### Problem Set #1b

Danny Edgel Econ 715: Econometric Methods Fall 2021

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#### Question 1

- (a) The attached file, functions.jl, includes all functions used in this problem set, including an OLS function. edgel\_ps1.tex includes the code the executes the commands for the problem set. Using these files, the coefficient for education is derived as 0.151.
- (b) The education coefficients for the .5 and .75 quantiles are below.

$$\hat{\beta}_{1}^{.5} = 0.139, \qquad \hat{\beta}_{1}^{.75} = 0.156$$

(c) The bootstrap SE of  $\hat{\beta}_1^{.75}$  for 100 simulations is 0.00001891 .

### Question 2

The moment function for GMM is:

$$m(y,x;\beta) = x \left[ \mathbbm{1} \left\{ y \leq x'\beta \right\} (1-\tau) - \mathbbm{1} \left\{ y > x'\beta \right\} \tau \right] = x \left[ \mathbbm{1} \left\{ y \leq x'\beta \right\} - \tau \right]$$

The attached code estimates  $\hat{\beta}^{.5}$  and  $\hat{\beta}^{.75}$  using this GMM moment condition.

The asymptotic variance-covatiance matrix is  $(\Gamma'\Omega^{-1}\Gamma)^{-1}$ , where, assuming correct specification:

$$\Omega = \mathbb{E} [X_i X_i'] \tau (1 - \tau)$$
  
$$\Gamma = \mathbb{E} [X_i X_i'] f_{\varepsilon_i | X_i}(0)$$

The estimated coefficient and standard error for  $\hat{\beta}^{.75}$  are

## Question 3

- (a)
- (b)
- (c)
- (d)
- (e)
- (f)

# Question 4

- (a)
- (b)