Through a variety of experimental work and sheoreetical development in the 1800's led to the fillowing set of equations,

$$\nabla \cdot \vec{E} = \beta/6$$
 Goves  
 $\nabla \times \vec{E} = -d\vec{B}/d + Faraday$   
 $\nabla \cdot \vec{B} = 0$   
 $\nabla \times \vec{B} = uo\vec{J}$  Auguene

F=g(E+VXB) herentz force on charges.

Maxwell had these equations and models in the 18603. He didn't invent these equations, he started home.

- Maxwell (and others) asked, "Could these be a complete theory of electromagnetism?"

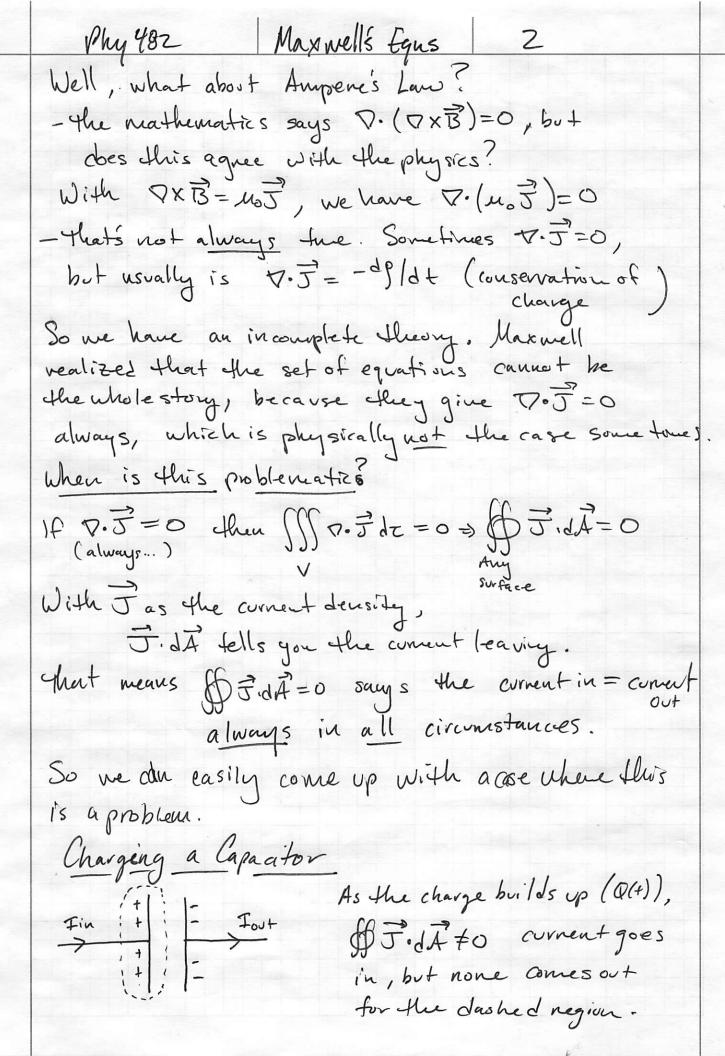
- We've used them for time dependent work and conjusted a number of experimentally verifiable results.

(so maybe it is?)

Is it complete?

- Let's do some mathematical manipulations to see what we find (this is similar to what Maxmell did).

Fact: the divergence of any curl is zero. - This is provable, mathematical result.  $\nabla \cdot (\nabla \times \vec{G}) = 0$ Let's check this with Faraday's Law,  $\nabla x\vec{E} = -d\vec{B}/dt$ the mathematics tells us  $\nabla \cdot (\nabla x\vec{E}) = 0$ so it must be that  $\nabla \cdot (-d\vec{B}) = 0$ and it is!  $\nabla \cdot (-d\vec{B}) = -d \cdot (\nabla \cdot \vec{B}) = 0$  (math sphysics) agree!



think about the "soap bubble" surface that has the same bounded loop,

I J J

This new surface isn't a flat circle, but 13 bounded by the same loop as the flat

for this surface I tem = 0, no current Tokes through the soup bubble surface!

Ampere's Law (as written) is failing here.

\$B.12 = M. JJ.12°

Mo JJJ: JA 3 we came up with 2

surfaces that give

any surface different results for

bounded by

the right-hand sill

The problem is that if to inside the bubble. -> charge builds up so that current in + current out. (If we had steady curents, like in Hepust, and df/dt = 0, we'd have no issue, like in the past.)

Maxwell's Cornection

D. (DXB) = 0 must be the! The mostle is undervable.

If  $\nabla \times \vec{B} = Mo\vec{\sigma}$ , we get  $\nabla \cdot (Mo\vec{J}) = 0$  instead of What consenation of commutacys,

7. (no =) = - no dp/dt

Let's see if we can fix Aupenes' Law. Add X to

TXB=10+ I let's see what happens with Hus.

マ・(マメる)=ル。マ・ディマ・文

from the math conservation of convent.

Maybe it's still not obvious what It is, but let's push forward. The form suggests we peck into Grass' Law.,

D. E= P/60 => P= 80 T. E thus,

( 1 = € 9+ ( 1. E) = 6 1. ( 9+ )

Oh! it looks like if \ = + MOEO JE,

then the equation is always satisfied!

(DXB = MoJ + MoE dE/dt | Ampere's Law w/ Marwell Conections

This extra term is the "displacement current", No Jo with Jo = E. VE/dt

> It has units of current density, but it's not a physical flow of charge. It's not a current. The name was Maxwell's but now its just what we have.

-> Note: In statics with dE/dt=0, we are back to the old Auperes Law, 7XB = M.F

the right hand side is just MOI. when we have the bubble Ithm = 0 but, If the dA = Mo I same result!

EXB that are not zero! They will be travelling waves with V= \( \frac{1}{500} = 3.108 m/s.