

# Priority Queue

insert(e)

removeMin / removeMax

min() / max()

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	<u>1 4 2 a 8 6</u>
	pq
insert(1)	1
insert(4)	1, 4
insert(2)	1, 2, 4
insert(a)	1, 2, 4, a
removeMin()	2, 4, a
min()	(2)
insert(8)	2, 4, 8, a
insert(6)	2, 4, 6, 8, a

# implementation of Priority Queue

## 1) Sequence

unsorted  
4-2-6-8-1

insert():  $O(1)$

remove Min()/max():  $O(n)$

1-2-5-8

insert():  $O(n)$

remove Min()/max():  $O(1)$

## 2)

## Heap

W 13

1. Show the output from the following sequence of priority queue ADT operations. The entries are key-element pairs, where sorting is based on the key value:

insert(5, a), insert(4, b), insert(7, i), insert(1, d), removeMin(), insert(3, j), insert(6, c), removeMin(), removeMin(), insert(8, g), removeMin(), insert(2, h), removeMin(), removeMin()

operation	PQ
insert(5,a)	(5, a)
insert(4,b)	(4, b), (5, a)
insert (7,i)	(4, b), (5, a), (7, i)
insert(1,d)	(1, d), (4, b), (5, a), (7, i)
<u>removeMin()</u>	(4, b), (5, a), (7, i)
insert(3,j)	(3, j), (4, b), (5, a), (7, i)
insert(6,c)	(3, j), (4, b), (5, a), (6, c), (7, i)
<u>removeMin()</u>	(4, b), (5, a), (6, c), (7, i)
<u>removeMin()</u>	(5, a), (6, c), (7, i)
insert(8,g)	(5, a), (6, c), (7, i), (8, g)
<u>removeMin()</u>	(6, c), (7, i), (8, g)
insert(2,h)	(2, h), (6, c), (7, i), (8, g)
<u>removeMin()</u>	(6, c), (7, i), (8, g)
<u>removeMin()</u>	(7, i), (8, g)

3) stack w/ PQ

Variable  $m = 0$

push  $\Rightarrow$  insert( $m, e$ );  $m--$ ;

pop  $\Rightarrow$  removeMin;  $m++$ ;

4) Queue w/ PQ

Variable  $m = 0$

enqueue insert( $m, e$ );  $m++$ ;

dequeue removeMin();  $m--$ ;