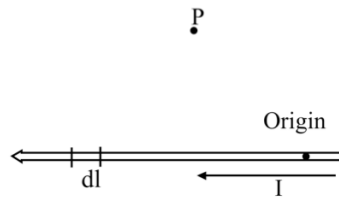
- A. $\frac{\partial \rho}{\partial t} = -\nabla \cdot \mathbf{J}$
- B. $\frac{\partial \rho}{\partial t} = -\nabla \cdot \mathbf{J}$
- C. $\frac{\partial \rho}{\partial t} = -\int \nabla \cdot \mathbf{J} d\tau$
- D. $\frac{\partial \rho}{\partial t} = -\oint \mathbf{J} \cdot d\mathbf{A}$

To find the magnetic field \mathbf{B} at P due to a current-carrying wire we use the Biot-Savart law,

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} I \int \frac{d\mathbf{l} \times \mathbf{R}}{\mathcal{R}^2}$$

What is the direction of the infinitesimal contribution $\mathbf{B}(P)$ created by current in $d\mathbf{l}$?

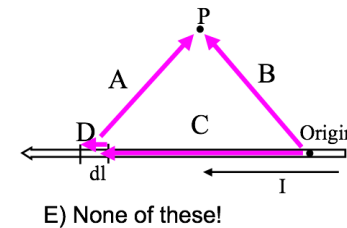
- A. Up the page
- B. Directly away from $d\mathbf{l}$ (in the plane of the page)
- C. Into the page
- D. Out of the page
- E. Some other direction



To find the magnetic field \mathbf{B} at P due to a current-carrying wire we use the Biot-Savart law,

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} I \int \frac{d\mathbf{l} \times \mathbf{R}}{\mathcal{R}^2}$$

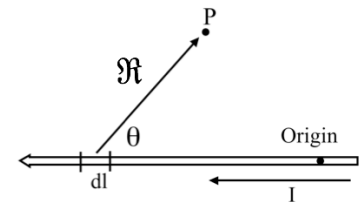
In the figure, with $d\mathbf{l}$ shown, which purple vector best represents \mathbf{R} ?



What is the magnitude of $\frac{d\mathbf{l} \times \mathbf{R}}{\mathcal{R}^2}$?

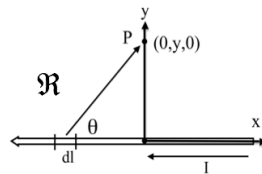
- A. $\frac{dl \sin \theta}{\mathcal{R}^2}$
- B. $\frac{dl \sin \theta}{\mathcal{R}^3}$
- C. $\frac{dl \cos \theta}{\mathcal{R}^2}$
- D. $\frac{dl \cos \theta}{\mathcal{R}^3}$

E. something else!

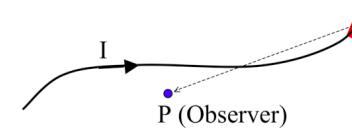


What is the value of $I \frac{d\mathbf{l} \times \mathbf{R}}{R^2}$?

- A. $\frac{I y dx'}{[(x')^2 + y^2]^{3/2}} \hat{z}$
- B. $\frac{I x' dx'}{[(x')^2 + y^2]^{3/2}} \hat{y}$
- C. $\frac{-I x' dx'}{[(x')^2 + y^2]^{3/2}} \hat{y}$
- D. $\frac{-I y dx'}{[(x')^2 + y^2]^{3/2}} \hat{z}$
- E. Other!



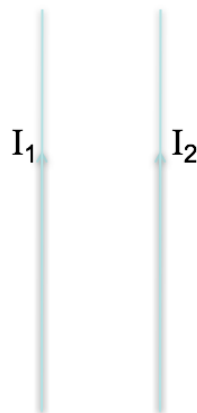
What do you expect for direction of $\mathbf{B}(P)$? How about direction of $d\mathbf{B}(P)$ generated JUST by the segment of current $d\mathbf{l}$ in red?



- A. $\mathbf{B}(P)$ in plane of page, ditto for $d\mathbf{B}(P)$, by red)
- B. $\mathbf{B}(P)$ into page, $d\mathbf{B}(P)$, by red) into page
- C. $\mathbf{B}(P)$ into page, $d\mathbf{B}(P)$, by red) out of page
- D. $\mathbf{B}(P)$ complicated, ditto for $d\mathbf{B}(P)$, by red)
- E. Something else!!

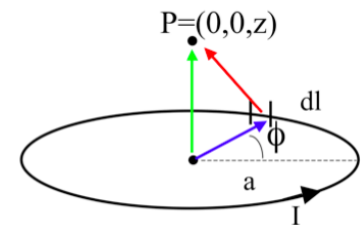
I have two very long, parallel wires each carrying a current I_1 and I_2 , respectively. In which direction is the force on the wire with the current I_2 ?

- A. Up
- B. Down
- C. Right
- D. Left
- E. Into or out of the page



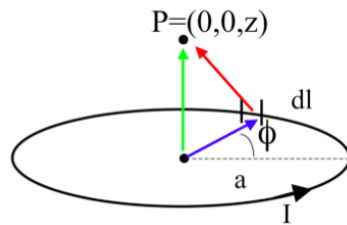
What is the magnitude of $\frac{d\mathbf{l} \times \mathbf{R}}{R^2}$?

- A. $\frac{dl \sin \phi}{z^2}$
- B. $\frac{dl}{z^2}$
- C. $\frac{dl \sin \phi}{z^2 + a^2}$
- D. $\frac{dl}{z^2 + a^2}$
- E. something else!

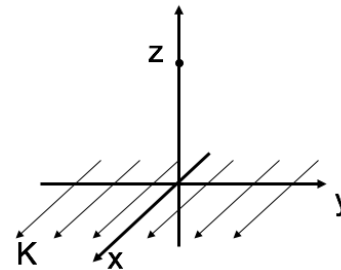


What is $d\mathbf{B}_z$ (the contribution to the vertical component of \mathbf{B} from this $d\mathbf{l}$ segment?)

- A. $\frac{dl}{z^2+a^2} \frac{a}{\sqrt{z^2+a^2}}$
- B. $\frac{dl}{z^2+a^2}$
- C. $\frac{dl}{z^2+a^2} \frac{z}{\sqrt{z^2+a^2}}$
- D. $\frac{dl \cos \phi}{\sqrt{z^2+a^2}}$
- E. Something else!



Consider the B-field a distance z from a current sheet (flowing in the $+x$ -direction) in the $z = 0$ plane. The B-field has:



- A. y-component only
- B. z-component only
- C. y and z-components
- D. x, y, and z-components
- E. Other