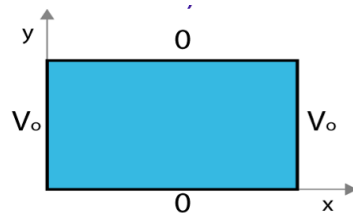


Given the two diff. eq's :

$$\frac{1}{X} \frac{d^2 X}{dx^2} = C_1 \quad \frac{1}{Y} \frac{d^2 Y}{dy^2} = C_2$$

where  $C_1 + C_2 = 0$ . Given the boundary conditions in the figure, which coordinate should be assigned to the negative constant (and thus the sinusoidal solutions)?

- A. x
- B. y
- C.  $C_1 = C_2 = 0$  here
- D. It doesn't matter.

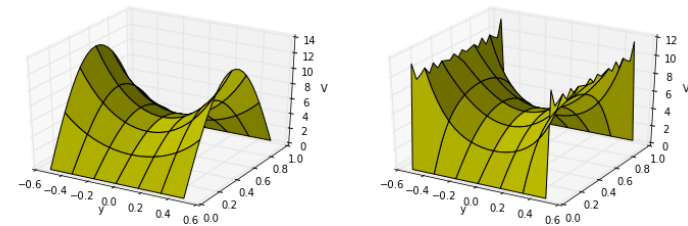


## EXACT SOLUTIONS:

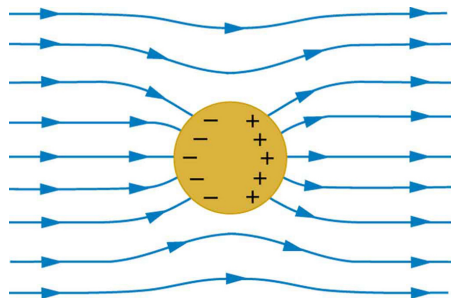
$$V(x, y) = \sum_{n=1}^{\infty} \frac{4V_0}{n\pi} \frac{1}{\cosh\left(\frac{n\pi}{2}\right)} \cosh\left(\frac{n\pi x}{a}\right) \sin\left(\frac{n\pi y}{b}\right)$$

## APPROXIMATE SOLUTIONS:

(1 TERM; 20 TERMS)



## SEPARATION OF VARIABLES (SPHERICAL)



$$V(r, \theta) = \sum_{l=0}^{\infty} \left( A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos \theta)$$

V everywhere on a spherical shell is a given constant, i.e.  $V(R, \theta) = V_0$ . There are no charges inside the sphere.

Which terms do you expect to appear when finding  $V(\text{inside})$ ?

- A. Many  $A_l$  terms (but no  $B_l$ 's)
- B. Many  $B_l$  terms (but no  $A_l$ 's)
- C. Just  $A_0$
- D. Just  $B_0$
- E. Something else!

Given  $V_0(\theta) = \sum_l C_l P_l(\cos \theta)$ , we want to get to the integral:

$$\int_{-1}^{+1} P_l(u) P_m(u) du = \frac{2}{2l+1} \text{ (for } l = m\text{)}$$

we can do this by multiplying both sides by:

- A.  $P_m(\cos \theta)$
- B.  $P_m(\sin \theta)$
- C.  $P_m(\cos \theta) \sin \theta$
- D.  $P_m(\sin \theta) \cos \theta$
- E.  $P_m(\sin \theta) \sin \theta$

F. Something else.

$$V(r, \theta) = \sum_{l=0}^{\infty} \left( A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos \theta)$$

Suppose  $V$  on a spherical shell is:

$$V(R, \theta) = V_0 (1 + \cos^2 \theta)$$

Which terms do you expect to appear when finding **V(outside)**?

- A. Many  $A_l$  terms (but no  $B_l$ 's)
- B. Many  $B_l$  terms (but no  $A_l$ 's)
- C. Just  $A_0$  and  $A_2$
- D. Just  $B_0$  and  $B_2$
- E. Something else!

$$V(r, \theta) = \sum_{l=0}^{\infty} \left( A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos \theta)$$

Suppose  $V$  on a spherical shell is:

$$V(R, \theta) = V_0 (1 + \cos^2 \theta)$$

Which terms do you expect to appear when finding **V(inside)**?

- A. Many  $A_l$  terms (but no  $B_l$ 's)
- B. Many  $B_l$  terms (but no  $A_l$ 's)
- C. Just  $A_0$  and  $A_2$
- D. Just  $B_0$  and  $B_2$
- E. Something else!

F. Something else.

How many boundary conditions (on the potential  $V$ ) do you use to find  $V$  inside the spherical plastic shell?

- A. 1
- B. 2
- C. 3
- D. 4
- E. It depends on  $V_0(\theta)$

