I have two very long, parallel wires each carrying a current  $I_1$  and  $I_2$ , respectively. In which direction is the force on the wire with the current  $I_2$ ?

 $I_2$ 

- A. Up
- B. Down
- C. Right
- D. Left
- E. Into or out of the page

## What is the magnitude of $\frac{d\mathbf{l} \times \hat{\mathbf{R}}}{\mathbf{R}^2}$ ?

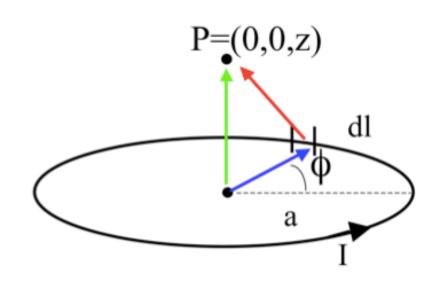
A. 
$$\frac{dl \sin \phi}{z^2}$$

B. 
$$\frac{dl}{r^2}$$

C. 
$$\frac{dl \sin \phi}{z^2 + a^2}$$

D. 
$$\frac{dl}{z^2 + a^2}$$

E. something else!



## What is $d\mathbf{B}_z$ (the contribution to the vertical component of $\mathbf{B}$ from this dl segment?)

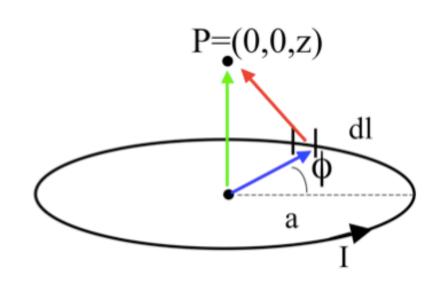
A. 
$$\frac{dl}{z^2 + a^2} \frac{a}{\sqrt{z^2 + a^2}}$$
B.  $\frac{dl}{z^2 + a^2}$ 
C.  $\frac{dl}{z^2 + a^2} \frac{z}{\sqrt{z^2 + a^2}}$ 

B. 
$$\frac{dl}{z^2 + a^2}$$

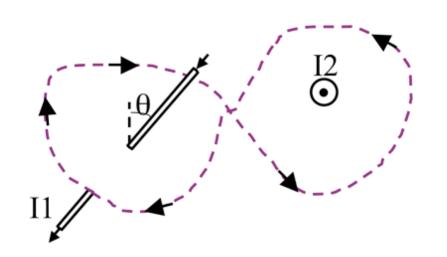
C. 
$$\frac{dl}{z^2 + a^2} \frac{z}{\sqrt{z^2 + a^2}}$$

D. 
$$\frac{dl\cos\phi}{\sqrt{z^2+a^2}}$$

E. Something else!



What is  $\oint \mathbf{B} \cdot d\mathbf{l}$  around this purple (dashed) Amperian loop?



A. 
$$\mu_0(|I_2| + |I_1|)$$

B. 
$$\mu_0(|I_2| - |I_1|)$$

C. 
$$\mu_0(|I_2| + |I_1| \sin \theta)$$

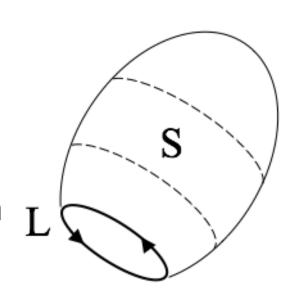
D. 
$$\mu_0(|I_2| - |I_1| \sin \theta)$$

E. 
$$\mu_0(|I_2| + |I_1| \cos \theta)$$

Stoke's Theorem says that for a surface S bounded by a perimeter L, any vector field  $\mathbf B$  obeys:

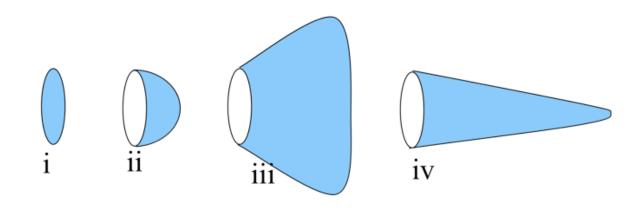
$$\int_{S} (\nabla \times \mathbf{B}) \cdot dA = \oint_{L} \mathbf{B} \cdot d\mathbf{l}$$

Does Stoke's Theorem apply for any surface S bounded by a perimeter L, even this balloon-shaped surface S?



- A. Yes
- B. No
- C. Sometimes

Rank order  $\int \mathbf{J} \cdot d\mathbf{A}$  (over blue surfaces) where  $\mathbf{J}$  is uniform, going left to right:



- A. iii > iv > ii > i
- B. iii > i > ii > iv
- C. i > ii > iii > iv
- D. Something else!!
- E. Not enough info given!!

Much like Gauss's Law, Ampere's Law is always true (for magnetostatics), but only useful when there's sufficient symmetry to "pull B out" of the integral.

So we need to build an argument for what **B** looks like and what it can depend on.

For the case of an infinitely long wire, can  $\bf B$  point radially (i.e., in the  $\hat{s}$  direction)?

A. Yes

B. No

C. ???

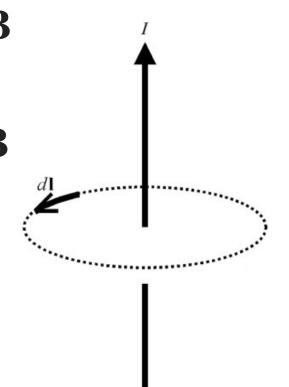
Continuing to build an argument for what **B** looks like and what it can depend on.

For the case of an infinitely long wire, can  ${\bf B}$  depend on z or  $\phi$ ?

A. Yes

B. No

C. ???



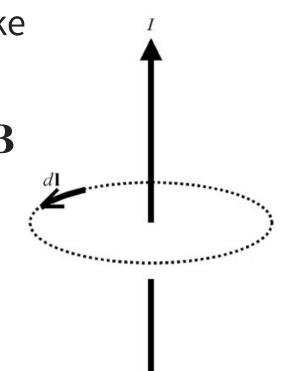
Finalizing the argument for what  ${f B}$  looks like and what it can depend on.

For the case of an infinitely long wire, can  ${\bf B}$  have a  $\hat{z}$  component?

A. Yes

B. No

C. ???



For the infinite wire, we argued that  $\mathbf{B}(\mathbf{r}) = B(s)\hat{\phi}$ . For the case of an infinitely long **thick** wire of radius a, is this functional form still correct? Inside and outside the wire?

A. Yes

B. Only inside the wire (s < a)

C. Only outside the wire (s > a)

D. No