

Problem Set #1b

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Question 1

- (a) The attached file, `functions.jl`, includes all functions used in this problem set, including an OLS function. `edgel_ps1.tex` includes the code that executes the commands for the problem set. Using these files, the coefficient for education is derived as 0.151 .

- (b) The education coefficients for the .5 and .75 quantiles are below.

$$\hat{\beta}_1^{.5} = 0.139, \quad \hat{\beta}_1^{.75} = 0.156$$

- (c) The bootstrap SE of $\hat{\beta}_1^{.75}$ for 100 simulations is 0.000014 .

Question 2

The moment function for GMM is:

$$m(y, x; \beta) = x [\mathbb{1}\{y \leq x'\beta\} (1 - \tau) - \mathbb{1}\{y > x'\beta\} \tau] = x [\mathbb{1}\{y \leq x'\beta\} - \tau]$$

The attached code estimates $\hat{\beta}^{.5}$ and $\hat{\beta}^{.75}$ using this GMM moment condition.

The asymptotic variance-covariance matrix is $(\Gamma'\Omega^{-1}\Gamma)^{-1}$, where, assuming correct specification:

$$\Omega = \mathbb{E}[X_i X_i'] \tau(1 - \tau)$$

$$\Gamma = \mathbb{E}[X_i X_i'] f_{\varepsilon_i|X_i}(0)$$

The estimated coefficient and standard error for $\hat{\beta}_1^{.75}$ are below.

$$\hat{\beta}_1^{.75} = 0.151, \quad se(\hat{\beta}_1^{.75}) = 0.352$$

Note that the estimated standard error is unrealistically high. This is true for the standard error of all coefficients in this model. While it is possible that I simply made a coding error that I cannot find, I believe that this is due to the use of a fitted normal distribution for the estimate of the conditional distribution of the residuals at zero. The value is above .7, which is very high. This value would likely be much lower under a different estimation method.

Question 3

The function `FGLS()` conducts all of the required steps for this question. The resulting standard error for $\hat{\beta}^{.75}$ is 3.940e-15 . This standard error is clearly a departure from those of the other methods. This is likely due to a coding error that I cannot find.

Question 4

(a) The results from 1 simulation are below.

Model	95% C.I.	Contains $\hat{\beta}_1^{.75}$?
Quantile Reg.	[-0.010, 0.010]	no
GMM	[-0.344, 0.371]	yes
FGLS	[0.585, 0.585]	no

(b) The results for $J = 10^1$ simulations are in the table below.

Model	95% Containing $\hat{\beta}_1^{.75}$
Quantile Reg.	0.000
GMM	100.000
FGLS	0.000

Note that the bootstrap and FGLS standard errors perform very poorly. The FGLS errors suffer from the unknown error mentioned in Question 3, and the bootstrap errors are likely due to the use of a small number of bootstrap samples (10). I chose this due to time constraints: The quantile regression code takes a long time to run, and I did not parallelize the bootstrap loop (again, due to time constraints).

¹I understand that this is far from “large”. I underestimated the amount of time each simulation takes and wasted the time I set aside for computation on waiting for 1000 iterations, which would not have finished before the deadline.