

Are  $\rho_b$  and  $\sigma_b$  due to real charges?

- A. Of course not! They are as fictitious as it gets!
- B. Of course they are! They are as real as it gets!
- C. I have no idea

# ANNOUNCEMENTS

- Exam 2 (Wednesday, November 7th 7-9pm)
- Covers through Homework 9 (solutions posted after class)
- "Comprehensive" exam (need to remember old stuff)
- 1 sheet of your own notes; old exam and formula sheet will be posted

# WHAT'S ON EXAM 2?

- Using Legendre polynomials and separation of variables in spherical coordinates, solve for the potential and distribution of charge in a boundary value problem
- Using the multipole expansion, find the approximate form of the potential for a distribution of charge
- Determine the bound charge in a material with a given polarization
- Find the electric potential for a 1D Laplace problem and explain how you would determine it using the method of relaxation
- (BONUS) Solve a 3D Laplace problem

If you put a polarizable material (a dielectric) in an external field  $\mathbf{E}_e$ , it polarizes, adding a new field,  $\mathbf{E}_p$  (from the bound charges). These superpose, making a total field,  $\mathbf{E}_T$ . What is the vector equation relating these three fields?

A.  $\mathbf{E}_T + \mathbf{E}_e + \mathbf{E}_p = 0$

B.  $\mathbf{E}_T = \mathbf{E}_e - \mathbf{E}_p$

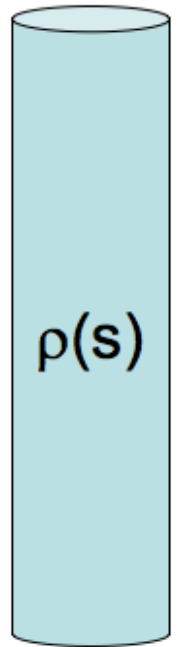
C.  $\mathbf{E}_T = \mathbf{E}_e + \mathbf{E}_p$

D.  $\mathbf{E}_T = -\mathbf{E}_e + \mathbf{E}_p$

E. Something else

A solid non-conducting dielectric rod has been injected ("doped") with a fixed, known charge distribution  $\rho(s)$ . (The material responds, polarizing internally.)

When computing  $D$  in the rod, do you treat this  $\rho(s)$  as the "free charges" or "bound charges"?



- A. "free charge"
- B. "bound charge"
- C. Neither of these -  $\rho(s)$  is some combination of free and bound
- D. Something else.

We define "Electric Displacement" or "D" field,

$$\mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P}$$

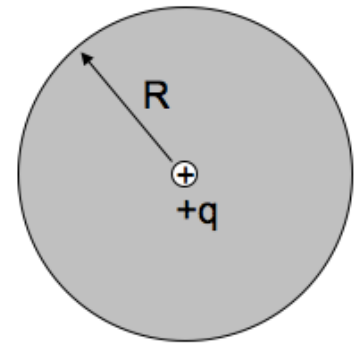
If you put a dielectric in an **external** field, it polarizes, adding a new **induced** field (from the bound charges). These superpose, making a **total** electric field. Which of these three E fields is the "E" in the formula for D above?

- A.  $\mathbf{E}_{ext}$
- B.  $\mathbf{E}_{induced}$
- C.  $\mathbf{E}_{tot}$

We define  $\mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P}$ , with

$$\oint \mathbf{D} \cdot d\mathbf{A} = Q_{free}$$

A point charge  $+q$  is placed at the center of a dielectric sphere (radius  $R$ ). There are no other free charges anywhere. What is  $|\mathbf{D}(r)|$ ?



- A.  $q/(4\pi r^2)$  everywhere
- B.  $q/(4\epsilon_0\pi r^2)$  everywhere
- C.  $q/(4\pi r^2)$  for  $r < R$ , but  $q/(4\epsilon_0\pi r^2)$  for  $r > R$
- D. None of the above, it's more complicated
- E. We need more info to answer!

For linear dielectrics the relationship between the polarization,  $\mathbf{P}$ , and the total electric field,  $\mathbf{E}$ , is given by:

$$\mathbf{P} = \epsilon_0 \chi_e \mathbf{E}$$

where  $\chi_e$  is typically a known constant. Think about what happens if (1)  $\chi_e \rightarrow 0$  or if (2)  $\chi_e \rightarrow \infty$ . What do each of these limits describe?

- A. (1) describes a metal and (2) describes vacuum
- B. (1) describes vacuum and (2) describes a metal
- C. Any material can give either  $\chi_e \rightarrow 0$  or  $\chi_e \rightarrow \infty$