



AR(1) Forecasting Summary

Model: $X_t = 3 + 0.8X_{t-1} + \varepsilon_t$
 $\sigma^2 = 4$, $X_{100} = 20$

Unconditional Mean:

$$\mu = c/(1-\phi) = 3/0.19999999999999996 = 15.000000000000004$$

Forecasts:

1. One-step ahead:

$$\begin{aligned} \hat{X}_{101|100} &= c + \phi X_{100} \\ &= 3 + 0.8 \times 20 \\ &= 19.0 \end{aligned}$$

2. Two-step ahead:

$$\begin{aligned} \hat{X}_{102|100} &= c + \phi \hat{X}_{101|100} \\ &= 3 + 0.8 \times 19.0 \\ &= 18.200000000000003 \end{aligned}$$

3. Long-run ($h \rightarrow \infty$):

$$\lim \hat{X}_{100+h|100} = \mu = 15.000000000000004$$

4. 95% CI for $\hat{X}_{101|100}$:

$$\begin{aligned} &19.0 \pm 1.96 \times \sqrt{4} \\ &= [15.08, 22.92] \end{aligned}$$