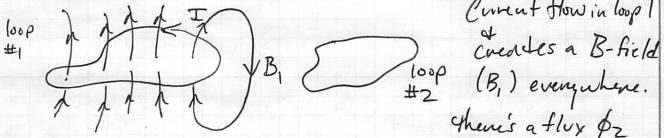
Application of Faraday's Law: Inductance.

Our study of circuits (coming soon) will require that we understand how Faraday's Law comes into situations with multiple loops.

Canonicial Conceptral Example



Current How in loop 1

If I, changes then Pz changes, Mis induces an EMF in loop 2 (

There's a flux \$2 through loop 2. Wireless communication)

In principle we could use Birt-Savart to find the field near loop 2,

 $B_{i}(\vec{r}) = \frac{u_{0}}{4\pi} \int_{0}^{\pi} I_{i} \frac{d\vec{l}_{i} \times \hat{n}}{n^{2}}$ where \vec{n} is the usual separation vector.

This could be a very rasty situation in practice (maybe record use a computer ??)

But note that B, & I, so we find that the flux through loop 2 is as well,

 $\Phi_2 = \iint \vec{B}_1 \cdot d\vec{a}_2$ due to $\log 1$ $\log 1$ $\log 1$ $\log 1$ $\log 2$

So that oz is,

But $\phi_2 \propto I_1$ so we can define a proportionality constant M_{21} which is,

Pz due to 1 = Mz, I,

M21 is the "untral inductance." (We will get to it's physical heaving soon.)

so if I, changes => \$\frac{1}{2}\$ changes => \$\frac{1}{2} = -\frac{d\partial z}{d\frac{1}{2}}\$ will be present.

Thus changing the arrent in loop I drives a cornent in loop 2.

$$\mathcal{E}_{2} = -\frac{d\phi_{2}}{dt} = -M_{21}\frac{d\mathcal{I}_{1}}{dt}$$

Mand to compute but if the loops one fixed in size, shape, a orientation M21 12 constant!

$$M_{21} = \iint \frac{\vec{B}_1 \cdot d\vec{a}_2}{\vec{I}_1} = \iint \frac{u_0}{4\pi} \oint \frac{d\vec{l}_1 \times \hat{\chi}}{\lambda^2} \cdot d\vec{a}_2$$

$$\lim_{z \to 0} \frac{|\cos z|}{2} = \lim_{z \to 0} \int \frac{d\vec{l}_1 \times \hat{\chi}}{\lambda^2} \cdot d\vec{a}_2$$

It's nasty looking, but only depends on geometry (size, shape, orientation of loops).

It's also measurable in the hab using the boxed formula.

We won't do it have, but you can use Stoke's theorem (see Emiffiths 7.2.3) to obtain the Nevmann formula for Mzi,

M₂₁ = Mo f f dl. dlz lts still punely geometrical loop loop loop (and not fun to compute), but...

it highlights that swapping I and 2 make Nor difference in the calculation so,

 $M_{21} = M_{12}$ this is the origin of the term surval inductance.

M= M12 = M21

Kunning II in loop I induces P2 = M21 I1 Kunning Iz in loop 2 induces & = MIZIZ

It M21 = M12 then a lamp convent in either loop induces the same flux in the other loop.

-So practical matter,

if B from loop 1 is easy to find, determine Mz, it B from loop 2 is easy to find, determine M12 Eigher way, M= M12 = M21,

Zz = - M dI Primary Secondary

Transformers use this:

but you need AC

Current (d/dt needed!)

Self Inductance

Changing I, changes of because there is a magnetic field B, generated by I, though A, (the loop we are considering).

So this change can produce an EMF Sterned a Back EMF for reasons that will become readily apparent.

Formally, $\phi_1 = M_{11} I_1$ L) self-inductance, L.

So, $\mathcal{E}_1 = -\frac{dd_1}{dt} = -L\frac{dI_1}{dt}$ By definition L>0. Is the induced EMF fights the change, hence the term Back EMF!

Big L helps damp out high frequency noise. Why? high f means large d/dt

So a large Back EMF is generaled to "frihtthe "ehenge." > result is that there signals get change.

Smoothed out. (We will study these circuits soon.)

In a circuit diagram, july inductor

units: [L] = [8] = $\frac{\sqrt{100}}{4/5} = \frac{\sqrt{100}}{4/5} = \frac{1$

Also, since $\phi_1 = LI$, $[\phi] = [B. Hrea] = [Tm^2] = Weber, w$ A henry is a weber/amp. IH = 1 1 1 1/4 [No] = H/m No = 411.107 H/m