

## Econ 711 – Fall 2020 – Problem Set 1

Due online Monday night September 14 at midnight.

*Please feel free to work together on these problems (and all homeworks), but each student needs to write up his/her own answers at the end, rather than directly copying from one master solution.*

### Question 1. The Law of Supply

Suppose  $k = 3$ , and a firm uses goods one and two as inputs and produces good three as output. (Formally,  $y \in Y$  requires  $y_1, y_2 \leq 0$ .) For each of the following, either give an example showing it's possible or prove that it's impossible. (Feel free to use examples where  $Y$  contains only a few points.)

- (a) If  $p_3$  falls and  $p_1$  and  $p_2$  stay the same, can the firm's output  $y_3$  go up?
- (b) If  $p_1$  rises and  $p_2$  and  $p_3$  stay the same, can the firm's output  $y_3$  go up?
- (c) (Harder:) If  $p_1$  and  $p_2$  both increase and  $p_3$  stays the same, can the firm's output  $y_3$  go up? What if  $p_1$  and  $p_2$  both increase by 10%?

### Question 2. Rationalizability

Consider the following two “datasets”:

Dataset 1		Dataset 2	
$p$	$y(p)$	$p$	$y(p)$
(7, 4)	(−20, 40)	(7, 4)	(−20, 40)
(5, 5)	(−50, 60)	(5, 5)	(−40, 70)
(4, 8)	(−70, 90)	(4, 8)	(−70, 90)

For each one, determine whether the three observations are consistent with a profit-maximizing firm. If not, explain why not. If so, draw or describe:

- (a) the smallest production set that can rationalize the data
- (b) the smallest *convex* production set *with free disposal and the shutdown property* that can rationalize the data
- (c) the *largest* production set that can rationalize the data

### Question 3. Aggregate Production

Suppose an industry consists of  $n$  profit-maximizing, price-taking firms, each with its own production set  $Y_1, Y_2, \dots, Y_n$ . You observe industry-level data at several price vectors: instead of observing individual firm production  $(y_1(p), y_2(p), \dots, y_n(p))$ , you observe only the sum  $y_1(p) + \dots + y_n(p)$ . Will this aggregate data satisfy the Weak Axiom? Can industry production be rationalized as if it were the choice of a single profit-maximizing firm? Explain. (You may find it helpful to use an example.)