Problem Set #7

$\begin{array}{c} {\rm Danny~Edgel} \\ {\rm Econ~710:~Economic~Statistics~and~Econometrics~II} \\ {\rm Spring~2021} \end{array}$

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 $Discussed\ and/or\ compared\ answers\ with\ Sarah\ Bass,\ Emily\ Case,\ Katherine\ Kwok,\ Michael\ Nattinger,\ and\ Alex\ Von\ Hafften$

Exercise 13.1	
Exercise 13.2	
Exercise 13.3	
Exercise 13.4	
(a)	
(b)	
(c)	
(d)	
Exercise 13.11	
Exercise 13.13	
(a)	
(b)	

(c) (d) (e)

- (f)
- (g)

Exercise 13.18

Exercise 13.19

Exercise 13.28

- (a)
- (b)
- (c)

Exercise 17.5

To show this statement, recognize that, since M_D is idempotent, the inequality can be reduced as follows:

$$\sigma_{\varepsilon}^{2} \left(\sum_{i=1}^{n} \dot{X}_{i}' \dot{X}_{i} \right)^{-1} \geq \sigma_{\varepsilon}^{2} \left(\sum_{i=1}^{n} X_{i}' X_{i} \right)^{-1}$$

$$\left(\sum_{i=1}^{n} X_{i}' X_{i} \right) \geq \left(\sum_{i=1}^{n} \dot{X}_{i}' \dot{X}_{i} \right)$$

$$\sum_{i=1}^{n} X_{i}' X_{i} \geq \sum_{i=1}^{n} (M_{D} X_{i})' (M_{D} X_{i})$$

$$\sum_{i=1}^{n} X_{i}' X_{i} \geq \sum_{i=1}^{n} (M_{D} X_{i})' (M_{D} X_{i})$$

$$\sum_{i=1}^{n} X_{i}' X_{i} \geq \sum_{i=1}^{n} X_{i}' M_{D} X_{i}$$

$$\sum_{i=1}^{n} X_{i}' X_{i} \geq \sum_{i=1}^{n} X_{i}' X_{i} - X_{i}' D (D' D)^{-1} X_{i}$$

Where $X_i'D(D'D)^{-1}X_i$ is positive semi-definite.