

**True or False** The following mathematical operation makes sense and is technically valid.

$$\nabla \cdot \nabla T(x, y, z)$$

- A. Yes, it will produce a vector field.
- B. Yes, it will produce a scalar field.
- C. No, you can not take the divergence of a scalar field.
- D. I don't remember what this means.

A certain fluid has a velocity field given by  $\mathbf{v} = x\hat{x} + z\hat{y}$ .  
Which component(s) of the field contributed to "fluid flux"  
integral  $(\int_S \mathbf{v} \cdot d\mathbf{A})$  through the x-z plane?

- A.  $v_x$
- B.  $v_y$
- C. both
- D. neither

A certain fluid has a velocity field given by  $\mathbf{v} = x\hat{x} + z\hat{y}$ . If we intend to calculate the "fluid flux" integral  $(\int_S \mathbf{v} \cdot d\mathbf{A})$  through the x-z plane, what is  $d\mathbf{A}$  in this case? Be specific!

- A.  $\langle dx dy, 0, 0 \rangle$
- B.  $\langle dx dz, 0, 0 \rangle$
- C.  $\langle dy dz, 0, 0 \rangle$
- D. It's none of these

For the same fluid with velocity field given by  $\mathbf{v} = x\hat{x} + z\hat{y}$ .  
What is the value of the "fluid flux" integral ( $\int_S \mathbf{v} \cdot d\mathbf{A}$ )  
through the entire x-y plane?

- A. It is zero
- B. It is something finite
- C. It is infinite
- D. I can't tell without doing the integral

A rod (radius  $R$ ) with a hole (radius  $r$ ) drilled down its entire length  $L$  has a mass density of  $\frac{\rho_0 \phi}{\phi_0}$  (where  $\phi$  is the normal polar coordinate).

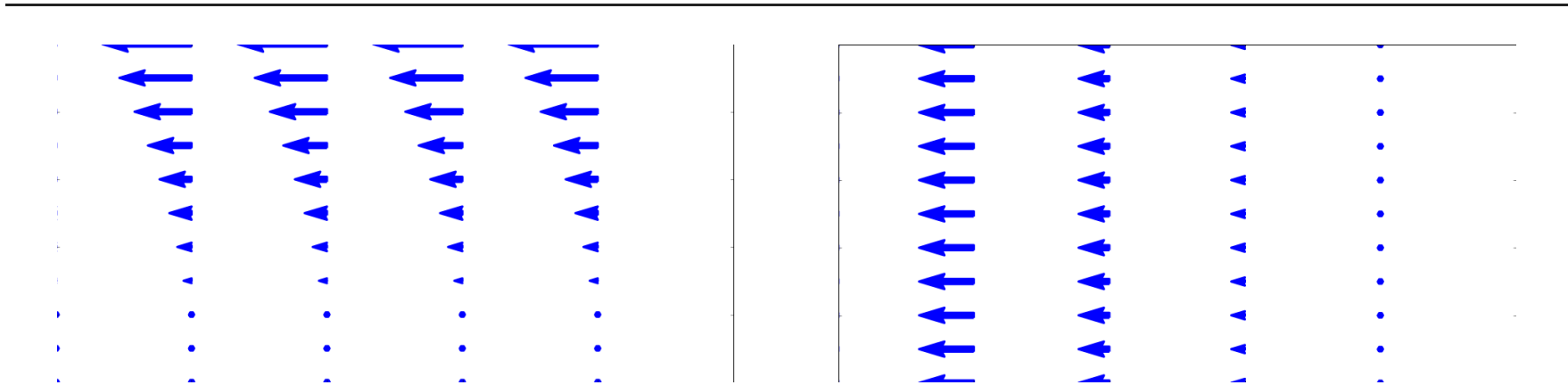
To find the total mass of this rod, which coordinate system should be used (take note that the mass density varies as a function of angle):

- A. Cartesian ( $x, y, z$ )
- B. Spherical ( $r, \phi, \theta$ )
- C. Cylindrical ( $s, \phi, z$ )
- D. It doesn't matter, just pick one.

Which of the following two fields has zero divergence?

I

II

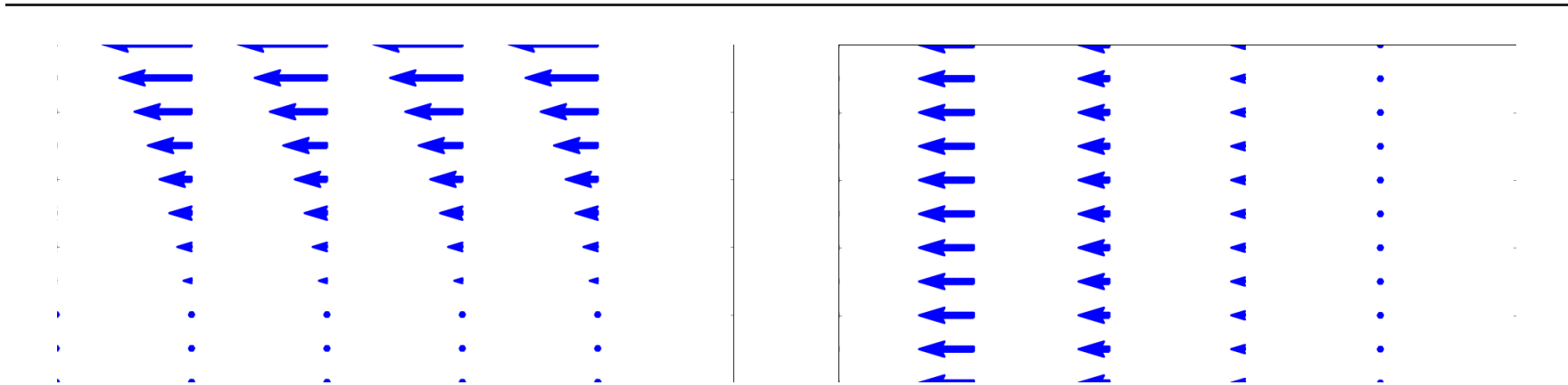


- A. Both do.
- B. Only I is zero
- C. Only II is zero
- D. Neither is zero
- E. ???

Which of the following two fields has zero curl?

I

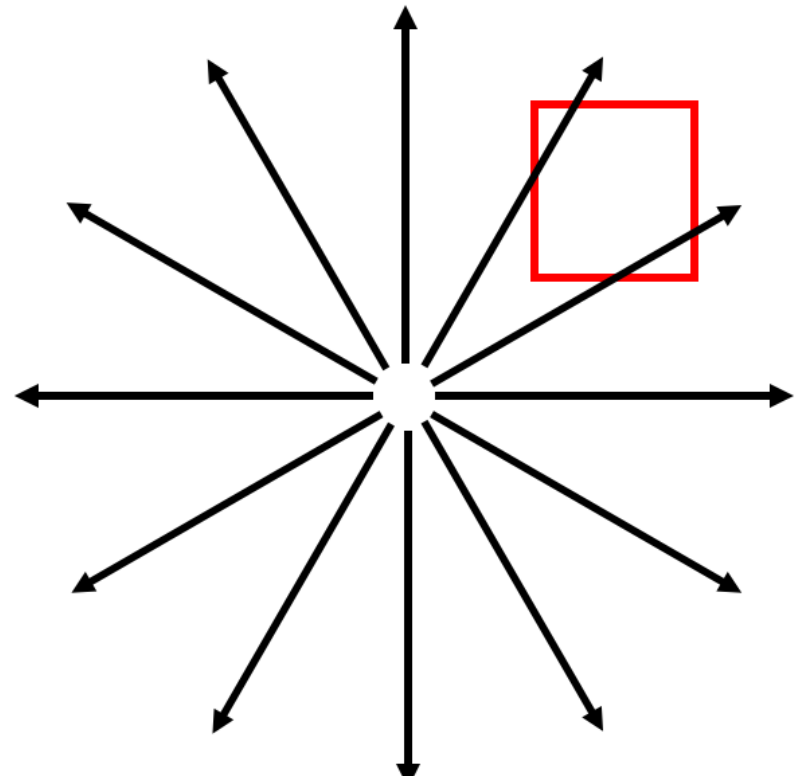
II



- A. Both do.
- B. Only I is zero
- C. Only II is zero
- D. Neither is zero
- E. ???

What is the divergence in the boxed region?

- A. Zero
- B. Not zero
- C. ???





Consider a vector field defined as the gradient of some well-behaved scalar function:

$$\mathbf{v}(x, y, z) = \nabla T(x, y, z).$$

What is the value of  $\oint_C \mathbf{v} \cdot d\mathbf{l}$ ?

- A. Zero
- B. Non-zero, but finite
- C. Can't tell without a function for  $T$