

HW #8

1. $x_1 + 3x_1 x_2 = 6x_2^2 + 8$
 $\Phi(x) + b = x_1 + 3x_1 x_2 - 6x_2^2 - 8 = 0$
 $w = (1, 0, 0, -6, \frac{3}{2})$

$2ad=4$ $2d + \binom{d}{2}$ $\dim(\Phi(x))$
 $2(4) + \binom{4}{2} = 14$

b. $\dim(w) = 14$

3. a. Yes, because the dataset is linearly separable
 b. No, as long as quadratic terms contribute to classification / decision boundary is quadratic

4. a. $\alpha = (0, 2, 2, 1)$
 b. $b = -1$

5. a. $\dim(\alpha) = 36$, # of training pts
 b. 6 entries, # of support vectors
 c. None, α is bounded by 0 and C,
 $0 \leq \alpha_i \leq C$
 d. The margin on the green side is larger because there are more support vectors on the green side than the purple side

hw8

March 2, 2025

```
[2]: %pip install tensorflow
%pip install torch torchvision

Requirement already satisfied: tensorflow in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(2.18.0)
Requirement already satisfied: absl-py>=1.0.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (2.1.0)
Requirement already satisfied: astunparse>=1.6.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (1.6.3)
Requirement already satisfied: flatbuffers>=24.3.25 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (25.2.10)
Requirement already satisfied: gast!=0.5.0,!0.5.1,!0.5.2,>=0.2.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (0.6.0)
Requirement already satisfied: google-pasta>=0.1.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (0.2.0)
Requirement already satisfied: libclang>=13.0.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (18.1.1)
Requirement already satisfied: opt-einsum>=2.3.2 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (3.4.0)
Requirement already satisfied: packaging in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (24.2)
Requirement already satisfied:
protobuf!=4.21.0,!4.21.1,!4.21.2,!4.21.3,!4.21.4,!4.21.5,<6.0.0dev,>=3.20.3
in /Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages (from tensorflow) (5.29.3)
Requirement already satisfied: requests<3,>=2.21.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (2.32.3)
Requirement already satisfied: setuptools in
```

```
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (75.8.0)
Requirement already satisfied: six>=1.12.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (1.17.0)
Requirement already satisfied: termcolor>=1.1.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (2.5.0)
Requirement already satisfied: typing-extensions>=3.6.6 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (4.12.2)
Requirement already satisfied: wrapt>=1.11.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (1.17.2)
Requirement already satisfied: grpcio<2.0,>=1.24.3 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (1.70.0)
Requirement already satisfied: tensorboard<2.19,>=2.18 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (2.18.0)
Requirement already satisfied: keras>=3.5.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (3.8.0)
Requirement already satisfied: numpy<2.1.0,>=1.26.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (2.0.2)
Requirement already satisfied: h5py>=3.11.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (3.13.0)
Requirement already satisfied: ml-dtypes<0.5.0,>=0.4.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorflow) (0.4.1)
Requirement already satisfied: wheel<1.0,>=0.23.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from astunparse>=1.6.0->tensorflow) (0.45.1)
Requirement already satisfied: rich in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from keras>=3.5.0->tensorflow) (13.9.4)
Requirement already satisfied: namex in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from keras>=3.5.0->tensorflow) (0.0.8)
Requirement already satisfied: optree in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from keras>=3.5.0->tensorflow) (0.14.1)
Requirement already satisfied: charset-normalizer<4,>=2 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from requests<3,>=2.21.0->tensorflow) (3.4.1)
Requirement already satisfied: idna<4,>=2.5 in
```

```
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from requests<3,>=2.21.0->tensorflow) (3.10)
Requirement already satisfied: urllib3<3,>=1.21.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from requests<3,>=2.21.0->tensorflow) (2.3.0)
Requirement already satisfied: certifi>=2017.4.17 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from requests<3,>=2.21.0->tensorflow) (2025.1.31)
Requirement already satisfied: markdown>=2.6.8 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorboard<2.19,>=2.18->tensorflow) (3.7)
Requirement already satisfied: tensorboard-data-server<0.8.0,>=0.7.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorboard<2.19,>=2.18->tensorflow) (0.7.2)
Requirement already satisfied: werkzeug>=1.0.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from tensorboard<2.19,>=2.18->tensorflow) (3.1.3)
Requirement already satisfied: MarkupSafe>=2.1.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from werkzeug>=1.0.1->tensorboard<2.19,>=2.18->tensorflow) (3.0.2)
Requirement already satisfied: markdown-it-py>=2.2.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from rich->keras>=3.5.0->tensorflow) (3.0.0)
Requirement already satisfied: pygments<3.0.0,>=2.13.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from rich->keras>=3.5.0->tensorflow) (2.19.1)
Requirement already satisfied: mdurl~0.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from markdown-it-py>=2.2.0->rich->keras>=3.5.0->tensorflow) (0.1.2)
Note: you may need to restart the kernel to use updated packages.
Requirement already satisfied: torch in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(2.6.0)
Requirement already satisfied: torchvision in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(0.21.0)
Requirement already satisfied: filelock in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (3.17.0)
Requirement already satisfied: typing-extensions>=4.10.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (4.12.2)
Requirement already satisfied: networkx in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (3.4.2)
Requirement already satisfied: jinja2 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (3.1.5)
```

```
Requirement already satisfied: fsspec in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (2025.2.0)
Requirement already satisfied: setuptools in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (75.8.0)
Requirement already satisfied: sympy==1.13.1 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torch) (1.13.1)
Requirement already satisfied: mpmath<1.4,>=1.1.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from sympy==1.13.1->torch) (1.3.0)
Requirement already satisfied: numpy in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torchvision) (2.0.2)
Requirement already satisfied: pillow!=8.3.*,>=5.3.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from torchvision) (11.1.0)
Requirement already satisfied: MarkupSafe>=2.0 in
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages
(from jinja2->torch) (3.0.2)
Note: you may need to restart the kernel to use updated packages.
```

```
[4]: import pandas as pd
import numpy as np
from sklearn.svm import LinearSVC
from sklearn.svm import SVC
import matplotlib.pyplot as plt
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import RBF
from tensorflow.keras.datasets import mnist
import os
import sys
import gzip
if sys.version_info[0] == 2:
    from urllib import urlretrieve
else:
    from urllib.request import urlretrieve
from sklearn.metrics import accuracy_score
from sklearn.preprocessing import StandardScaler
from sklearn.model_selection import train_test_split
```

```
[2]: df1 = np.loadtxt('week8/data1.txt')
df2 = np.loadtxt('week8/data2.txt')
```

```
[3]: def quadratic_kernel(x1, x2):
    return (np.dot(x1, x2) + 1) ** 2
```

```
def rbf_kernel(x1, x2, gamma=0.1):
    return np.exp(-gamma * np.linalg.norm(x1 - x2) ** 2)
```

```
[12]: class KernelPerceptron:
    def __init__(self, kernel=quadratic_kernel):
        self.kernel = kernel
        self.alpha = None
        self.b = 0
        self.labels = None
        self.X = None

    def fit(self, X, y):
        n_samples = X.shape[0]
        self.alpha = np.zeros(n_samples)
        self.labels = y
        self.X = X
        misclassified = True

        while misclassified:
            misclassified = False
            for i in range(n_samples):
                pred_sum = 0
                for j in range(n_samples):
                    pred_sum += self.alpha[j] * y[j] * self.kernel(X[j], X[i])
                pred = np.sign(pred_sum + self.b)
                if pred != y[i]:
                    self.alpha[i] += 1
                    self.b += y[i]
                    misclassified = True

    def predict(self, X):
        predictions = []
        for x in X:
            pred_sum = 0
            for i in range(len(self.alpha)):
                pred_sum += self.alpha[i] * self.labels[i] * self.kernel(self.X[i], x)
            pred_sum += self.b
            pred = np.sign(pred_sum)
            predictions.append(pred)

        return np.array(predictions)
```

```
[13]: def plot_decision_boundary(X, y, model, title="Decision Boundary"):
    h = 0.01
    x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
```

```

y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1

xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                     np.arange(y_min, y_max, h))

Z = model.predict(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)

plt.contourf(xx, yy, Z, alpha=0.3, cmap=plt.cm.coolwarm)
plt.scatter(X[:, 0], X[:, 1], c=y, s=30, cmap=plt.cm.coolwarm, 
            edgecolors='k')
plt.title(title)
plt.show()

```

[14]:

```

X1, y1 = df1[:, :2], df1[:, 2]
X2, y2 = df2[:, :2], df2[:, 2]

model_quadratic = KernelPerceptron(kernel=quadratic_kernel)
model_quadratic.fit(X1, y1)
plot_decision_boundary(X1, y1, model_quadratic, title="Quadratic Kernel - df1")

model_quadratic_data2 = KernelPerceptron(kernel=quadratic_kernel)
model_quadratic_data2.fit(X2, y2)
plot_decision_boundary(X2, y2, model_quadratic_data2, title="Quadratic Kernel - df2")

gamma_1 = 0.1
model_rbf_data1 = KernelPerceptron(kernel=lambda x1, x2: rbf_kernel(x1, x2, 
            gamma_1))
model_rbf_data1.fit(X1, y1)
plot_decision_boundary(X1, y1, model_rbf_data1, title=f"RBF Kernel - 
            (gamma={gamma_1}) - df1")

model_rbf_data2 = KernelPerceptron(kernel=lambda x1, x2: rbf_kernel(x1, x2, 
            gamma_1))
model_rbf_data2.fit(X2, y2)
plot_decision_boundary(X2, y2, model_rbf_data2, title=f"RBF Kernel - 
            (gamma={gamma_1}) - df2")

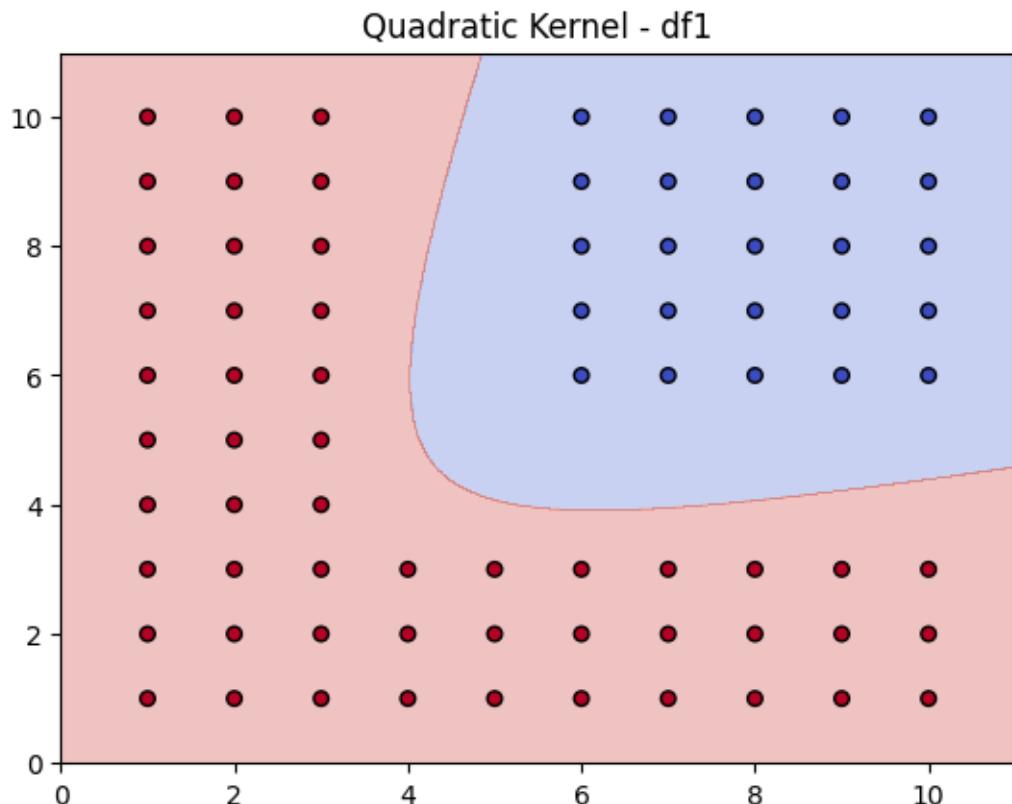
gamma_2 = 0.5
model_rbf_data1_2 = KernelPerceptron(kernel=lambda x1, x2: rbf_kernel(x1, x2, 
            gamma_2))
model_rbf_data1_2.fit(X1, y1)
plot_decision_boundary(X1, y1, model_rbf_data1_2, title=f"RBF Kernel - 
            (gamma={gamma_2}) - df1")

```

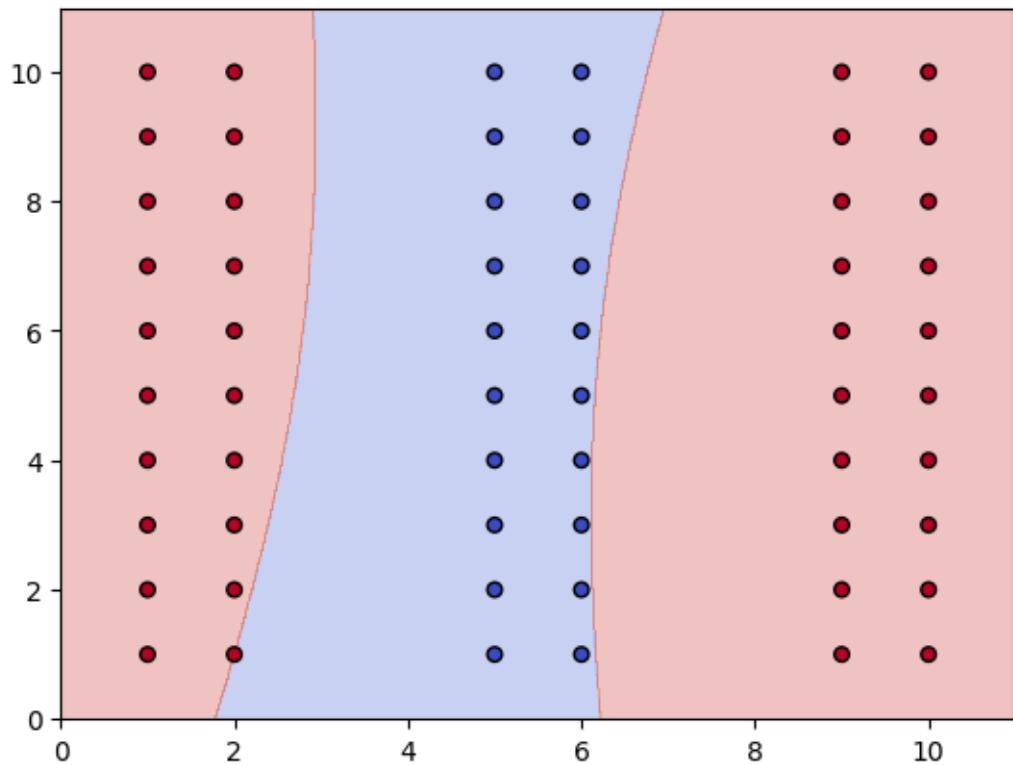
```

model_rbf_data2_2 = KernelPerceptron(kernel=lambda x1, x2: rbf_kernel(x1, x2,
    ↪gamma_2))
model_rbf_data2_2.fit(X2, y2)
plot_decision_boundary(X2, y2, model_rbf_data2_2, title=f"RBF Kernel ↪
    ↪(gamma={gamma_2}) - df2")

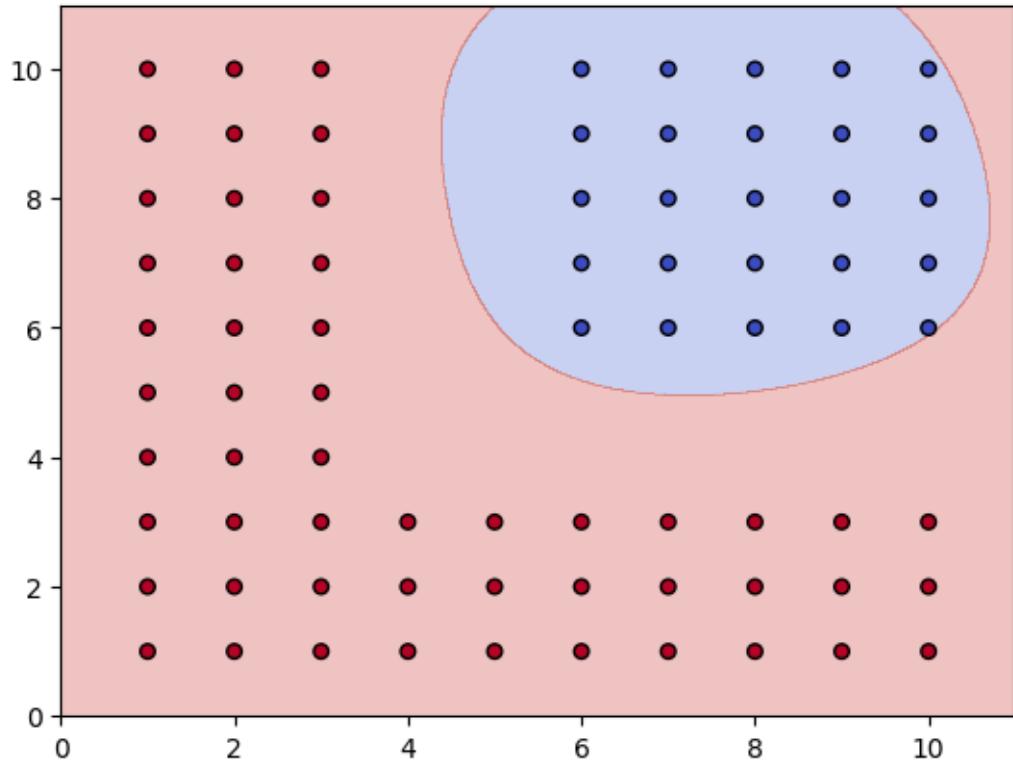
```



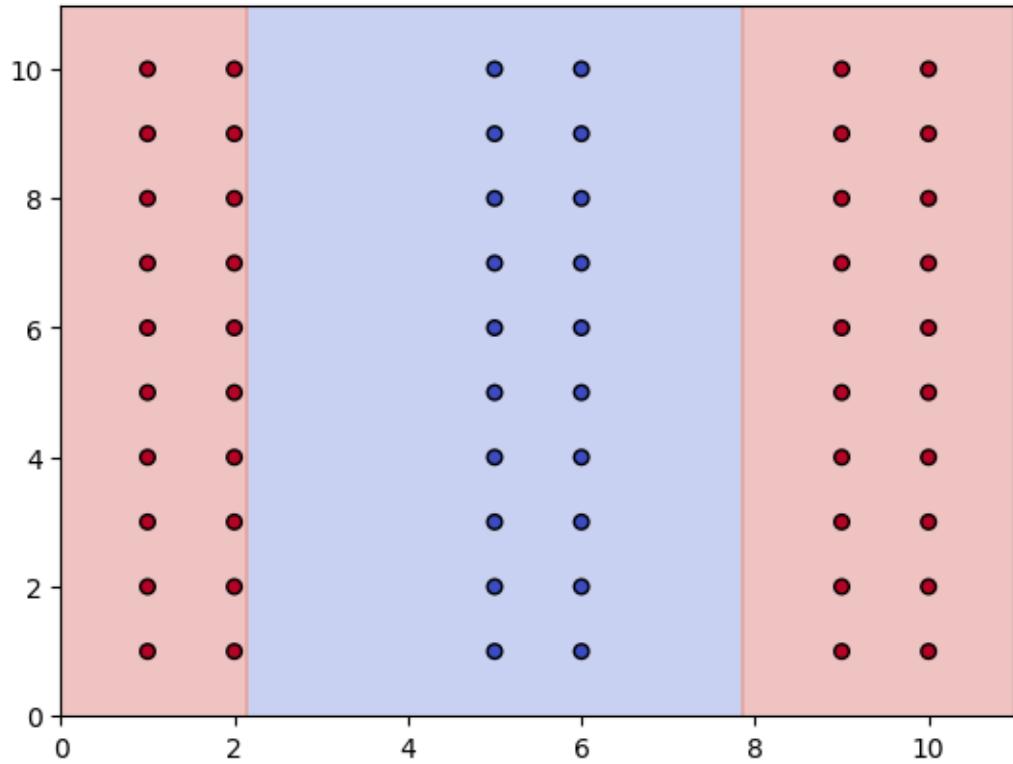
Quadratic Kernel - df2



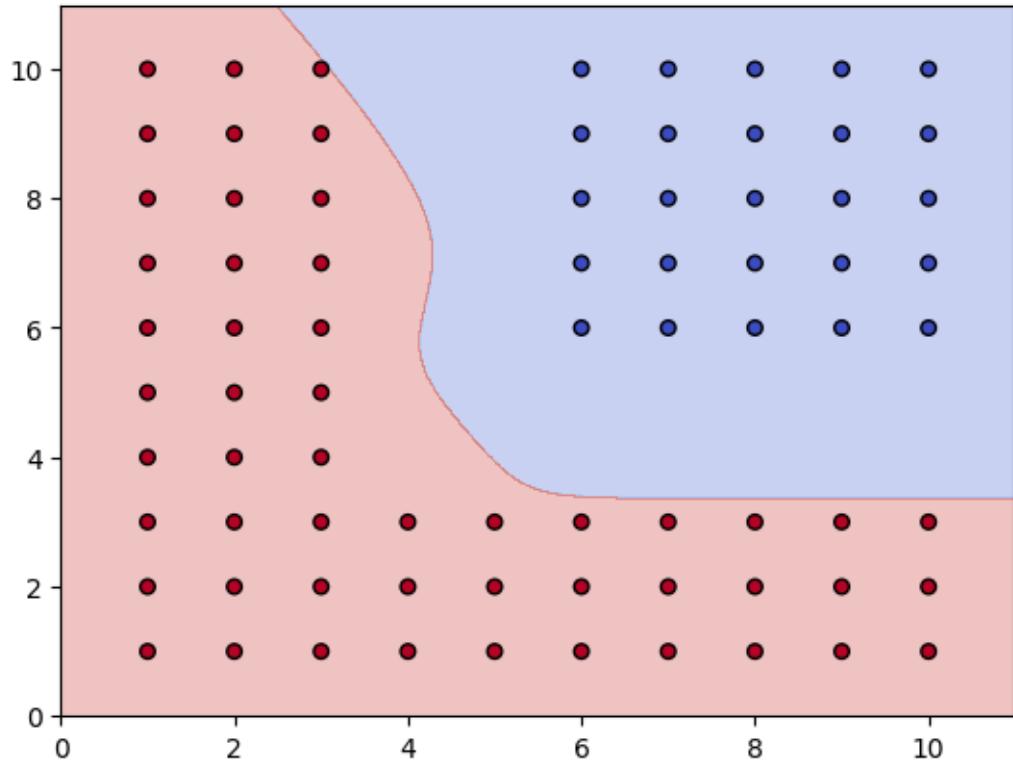
RBF Kernel (gamma=0.1) - df1

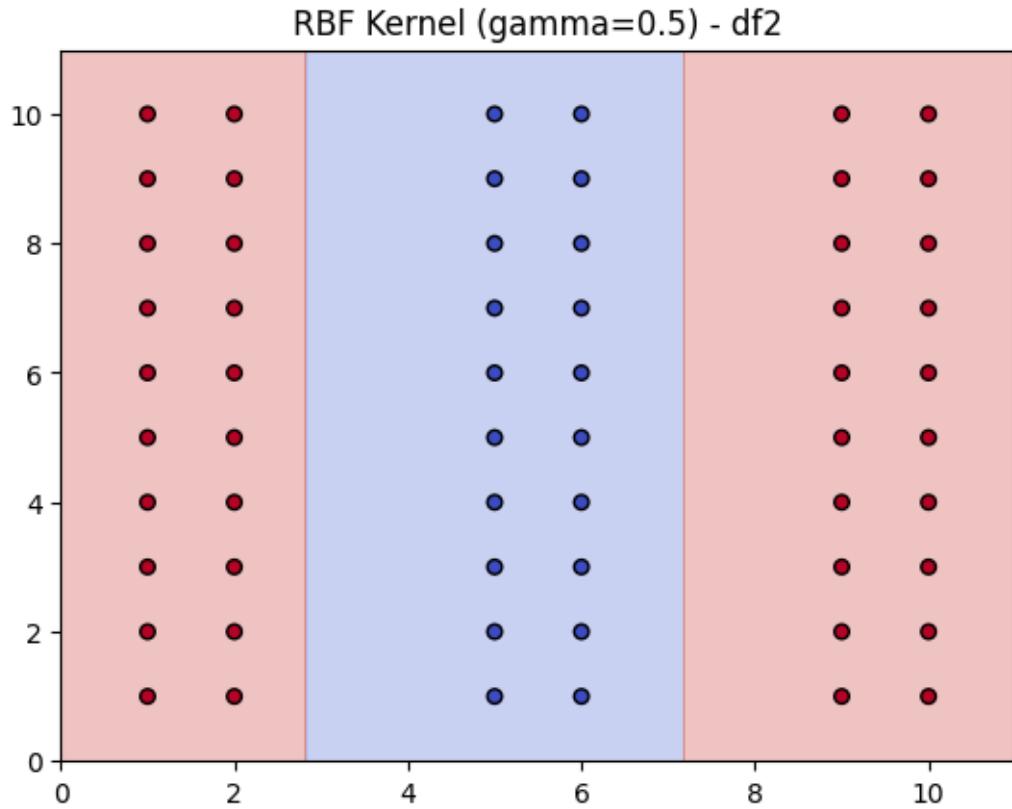


RBF Kernel (gamma=0.1) - df2



RBF Kernel (gamma=0.5) - df1





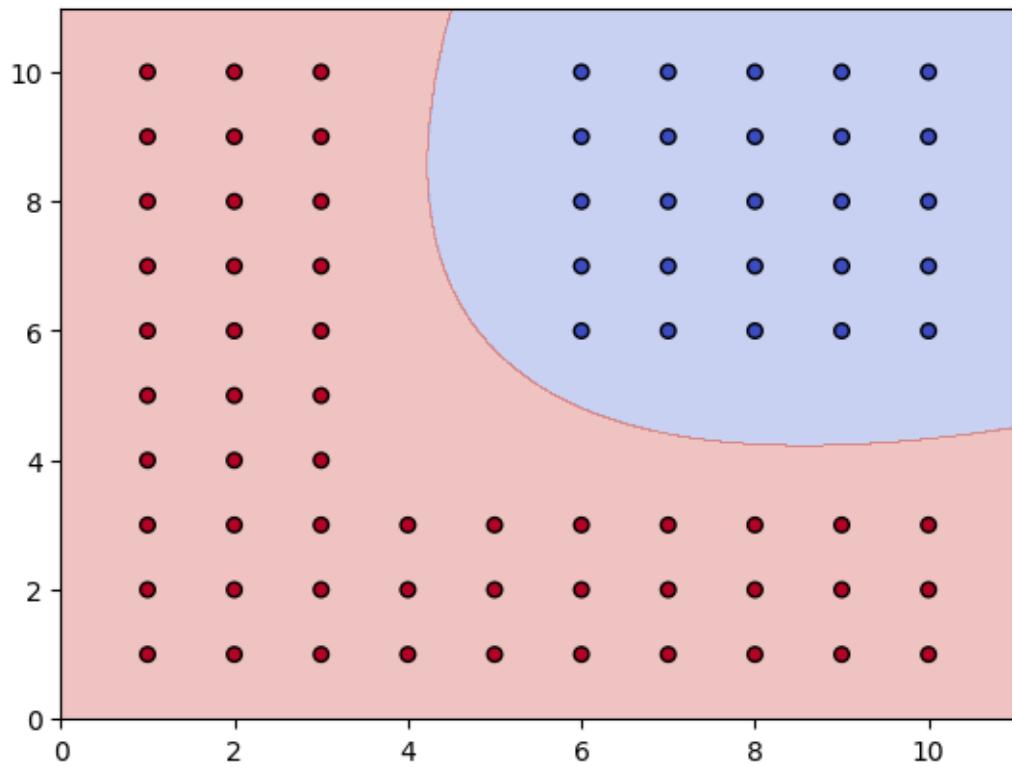
```
[11]: kernel = 1.0 * RBF(1.0)
gpc = GaussianProcessClassifier(kernel=kernel,
                                 random_state=0).fit(X1, y1)
plot_decision_boundary(X1, y1, gpc, title='RBF Kernel - df1, gamma = 1')

kernel = 1.0 * RBF(0.1)
gpc = GaussianProcessClassifier(kernel=kernel,
                                 random_state=0).fit(X1, y1)
plot_decision_boundary(X1, y1, gpc, title='RBF Kernel - df1, gamma = 0.1')

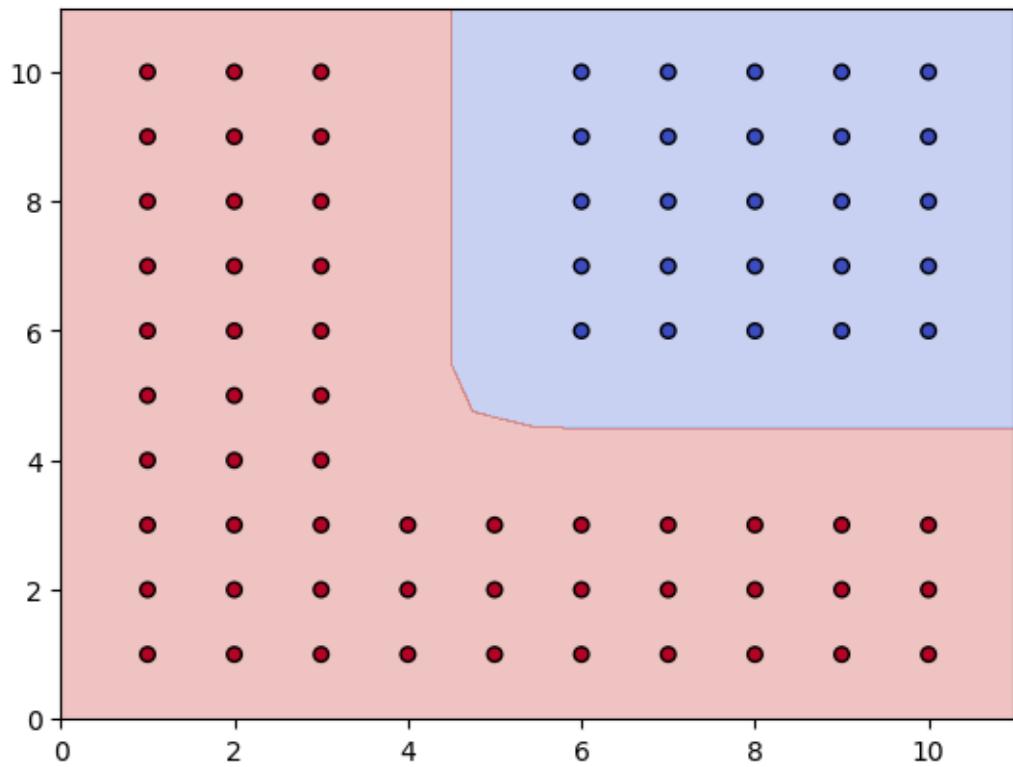
kernel = 1.0 * RBF(1.0)
gpc = GaussianProcessClassifier(kernel=kernel,
                                 random_state=0).fit(X2, y2)
plot_decision_boundary(X2, y2, gpc, title='RBF Kernel - df2, gamma = 1')

kernel = 1.0 * RBF(0.1)
gpc = GaussianProcessClassifier(kernel=kernel,
                                 random_state=0).fit(X2, y2)
plot_decision_boundary(X2, y2, gpc, title='RBF Kernel - df2, gamma = 0.1')
```

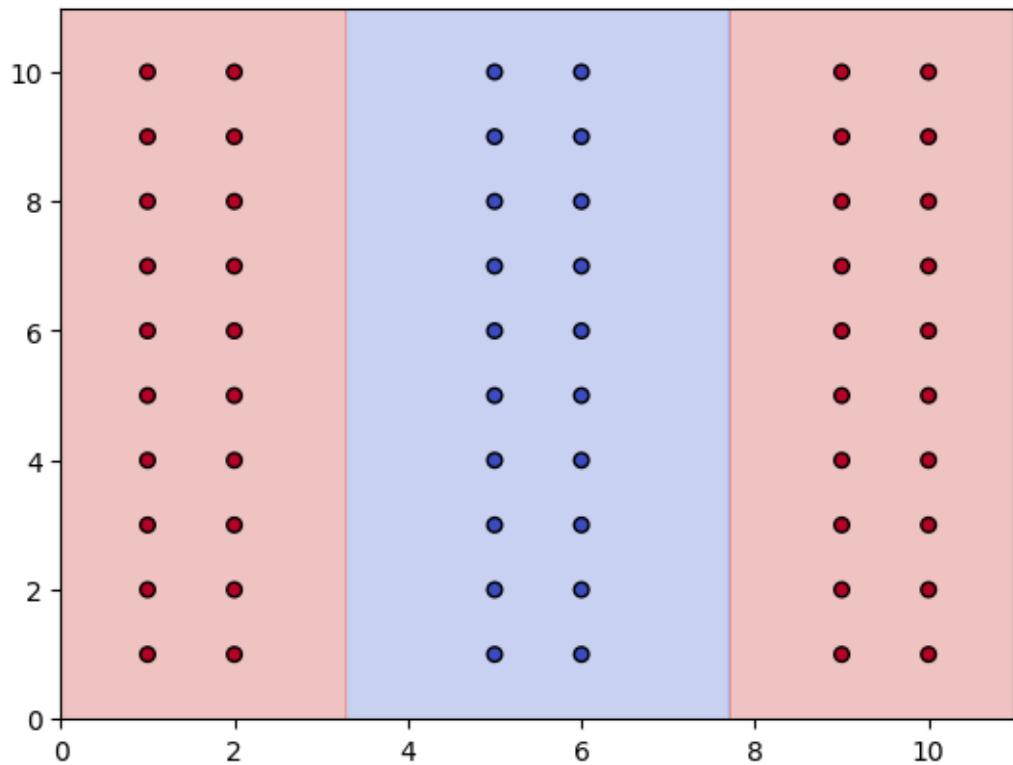
RBF Kernel - df1

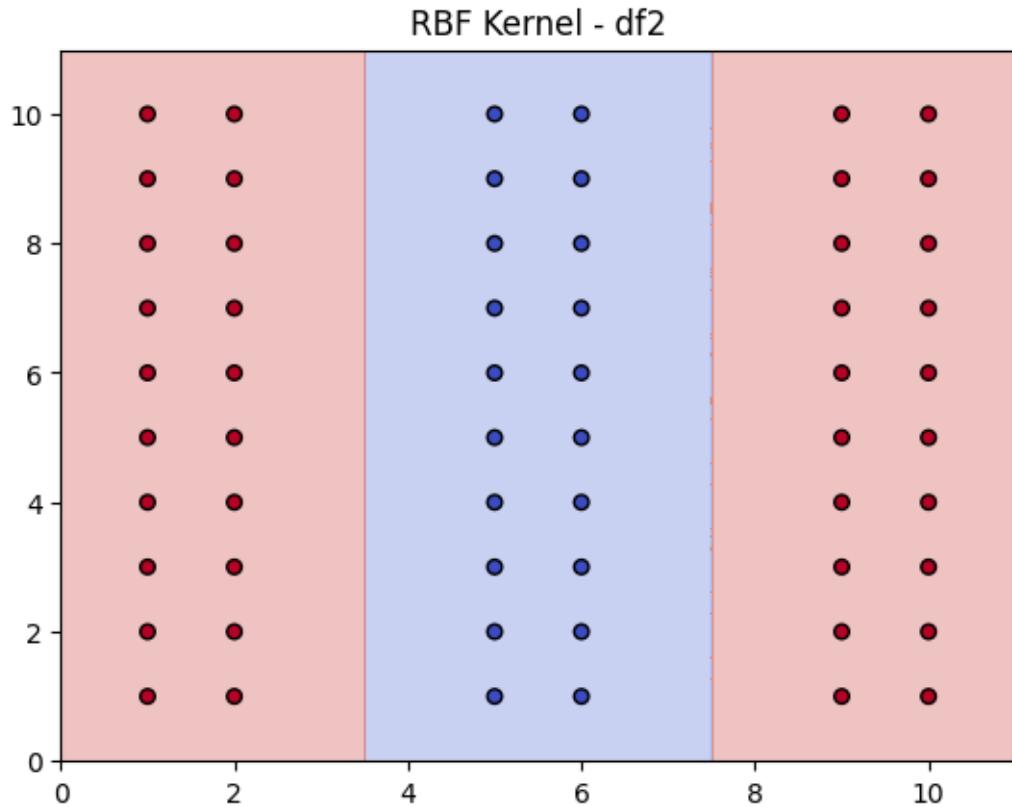


RBF Kernel - df1



RBF Kernel - df2





```
[9]: def download(filename, source='http://yann.lecun.com/exdb/mnist/'):
    print("Downloading %s" % filename)
    urlretrieve(source + filename, filename)

# Invokes download() if necessary, then reads in images
def load_mnist_images(filename):
    if not os.path.exists(filename):
        download(filename)
    with gzip.open(filename, 'rb') as f:
        data = np.frombuffer(f.read(), np.uint8, offset=16)
    data = data.reshape(-1,784)
    return data

def load_mnist_labels(filename):
    if not os.path.exists(filename):
        download(filename)
    with gzip.open(filename, 'rb') as f:
        data = np.frombuffer(f.read(), np.uint8, offset=8)
    return data
```

```
[10]: X_train = load_mnist_images('train-images-idx3-ubyte.gz')
y_train = load_mnist_labels('train-labels-idx1-ubyte.gz')

X_test = load_mnist_images('t10k-images-idx3-ubyte.gz')
y_test = load_mnist_labels('t10k-labels-idx1-ubyte.gz')

print(f"Training data shape: {X_train.shape}")
print(f"Test data shape: {X_test.shape}")
print(f"Training labels shape: {y_train.shape}")
print(f"Test labels shape: {y_test.shape}")
```

Training data shape: (60000, 784)
 Test data shape: (10000, 784)
 Training labels shape: (60000,)
 Test labels shape: (10000,)

```
[11]: X_train = X_train.astype('float32') / 255.0 # Normalize
X_test = X_test.astype('float32') / 255.0 # Normalize

X_train = X_train.reshape(-1, 28 * 28)
X_test = X_test.reshape(-1, 28 * 28)

scaler = StandardScaler()
X_train = scaler.fit_transform(X_train)
X_test = scaler.transform(X_test)
```

```
[ ]: C_values = [0.01, 0.1, 1.0, 10.0, 100.0]
linear_svm_results = {}

for C in C_values:
    print(f"Training Linear SVM with C={C}...")
    model = LinearSVC(C=C, loss='hinge', max_iter=10000)
    model.fit(X_train, y_train)

    train_pred = model.predict(X_train)
    test_pred = model.predict(X_test)

    train_accuracy = accuracy_score(y_train, train_pred)
    test_accuracy = accuracy_score(y_test, test_pred)

    linear_svm_results[C] = {'train_accuracy': train_accuracy, 'test_accuracy': test_accuracy}
    print(f"Training Accuracy: {train_accuracy}")
    print(f"Test Accuracy: {test_accuracy}")
    print("-----")

print("Training Kernel SVM with quadratic kernel (degree=2)...")
```

```

kernel_svm_model = SVC(kernel='poly', degree=2, C=1.0)
kernel_svm_model.fit(X_train, y_train)

train_pred_kernel = kernel_svm_model.predict(X_train)
test_pred_kernel = kernel_svm_model.predict(X_test)

train_accuracy_kernel = accuracy_score(y_train, train_pred_kernel)
test_accuracy_kernel = accuracy_score(y_test, test_pred_kernel)

n_support_vectors = len(kernel_svm_model.support_vectors_)

print(f"Kernel SVM (quadratic kernel) Training Accuracy:{train_accuracy_kernel}")
print(f"Kernel SVM (quadratic kernel) Test Accuracy: {test_accuracy_kernel}")
print(f"Number of Support Vectors: {n_support_vectors}")

```

Training Linear SVM with C=0.01...

```

/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages/sklearn/svm/_base.py:1249: ConvergenceWarning: Liblinear failed to
converge, increase the number of iterations.

warnings.warn(

```

Training Accuracy: 0.92115

Test Accuracy: 0.9157

Training Linear SVM with C=0.1...

```

/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages/sklearn/svm/_base.py:1249: ConvergenceWarning: Liblinear failed to
converge, increase the number of iterations.

warnings.warn(

```

Training Accuracy: 0.92915

Test Accuracy: 0.9195

Training Linear SVM with C=1.0...

```

/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages/sklearn/svm/_base.py:1249: ConvergenceWarning: Liblinear failed to
converge, increase the number of iterations.

warnings.warn(

```

Training Accuracy: 0.9309

Test Accuracy: 0.9182

Training Linear SVM with C=10.0...

1 Problem 7b.

1.1 The dataset does not seem to be linearly separable because for larger values of C, the test error increases, thus indicating that the model is overfitting and the data is not well-separated.

1.1.1 The training was taking too long for the higher values of C, but I would use more max iterations if possible to increase the accuracies.

```
[14]: linear_svm_results = {}
C = 10.0
print(f"Training Linear SVM with C={10.0}...")
model = LinearSVC(C=C, loss='hinge', max_iter=1000)
model.fit(X_train, y_train)

train_pred = model.predict(X_train)
test_pred = model.predict(X_test)

train_accuracy = accuracy_score(y_train, train_pred)
test_accuracy = accuracy_score(y_test, test_pred)

linear_svm_results[C] = {'train_accuracy': train_accuracy, 'test_accuracy': test_accuracy}
print(f"Training Accuracy: {train_accuracy}")
print(f"Test Accuracy: {test_accuracy}")
print("-----")

C = 100.0
print(f"Training Linear SVM with C={100.0}...")
model = LinearSVC(C=C, loss='hinge', max_iter=1000)
model.fit(X_train, y_train)

train_pred = model.predict(X_train)
test_pred = model.predict(X_test)

train_accuracy = accuracy_score(y_train, train_pred)
test_accuracy = accuracy_score(y_test, test_pred)

linear_svm_results[C] = {'train_accuracy': train_accuracy, 'test_accuracy': test_accuracy}
print(f"Training Accuracy: {train_accuracy}")
print(f"Test Accuracy: {test_accuracy}")
print("-----")
```

Training Linear SVM with C=10.0...

/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-packages/sklearn/svm/_base.py:1249: ConvergenceWarning: Liblinear failed to converge, increase the number of iterations.

```

warnings.warn(
Training Accuracy: 0.8850166666666667
Test Accuracy: 0.876
-----
Training Linear SVM with C=100.0...
/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages/sklearn/svm/_base.py:1249: ConvergenceWarning: Liblinear failed to
converge, increase the number of iterations.
warnings.warn(
Training Accuracy: 0.88225
Test Accuracy: 0.8762
-----
[ ]: %%timeit
print("Training Kernel SVM with quadratic kernel (degree=2)...")
kernel_svm_model = SVC(kernel='poly', degree=2, C=1.0, max_iter=1000)
kernel_svm_model.fit(X_train, y_train)

train_pred_kernel = kernel_svm_model.predict(X_train)
test_pred_kernel = kernel_svm_model.predict(X_test)

train_accuracy_kernel = accuracy_score(y_train, train_pred_kernel)
test_accuracy_kernel = accuracy_score(y_test, test_pred_kernel)

n_support_vectors = len(kernel_svm_model.support_vectors_)

print(f"Kernel SVM (quadratic kernel) Training Accuracy:{train_accuracy_kernel}")
print(f"Kernel SVM (quadratic kernel) Test Accuracy: {test_accuracy_kernel}")
print(f"Number of Support Vectors: {n_support_vectors}")

```

```

Training Kernel SVM with quadratic kernel (degree=2)...

/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages/sklearn/svm/_base.py:305: ConvergenceWarning: Solver terminated early
(max_iter=1000). Consider pre-processing your data with StandardScaler or
MinMaxScaler.
warnings.warn(
Kernel SVM (quadratic kernel) Training Accuracy: 0.98055
Kernel SVM (quadratic kernel) Test Accuracy: 0.966
Number of Support Vectors: 15601
Training Kernel SVM with quadratic kernel (degree=2)...

/Library/Frameworks/Python.framework/Versions/3.12/lib/python3.12/site-
packages/sklearn/svm/_base.py:305: ConvergenceWarning: Solver terminated early
(max_iter=1000). Consider pre-processing your data with StandardScaler or
MinMaxScaler.

```

```
warnings.warn(  
[ ]:
```