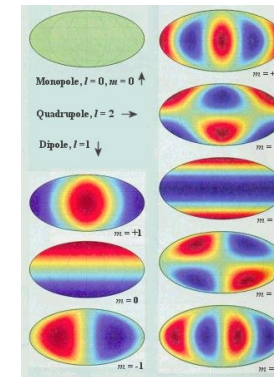
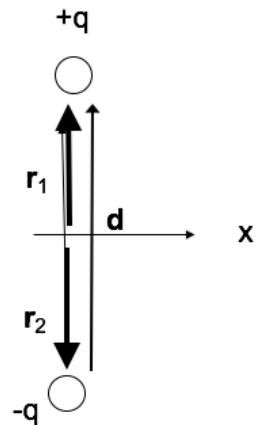


# MULTIPOLE EXPANSION

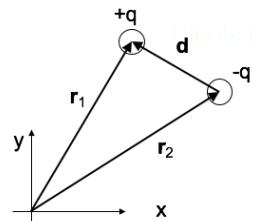


Multipole Expansion of the Power Spectrum of CMBR



Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the value of the dipole moment?  $\sum_i q_i \mathbf{r}_i$

- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these



Two charges are positioned as shown to the left. The relative position vector between them is  $\mathbf{d}$ . What is the dipole moment of this configuration?

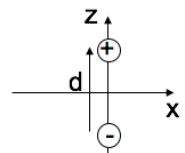
$$\sum_i q_i \mathbf{r}_i$$

- A.  $+q\mathbf{d}$
- B.  $-q\mathbf{d}$
- C. Zero
- D. None of these; it's more complicated than before!

For a dipole at the origin pointing in the z-direction, we have derived:

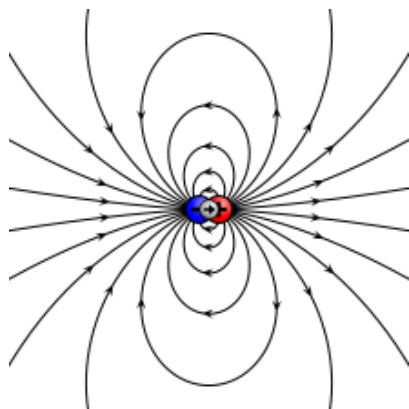
$$\mathbf{E}_{dip}(\mathbf{r}) = \frac{p}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

For the dipole  $\mathbf{p} = q\mathbf{d}$  shown, what does the formula predict for the direction of  $\mathbf{E}(\mathbf{r} = 0)$ ?



- A. Down
- B. Up
- C. Some other direction
- D. The formula doesn't apply

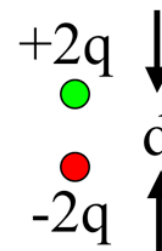
## IDEAL VS. REAL DIPOLE



$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the magnitude of the dipole moment of this charge distribution?

- A.  $qd$
- B.  $2qd$
- C.  $3qd$
- D.  $4qd$
- E. It's not determined

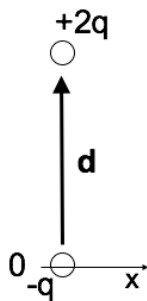


$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the dipole moment of this system?

(BTW, it is NOT overall neutral!)

- A.  $q\mathbf{d}$
- B.  $2q\mathbf{d}$
- C.  $\frac{3}{2}q\mathbf{d}$
- D.  $3q\mathbf{d}$
- E. Something else (or not defined)

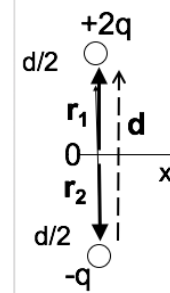


$$\mathbf{p} = \sum_i q_i \mathbf{r}_i$$

What is the dipole moment of this system?

(Same as last question, just shifted in  $z$ .)

- A.  $q\mathbf{d}$
- B.  $2q\mathbf{d}$
- C.  $\frac{3}{2}q\mathbf{d}$
- D.  $3q\mathbf{d}$
- E. Something else (or not defined)



You have a physical dipole,  $+q$  and  $-q$  a finite distance  $d$  apart. When can you use the expression:

$$V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \frac{\mathbf{p} \cdot \hat{\mathbf{r}}}{r^2}$$

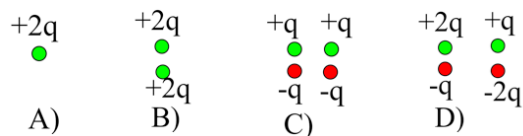
- A. This is an exact expression everywhere.
- B. It's valid for large  $r$
- C. It's valid for small  $r$
- D. No idea...

You have a physical dipole,  $+q$  and  $-q$  a finite distance  $d$  apart. When can you use the expression:

$$V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{\mathfrak{R}_i}$$

- A. This is an exact expression everywhere.
- B. It's valid for large  $r$
- C. It's valid for small  $r$
- D. No idea...

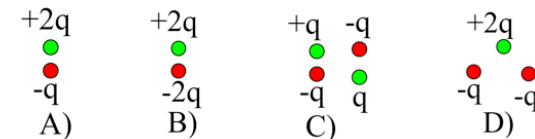
Which charge distributions below produce a potential that looks like  $\frac{C}{r^2}$  when you are far away?



E) None of these, or more than one of these!

(For any which you did not select, how DO they behave at large  $r$ ?)

Which charge distributions below produce a potential that looks like  $\frac{C}{r^2}$  when you are far away?



E) None of these, or more than one of these!

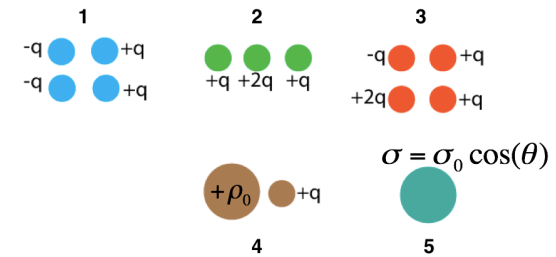
(For any which you did not select, how DO they behave at large  $r$ ?)

In terms of the multipole expansion  
 $V(r) = V(mono) + V(dip) + V(quad) + \dots$ , the following  
charge distribution has the form:



- A.  $V(r) = V(mono) + V(dip) +$  higher order terms
- B.  $V(r) = V(dip) +$  higher order terms
- C.  $V(r) = V(dip)$
- D.  $V(r) =$  only higher order terms than dipole
- E. No higher terms,  $V(r) = 0$  for this one.

In which situation is the dipole term the leading non-zero contribution to the potential?



- A. 1 and 3
- B. 2 and 4
- C. only 5
- D. 1 and 5
- E. Some other combo