STA302H1 – Final Report

Danny Chen

August 21, 2021

Introduction

The purpose of this report is to study the relationship between a student's country of origin, the time they spent studying for STA302H1 (weeks 1 - 4), the time they spent thinking about COVID-19 (weeks 1 - 4), and their interim STA302H1 quiz scores (quizzes 1 - 3) versus final STA302H1 quiz scores (quiz 4).

Existing studies in pedagogy tend to focus on individual factors that affect course performance, such as the number of hours slept, or the number of hours spent studying for a course. However, this study intends to explore multiple covariates simultaneously to assess their collective effect on final quiz grades, as well as the effects of two covariates on each other.

Information about Our Popoulation

The population of interest is a group of students from the online summer 2021 (July - August) STA302H1S cohort, which originally had 227 students at the start of the term, but has 198 students enrolled as of August 13, 2021.

Experiment Description

For this study, students were surveyed on Quercus at the end of each week for the first 4 weeks of STA302H1. Each week is specified by a date range below:

- End of Week 1 (July 5 – July 9)
- End of Week 2 (July 12 – July 16)
- End of Week 3 (July 19 – July 23)
- End of Week 4 (July 26 – July 30)

The survey asked about their country of origin (first week only), the number of hours they spent thinking about COVID-19, and the number of hours they spent studying for STA302H1. Quiz scores were also collected and combined into a dataset, where student names were anonymized before the dataset was made available to all STA302H1 students on Quercus for analysis during the STA302H1 final report.

Purpose of Developing A Model

The purpose of developing a model is to try to understand the relationship between quiz 4 scores and the other predictor variables (interim STA302H1 quiz scores, study time, COVID contemplation time, country, or some combination of these factors) in explaining the variability among quiz 4 marks.

If the model shows some relationship, it may be possible to use the regression model to determine which of the variables are strong predictors of Quiz 4 grades, and estimate unknown values for quiz 4 scores whenever the values of the independent variables are known.

Developing this model primarily benefits professors and students. Current professors can identify possible weak topics by identifying topics that yield the lowest quiz scores, reflect on things they did/did not help students, and then devote resources to improving lectures or creating carefully curated tutorials that address topics that students find challenging. Teaching stream professors and future STA302H1 professors would inherit these resources so they can establish reasonable STA302H1 learning goals, thoroughly prepare for more formative lectures, and address common student conceptual pitfalls that undermine student quiz scores.

When current STA302H1 students understand the most important factors that contribute to high quiz 4 grades, they can develop informed strategies that can help them effectively learn key material and maximize their grades on formative quizzes. Future students can establish reasonable expectations about workload and develop strategies to maximize their time and success in STA302H1 with available resources.

Plan for Developing Model

The dataset contained a small number of typos, which were cleaned manually rather than programatically. This included removing the word "hours" to safely cast numeric parts of strings as integers, removing non-Unicode characters like "UTF-098", and capitalizing "canada" and "china", so that they would be treated the same as the countries "Canada" and "China." To finish off the data cleaning process, similar columns (i.e., COVID times, study times, and quiz scores) were grouped together to make further data analysis more convenient.

Although some entries in the dataset contained missing (NA) data, missing quiz grades were considered more problematic than rows with only missing number of COVID hours, number of STA302H1 study hours, or even missing countries of origin. To preserve as much of the original dataset as possible, NA countries were categorized as unknown, and NA COVID hours and STA302H1 hours were ignored.

Students who miss 3 or more quizzes were removed from the original dataset, since they may not have quiz 4 scores available. Additionally, students without Quiz 4 scores were also removed.

(TODO: Also remove students without Quiz 4 scores either way?)

Due to the fact that influential outliers tend to have high residuals, they will be removed to prevent them from influencing the magnitude and direction of the regression coefficients, as well as the power of the overall power.

(TODO: Add influential outlier checks later on.)

Descriptive statistics such as histograms, boxplots, 5-number summaries, and pairs scatterplots will be created to reveal useful relationships that will help to inform the model selection.

Model diagnostics will be used to verify assumptions of the final model, and address whether or not any variable transformation or variable re-centering is necessary.

Lastly, scholarly research will be consulted to confirm the results and propose ways to improve the final model.

(TODO: Consult scholarly research.)

Explanatory Data Analysis

There are a total of 13 variables in the dataset. The response variable is a student's quiz 4 score, and the predictor variables are the remaining 12 variables: a student's country of origin, the time they spent thinking about COVID-19 during weeks 1 - 4, the time they spent studying for STA302H1 during weeks 1 - 4, and their Quiz 1 - 3 scores.

The following table describes each variable, its meaning, and its type:

Variable	Meaning	Type of Variable
Country	Student's country of origin	Categorical/nominal
Quiz_1_Score	Student's quiz 1 score out of 10	Ordinal numeric
Quiz_2_Score	Student's quiz 2 score out of 10	Ordinal numeric
Quiz_3_Score	Student's quiz 3 score out of 10	Ordinal numeric
Quiz_4_Score	Student's quiz 4 score out of 10	Ordinal numeric
COVID..hours.W1	Time student spent thinking about COVID-19 during Week 1 in hours	Continuous numeric
COVID..hours.W2	Time student spent thinking about COVID-19 during Week 2 in hours	Continuous numeric
COVID..hours.W3	Time student spent thinking about COVID-19 during Week 3 in hours	Continuous numeric
COVID..hours.W4	Time student spent thinking about COVID-19 during Week 4 in hours	Continuous numeric
STA302..hours.W1	Time student spent studying for STA302H1 during Week 1	Continuous numeric
STA302..hours.W2	Time student spent studying for STA302H1 during Week 2	Continuous numeric
STA302..hours.W3	Time student spent studying for STA302H1 during Week 3	Continuous numeric
STA302..hours.W4	Time student spent studying for STA302H1 during Week 4	Continuous numeric

Note that time spent studying for STA302H1 can include lecture time, review time, quiz time, or assignment time.

Relevant Tables and Figures for Noteworthy Variables

Histograms

Times spent thinking about COVID-19, study times, and quiz scores among all students were summarized using histograms. The green dotted vertical line represents the mean and the solid blue vertical line represents the median. Seven-number summaries were also included to display meaningful statistics such as the mean, median, minimum, maximum, 1st quartile, 3rd quartile, and the number of NAs.

The histograms for COVID hours during weeks 1 - 4 are all right skewed (mean > median), indicating that a few students tend to spend a lot of time thinking about COVID-19 during the week. The median times spent thinking about COVID-19 remained constant at 1 hour/week across all 4 weeks, however the mean time spent thinking about COVID-19 decreased for the first 3 weeks from a maximum of 3.7 hours in week 1 to a minimum of 2.227 hours in week 3, and increased from week 3 to week 4.

The histograms for study hours during weeks 1 - 3 are approximately normal with a few outliers in the right tail. However, study hours week 4 exhibits a right skewed distribution. In fact, the mean study time increased by approximately 23%, and the median study time increased by approximately 44% from week 3 to week 4.

The histograms for quiz scores during weeks 1 - 4 are all left skewed (mean < median), as few students tend to underperform on quizzes. The median for weeks 1, 3, and 4 remain at 8/10 points, except for week 3 which had a median of 8.8/10. Week 1 had the smallest difference between mean and median quiz scores (about 0.26/10 points), while week 2 has the largest divide between mean and median quiz scores (about 1.38/10 points).

Week 1 Time Spent on COVID-19

Week 2 Time Spent on COVID-19

Week 3 Time Spent on COVID-19

Week 4 Time Spent on COVID-19

Week 1 Time Spent Studying for STA302H1

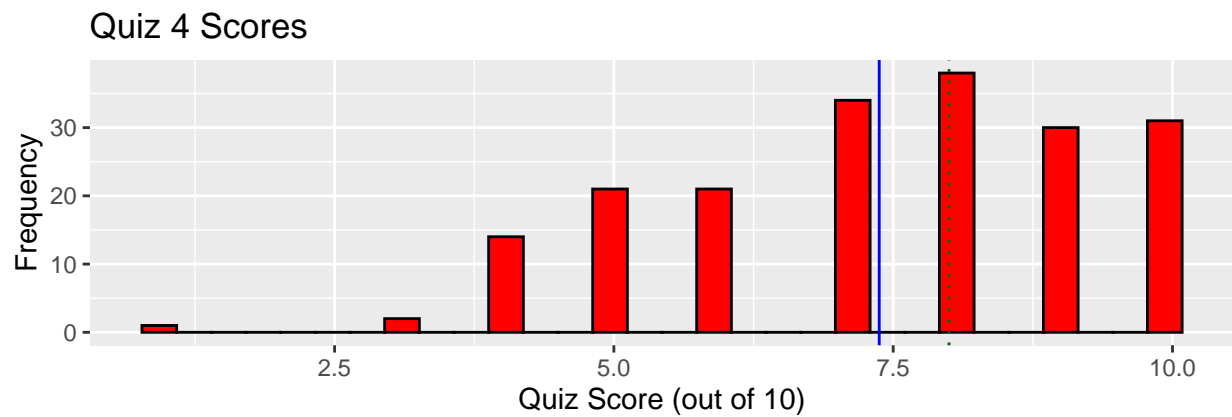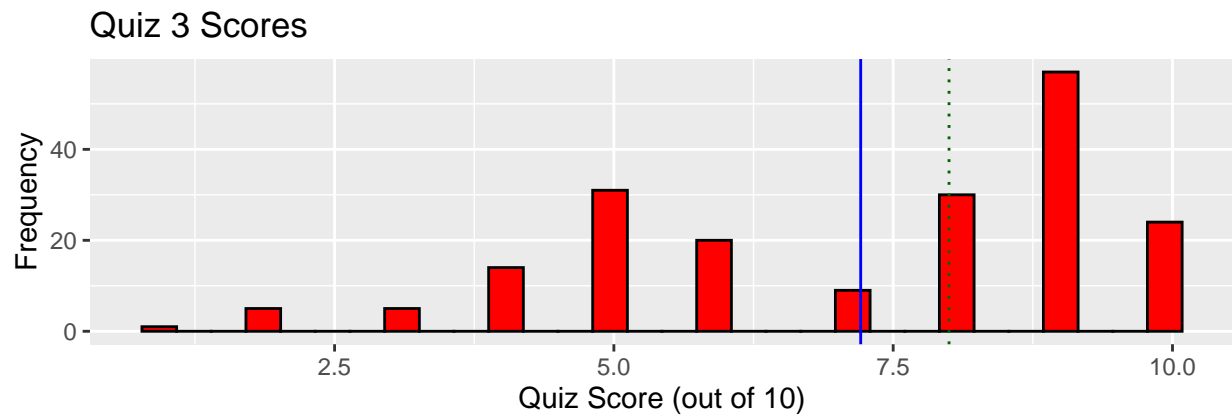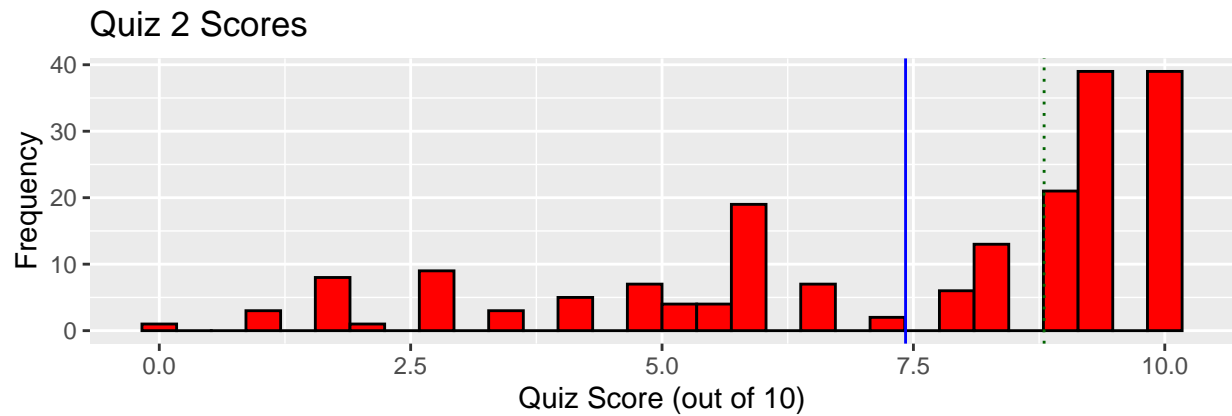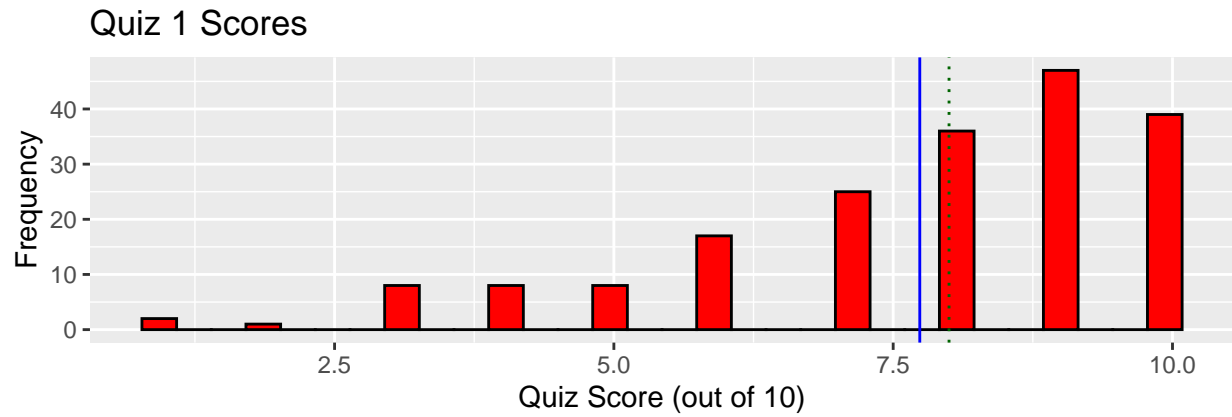## Week 2 Time Spent Studying for STA302H1

Week 3 Time Spent Studying for STA302H1

Week 4 Time Spent Studying for STA302H1

Quiz 1 Scores

Quiz 2 Scores

Quiz 3 Scores

Quiz 4 Scores

Boxplots

Side-by-side boxplots were used to compare COVID-19 times, study times, and quiz scores among students from various countries.

In week 1, most students from all countries spent a small amount of time thinking about COVID-19. Japan has the highest median COVID times, whereas India and USA have the lowest median COVID times. Clear outliers for Canada and China in all 4 weeks indicate that some Canadian and Chinese STA302H1 students were spending an above average amount of time thinking about COVID-19. Among all countries, Mongolia had the highest median COVID time during weeks 2 - 4. Pakistan and Singapore students also showed increased median and IQR COVID times between week 1 and week 2. Additionally, China and USA have the lowest median COVID times in week 2. In week 4, all countries returned to low median COVID-19 times, except for Mongolia which increased by approximately 150% from about 20 hours to about 50 hours).

Clear outliers exist for Canada in weeks 1 - 4, and China in weeks 1, 2, and 4. South Korea has the lowest median study time, wheras Japan has the highest median study time in week 1. Median study times in week 1 for a given country seem to fall within the IQR of other countries. This may indicate that median week 1 study times might not be statistically different from each other. More specifically, median study times for all countries fall between 0 - 10 hours.

In week 2, all countries have higher median study times compated to week 1, with Canada and China both having median study times of approximately 8 hours. The majority of median study times cluster between 5 - 10 hours, except for USA which has a median study time of approximately 20 hours – 300% more than week 1.

Roughly half of the countries saw a decrease in median study time, and other half saw an increase median study times in week 3. The boxplots for 7 out of 12 countries (China, India, Pakistan, Singapore, South Korea, UAE, and USA) all display approximately normally distributed study times. From week 3 to week 4, students from some countries increased their median study times from a range of 5 - 10 hours, to a range of 10 - 20 hours.

During week 1, the quiz scores for India, Singapore, Taiwan, and UAE students are all approximately normally distributed. Mongolia, Pakistan, and South Korea all had the highest median quiz scores roughly equal to the 75th percentile of Canada, China, and Singapore: around 9/10.

There were clear outliers for quiz scores among Chinese students in week 2. UAE has lowest median quiz score among all countries (1.25/10), while China and Taiwan have the highest median quiz scores among all countries (9.375/10). Among all countries, Canada and NA have the largest spread of quiz scores. Additionally, UAE decreased median quiz score from 4/10 to 1.25/10 (-68.75%), while Mongolia decreased median quiz score from 9/10 to 2/10 (-77.78%).

The median quiz scores for Canada, Pakistan, Singapore, Taiwan, and USA were all 7/10, whereas Japan and Mongolia have median quiz scores of 9/10 for week 4. The median quiz scores for most countries was between 7/10 and 9/10, with Japan, Mongolia, Singapore, South Korea, Taiwan, and USA having the smallest spread of quiz 4 scores.

(TODO: Display boxplot of COVID times weeks 1 - 4 against quiz 4 score.)
(TODO: Display boxplot of study times weeks 1 - 4.)
(TODO: Display boxplot of quiz scores 1 - 3.)

Pairwise Scatterplots and Correlation Matrix

Pairwise scatterplots were created to observe the relationships between all combinations of variables, especially between the response variable and the explanatory variables. Since the pairs scatterplot were symmetric along its main diagonal, the bottom half of the pairs scatterplot could be safely omitted.

Furthermore, a correlation matrix was constructed to determine the correlations of each pair of covariates along with the response variable and each covariate. Since the correlation matrices for underrepresented countries (i.e. every country except Canada, China, and NA) contained a lot of NA or ± 1 entries, it made more sense to use the correlation matrix for all countries. A correlation between 0.0 - 0.3 is considered low, 0.3 - 0.5 is moderate, and 0.5 - 1.0 is high.
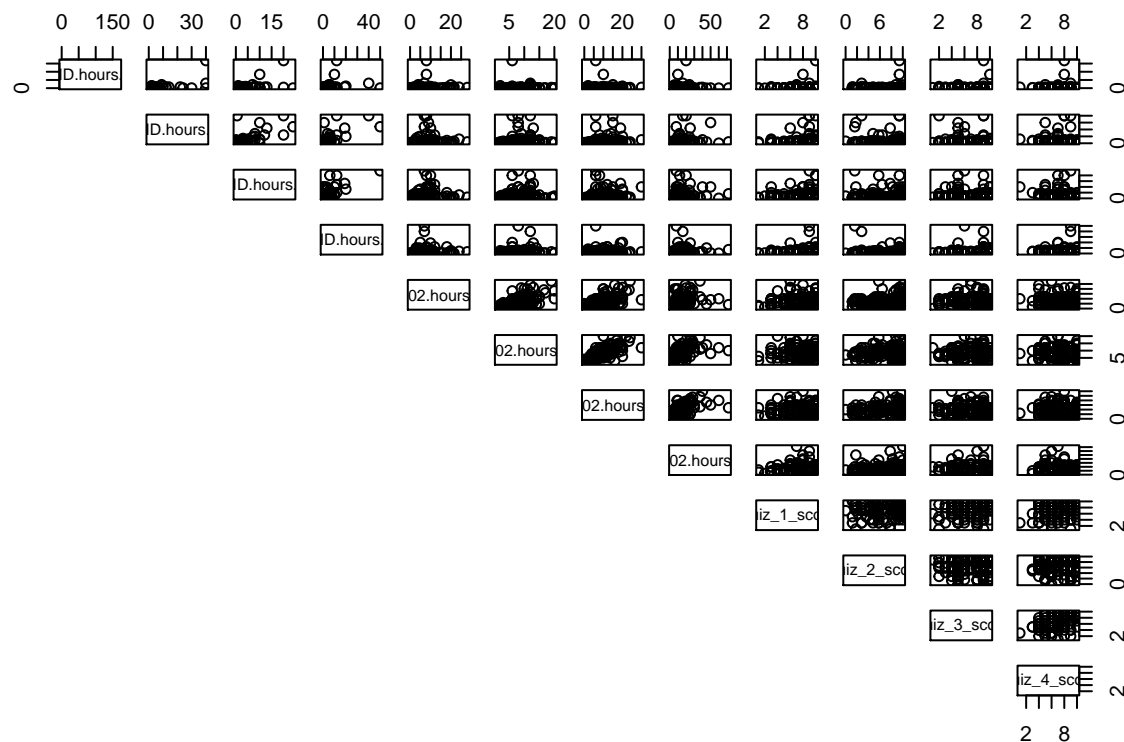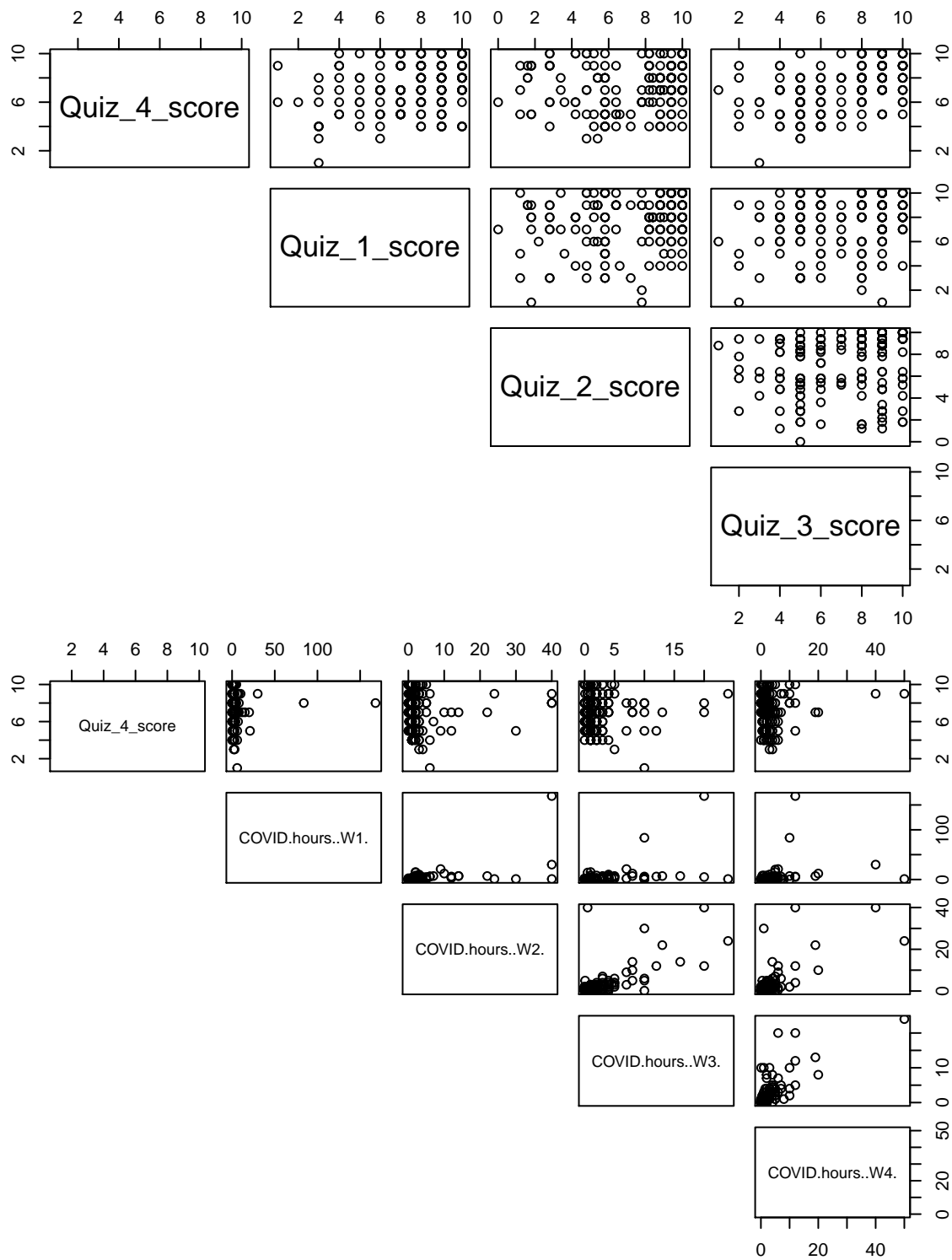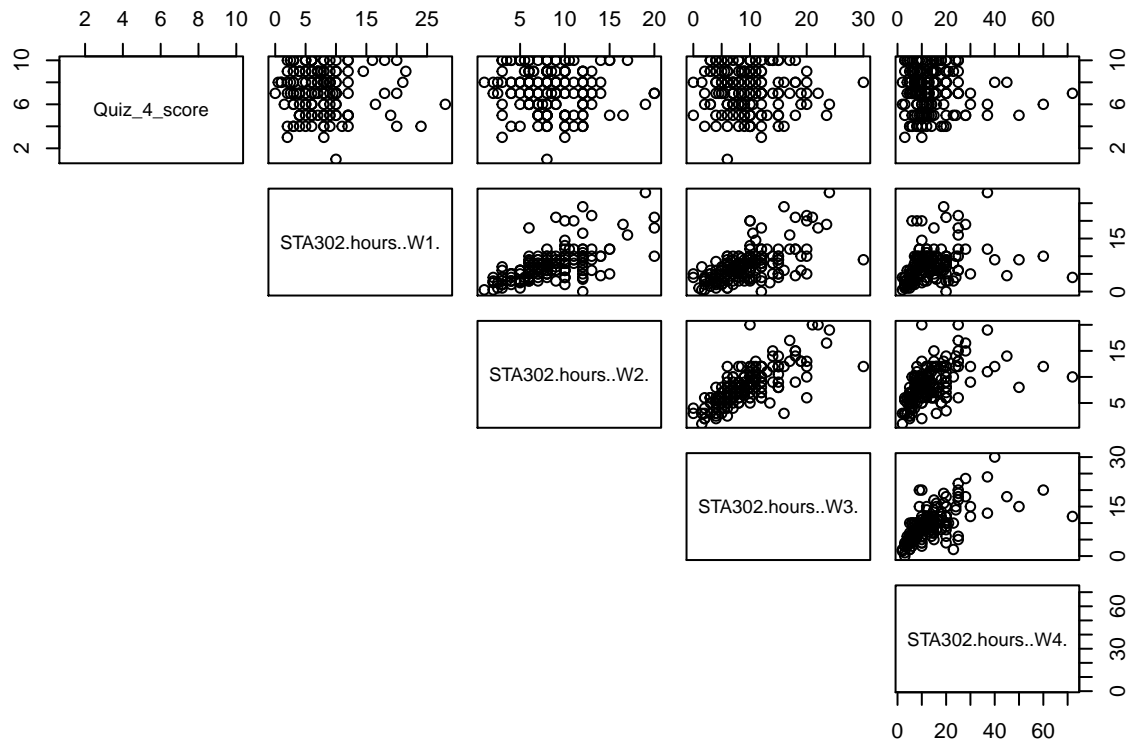
Model Development Section

Process Used to Determine Final Model

Checking for Influential Outliers

First, influential outliers were identified in the original dataset using (what method?)

(TODO: Use Cook's distance and leverage points to find influential outliers?)
(TODO: Use VIF method to find influential outliers?)
(TODO: Use DDFITS, DDBETA to find influential outliers?)

Notice that there are no influential outliers because no points outside of cook's distance in upper right and lower left quadrants of plot, so there are no points to remove.

Proposing an Initial Model

Simpler (e.g., linear, quadratic) relationships were prioritized over more complex relationships (e.g., higher order polynomial, logarithmic, square root) for the sake of straightforward analysis and intuitive interpretation. The pairs scatterplot and the correlation matrix were primarily used to derive most of the terms for the initial model.

The non-interactive covariate terms were determined by examining the pairs scatterplots for quiz 4 scores regressed on quiz 1 - 3 scores, weeks 1 - 4 COVID-19 times, and weeks 1 - 4 STA302H1 study times to hypothesize a relationship between quiz 4 scores and each predictor variable.

The weeks 1 - 4 COVID times vs. quiz 4 scatterplots show a moderate quadratic relationship between quiz 4 scores and weeks 1 - 4 COVID times (except for week 3 COVID, which seems to have a stronger linear relationship than a quadratic relationship). Therefore, both the linear and quadratic terms for weeks 1, 2, and 4 COVID times (i.e., `covid1`, `covid1 ** 2`, `covid2`, `covid2 ** 2`, `covid4`, and `covid4 ** 2` – along with `covid3` only) were included in the initial model.

Further analysis indicates that there is a possibly moderate linear relationship between quiz 4 scores and weeks 1 - 4 study times. Therefore, only the linear terms for weeks 1 - 4 study times (i.e., `study1`, `study2`, `study3`, and `study4`) were included in the model.

Similarly, there might be a moderate linear relationship between quiz 4 scores and quiz 1 - 3 scores. Therefore, only the linear terms for quiz 1 - 3 scores (i.e., `quiz1`, `quiz2`, and `quiz3`) were included in the model.

(TODO: Show scatterplot of covid1 vs. quiz4.)
(TODO: Display summary statistics for covid1 vs. quiz4 in appendix.)
(TODO: Show scatterplot of covid2 vs. quiz4.)
(TODO: Display summary statistics for covid2 vs. quiz4 in appendix.)
(TODO: Show scatterplot of covid3 vs. quiz4.)
(TODO: Display summary statistics for covid3 vs. quiz4 in appendix.)
(TODO: Show scatterplot of covid4 vs. quiz4.)
(TODO: Display summary statistics for covid4 vs. quiz4 in appendix.)

(TODO: Show scatterplot of study1 vs. quiz4.)
(TODO: Display summary statistics for study1 vs. quiz4 in appendix.)
(TODO: Show scatterplot of study2 vs. quiz4.)
(TODO: Display summary statistics for study2 vs. quiz4 in appendix.)
(TODO: Show scatterplot of study3 vs. quiz4.)
(TODO: Display summary statistics for study3 vs. quiz4 in appendix.)
(TODO: Show scatterplot of study4 vs. quiz4.)
(TODO: Display summary statistics for study4 vs. quiz4 in appendix.)

(TODO: Show scatterplot of quiz1 vs. quiz4.)
(TODO: Display summary statistics for quiz1 vs. quiz4 in appendix.)
(TODO: Show scatterplot of quiz2 vs. quiz4.)
(TODO: Display summary statistics for quiz2 vs. quiz4 in appendix.)
(TODO: Show scatterplot of quiz3 vs. quiz4.)
(TODO: Display summary statistics for quiz3 vs. quiz4 in appendix.)

Pairs of covariates, as well as response variable-covariate combinations from the correlation matrix with high correlation were used as a heuristic for determining potentially significant interaction terms in the initial model.

The initial model was fitted using `quiz4` as the response variable; and `quiz1`, `quiz2`, `quiz3`, `covid1`, `covid2`, `covid3`, `covid4`, (including 3 quadratic terms 8 interaction terms), and `country` as predictor variables. However, only the predictor variables `quiz3`, `I(covid1 ** 2)`, `I(covid2 ** 2)`, `I(covid1 * covid2)`, and `I(study1 * study2)` were significant at the 5% significance level. The global F-statistic value is 3.098, and the global p-value is approximately 1.436×10^{-5}. The residual standard error is 1.582. The multiple R^2 value is 0.4211 and the adjusted R^2 value of 0.2851.

Characteristic	Beta	95% CI	p-value
quiz1	0.03	-0.13, 0.20	0.7
quiz2	0.05	-0.07, 0.17	0.4
quiz3	0.48	0.32, 0.63	<0.001
covid1	0.18	-0.07, 0.43	0.2
I(covid1^2)	0.02	0.00, 0.03	0.029
covid2	0.29	-0.09, 0.67	0.13
I(covid2^2)	-0.02	-0.05, 0.00	0.046
covid3	-0.05	-0.30, 0.20	0.7
covid4	-0.25	-0.55, 0.06	0.11
I(covid4^2)	0.02	-0.01, 0.05	0.2
I(covid1 * covid2)	-0.07	-0.14, -0.01	0.029
I(covid2 * covid3)	0.05	-0.01, 0.11	0.12
I(covid2 * covid4)	0.04	-0.01, 0.09	0.093
I(covid3 * covid4)	-0.08	-0.18, 0.02	0.13
I(study1 * study2)	-0.02	-0.03, 0.00	0.018
I(study1 * study3)	0.01	0.00, 0.02	0.14
I(study2 * study3)	0.01	0.00, 0.02	0.095
I(study3 * study4)	0.00	0.00, 0.00	0.14
country			
Canada			
China	0.59	-0.10, 1.3	0.092
India	0.87	-1.5, 3.2	0.5
Mongolia	-13	-51, 26	0.5
Pakistan	-0.15	-3.3, 3.0	>0.9
Singapore	1.2	-2.1, 4.5	0.5
South Korea	-0.02	-2.3, 2.3	>0.9
Taiwan	-1.2	-3.5, 1.1	0.3
UAE	-0.63	-3.9, 2.6	0.7
USA	1.5	-2.0, 5.0	0.4

Improving the Original Model

To refine the original model, backwards selection was used to remove insignificant terms (terms whose p-values were > 0.05) and find the subset model with the lowest AIC value.

The final model has `quiz4` as the response variable; `quiz3`, the quadratic term `I(covid1 ** 2)`, and the interaction terms `I(covid1 * covid2)`, `I(covid2 * covid3)`, `study1 * study2`, `study1 * study3`, `study2 * study3`, `study3 * study4` as the predictor variables. Out of all of the predictors variables in the final model, only the predictor variables `quiz3`, `I(covid1 ** 2`, `I(covid1 * covid2)`, `I(study1 * study2)`, `I(study2 * study3)`, and `I(study3 * study4)` are significant at the 5% significance level. The global F-statistic value increased to 8.764, the global p-value increased to 1.374×10^{-9}. The residual standard error decreased marginally to 1.561. Even though the multiple R^2 value dropped significantly to 0.3435, the adjusted R^2 value increase slightly to 0.3043 – there is a smaller difference between the R^2 value and the adjusted R^2 value in the final model than the original model. The coefficient of 0.499110 for `quiz3` suggests that for every 1 point increase in quiz 3, there is an increase in quiz 4 grades by about 0.50/10 points. There also exists a quadratic relationship between variables `covid1` and `quiz4`, as well as an interaction effect between `covid1` and `covid2`, `study1` and `study2`, `study2` and `study3`, and `study3` and `study4`. I perform all further analyses on the final model.

| Characteristic	Beta	95% CI	p-value
quiz3	0.50	0.38, 0.62	<0.001
I(covid1^2)	0.00	0.00, 0.01	0.046
I(covid1 * covid2)	-0.02	-0.04, 0.00	0.043
I(covid2 * covid3)	0.00	0.00, 0.01	0.066
I(study1 * study2)	-0.02	-0.03, 0.00	0.014
I(study1 * study3)	0.01	0.00, 0.02	0.2
I(study2 * study3)	0.01	0.00, 0.02	0.029
I(study3 * study4)	0.00	0.00, 0.00	0.035

Statistical and Empirical Justifications for Final Model

To show that a quadratic relationship for the final model is valid, the following assumptions must hold.

### Assumption 1. Quadratic Relationship

Since the quiz 4 vs. covid1 scatterplot in figure X indicates a moderate quadratic relationship between the variable, and the residual vs. covid1 plot for the fitted model is random, the final model has a quadratic relationship.

Residual Plot for Variable covid1
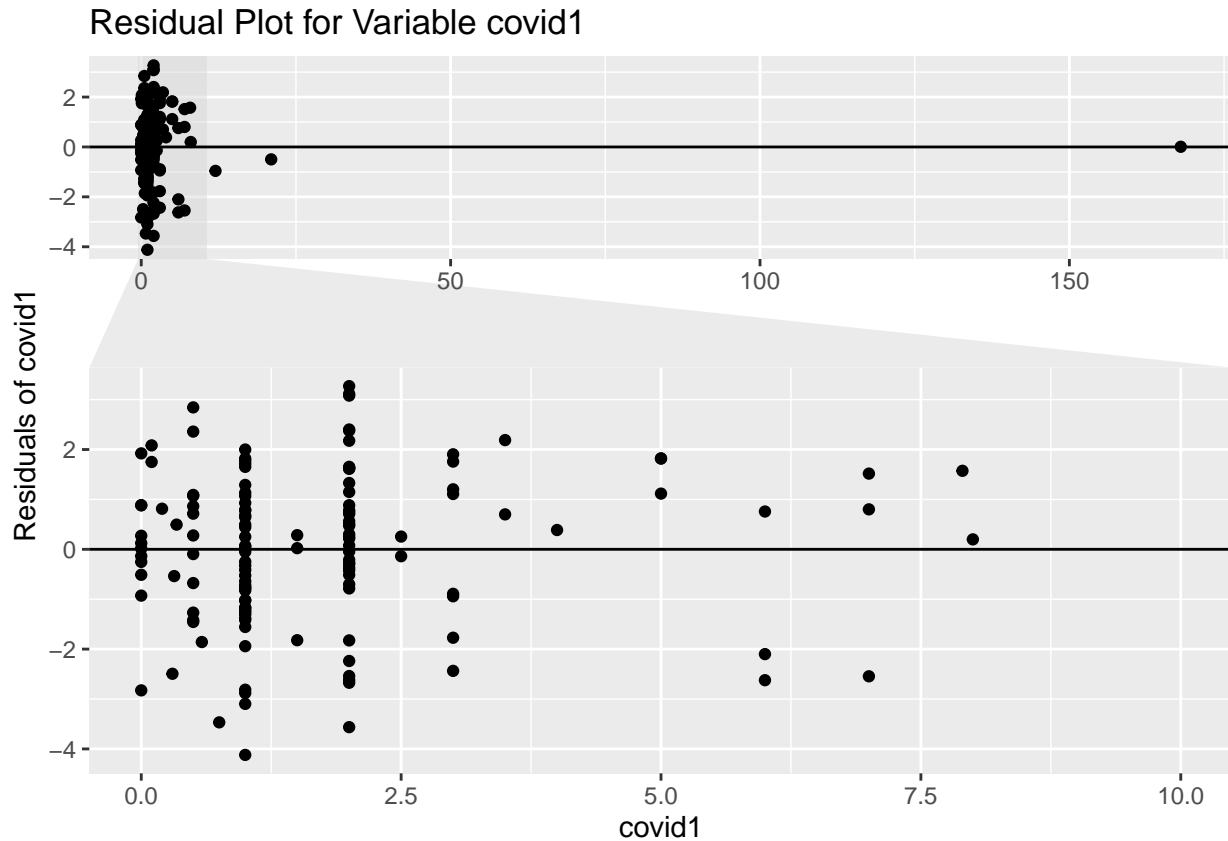
Assumption 2. Independence of Errors

From above, the residual vs. covid1 plot for the fitted model show no discernible relationship, and neither do the residual plots for the other predictor variables (ingoring all outliers). The dataset comes from a random sample, so the error terms must be independent.

Residual Plot for Variable quiz3
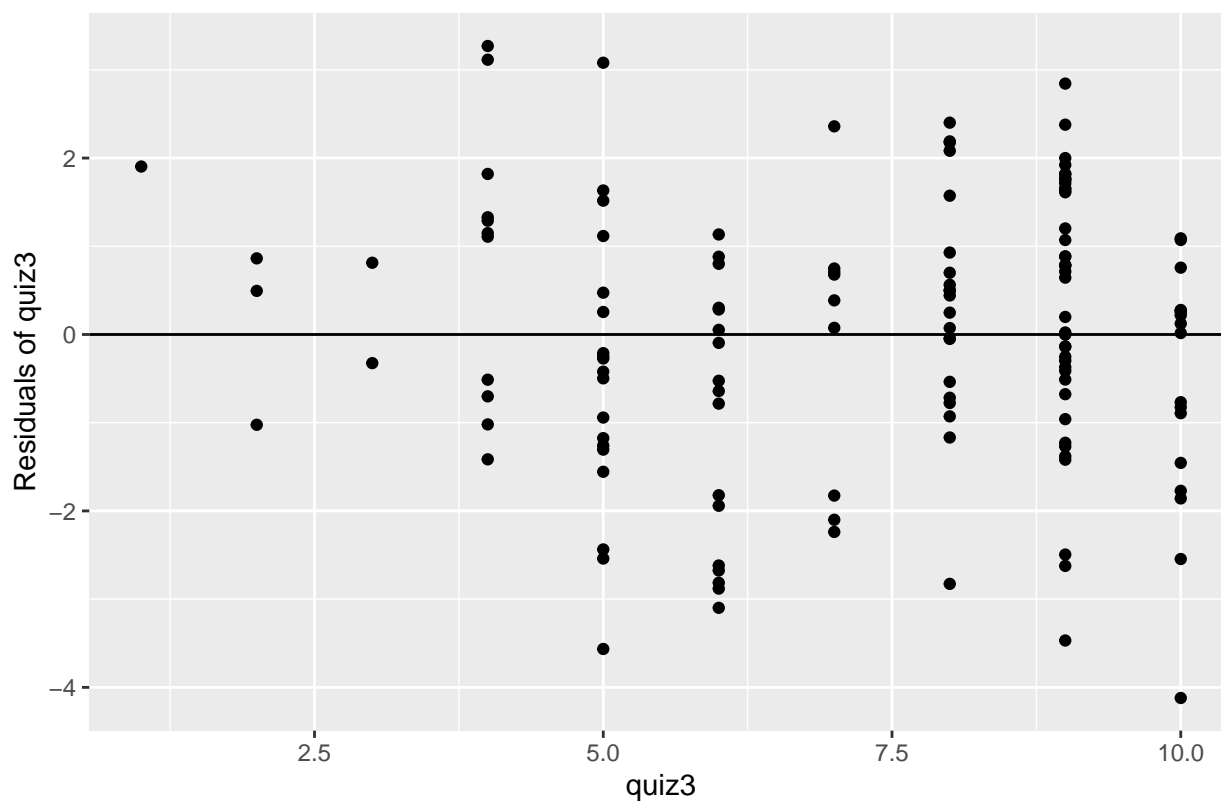
Residual Plot for Variable covid1 ^ 2
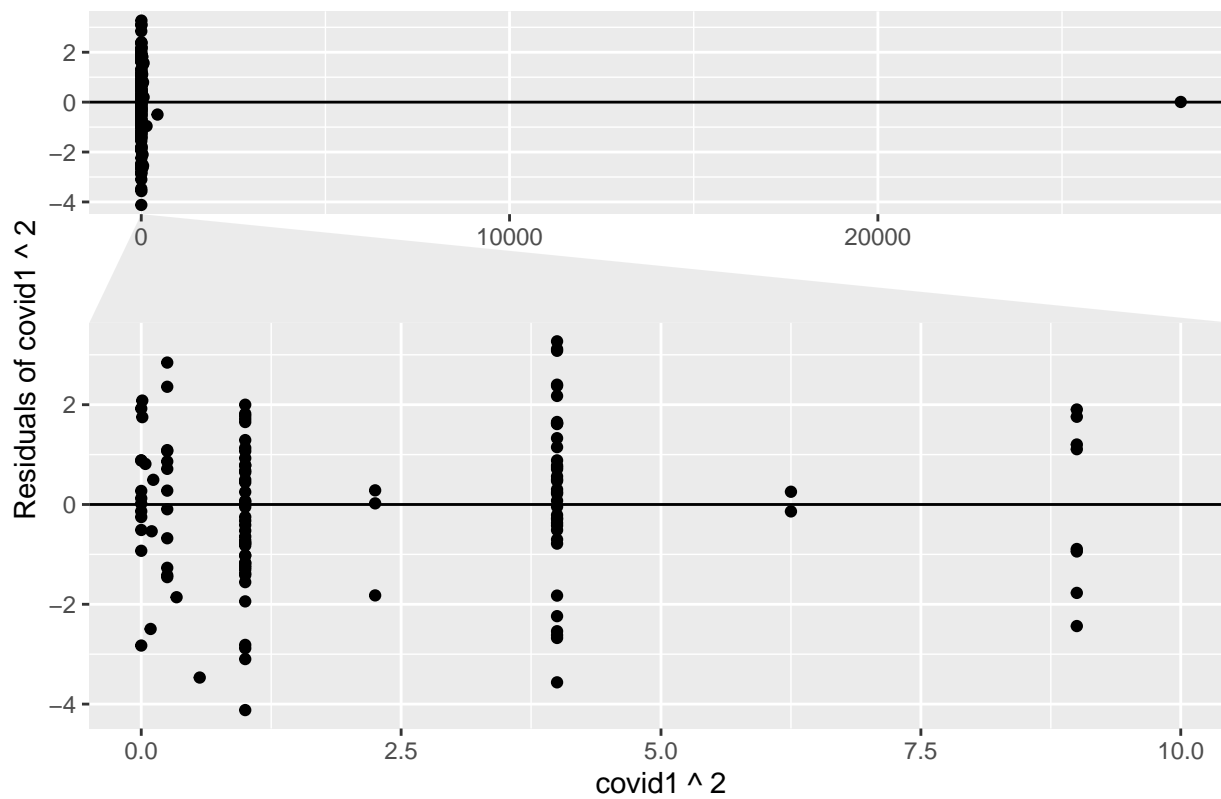
Residual Plot for Variable covid1 * covid2

Residual Plot for Variable covid2 * covid3

Residual Plot for Variable study1 * study2

Residual Plot for Variable study1 * study3
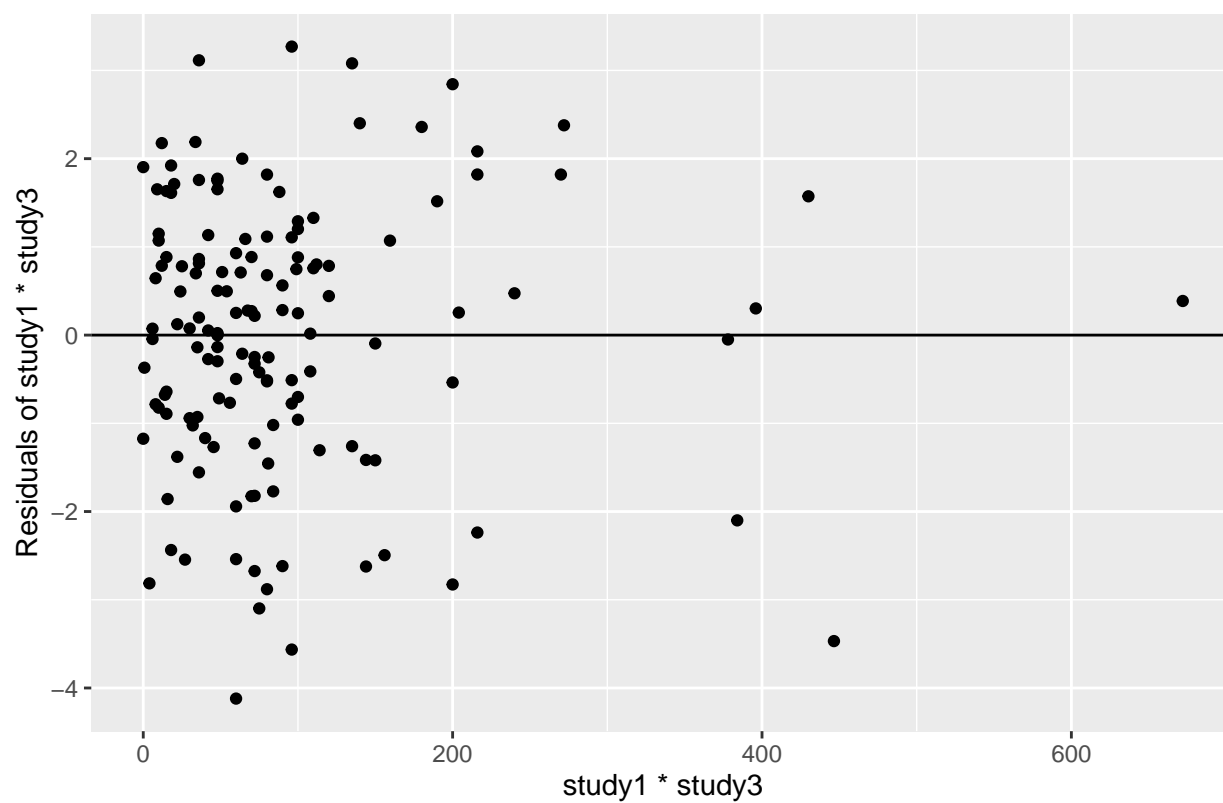
Residual Plot for Variable study2 * study3
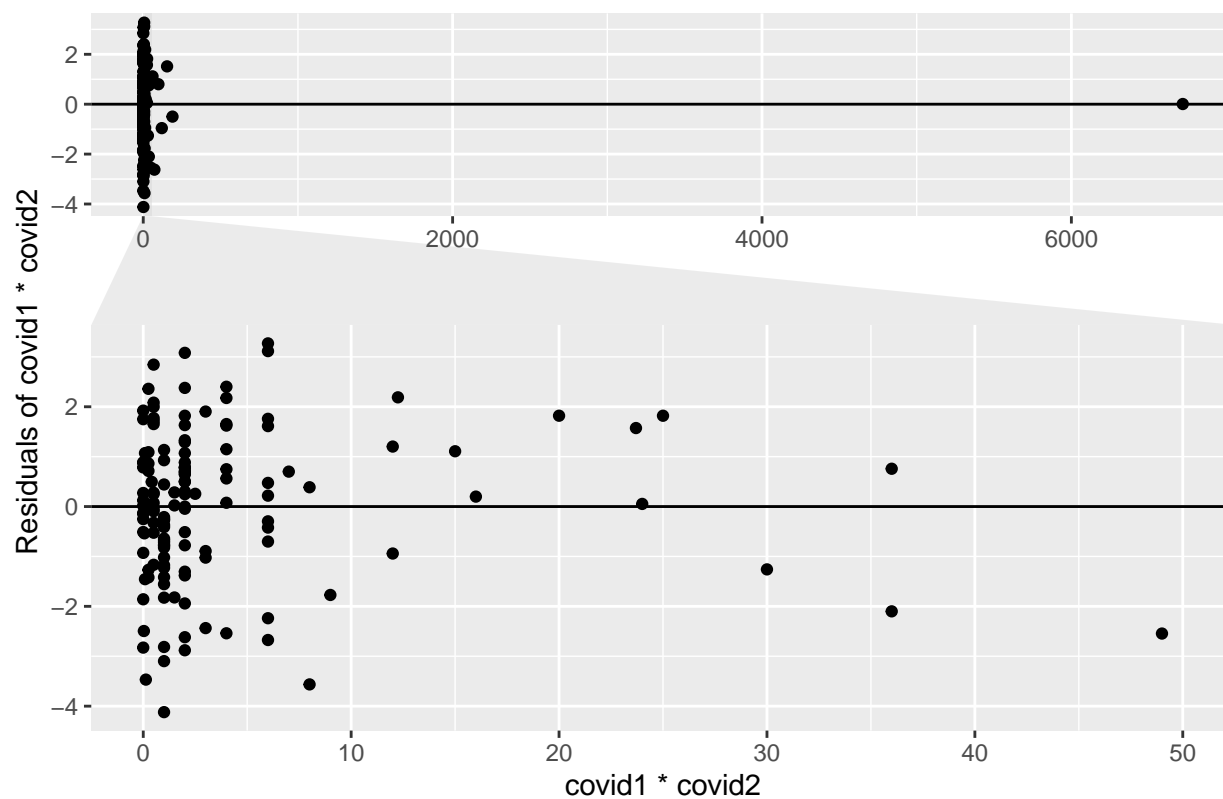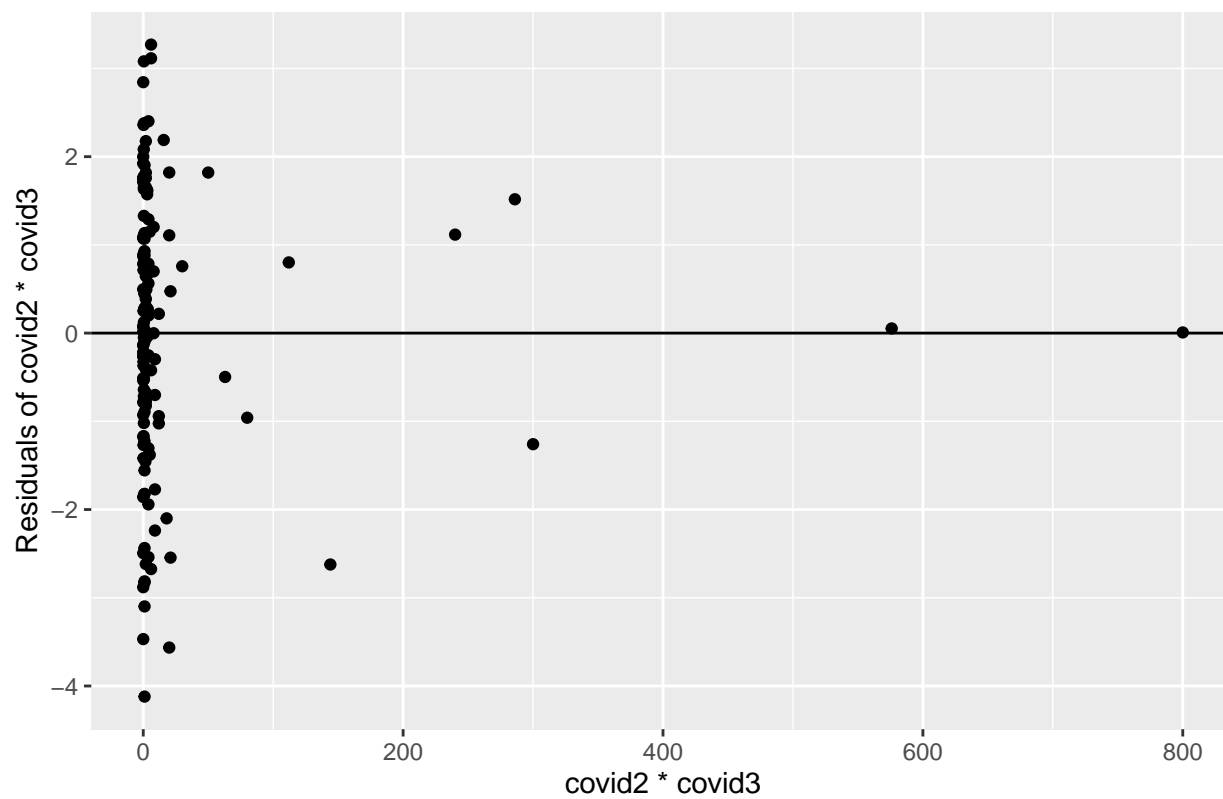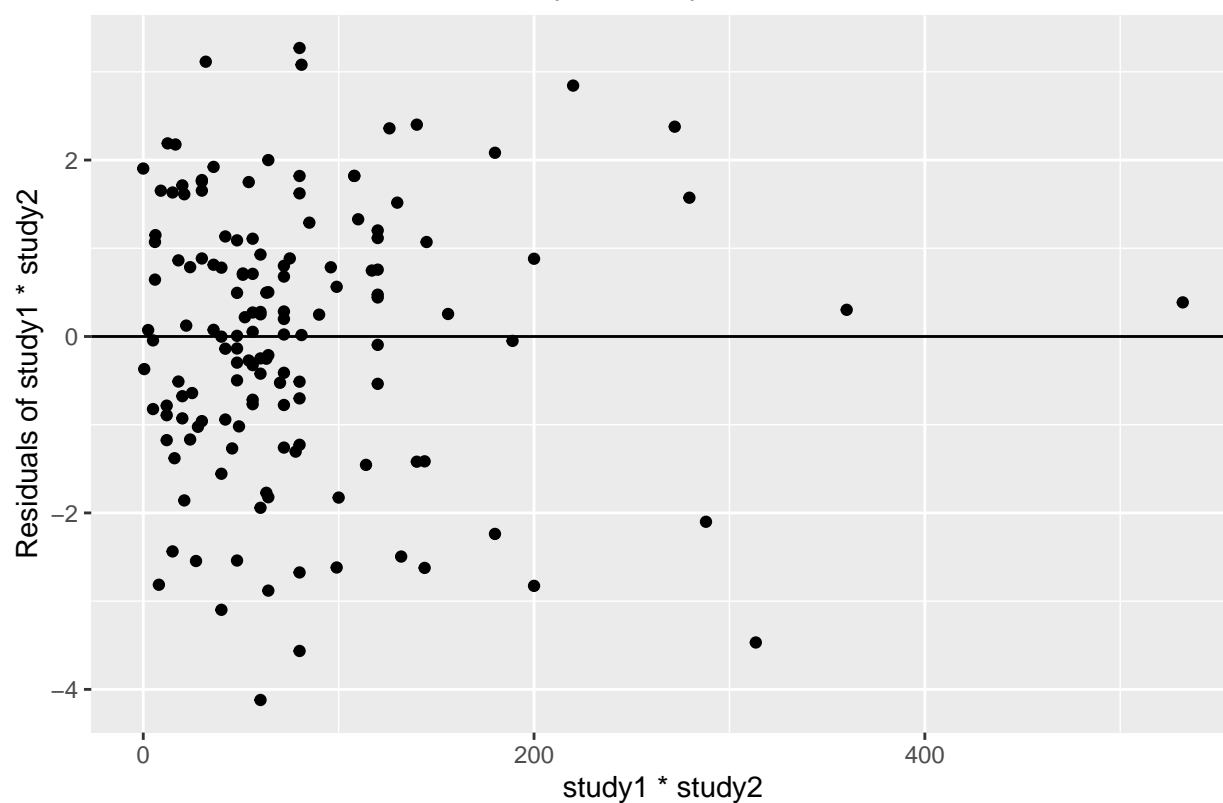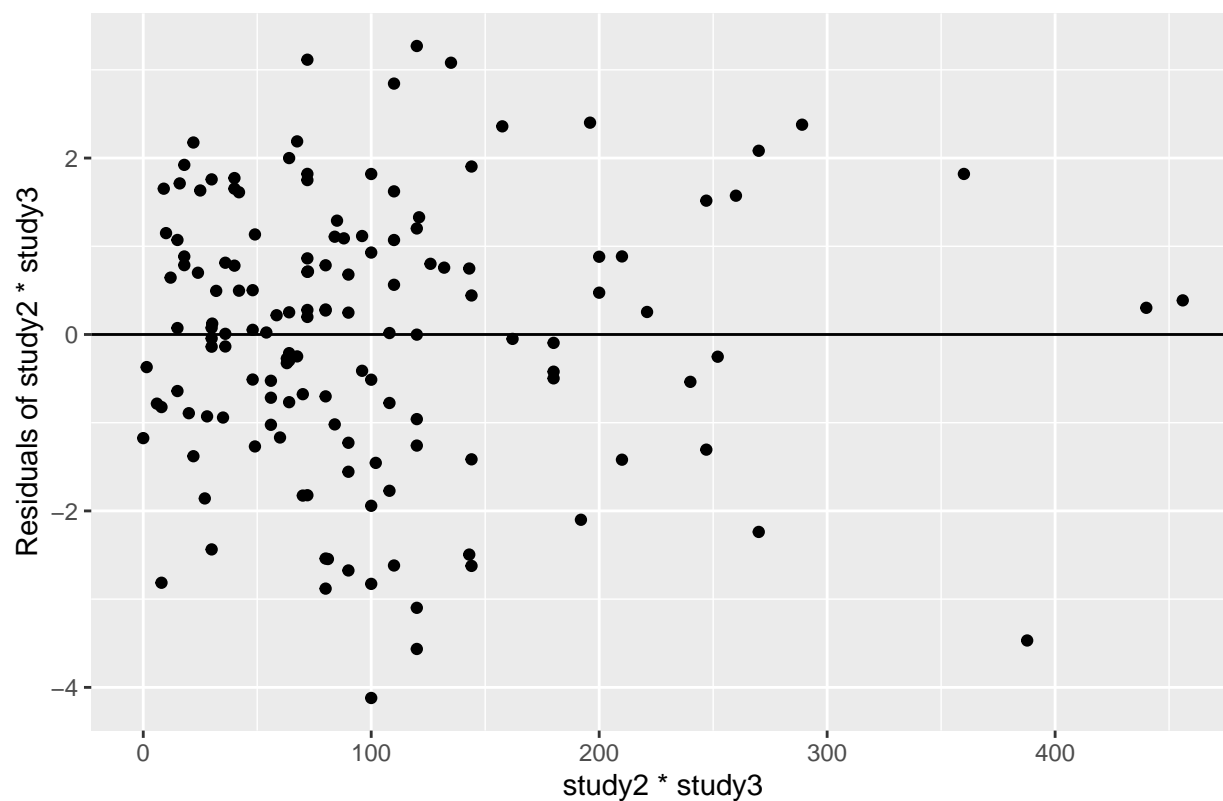

Residual Plot for Variable study3 * study4
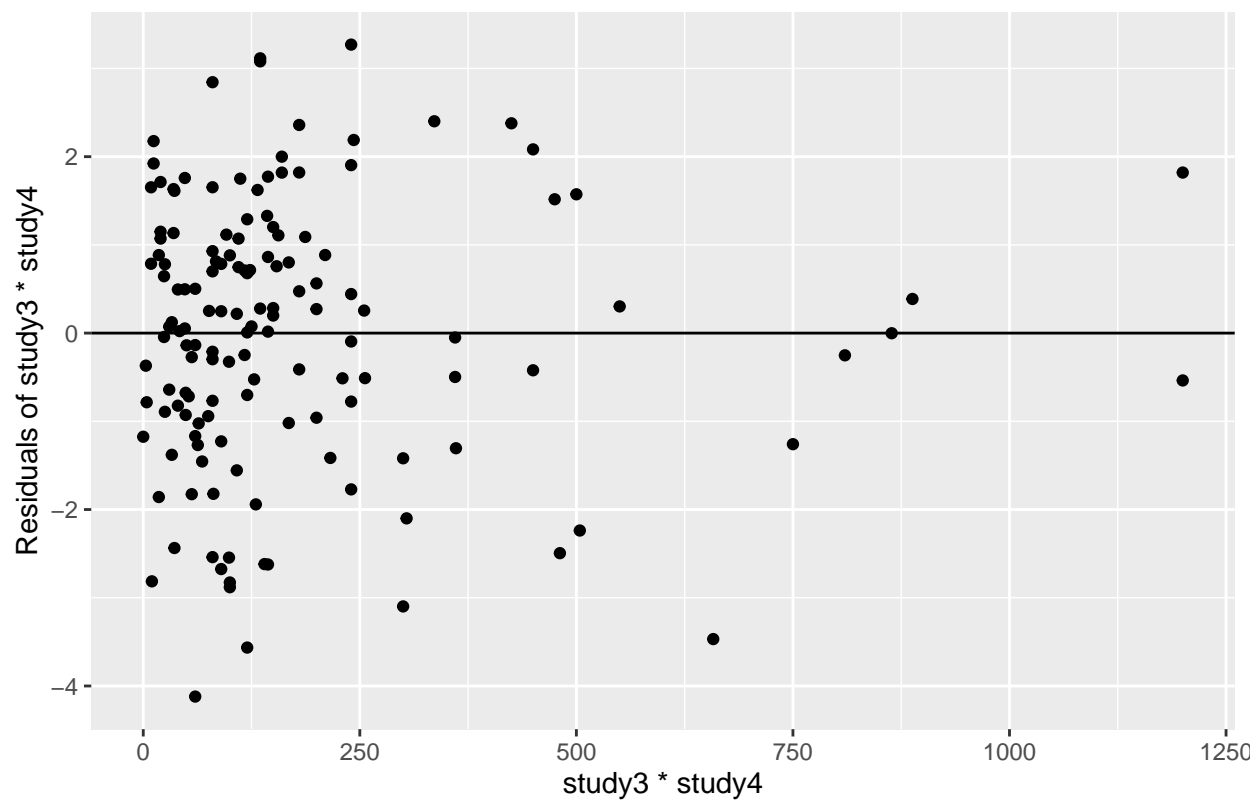
Assumption 3. Homoscedasticity (constant variance)

The scale-location model appears to have a straight horizontal line with randomly spread points, and the residual vs. fitted model show equally spread residuals around the horizontal line. Additionally, the residual plots for all predictor variables do not show any trend as fits increase. Therefore, the errors terms have constant variance.

Assumption 4. Normality of Error

Almost all of the points in the middle follow the QQplot line very closely, except for the last 2 points in the right-tail which is only a little bit right-skewed. By inspection, the histograms of residuals for the final model looks approximately normal. Therefore, the error terms are approximately normal.

Hence, our model satisfies the assumptions for a quadratic model.

Residuals vs Fitted

Fitted values
lm(quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) + I(covid2 * covid3) + ...

Normal Q–Q

Theoretical Quantiles
lm(quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) + I(covid2 * covid3) + ...

Scale–Location

Fitted values
lm(quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) + I(covid2 * covid3) + ...

Residuals vs Leverage

lm(quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) + I(covid2 * covid3) + ...

Histogram of Residuals
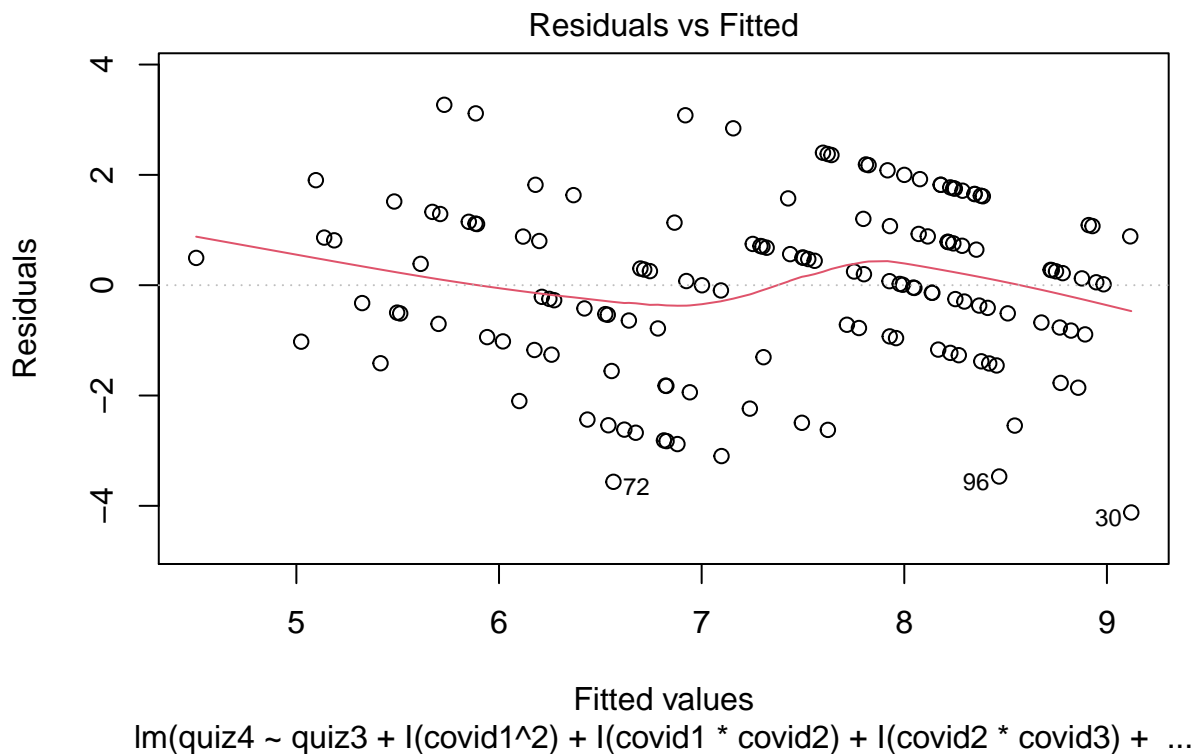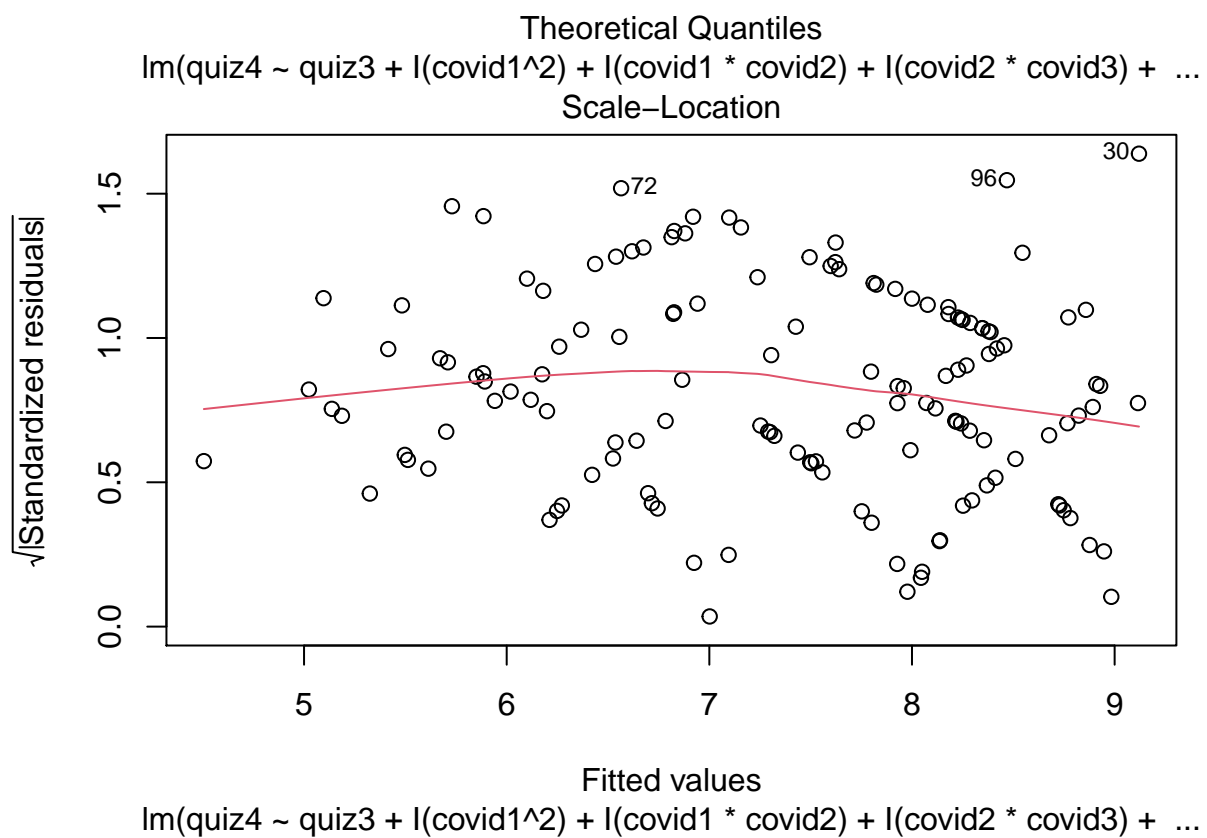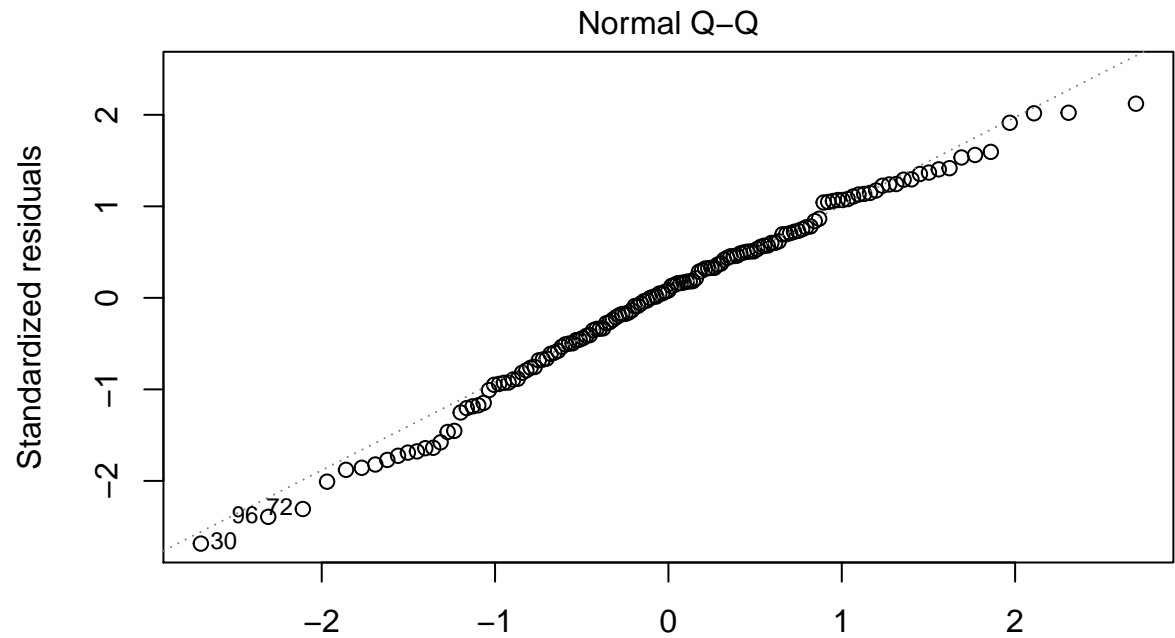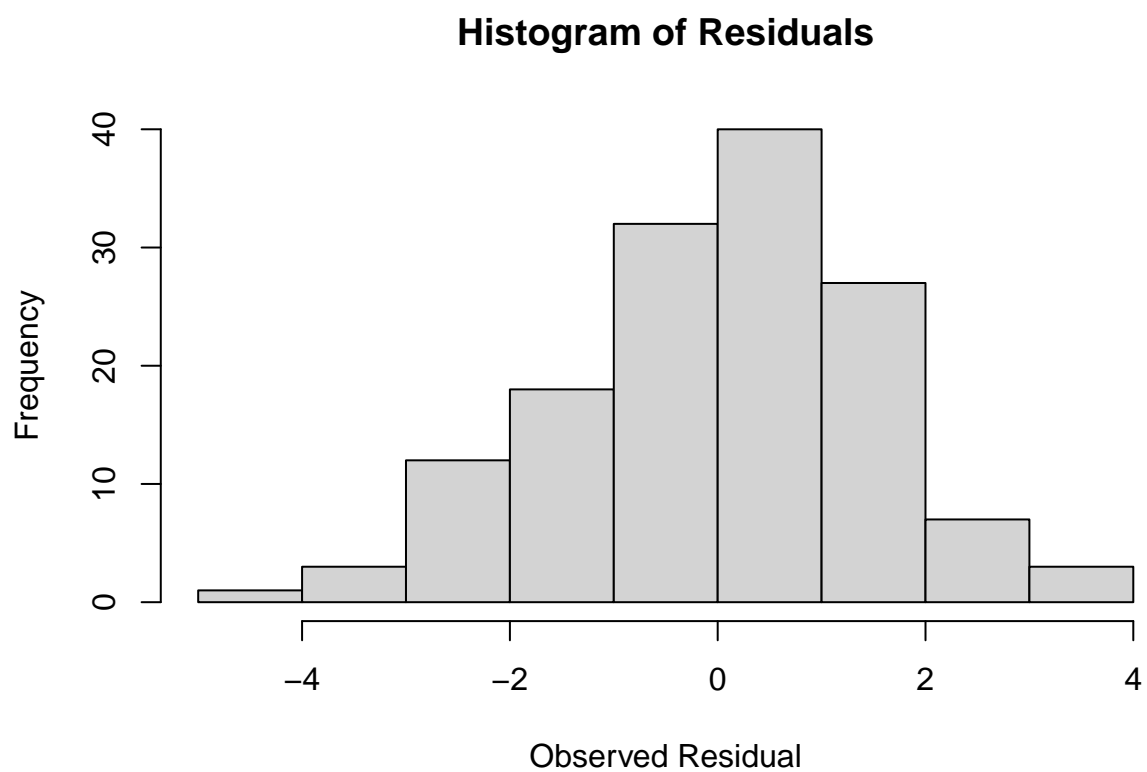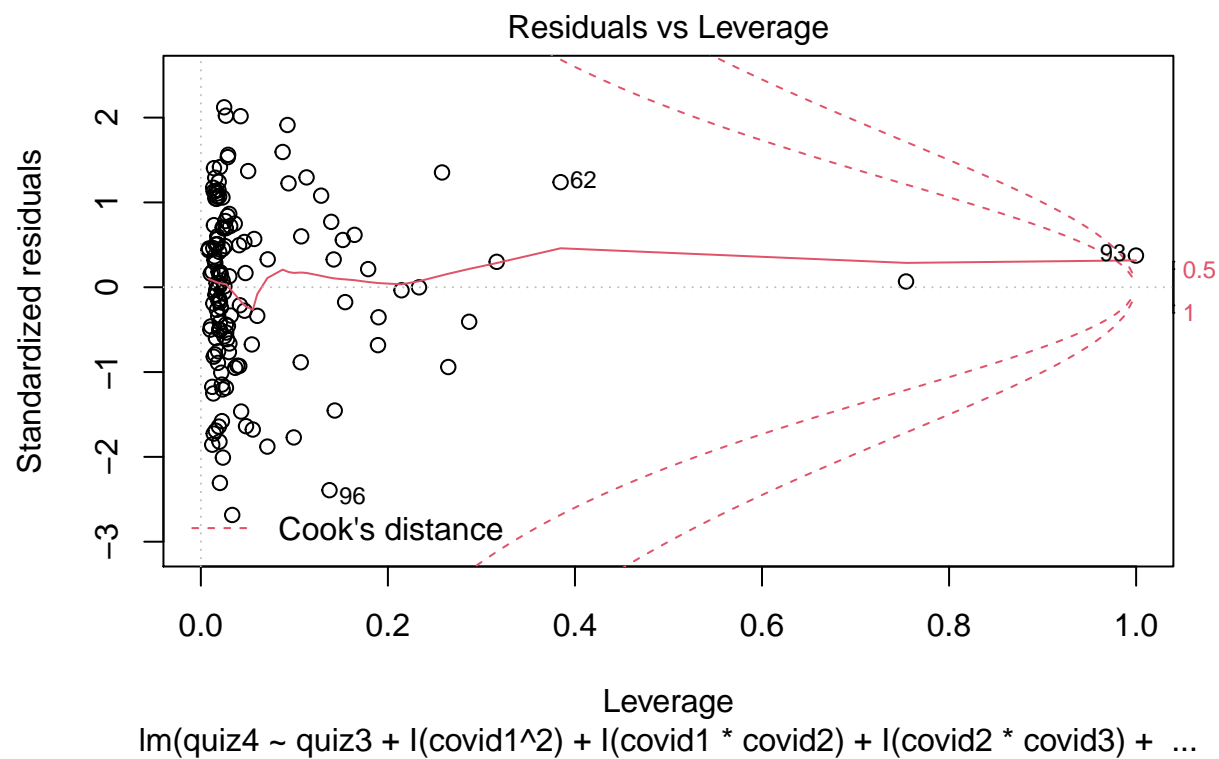
Any Variable Transformation or Recentering Necessary?

No variable transformations were performed on the final model because the error terms are independent, homoscedastic, and approximately normal.

No variable re-centering was required since only a few entries in the correlation matrix have high correlation. Most of the entries in the correlation matrix had low to moderate correlation, so re-centering variables likely has negligible effect on the correlation matrix.

In-Depth Diagnostics to Verify Goodness of Model

To validate my linear model, I decided to use a 55/45 training-testing strategy, as well as perform a t-test for significance.

55/45 Training/Testing Split

Out of $n = 142$ data points, I want to use 55% of the data points to train my linear model, and the remaining 45% to try to predict new values and create a new distribution to see if the mean of this new distribution is close to 0.

I found that the mean of this new distribution is 8.124×10^{-15} (see figure X in appendix).

(TODO: Add histogram of residuals for trained model.)
(TODO: Add mean/median residual output.)

Moreover, the histogram of residuals looks approximately symmetric, with the mean of this new distribution being -0.2102 (see figure X in appendix). To be sure, since there are $n = 142$ points, the central limit theorem states that the sample mean is approximately normally distributed.

T-test for significance

For our t-test, we hypothesized that the mean of residuals was identically equal to 0. More formally,

- $H_0 : \mu_{residuals} = 0$
- $H_1 : \mu_{residuals} \neq 0$

(TODO: Add t-test results in a nice table.)

The t-test results showed that the p-value is 0.7938, which means that we fail to reject H_0, meaning that $\mu_{residuals} = 0$ holds. The 95% confidence interval for the mean of residuals is $(-0.4510668, 0.3462948)$, and since $0 \in (-0.4510668, 0.3462948)$, we again fail to reject H_0 and conclude that $\mu_{residuals} = 0$.

(TODO: See figure X in appendix for t-test output.)

Therefore, we've shown that our linear model is a reasonable model.

Conclusion

Purpose of Final Model

Recall that the purpose of the model is to see whether previous quiz scores, time spent thinking about COVID, and study time can predict future quiz scores.

Interpretation of Final Model

The final model suggests a strong evidence of a positive relationship between quiz 3 scores and quiz 4 scores, as well as study times between consecutive weeks (i.e., (STA302W1, STA302W2), (STA302W2, STA302W3), (STA302W3, STA302W4)), keeping all other variables constant.

Quiz 3 is much closer in difficulty to Quiz 4 because students are used to the online Quercus quiz format. Students better understood how many decimal places they should round their final answers to from Quizzes 1 and 2, and the style of Quiz 3 questions are very similar to Quiz 4. Students also ramped up their study efforts as they anticipated more challenging quizzes as the semester progressed.

Although STA302H1 studying increased throughout the semester, the final model suggests that students who made a consistent effort to start studying during the 1st week of classes tend to score higher than students who started studying during the 2nd or 3rd week of classes. (TODO: Insert author here) shows that studying many hours last minute (mass learning) is less effective than studying a few hours a day throughout the term (spaced learning). By studying frequently throughout the semester, students have more opportunities to review STA302H1 material and their STA302H1 knowledge has more time to "compound" throughout the semester.

(TODO: Insert scholarly source about how far students start studying for quizzes in advance vs. test scores.) (TODO: Insert scholarly source about how far students start studying for quizzes in advance improves material retention.)

Generalizability of Model

This model is only generalizable to online courses rather than in-person courses. Students may enroll in online courses from various time zones, as opposed to a standardized time zone for in person courses. STA302H1 is also a 3rd year course, so naturally 3rd year students tend to study more for their courses and score higher on average on quizzes than 1st year students.

Remaining Limitations and Problems with Model

This model fails to capture variables such as weekly anxiety levels, the weekly number of hours students sleep, and the weekly number of hours students participate in physical activity.

(TODO: Studies show high anxiety impairs course performance) (TODO: Studies show high anxiety and more COVID think time) (TODO: Studies show moderate sleep improves course performance) (TODO: Studies show moderate exercise improves course performance)

The final dataset excluded 28 STA302H1 dropped students, and some blank entries remained for missing survey responses, and missing quiz scores remained due to some students skipping quizzes.

Some students may have underreported the number of study hours under the assumption that it only involves the number of hours spent attending lectures and the number of hours spend reviewing lecture notes, when in fact some students included hours spent doing assignments, writing quizzes, and even hours spent attending office hours – overall the number of hours spent doing any kind of coursework for STA302H1.

Despite these limitations, further research may help inform us on benefits of study and COVID think times vs. quiz scores.

Proposed Improvements with Model

One way to improve the model is to introduce composite variables in the model, such as a student happiness index as a function of a student's anxiety levels, COVID, and physical activity.

Another improvement is to use empirical research to propose some more new terms to improve model.

Another improvement to this model is to take the median of a student's 1 - 3 quizzes that they wrote, the median of a student's 1 - 4 COVID hours they report, and the median of a student's 1 - 4 study hours they report. Using the median as opposed to the mean makes these values less prone to skewness, and even smaller residuals since medians are more reliable statistic than mean.

Appendix

```
summary(remaining_data$COVID.hours..W1.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##     0.0     1.0     1.0     3.7     2.0   168.0      21
```

```
summary(remaining_data$COVID.hours..W2.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   0.000   1.000   1.000   2.869   2.000  40.000      19
```

```
summary(remaining_data$COVID.hours..W3.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   0.000   0.500   1.000   2.227   2.000  24.000      11
```

```
summary(remaining_data$COVID.hours..W4.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   0.000   1.000   1.500   2.917   3.000  50.000      13
```

```
summary(remaining_data$STA302.hours..W1.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   0.000   5.000   7.000   7.539   9.000  28.000      21
```

```
summary(remaining_data$STA302.hours..W2.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   1.000   6.000   8.000   8.403  10.000  20.000      19
```

```
summary(remaining_data$STA302.hours..W3.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##    0.00    6.00    9.00    9.32   12.00   30.00      10
```

```
summary(remaining_data$STA302.hours..W4.)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##    2.00    7.00   11.00   13.44   16.00   72.00      13
```

```r
summary(remaining_data$Quiz_1_score)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   1.000   7.000   8.000   7.738   9.000  10.000       8
```

```r
summary(remaining_data$Quiz_2_score)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   0.000   5.800   8.800   7.422   9.400  10.000       8
```

```r
summary(remaining_data$Quiz_3_score)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   1.000   5.000   8.000   7.209   9.000  10.000       3
```

```r
summary(remaining_data$Quiz_4_score)
```

```
##    Min. 1st Qu.  Median    Mean 3rd Qu.    Max.    NA's
##   1.000   6.000   8.000   7.375   9.000  10.000       7
```

```r
canada <- remaining_data %>%
  filter(as.character(country) == "Canada") %>%
  dplyr::select(-country)

unknown <- remaining_data %>%
  filter(is.na(as.character(country))) %>%
  dplyr::select(-country)
```

```
##              Country
## Canada            97
## China             63
## India              2
## Japan              1
## Mongolia           1
## Pakistan           3
## Singapore          2
## South_Korea        2
## Taiwan             3
## UAE                2
## USA                2
## Unknown           21
```

```r
display_correlation_matrix(canada)
```

```
##        W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302   Q1    Q2    Q3    Q4
## W1COV   1.00  0.60  0.72  0.39 -0.01 -0.05 -0.05  0.10  0.10  0.06  0.11  0.06
## W2COV   0.60  1.00  0.67  0.72  0.00  0.02  0.15  0.29  0.13 -0.07 -0.06  0.05
## W3COV   0.72  0.67  1.00  0.61 -0.01 -0.01  0.23  0.31  0.09  0.03 -0.08 -0.07
## W4COV   0.39  0.72  0.61  1.00 -0.04  0.04  0.16  0.02  0.10 -0.04  0.10  0.04
```

27

```
## W1302 -0.01  0.00 -0.01 -0.04  1.00  0.70  0.64  0.55 -0.09  0.09 -0.02 -0.16
## W2302 -0.05  0.02 -0.01  0.04  0.70  1.00  0.73  0.62 -0.15 -0.09 -0.01 -0.11
## W3302 -0.05  0.15  0.23  0.16  0.64  0.73  1.00  0.68 -0.09  0.05 -0.13 -0.12
## W4302  0.10  0.29  0.31  0.02  0.55  0.62  0.68  1.00 -0.12 -0.08 -0.09 -0.12
## Q1     0.10  0.13  0.09  0.10 -0.09 -0.15 -0.09 -0.12  1.00  0.16  0.38  0.35
## Q2     0.06 -0.07  0.03 -0.04  0.09 -0.09  0.05 -0.08  0.16  1.00  0.07  0.14
## Q3     0.11 -0.06 -0.08  0.10 -0.02 -0.01 -0.13 -0.09  0.38  0.07  1.00  0.50
## Q4     0.06  0.05 -0.07  0.04 -0.16 -0.11 -0.12 -0.12  0.35  0.14  0.50  1.00
```

`display_correlation_matrix`(china)

```
##         W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302    Q1    Q2    Q3    Q4
## W1COV    1.00  0.70  0.51  0.40  0.12  0.08  0.05 -0.07  0.06  0.09  0.10 -0.01
## W2COV    0.70  1.00  0.67  0.67  0.25  0.34  0.27  0.08  0.14 -0.05  0.05 -0.12
## W3COV    0.51  0.67  1.00  0.62  0.15  0.28  0.19  0.04  0.14  0.04  0.20 -0.19
## W4COV    0.40  0.67  0.62  1.00  0.13  0.25  0.19  0.28  0.24  0.07  0.08 -0.10
## W1302    0.12  0.25  0.15  0.13  1.00  0.56  0.49  0.02  0.21  0.28 -0.06  0.07
## W2302    0.08  0.34  0.28  0.25  0.56  1.00  0.76  0.42  0.15  0.27 -0.02 -0.08
## W3302    0.05  0.27  0.19  0.19  0.49  0.76  1.00  0.57  0.11  0.14 -0.07  0.00
## W4302   -0.07  0.08  0.04  0.28  0.02  0.42  0.57  1.00  0.07  0.15  0.04 -0.03
## Q1       0.06  0.14  0.14  0.24  0.21  0.15  0.11  0.07  1.00  0.44  0.36  0.25
## Q2       0.09 -0.05  0.04  0.07  0.28  0.27  0.14  0.15  0.44  1.00  0.19  0.15
## Q3       0.10  0.05  0.20  0.08 -0.06 -0.02 -0.07  0.04  0.36  0.19  1.00  0.61
## Q4      -0.01 -0.12 -0.19 -0.10  0.07 -0.08  0.00 -0.03  0.25  0.15  0.61  1.00
```

`display_correlation_matrix`(india)

```
##         W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV       1     1     1     1    -1    NA    -1    NA -1  1 -1 -1
## W2COV       1     1     1     1    -1    NA    -1    NA -1  1 -1 -1
## W3COV       1     1     1     1    -1    NA    -1    NA -1  1 -1 -1
## W4COV       1     1     1     1    -1    NA    -1    NA -1  1 -1 -1
## W1302      -1    -1    -1    -1     1    NA     1    NA  1 -1  1  1
## W2302      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3302      -1    -1    -1    -1     1    NA     1    NA  1 -1  1  1
## W4302      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q1         -1    -1    -1    -1     1    NA     1    NA  1 -1  1  1
## Q2          1     1     1     1    -1    NA    -1    NA -1  1 -1 -1
## Q3         -1    -1    -1    -1     1    NA     1    NA  1 -1  1  1
## Q4         -1    -1    -1    -1     1    NA     1    NA  1 -1  1  1
```

```r
display_correlation_matrix(japan)
```

```
##       W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W2COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W4COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W1302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W2302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W4302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q1       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q2       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q3       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q4       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
```

```r
display_correlation_matrix(mongolia)
```

```
##       W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W2COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W4COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W1302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W2302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W4302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q1       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q2       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q3       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q4       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
```

```r
display_correlation_matrix(unknown)
```

```
##       W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302    Q1    Q2    Q3    Q4
## W1COV    NA    NA    NA    NA    NA    NA    NA    NA    NA    NA    NA    NA
## W2COV    NA  1.00  0.70 -0.09    NA -0.19  0.30  0.41  0.41  0.06 -0.50  0.11
## W3COV    NA  0.70  1.00  0.48    NA -0.25  0.06  0.21  0.01  0.09 -0.23  0.16
## W4COV    NA -0.09  0.48  1.00    NA  0.06 -0.05 -0.09  0.07  0.12  0.12  0.39
## W1302    NA    NA    NA    NA    NA    NA    NA    NA    NA    NA    NA    NA
## W2302    NA -0.19 -0.25  0.06    NA  1.00  0.06  0.38 -0.09 -0.24  0.14  0.17
## W3302    NA  0.30  0.06 -0.05    NA  0.06  1.00  0.48 -0.34  0.03 -0.22 -0.13
## W4302    NA  0.41  0.21 -0.09    NA  0.38  0.48  1.00  0.04  0.02 -0.35 -0.02
## Q1       NA  0.41  0.01  0.07    NA -0.09 -0.34  0.04  1.00  0.46  0.24  0.47
## Q2       NA  0.06  0.09  0.12    NA -0.24  0.03  0.02  0.46  1.00  0.57  0.47
## Q3       NA -0.50 -0.23  0.12    NA  0.14 -0.22 -0.35  0.24  0.57  1.00  0.58
## Q4       NA  0.11  0.16  0.39    NA  0.17 -0.13 -0.02  0.47  0.47  0.58  1.00
```

```
display_correlation_matrix(pakistan)
```

```
##        W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302    Q1 Q2 Q3    Q4
## W1COV  1.00     1     1  0.99  0.60     1  0.75  0.57 -0.99 -1 -1  0.36
## W2COV  1.00     1     1  1.00  1.00     1  1.00  1.00 -1.00 -1 -1    NA
## W3COV  1.00     1     1  1.00  1.00     1  1.00  1.00 -1.00 -1 -1    NA
## W4COV  0.99     1     1  1.00  0.68     1  0.82  0.65 -1.00 -1 -1  0.45
## W1302  0.60     1     1  0.68  1.00     1  0.98  1.00 -0.72 -1 -1  0.96
## W2302  1.00     1     1  1.00  1.00     1  1.00  1.00 -1.00 -1 -1    NA
## W3302  0.75     1     1  0.82  0.98     1  1.00  0.97 -0.85 -1 -1  0.88
## W4302  0.57     1     1  0.65  1.00     1  0.97  1.00 -0.69 -1 -1  0.97
## Q1    -0.99    -1    -1 -1.00 -0.72    -1 -0.85 -0.69  1.00  1  1 -0.50
## Q2    -1.00    -1    -1 -1.00 -1.00    -1 -1.00 -1.00  1.00  1  1    NA
## Q3    -1.00    -1    -1 -1.00 -1.00    -1 -1.00 -1.00  1.00  1  1    NA
## Q4     0.36    NA    NA  0.45  0.96    NA  0.88  0.97 -0.50 NA NA  1.00
```

```
display_correlation_matrix(singapore)
```

```
##        W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV     1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## W2COV     1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## W3COV     1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## W4COV     1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## W1302     1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## W2302    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3302    -1    -1    -1    -1    -1    NA     1     1 -1  1 -1 NA
## W4302    -1    -1    -1    -1    -1    NA     1     1 -1  1 -1 NA
## Q1        1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## Q2       -1    -1    -1    -1    -1    NA     1     1 -1  1 -1 NA
## Q3        1     1     1     1     1    NA    -1    -1  1 -1  1 NA
## Q4       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
```

```
display_correlation_matrix(south_korea)
```

```
##        W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV     1    -1    NA    NA     1    -1     1     1 NA -1 -1 NA
## W2COV    -1     1    NA    NA    -1     1    -1    -1 NA  1  1 NA
## W3COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W4COV    NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W1302     1    -1    NA    NA     1    -1     1     1 NA -1 -1 NA
## W2302    -1     1    NA    NA    -1     1    -1    -1 NA  1  1 NA
## W3302     1    -1    NA    NA     1    -1     1     1 NA -1 -1 NA
## W4302     1    -1    NA    NA     1    -1     1     1 NA -1 -1 NA
## Q1       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q2       -1     1    NA    NA    -1     1    -1    -1 NA  1  1 NA
## Q3       -1     1    NA    NA    -1     1    -1    -1 NA  1  1 NA
## Q4       NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
```

```r
display_correlation_matrix(taiwan)
```

```
##         W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302   Q1    Q2    Q3 Q4
## W1COV    1.00  1.00  0.99  0.99  0.50 -0.28  0.80  0.75 0.94  0.00  0.50 NA
## W2COV    1.00  1.00  0.99  0.99  0.50 -0.28  0.80  0.75 0.94  0.00  0.50 NA
## W3COV    0.99  0.99  1.00  1.00  0.61 -0.40  0.72  0.65 0.89 -0.13  0.38 NA
## W4COV    0.99  0.99  1.00  1.00  0.59 -0.38  0.73  0.67 0.90 -0.11  0.40 NA
## W1302    0.50  0.50  0.61  0.59  1.00 -0.97 -0.11 -0.20 0.19 -0.87 -0.50 NA
## W2302   -0.28 -0.28 -0.40 -0.38 -0.97  1.00  0.35  0.43 0.05  0.96  0.69 NA
## W3302    0.80  0.80  0.72  0.73 -0.11  0.35  1.00  1.00 0.95  0.60  0.92 NA
## W4302    0.75  0.75  0.65  0.67 -0.20  0.43  1.00  1.00 0.92  0.67  0.95 NA
## Q1       0.94  0.94  0.89  0.90  0.19  0.05  0.95  0.92 1.00  0.33  0.76 NA
## Q2       0.00  0.00 -0.13 -0.11 -0.87  0.96  0.60  0.67 0.33  1.00  0.87 NA
## Q3       0.50  0.50  0.38  0.40 -0.50  0.69  0.92  0.95 0.76  0.87  1.00 NA
## Q4         NA    NA    NA    NA    NA    NA    NA    NA   NA    NA    NA NA
```

```r
display_correlation_matrix(uae)
```

```
##         W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV       1     1     1    NA     1     1    -1    NA -1 NA -1 -1
## W2COV       1     1     1    NA     1     1    -1    NA -1 NA -1 -1
## W3COV       1     1     1    NA     1     1    -1    NA -1 NA -1 -1
## W4COV      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W1302       1     1     1    NA     1     1    -1    NA -1 NA -1 -1
## W2302       1     1     1    NA     1     1    -1    NA -1 NA -1 -1
## W3302      -1    -1    -1    NA    -1    -1     1    NA  1 NA  1  1
## W4302      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q1         -1    -1    -1    NA    -1    -1     1    NA  1 NA  1  1
## Q2         NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q3         -1    -1    -1    NA    -1    -1     1    NA  1 NA  1  1
## Q4         -1    -1    -1    NA    -1    -1     1    NA  1 NA  1  1
```

```r
display_correlation_matrix(usa)
```

```
##         W1COV W2COV W3COV W4COV W1302 W2302 W3302 W4302 Q1 Q2 Q3 Q4
## W1COV      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W2COV      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3COV      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W4COV      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W1302      NA    NA    NA    NA     1    NA     1     1 NA  1  1 NA
## W2302      NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## W3302      NA    NA    NA    NA     1    NA     1     1 NA  1  1 NA
## W4302      NA    NA    NA    NA     1    NA     1     1 NA  1  1 NA
## Q1         NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
## Q2         NA    NA    NA    NA     1    NA     1     1 NA  1  1 NA
## Q3         NA    NA    NA    NA     1    NA     1     1 NA  1  1 NA
## Q4         NA    NA    NA    NA    NA    NA    NA    NA NA NA NA NA
```

```r
summary(first_model)
```

```
##
```

```
## Call:
## lm(formula = quiz4 ~ quiz1 + quiz2 + quiz3 + covid1 + I(covid1^2) +
##     covid2 + I(covid2^2) + covid3 + covid4 + I(covid4^2) + I(covid1 *
##     covid2) + I(covid2 * covid3) + I(covid2 * covid4) + I(covid3 *
##     covid4) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4) + country)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -3.5884 -0.8610  0.1800  0.8824  3.2815
##
## Coefficients:
##                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)         3.184400   0.797065   3.995 0.000114 ***
## quiz1               0.034421   0.081102   0.424 0.672054
## quiz2               0.047852   0.061074   0.784 0.434941
## quiz3               0.477087   0.079290   6.017 2.16e-08 ***
## covid1              0.178659   0.126969   1.407 0.162094
## I(covid1^2)         0.016115   0.007279   2.214 0.028818 *
## covid2              0.289324   0.192110   1.506 0.134802
## I(covid2^2)        -0.023657   0.011719  -2.019 0.045850 *
## covid3             -0.053594   0.125976  -0.425 0.671317
## covid4             -0.248941   0.154339  -1.613 0.109497
## I(covid4^2)         0.020698   0.014617   1.416 0.159476
## I(covid1 * covid2) -0.074201   0.033661  -2.204 0.029489 *
## I(covid2 * covid3)  0.050008   0.031997   1.563 0.120826
## I(covid2 * covid4)  0.040835   0.024083   1.696 0.092671 .
## I(covid3 * covid4) -0.076459   0.050768  -1.506 0.134798
## I(study1 * study2) -0.016578   0.006879  -2.410 0.017537 *
## I(study1 * study3)  0.007613   0.005076   1.500 0.136424
## I(study2 * study3)  0.007761   0.004604   1.686 0.094568 .
## I(study3 * study4) -0.001958   0.001328  -1.474 0.143221
## countryChina        0.585571   0.344768   1.698 0.092127 .
## countryIndia        0.873927   1.174061   0.744 0.458175
## countryMongolia   -12.901734  19.426608  -0.664 0.507938
## countryPakistan    -0.148747   1.593692  -0.093 0.925800
## countrySingapore    1.191079   1.651695   0.721 0.472296
## countrySouth Korea -0.015750   1.146622  -0.014 0.989064
## countryTaiwan      -1.213168   1.161154  -1.045 0.298309
## countryUAE         -0.631273   1.649231  -0.383 0.702598
## countryUSA          1.456298   1.765878   0.825 0.411256
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.582 on 115 degrees of freedom
## Multiple R-squared:  0.4211, Adjusted R-squared:  0.2851
## F-statistic: 3.098 on 27 and 115 DF,  p-value: 1.436e-05


## Start:  AIC=156.09
## quiz4 ~ quiz1 + quiz2 + quiz3 + covid1 + I(covid1^2) + covid2 +
##     I(covid2^2) + covid3 + covid4 + I(covid4^2) + I(covid1 *
##     covid2) + I(covid2 * covid3) + I(covid2 * covid4) + I(covid3 *
##     covid4) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4) + country
```

```
##
##                         Df Sum of Sq     RSS    AIC
## - country                9    17.220  305.16 146.39
## - quiz1                  1     0.451  288.39 154.31
## - covid3                 1     0.453  288.39 154.31
## - quiz2                  1     1.537  289.48 154.85
## <none>                             287.94 156.09
## - covid1                 1     4.957  292.90 156.53
## - I(covid4^2)            1     5.020  292.96 156.56
## - I(study3 * study4)     1     5.440  293.38 156.76
## - I(study1 * study3)     1     5.632  293.57 156.86
## - covid2                 1     5.679  293.62 156.88
## - I(covid3 * covid4)     1     5.679  293.62 156.88
## - I(covid2 * covid3)     1     6.116  294.05 157.09
## - covid4                 1     6.514  294.45 157.28
## - I(study2 * study3)     1     7.115  295.05 157.58
## - I(covid2 * covid4)     1     7.198  295.14 157.62
## - I(covid2^2)            1    10.203  298.14 159.06
## - I(covid1 * covid2)     1    12.167  300.11 160.00
## - I(covid1^2)            1    12.271  300.21 160.05
## - I(study1 * study2)     1    14.543  302.48 161.13
## - quiz3                  1    90.647  378.59 193.22
##
## Step:  AIC=146.39
## quiz4 ~ quiz1 + quiz2 + quiz3 + covid1 + I(covid1^2) + covid2 +
##     I(covid2^2) + covid3 + covid4 + I(covid4^2) + I(covid1 *
##     covid2) + I(covid2 * covid3) + I(covid2 * covid4) + I(covid3 *
##     covid4) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4)
##
##                         Df Sum of Sq     RSS    AIC
## - quiz1                  1     0.013  305.17 144.40
## - covid3                 1     0.516  305.67 144.63
## - covid2                 1     2.908  308.07 145.75
## - covid1                 1     2.914  308.07 145.75
## - quiz2                  1     3.587  308.75 146.06
## - covid4                 1     3.867  309.03 146.19
## - I(covid4^2)            1     4.193  309.35 146.34
## <none>                             305.16 146.39
## - I(study1 * study3)     1     5.244  310.40 146.83
## - I(study3 * study4)     1     5.879  311.04 147.12
## - I(covid2 * covid4)     1     8.357  313.52 148.26
## - I(covid3 * covid4)     1     8.439  313.60 148.29
## - I(study2 * study3)     1     8.640  313.80 148.38
## - I(covid1 * covid2)     1    10.319  315.48 149.15
## - I(covid1^2)            1    10.436  315.60 149.20
## - I(covid2 * covid3)     1    12.174  317.33 149.99
## - I(covid2^2)            1    12.626  317.79 150.19
## - I(study1 * study2)     1    15.842  321.00 151.63
## + country                9    17.220  287.94 156.09
## - quiz3                  1   133.023  438.18 196.13
##
## Step:  AIC=144.4
## quiz4 ~ quiz2 + quiz3 + covid1 + I(covid1^2) + covid2 + I(covid2^2) +
```

33

```
##      covid3 + covid4 + I(covid4^2) + I(covid1 * covid2) + I(covid2 *
##      covid3) + I(covid2 * covid4) + I(covid3 * covid4) + I(study1 *
##      study2) + I(study1 * study3) + I(study2 * study3) + I(study3 *
##      study4)
##
##                        Df Sum of Sq    RSS    AIC
## - covid3               1     0.519 305.69 142.64
## - covid2               1     2.895 308.07 143.75
## - covid1               1     2.905 308.08 143.75
## - quiz2                1     3.644 308.82 144.10
## - covid4               1     3.871 309.04 144.20
## - I(covid4^2)          1     4.183 309.35 144.34
## <none>                             305.17 144.40
## - I(study1 * study3)   1     5.231 310.40 144.83
## - I(study3 * study4)   1     5.868 311.04 145.12
## - I(covid2 * covid4)   1     8.369 313.54 146.27
## - I(covid3 * covid4)   1     8.430 313.60 146.29
## - I(study2 * study3)   1     8.629 313.80 146.39
## + quiz1                1     0.013 305.16 146.39
## - I(covid1 * covid2)   1    10.307 315.48 147.15
## - I(covid1^2)          1    10.425 315.60 147.20
## - I(covid2 * covid3)   1    12.209 317.38 148.01
## - I(covid2^2)          1    12.665 317.84 148.21
## - I(study1 * study2)   1    15.850 321.02 149.64
## + country              9    16.782 288.39 154.31
## - quiz3                1   147.206 452.38 198.69
##
## Step:  AIC=142.64
## quiz4 ~ quiz2 + quiz3 + covid1 + I(covid1^2) + covid2 + I(covid2^2) +
##     covid4 + I(covid4^2) + I(covid1 * covid2) + I(covid2 * covid3) +
##     I(covid2 * covid4) + I(covid3 * covid4) + I(study1 * study2) +
##     I(study1 * study3) + I(study2 * study3) + I(study3 * study4)
##
##                        Df Sum of Sq    RSS    AIC
## - covid2               1     2.653 308.34 141.88
## - covid1               1     2.820 308.51 141.95
## - quiz2                1     3.471 309.16 142.25
## <none>                             305.69 142.64
## - I(study1 * study3)   1     5.017 310.71 142.97
## - I(covid4^2)          1     5.296 310.99 143.10
## - covid4               1     5.314 311.00 143.11
## - I(study3 * study4)   1     5.697 311.39 143.28
## + covid3               1     0.519 305.17 144.40
## - I(study2 * study3)   1     8.239 313.93 144.44
## + quiz1                1     0.016 305.67 144.63
## - I(covid3 * covid4)   1    10.263 315.95 145.36
## - I(covid1 * covid2)   1    10.616 316.31 145.52
## - I(covid2 * covid4)   1    10.762 316.45 145.59
## - I(covid1^2)          1    10.814 316.50 145.61
## - I(covid2 * covid3)   1    11.692 317.38 146.01
## - I(covid2^2)          1    12.258 317.95 146.26
## - I(study1 * study2)   1    15.364 321.05 147.65
## + country              9    16.843 288.85 152.54
## - quiz3                1   147.526 453.22 196.95
```

```
##
## Step:  AIC=141.88
## quiz4 ~ quiz2 + quiz3 + covid1 + I(covid1^2) + I(covid2^2) +
##     covid4 + I(covid4^2) + I(covid1 * covid2) + I(covid2 * covid3) +
##     I(covid2 * covid4) + I(covid3 * covid4) + I(study1 * study2) +
##     I(study1 * study3) + I(study2 * study3) + I(study3 * study4)
##
##                         Df Sum of Sq    RSS    AIC
## - covid4                 1     3.598 311.94 141.54
## - covid1                 1     3.718 312.06 141.59
## - quiz2                  1     3.720 312.06 141.59
## - I(covid4^2)            1     4.291 312.63 141.85
## <none>                             308.34 141.88
## - I(study1 * study3)     1     5.110 313.45 142.23
## + covid2                 1     2.653 305.69 142.64
## - I(study3 * study4)     1     6.430 314.77 142.83
## - I(covid1 * covid2)     1     8.219 316.56 143.64
## - I(covid1^2)            1     8.251 316.59 143.65
## - I(covid3 * covid4)     1     8.431 316.77 143.74
## - I(covid2 * covid4)     1     8.457 316.80 143.75
## + covid3                 1     0.276 308.07 143.75
## + quiz1                  1     0.000 308.34 143.88
## - I(study2 * study3)     1     9.129 317.47 144.05
## - I(covid2^2)            1     9.860 318.20 144.38
## - I(covid2 * covid3)     1    11.044 319.39 144.91
## - I(study1 * study2)     1    15.548 323.89 146.91
## + country                9    14.020 294.32 153.22
## - quiz3                  1   145.086 453.43 195.02
##
## Step:  AIC=141.54
## quiz4 ~ quiz2 + quiz3 + covid1 + I(covid1^2) + I(covid2^2) +
##     I(covid4^2) + I(covid1 * covid2) + I(covid2 * covid3) + I(covid2 *
##     covid4) + I(covid3 * covid4) + I(study1 * study2) + I(study1 *
##     study3) + I(study2 * study3) + I(study3 * study4)
##
##                         Df Sum of Sq    RSS    AIC
## - I(covid4^2)            1     2.711 314.65 140.77
## - quiz2                  1     3.034 314.97 140.92
## - covid1                 1     4.063 316.00 141.39
## <none>                             311.94 141.54
## + covid4                 1     3.598 308.34 141.88
## - I(study1 * study3)     1     5.551 317.49 142.06
## + covid3                 1     1.353 310.59 142.91
## + covid2                 1     0.937 311.00 143.11
## - I(covid3 * covid4)     1     8.048 319.99 143.18
## - I(study3 * study4)     1     8.556 320.50 143.41
## + quiz1                  1     0.005 311.94 143.53
## - I(covid2^2)            1     9.046 320.99 143.62
## - I(covid2 * covid4)     1     9.180 321.12 143.68
## - I(study2 * study3)     1    10.167 322.11 144.12
## - I(covid2 * covid3)     1    10.834 322.78 144.42
## - I(covid1 * covid2)     1    14.592 326.53 146.07
## - I(covid1^2)            1    15.537 327.48 146.49
## - I(study1 * study2)     1    16.267 328.21 146.81
```

```
## + country              9    14.516 297.43 152.72
## - quiz3               1   145.118 457.06 194.16
##
## Step:  AIC=140.77
## quiz4 ~ quiz2 + quiz3 + covid1 + I(covid1^2) + I(covid2^2) +
##     I(covid1 * covid2) + I(covid2 * covid3) + I(covid2 * covid4) +
##     I(covid3 * covid4) + I(study1 * study2) + I(study1 * study3) +
##     I(study2 * study3) + I(study3 * study4)
##
##                      Df Sum of Sq    RSS    AIC
## - quiz2               1     2.945 317.60 140.11
## - covid1              1     3.910 318.56 140.54
## <none>                             314.65 140.77
## - I(study1 * study3)  1     5.793 320.45 141.38
## + I(covid4^2)         1     2.711 311.94 141.54
## + covid3              1     2.060 312.59 141.83
## + covid4              1     2.018 312.63 141.85
## - I(covid2 * covid4)  1     7.249 321.90 142.03
## - I(covid2^2)         1     7.496 322.15 142.14
## - I(covid3 * covid4)  1     8.020 322.67 142.37
## + covid2              1     0.706 313.95 142.45
## - I(study3 * study4)  1     8.306 322.96 142.50
## + quiz1               1     0.004 314.65 142.77
## - I(study2 * study3)  1    10.415 325.07 143.43
## - I(covid2 * covid3)  1    10.841 325.49 143.62
## - I(covid1 * covid2)  1    13.803 328.46 144.91
## - I(covid1^2)         1    14.749 329.40 145.32
## - I(study1 * study2)  1    17.243 331.90 146.40
## + country             9    15.728 298.92 151.44
## - quiz3               1   145.685 460.34 193.18
##
## Step:  AIC=140.11
## quiz4 ~ quiz3 + covid1 + I(covid1^2) + I(covid2^2) + I(covid1 *
##     covid2) + I(covid2 * covid3) + I(covid2 * covid4) + I(covid3 *
##     covid4) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4)
##
##                      Df Sum of Sq    RSS    AIC
## - covid1              1     3.516 321.11 139.68
## <none>                             317.60 140.11
## + quiz2               1     2.945 314.65 140.77
## - I(study1 * study3)  1     6.076 323.67 140.82
## + I(covid4^2)         1     2.623 314.97 140.92
## - I(covid2 * covid4)  1     7.003 324.60 141.22
## + covid4              1     1.559 316.04 141.40
## + covid3              1     1.544 316.05 141.41
## - I(covid2^2)         1     7.498 325.10 141.44
## - I(covid3 * covid4)  1     7.653 325.25 141.51
## - I(study3 * study4)  1     8.030 325.63 141.68
## + covid2              1     0.920 316.68 141.69
## + quiz1               1     0.168 317.43 142.03
## - I(covid2 * covid3)  1     9.966 327.56 142.52
## - I(study2 * study3)  1    10.228 327.83 142.64
## - I(covid1 * covid2)  1    12.608 330.21 143.67
```

```
## - I(covid1^2)            1     13.517 331.11 144.06
## - I(study1 * study2)     1     17.109 334.71 145.61
## + country                9     17.021 300.58 150.23
## - quiz3                  1    157.581 475.18 195.72
##
## Step:  AIC=139.68
## quiz4 ~ quiz3 + I(covid1^2) + I(covid2^2) + I(covid1 * covid2) +
##     I(covid2 * covid3) + I(covid2 * covid4) + I(covid3 * covid4) +
##     I(study1 * study2) + I(study1 * study3) + I(study2 * study3) +
##     I(study3 * study4)
##
##                         Df Sum of Sq    RSS    AIC
## - I(covid2 * covid4)  1      3.650 324.76 139.30
## - I(covid3 * covid4)  1      4.211 325.33 139.54
## <none>                             321.11 139.68
## - I(covid2^2)         1      4.857 325.97 139.83
## + covid1              1      3.516 317.60 140.11
## - I(study1 * study3)  1      6.198 327.31 140.41
## + quiz2               1      2.551 318.56 140.54
## + I(covid4^2)         1      2.486 318.63 140.57
## - I(covid2 * covid3)  1      6.560 327.67 140.57
## + covid4              1      1.823 319.29 140.87
## + covid3              1      1.402 319.71 141.05
## + covid2              1      1.378 319.74 141.06
## - I(study3 * study4)  1      7.695 328.81 141.07
## + quiz1               1      0.205 320.91 141.59
## - I(study2 * study3)  1      9.490 330.60 141.84
## - I(covid1 * covid2)  1     12.332 333.45 143.07
## - I(covid1^2)         1     12.474 333.59 143.13
## - I(study1 * study2)  1     16.166 337.28 144.70
## + country             9     16.861 304.25 149.97
## - quiz3               1    154.066 475.18 193.72
##
## Step:  AIC=139.3
## quiz4 ~ quiz3 + I(covid1^2) + I(covid2^2) + I(covid1 * covid2) +
##     I(covid2 * covid3) + I(covid3 * covid4) + I(study1 * study2) +
##     I(study1 * study3) + I(study2 * study3) + I(study3 * study4)
##
##                         Df Sum of Sq    RSS    AIC
## - I(covid3 * covid4)  1      0.700 325.46 137.60
## - I(covid2^2)         1      1.738 326.50 138.06
## - I(covid2 * covid3)  1      3.190 327.95 138.69
## <none>                             324.76 139.30
## + I(covid2 * covid4)  1      3.650 321.11 139.68
## - I(study1 * study3)  1      5.613 330.38 139.75
## + covid3              1      3.454 321.31 139.77
## + quiz2               1      2.616 322.15 140.14
## + covid4              1      2.474 322.29 140.20
## + I(covid4^2)         1      0.854 323.91 140.92
## - I(study3 * study4)  1      8.966 333.73 141.19
## + covid1              1      0.163 324.60 141.22
## + quiz1               1      0.056 324.71 141.27
## + covid2              1      0.037 324.73 141.28
## - I(covid1 * covid2)  1      9.459 334.22 141.40
```

37

```
## - I(covid1^2)              1       9.536 334.30 141.44
## - I(study2 * study3)  1      10.509 335.27 141.85
## - I(study1 * study2)  1      15.455 340.22 143.94
## + country                   9      14.961 309.80 150.55
## - quiz3                     1     152.570 477.33 192.37
##
## Step:  AIC=137.6
## quiz4 ~ quiz3 + I(covid1^2) + I(covid2^2) + I(covid1 * covid2) +
##     I(covid2 * covid3) + I(study1 * study2) + I(study1 * study3) +
##     I(study2 * study3) + I(study3 * study4)
##
##                         Df Sum of Sq    RSS    AIC
## - I(covid2^2)            1     1.050 326.51 136.06
## <none>                               325.46 137.60
## - I(study1 * study3)  1     5.152 330.62 137.85
## - I(covid2 * covid3)  1     6.340 331.80 138.36
## + covid4                 1     2.632 322.83 138.44
## + quiz2                  1     2.454 323.01 138.52
## + covid3                 1     1.795 323.67 138.81
## - I(study3 * study4)  1     8.451 333.91 139.27
## + I(covid3 * covid4)  1     0.700 324.76 139.30
## + I(covid4^2)            1     0.504 324.96 139.38
## + I(covid2 * covid4)  1     0.139 325.33 139.54
## + quiz1                  1     0.094 325.37 139.56
## + covid1                 1     0.069 325.39 139.57
## + covid2                 1     0.067 325.40 139.57
## - I(covid1^2)            1     9.205 334.67 139.59
## - I(covid1 * covid2)  1     9.235 334.70 139.60
## - I(study2 * study3)  1    10.038 335.50 139.95
## - I(study1 * study2)  1    14.771 340.23 141.95
## + country                9    14.925 310.54 148.89
## - quiz3                  1   152.957 478.42 190.69
##
## Step:  AIC=136.06
## quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) + I(covid2 *
##     covid3) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4)
##
##                         Df Sum of Sq    RSS    AIC
## <none>                               326.51 136.06
## - I(study1 * study3)  1     5.058 331.57 136.26
## + quiz2                  1     2.723 323.79 136.87
## + I(covid2^2)            1     1.050 325.46 137.60
## - I(covid2 * covid3)  1     8.366 334.88 137.68
## + covid4                 1     0.642 325.87 137.78
## + covid3                 1     0.586 325.93 137.81
## + covid2                 1     0.408 326.11 137.89
## + covid1                 1     0.222 326.29 137.97
## + quiz1                  1     0.120 326.39 138.01
## + I(covid2 * covid4)  1     0.080 326.43 138.03
## + I(covid3 * covid4)  1     0.013 326.50 138.06
## + I(covid4^2)            1     0.001 326.51 138.06
## - I(covid1^2)            1     9.902 336.42 138.34
## - I(covid1 * covid2)  1    10.151 336.66 138.44
```

```
## - I(study3 * study4)  1    11.051 337.57 138.82
## - I(study2 * study3)  1    11.803 338.32 139.14
## - I(study1 * study2)  1    14.973 341.49 140.48
## + country             9    15.898 310.62 146.93
## - quiz3               1   154.675 481.19 189.52


## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## quiz4 ~ quiz1 + quiz2 + quiz3 + covid1 + I(covid1^2) + covid2 +
##     I(covid2^2) + covid3 + covid4 + I(covid4^2) + I(covid1 *
##     covid2) + I(covid2 * covid3) + I(covid2 * covid4) + I(covid3 *
##     covid4) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4) + country
##
## Final Model:
## quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) + I(covid2 *
##     covid3) + I(study1 * study2) + I(study1 * study3) + I(study2 *
##     study3) + I(study3 * study4)
##
##
##                     Step Df   Deviance Resid. Df Resid. Dev      AIC
## 1                                            115   287.9384 156.0860
## 2            - country  9 17.2202459        124   305.1587 146.3922
## 3              - quiz1  1  0.0132315        125   305.1719 144.3984
## 4             - covid3  1  0.5185280        126   305.6904 142.6411
## 5             - covid2  1  2.6530372        127   308.3435 141.8769
## 6             - covid4  1  3.5979031        128   311.9414 141.5358
## 7        - I(covid4^2)  1  2.7110239        129   314.6524 140.7732
## 8              - quiz2  1  2.9452731        130   317.5977 140.1055
## 9             - covid1  1  3.5163942        131   321.1141 139.6801
## 10 - I(covid2 * covid4)  1  3.6497154        132   324.7638 139.2962
## 11 - I(covid3 * covid4)  1  0.7000985        133   325.4639 137.6042
## 12        - I(covid2^2)  1  1.0504757        134   326.5143 136.0650
```

```r
summary(final_model)
```

```
##
## Call:
## lm(formula = quiz4 ~ quiz3 + I(covid1^2) + I(covid1 * covid2) +
##     I(covid2 * covid3) + I(study1 * study2) + I(study1 * study3) +
##     I(study2 * study3) + I(study3 * study4))
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -4.1202 -0.9349  0.0755  1.0711  3.2701
##
## Coefficients:
##                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)     3.874214   0.518252   7.476 8.98e-12 ***
## quiz3           0.499110   0.062645   7.967 6.22e-13 ***
## I(covid1^2)     0.004241   0.002104   2.016   0.0458 *
```

```
## I(covid1 * covid2) -0.018384   0.009007  -2.041   0.0432 *
## I(covid2 * covid3)  0.004796   0.002588   1.853   0.0661 .
## I(study1 * study2) -0.015069   0.006079  -2.479   0.0144 *
## I(study1 * study3)  0.006443   0.004472   1.441   0.1520
## I(study2 * study3)  0.009345   0.004246   2.201   0.0295 *
## I(study3 * study4) -0.002544   0.001195  -2.130   0.0350 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.561 on 134 degrees of freedom
## Multiple R-squared:  0.3435, Adjusted R-squared:  0.3043
## F-statistic: 8.764 on 8 and 134 DF,  p-value: 1.374e-09
```