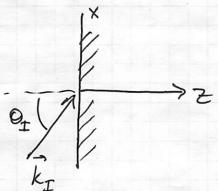
So we're developed a description for what happens when a wave strikes the boundary between two hedia, normally incident to the boundary. What happens when it strikes at a oblique angle!

Consider a wave entering at some augle,



There is a plane defined by ke and z, which

is called the plane
of incidence". It's
the plane of the pagehene.

We define the xaxis as shown so thathe "plane of incidence" is the XZ plane.

Assumptions: Again me assume monochonentre plane waves. And Mus, our Banday conditions will Jells us everything we need to know.

Er=Erei(kr. r-wt) B= krxEr Par Kr Car 1017 2 Er = Eore (Krir-wt) Br - krxEr

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V2 Material P material

As before, we cannot get that  $\vec{E} + \vec{B}$  are continuous without all the wis being the same (i.e.,  $W = W_I = W_R = W_T$ )  $\vec{E}_{oI} = \vec{E}_{oI} e^{i(\vec{K}_I \cdot \vec{r} - u +)}$ Er = Esre (Erir-wt)

Er = Eore (Erir-wt)

All of our Boundary Conditions result in the some expression (Blah T) e i(kI.7-w+) + (Blah R) e i(kR.7-w+) = Blah T) e We can examine there to see in what plane (s) the waves progagate.

The blak's are accomplex vectors but have no Fort

dependence.

When we watch boundary conditions in the z=0 plane, the vector ? will be, ?= <x, y, 0>. Each term has an e-int that cancels out so you are loft with. left with, (Blah\_)ei(kror) (Blahe)ei(kror) = (Blah)ei(kror)

By the same logic as before the exponential terms must all he the same in the = plane,

KIOT = Root = KTOT for all 7 in z=0 plane.

 $K_{I} = k_{IX}\hat{x} + k_{IZ}\hat{z}$  is given (it's the incident wave)

We can argue that,  $(\vec{k}_{\perp} - \vec{k}_{p}) \cdot \vec{r} = 0$  for any  $\vec{r} = (x, y, 0)$ As Pis some arbitrumy vector we find that, o

KIXX-(Kexx+keyy)=0 for all x andy So key = 0 (it must be for the above to hold for )

La the reflected wave is also in the page! also KIX= Kex ( we will come back to this).

The Te WE LA Case 1

Cuse is a > = linear combination! We'll nork out case 1 (case 2 is

part of your hw)

So that,

E((E) (-1) + EOR) = EZEO+(-1)(N1)

er (For-EDE) = -EZMI For for B.C. #1.

We now use the B.C., E"= E"

(Il to boundary),

Fot cosOf + EorcosOK = Eot cosOT (B" gives no new ito)

We have Zegn's and Zunknowns (For and FOR),

Fox - For = EN FOT = BEOT ( Same Bas )

Eot + Eor = Eot COSOT = O.EOT

d is a constant given OI Snell's gives us OR 50 x 13 determined

These equations produce!

 $E_{oT} = \frac{\alpha}{(\alpha + \beta)} \sum_{i=1}^{\infty} E_{ot} = \frac{\alpha - \beta}{\alpha + \beta} \sum_{i=1}^{\infty} E_{ot}$ 

Again these are the fresnel equations when  $\Theta_R = \Theta_T = \Theta_I = 0^\circ \cos \rightarrow 1 \cos \alpha \rightarrow 1$ !

	phy 482	RdT	5	
	Case 1) ĥ = has no y component so that,			
	$\hat{K}_{I} = 88 \sin \theta_{I} \hat{x} + (\cos \theta \hat{z}) $ $\hat{N}_{I} = (08\theta_{I} \hat{x} - \sin \theta \hat{z}) $ $\text{Mathbese}$ $\text{Make sense!}$ $\text{Quick theck } \hat{K}_{I} \cdot \hat{N}_{I} = \sin \theta_{I} \cos \theta_{I} - \cos \theta_{I} \sin \theta_{I} = 0 $ $\text{Reminder about Boundary Conditions}$			
	$\mathcal{E}_{1} = \mathcal{E}_{2} = \mathcal{E}_{2}^{\perp}$ $B_{1}^{\perp} = B_{2}^{\perp}$ $E_{1}^{"} = E_{2}^{"}$ $B_{1}^{"} = B_{2}^{"} \text{ (where } \mu_{1}$	- All of - for case us not	these hold at z=0  to boundary  e1 B1=B2 tells  hing b/c no B component  oundary.  n is redundant (asit	
	E Eorna Hene's our picture  ORT FOT How with  The direction of  When electric field  dabelled.			
Using $\mathcal{E}_{1}E_{1}^{\perp} = \mathcal{E}_{2}E_{2}^{\perp}$ , $\mathcal{E}_{1}\left(\widehat{E}_{10}(\widehat{n}_{1})_{z} + \widehat{E}_{0R}(\widehat{n}_{p})_{z}\right) = \mathcal{E}_{2}\widehat{E}_{0T}(\widehat{n}_{T})_{z}  \text{(we cancell either the z-components give)}$ The z-components give,				
	E, (EIO (- sinox) +	Epr(sinor)) = 82 E	TO (-sikeT)	

Using snell's law gives us  $SiNO_{I} = SinO_{P}$  and  $SinO_{T} = \frac{n_{1}}{n_{2}} SinO_{I}$ 

A few observations:

- DEOT is always in phase w/ Eot. The reflected wave comprekup a mitture sign when a<B.

  But no complex phases are introduced.
- 2) The Bifields all come from kxE/V.
- 3) Unlike the normal incidence Example, For and Fot do depend on  $\Theta_{\rm E}$ , they are not simply determined by  $n_1 d n_2$ .
- 4) If  $\alpha = \beta$ , then For = 0. Whoa! that's interesting.

  This is a special angle (Brewster's Angle)

  Defined by  $\alpha = \beta \Rightarrow \frac{\cos \theta_{I}}{\cos \theta_{T}} = \frac{n_{I}}{n_{Z}}$ At this angle all the light transmits, but this only for case I. when the polarization is in the plane.