

Gauss' Law for magnetism,  $\nabla \cdot \mathbf{B} = 0$  suggests we can generate a potential for  $\mathbf{B}$ . What form should the definition of this potential take ( $\Phi$  and  $\mathbf{A}$  are placeholder scalar and vector functions, respectively)?

A.  $\mathbf{B} = \nabla \Phi$

B.  $\mathbf{B} = \nabla \times \Phi$

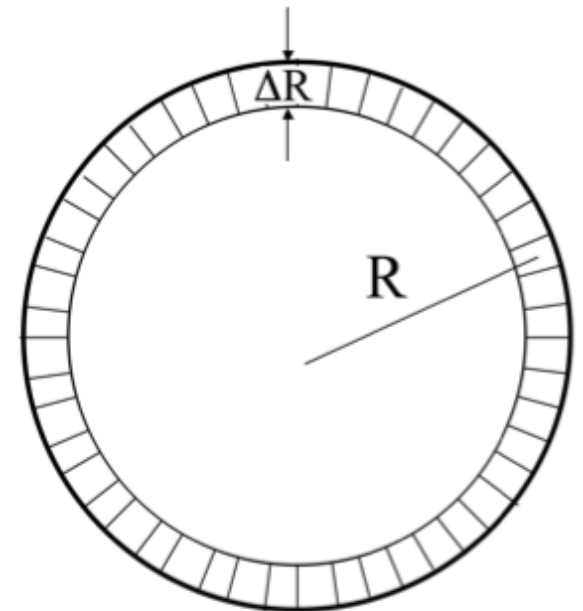
C.  $\mathbf{B} = \nabla \cdot \mathbf{A}$

D.  $\mathbf{B} = \nabla \times \mathbf{A}$

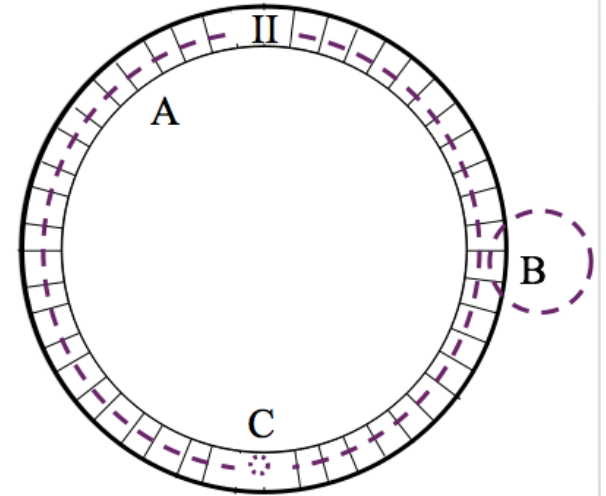
E. Something else?!

Consider a toroid, which is like a finite solenoid connected end to end. In which direction do you expect the B field to point?

- A. Azimuthally ( $\hat{\phi}$  direction)
- B. Radially ( $\hat{s}$  direction)
- C. In the  $\hat{z}$  direction (perp. to page)
- D. Loops around the rim
- E. Mix of the above...



Which Amperian loop would you draw to find  $B$  “inside” the Torus (region II)?



- A. Large "azimuthal" loop
- B. Smallish loop from region II to outside (where  $B=0$ )
- C. Small loop in region II
- D. Like A, but perp to page
- E. Something entirely different

With  $\nabla^2 \mathbf{A} = -\mu_0 \mathbf{J}$ , we can write (in Cartesian coordinates):

$$\nabla^2 A_x = -\mu_0 J_x$$

Does that also mean in spherical coordinates that

$$\nabla^2 A_r = -\mu_0 J_r?$$

A. Yes

B. No

We can compute  $\mathbf{A}$  using the following integral:

$$\mathbf{A}(\mathbf{r}) = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J}(\mathbf{r}')}{\mathfrak{R}} d\tau'$$

Can you calculate that integral using spherical coordinates?

- A. Yes, no problem
- B. Yes,  $r'$  can be in spherical, but  $\mathbf{J}$  still needs to be in Cartesian components
- C. No.

For a infinite solenoid of radius  $R$ , with current  $I$ , and  $n$  turns per unit length, which is the current density  $\mathbf{J}$ ?

A.  $\mathbf{J} = nI\hat{\phi}$

B.  $\mathbf{J} = nI\delta(r - R)\hat{\phi}$

C.  $\mathbf{J} = \frac{I}{n}\delta(r - R)\hat{\phi}$

D.  $\mathbf{J} = \mu_0 nI\delta(r - R)\hat{\phi}$

E. Something else?!