

Suppose you have a circuit driven by a voltage:

$$V(t) = V_0 \cos(\omega t)$$

You observe the resulting current is:

$$I(t) = I_0 \cos(\omega t - \pi/4)$$

Would you say the current is

A. leading

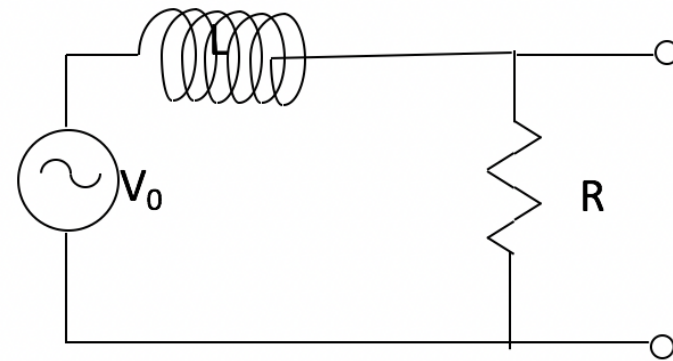
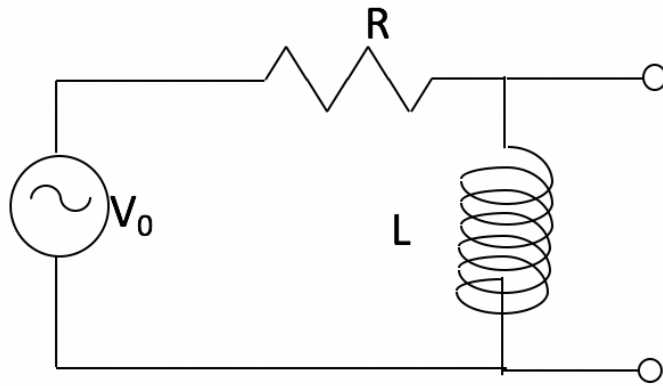
B. lagging

the voltage by 45 degrees?

ANNOUNCEMENTS

- Quiz 3 (Friday 2/14) - RLC circuits
 - Solve a circuit problem using the phasor method
 - Discuss limits on the response and how it might act as a filter

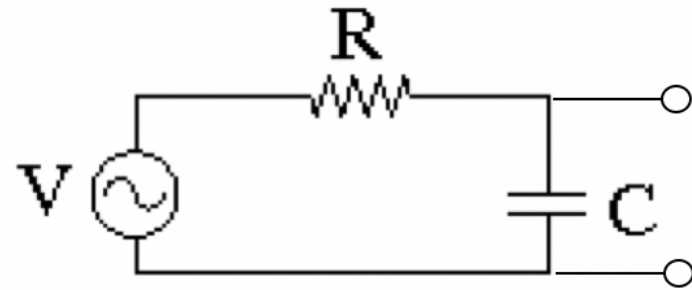
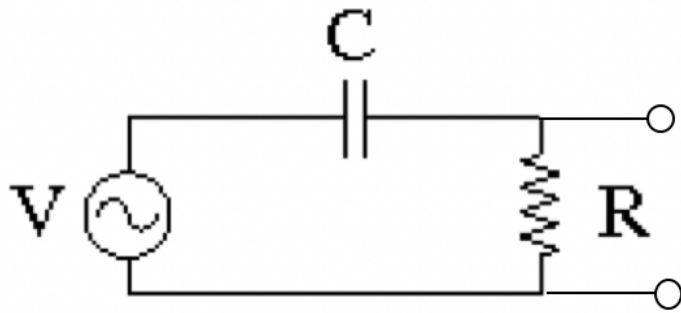
Two LR circuits driven by an AC power supply are shown below.



Which circuit is a low pass filter?

- A. The left circuit
- B. The right circuit
- C. Both circuits
- D. Neither circuit

Two RC circuits driven by an AC power supply are shown below.



Which circuit is a high pass filter?

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- B. The right circuit
- C. Both circuits
- D. Neither circuit

Ampere's Law relates the line integral of \mathbf{B} around some closed path, to a current flowing through a surface bounded by the chosen closed path.

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$$

By calling it a "Law", we expect that:

- A. It is neither correct nor useful.
- B. It is sometimes correct and sometimes easy to use.
- C. It is correct and sometimes easy to use.
- D. It is correct and always easy to use.
- E. None of the above.

Take the divergence of the curl of any (well-behaved) vector function \mathbf{F} , what do you get?

$$\nabla \cdot (\nabla \times \mathbf{F}) = ???$$

- A. Always 0
- B. A complicated partial differential of \mathbf{F}
- C. The Laplacian: $\nabla^2 \mathbf{F}$
- D. Wait, this vector operation is ill-defined!

Take the divergence of both sides of Faraday's law:

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

What do you get?

- A. $0 = 0$ (is this interesting?)
- B. A complicated partial differential equation (perhaps a wave equation of some sort ?!) for \mathbf{B}
- C. Gauss' law!
- D. ???

Take the divergence of both sides of Ampere's law:

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J}$$

According to this, the divergence of **J** is:

A. $-\partial\rho/\partial t$

B. A complicated partial differential of **B**

C. Always 0

D. ???

Ampere's Law relates the line integral of **B** around some closed path, to a current flowing through a surface bounded by the chosen closed path.

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$$

The **path** can be:

- A. Any closed path
- B. Only circular paths
- C. Only sufficiently symmetrical paths
- D. Paths that are parallel to the B-field direction.
- E. None of the above.

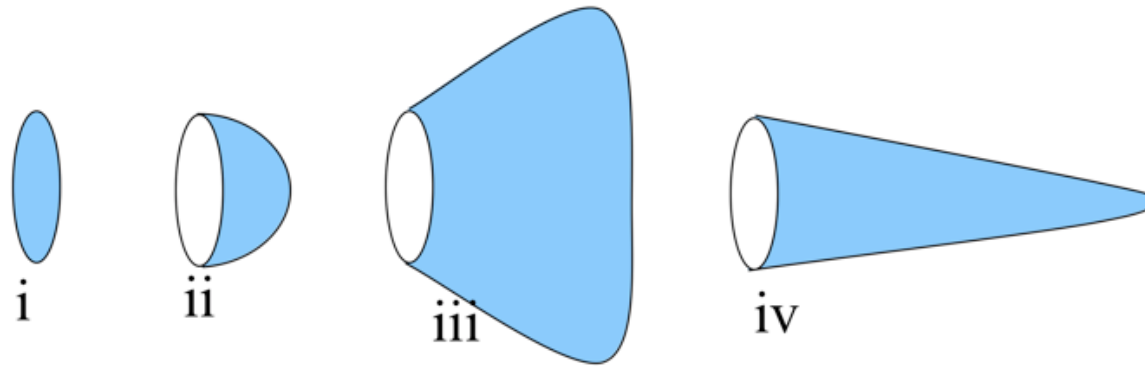
Ampere's Law relates the line integral of **B** around some closed path, to a current flowing through a surface bounded by the chosen closed path.

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$$

The **surface** can be:

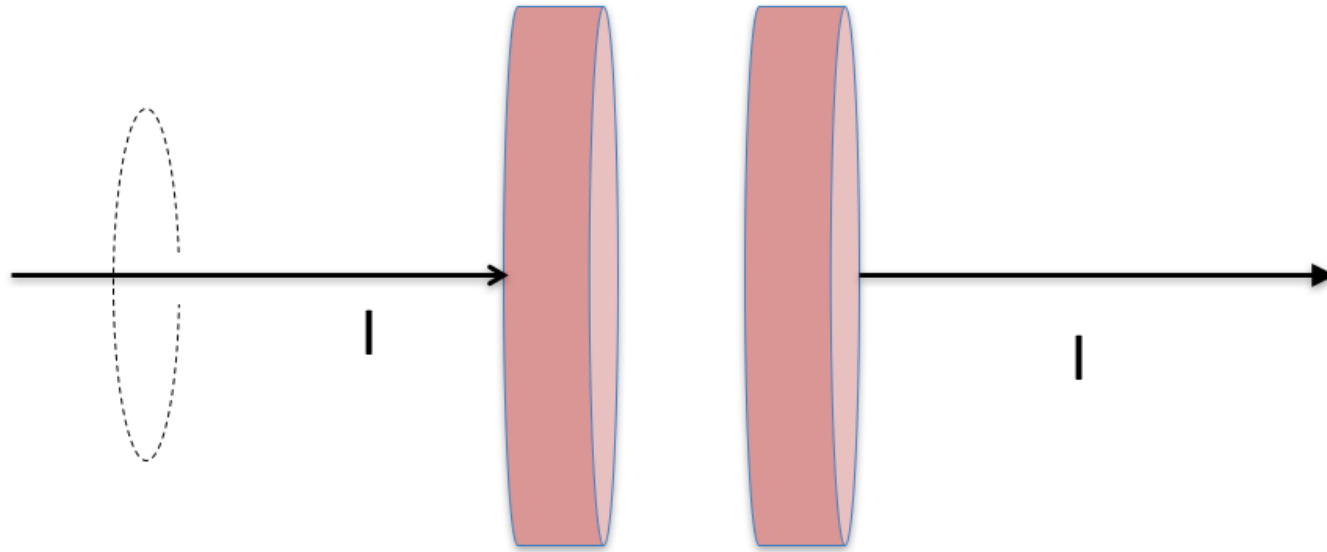
- A. Any closed bounded surface
- B. Any open bounded surface
- C. Only surfaces perpendicular to **J**.
- D. Only surfaces tangential to the B-field direction.
- E. None of the above.

Rank order $\int \mathbf{J} \cdot d\mathbf{A}$ (over blue surfaces) where \mathbf{J} is uniform, going left to right:



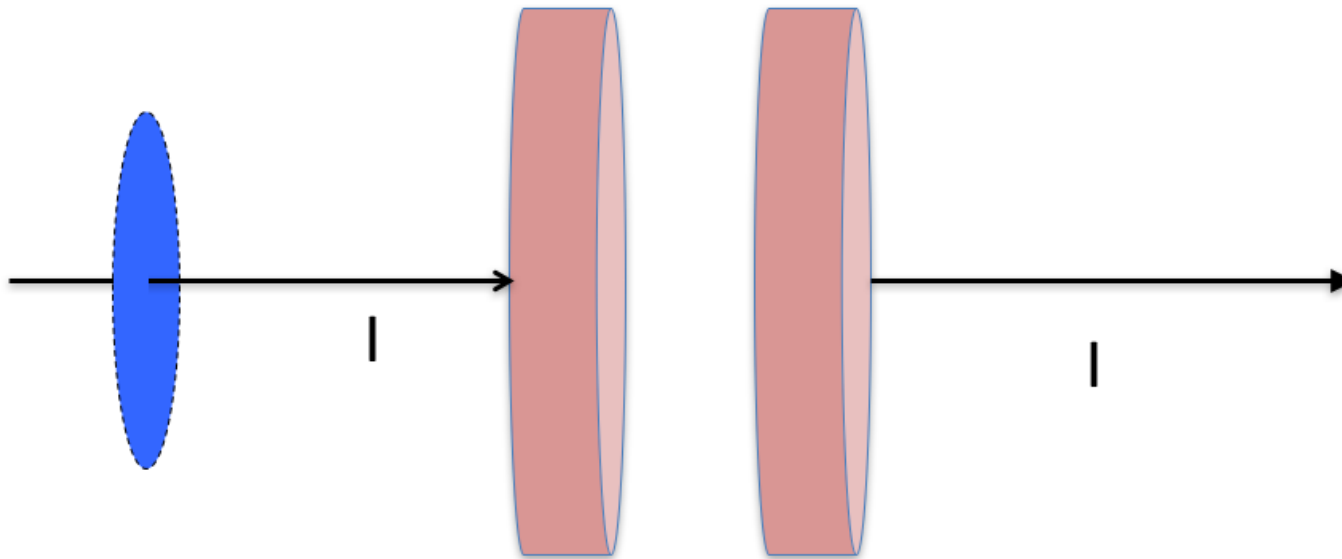
- A. $\text{iii} > \text{iv} > \text{ii} > \text{i}$
- B. $\text{iii} > \text{i} > \text{ii} > \text{iv}$
- C. $\text{i} > \text{ii} > \text{iii} > \text{iv}$
- D. Something else!!
- E. Not enough info given!!

We are interested in \mathbf{B} on the dashed "Amperian loop", and plan to use $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_t$ to figure it out. What is I_t here?



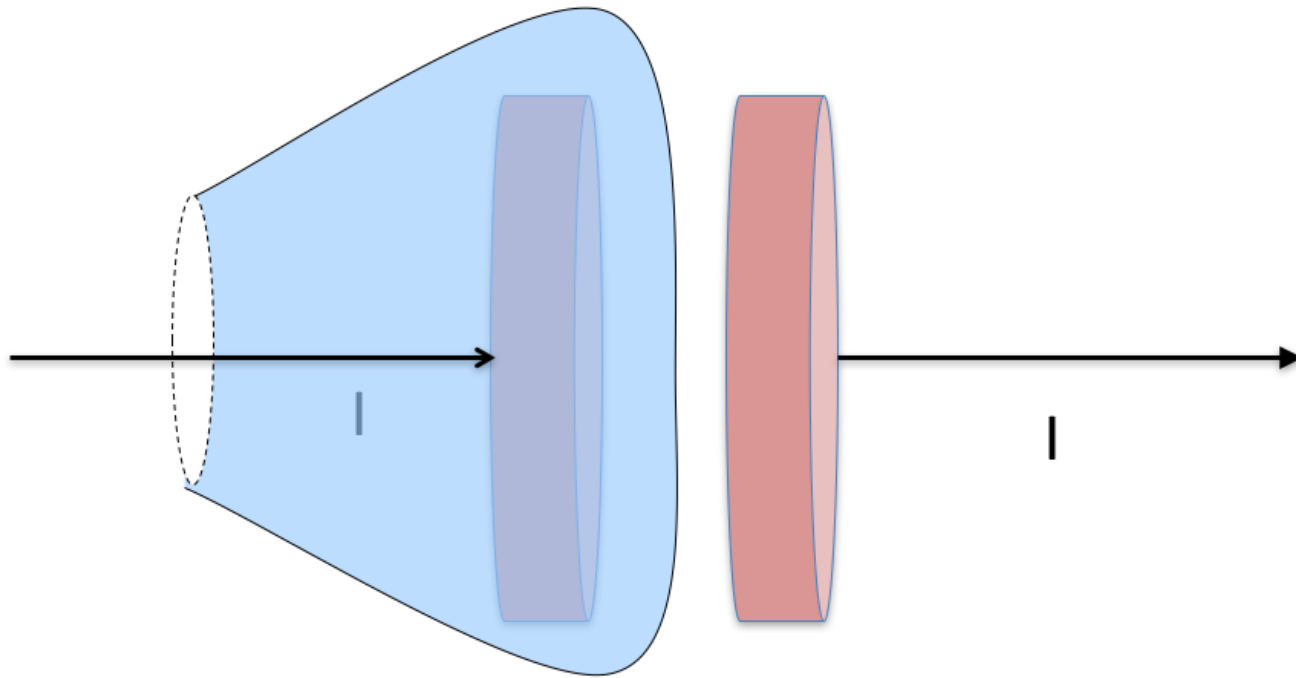
- A. I
- B. $I/2$
- C. 0
- D. Something else

We are interested in \mathbf{B} on the dashed "Amperian loop", and plan to use $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_t$ to figure it out. What is I_t here?
The surface over which we integrate $\mathbf{J} \cdot d\mathbf{A}$ is shown in blue.



- A. I
- B. $I/2$
- C. 0
- D. Something else

We are interested in \mathbf{B} on the dashed "Amperian loop", and plan to use $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_t$ to figure it out. What is I_t here? *The surface over which we integrate $\mathbf{J} \cdot d\mathbf{A}$ is shown in blue.*



A. I

B. $I/2$

C. 0

D. Something else

The complete differential form of Ampere's Law is now argued to be:

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}$$

The integral form of this equation is:

- A. $\iint \mathbf{B} \cdot d\mathbf{A} = \mu_0 I + \mu_0 \epsilon_0 \frac{d}{dt} \oint \mathbf{E} \cdot d\mathbf{l}$
- B. $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I + \mu_0 \epsilon_0 \frac{d}{dt} \oint \mathbf{E} \cdot d\mathbf{l}$
- C. $\iint \mathbf{B} \cdot d\mathbf{A} = \mu_0 I + \mu_0 \epsilon_0 \frac{d}{dt} \iint \mathbf{E} \cdot d\mathbf{A}$
- D. $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I + \mu_0 \epsilon_0 \frac{d}{dt} \iint \mathbf{E} \cdot d\mathbf{A}$
- E. Something else/???