

Design Review #2: Resonant-Cavity Enhanced Photodetector (RCE-PD)

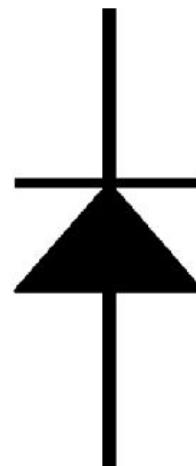
3.46 Photonic Materials and Devices

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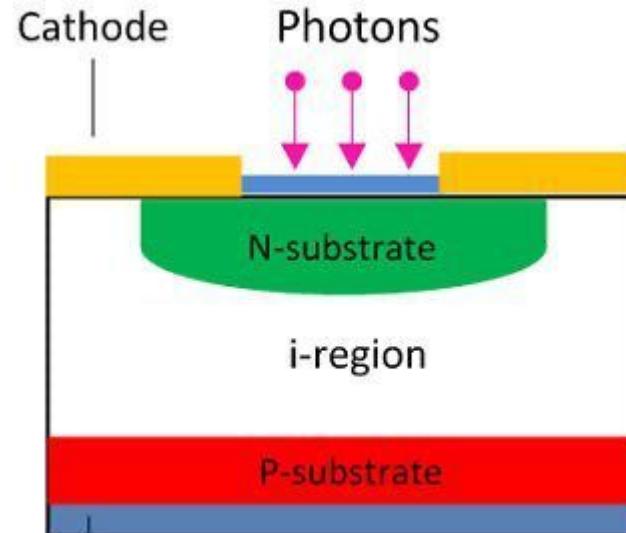
PIN Photodiode Fundamentals

Components:

- N-substrate
- I-region
 - Incident light → e-h pairs made
→ photocurrent
- P-substrate
- Cathode+Anode



[Diode Equivalent Diagram](#)



[PIN Photodiode Diagram](#)

Circuit Globe

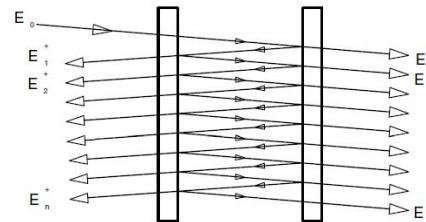
Resonant Cavity

Why?

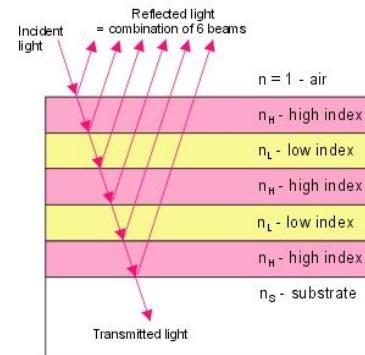
- Enhance absorption

How?

Use Distributed Bragg Reflectors (DBRs)



Fabry-Perot cavity
(INTERCONNECT) -
Ansys Optics



Bragg Reflector Example

Design Project RCE-PD Requirements

1. Stack height < 3[um]
2. 5[um] x 5[um] detector area
3. >50GHz 3dB Bandwidth
4. QE($\lambda=850[\text{nm}]$) > 50%
5. Optimized SNR

Refractive Indices (Cavity Layer)

Hard Requirement: intrinsic layer is Si

$$n_{cav}(\lambda = 850[\text{nm}]) = 3.6393 + j \cdot 0.0047757 \quad \text{Source, c-Si}$$

Assume indecent angle is 0[rad]. Resonant cavity length:

$$d = \frac{m\lambda}{2Re\{n\}}$$

Length cost per m: 116.8[nm]

P-N Features

From internet, doping level is appropriate at $\sim 1e18[\text{cm}^{-3}]$

- P: $N_A = 1e18 \text{ [cm}^{-3}\text{]}$
- N: $N_D = 1e18 \text{ [cm}^{-3}\text{]}$

From internet, thickness of $\sim 75[\text{nm}]$ is acceptable

Thus,...

$$d_i = d_{cav} - 2 * 75[\text{nm}]$$

3dB bandwidth

Two Restraints:

1. Carrier-transport time limit
2. RC delay

$$f_{tr} = \frac{0.44v_{sat}}{d}$$

$$f_{RC} = \frac{1}{2\pi RC} \sim \frac{d}{2\pi R\varepsilon A}$$

Considering Both...

$$f_{3dB} = \sqrt{\frac{1}{(1/f_{tr})^2 + (1/f_{RC})^2}}$$

Detector Area

Locks A to 25[um^2], setting f_{RC}

$$f_{RC} = \frac{1}{2\pi RC} \sim \frac{d}{2\pi R\varepsilon A}$$

Also means front DBR must be 5[um] x [5um]

50GHz 3dB Requirement

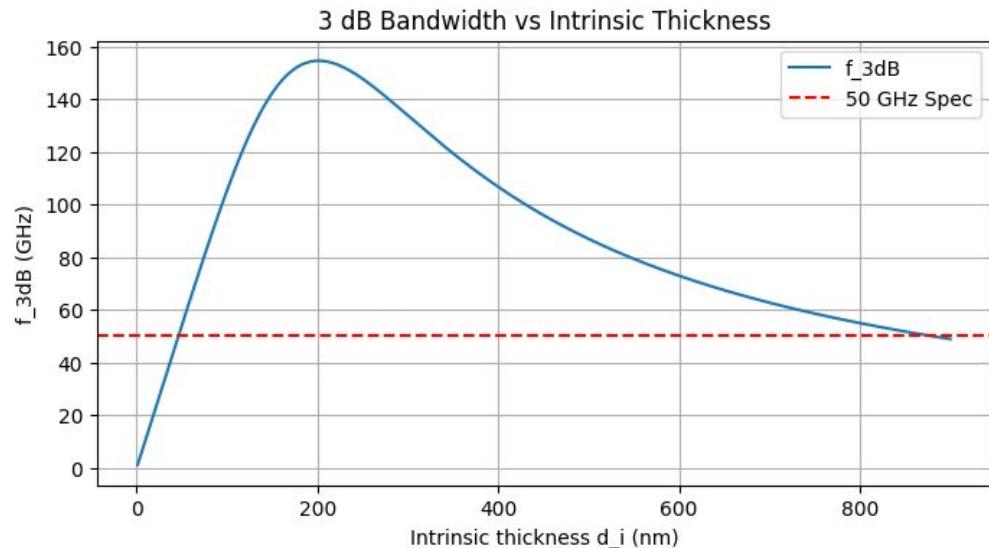
Looking at the entire 3dB formula...

$$f_{3dB} = \sqrt{\frac{1}{(1/f_{tr})^2 + (1/f_{RC})^2}}$$

f_{RC} known (last slide)

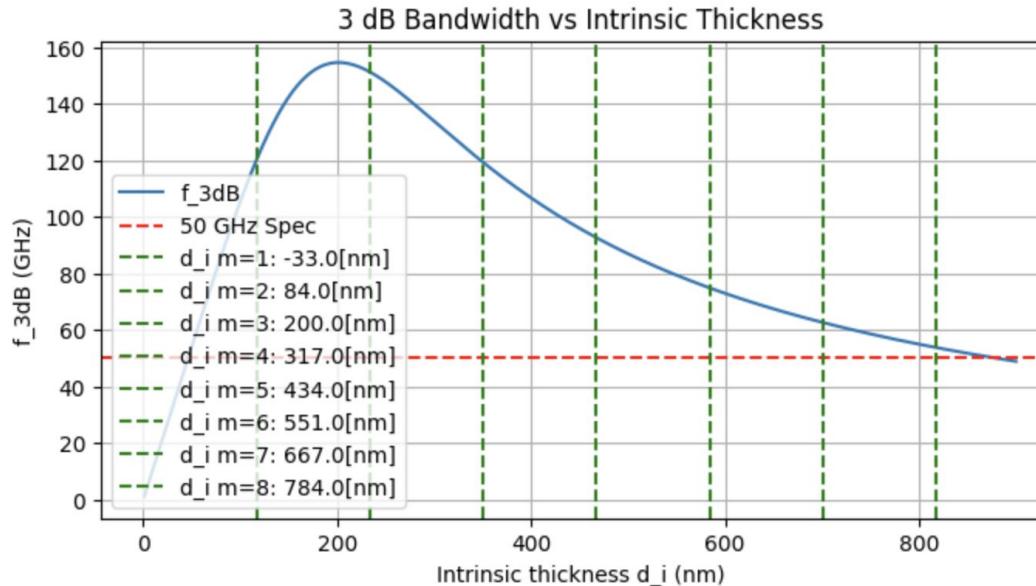
$$f_{tr} = \frac{0.44v_{sat}}{d}$$

For Si, $v_{sat} = 1 \cdot 10^5 [m/s]$



Graph as a function of d (left)

Intrinsic Layer Thickness Restrained by Cavity



We can safely use $m=2$ to $m=8$

Refractive Indices (Distributed Bragg Reflectors)

DBR requirements:

1. High index difference (high reflection with less thickness)
2. Almost lossless at 850[nm] wavelength

Solution: GaP + SiO₂

GaP onto SiO₂: MetalOrganic Vapor Phase Epitaxy (MOVPE)

Implementation paper

GaP onto Si: Wafer Bonding

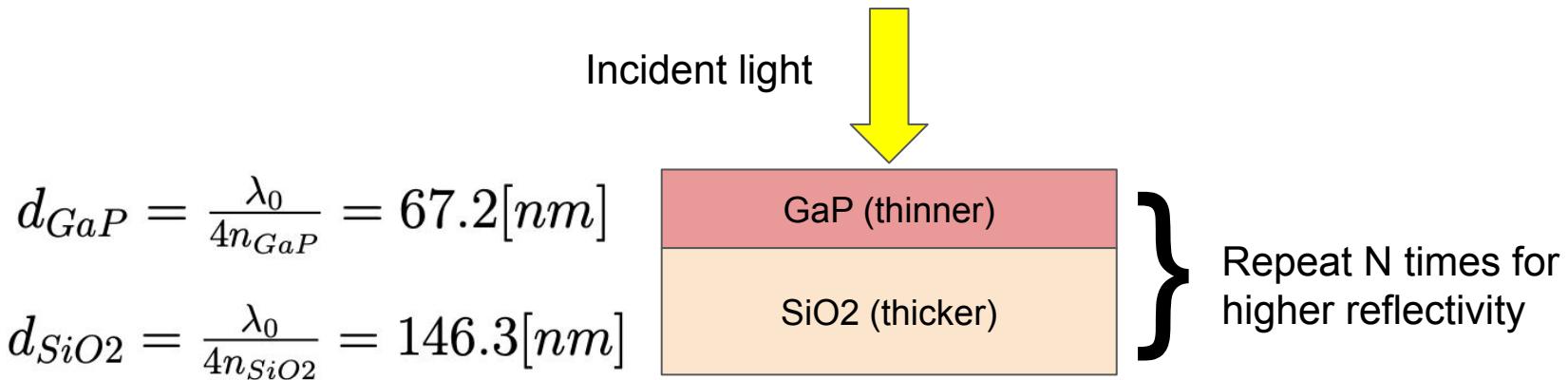
Implementation paper

At wavelength=850[nm]...

$$n_{SiO_2} = 1.4525 \quad \text{source}$$

$$n_{GaP} = 3.1621 \quad \text{source}$$

Constructing a Bragg Mirror



Length cost per layer: 213.5[nm]

Bottom DBR

From [literature](#), bottom DBR usually reflects >99.9%

Determine N using TMM matrix method

- Assume TE, angle of incidence is 0[rad]

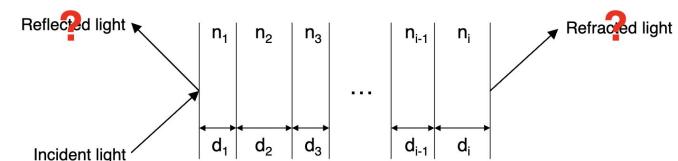
Interface matrix (TE):

$$D_{TE} = \frac{1}{2} \begin{bmatrix} 1 + \frac{n_t \cos \theta_t}{n_i \cos \theta_i} & 1 - \frac{n_t \cos \theta_t}{n_i \cos \theta_i} \\ 1 - \frac{n_t \cos \theta_t}{n_i \cos \theta_i} & 1 + \frac{n_t \cos \theta_t}{n_i \cos \theta_i} \end{bmatrix}$$

Propagation matrix

$$P_i = \begin{bmatrix} \exp(-ik_{i,z}d_i) & 0 \\ 0 & \exp(ik_{i,z}d_i) \end{bmatrix}$$

Post-simulation: N=7



$$\text{Transfer matrix } M = \begin{bmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{bmatrix} = D_{01} \cdot P_1 \cdot D_{12} \cdot P_2 \cdot \dots \cdot P_i \cdot D_{i,i+1}$$

$$\begin{pmatrix} E_i \\ E_r \end{pmatrix} = M \begin{pmatrix} E_i \\ 0 \end{pmatrix} \quad \begin{cases} \text{Transmittance: } T = \frac{|E_t|^2}{|E_i|^2} = \frac{1}{|M_{11}|^2} \\ \text{Reflectance: } R = \frac{|E_r|^2}{|E_i|^2} = \left| \frac{M_{21}}{M_{11}} \right|^2 \end{cases}$$

Length cost for bottom DBR: 1.50[um]

Top DBR

Absorbed power:

$$R + T + A = 1$$

Where,...

$R \rightarrow$ Reflectance

$T \rightarrow$ Transmittance

$A \rightarrow$ Absorbance

Can solve for A with TMM of entire stack

Varying N with fixed bottom DBR, max absorption at N=3

Length cost for top DBR: 0.64[um]

Use on M for entire stack:

$$T = \frac{|E_t|^2}{|E_i|^2} = \frac{1}{|M_{11}|^2}$$

$$R = \frac{|E_r|^2}{|E_i|^2} = \left| \frac{M_{21}}{M_{11}} \right|^2$$

Finalizing Cavity Thickness

In general, thicker intrinsic region gives higher absorption

Looking at m=5...

- TMM absorption = 93.9%
- TMM reflection = 6%
- Length = $5 \times 116.8[\text{nm}] = 584[\text{nm}]$

Total Length: 2.719[um] (satisfied!)

Intrinsic Thickness: 434[nm]

Determining Quantum Efficiency

No “direct” formula for photocurrent generation (Python not enough)

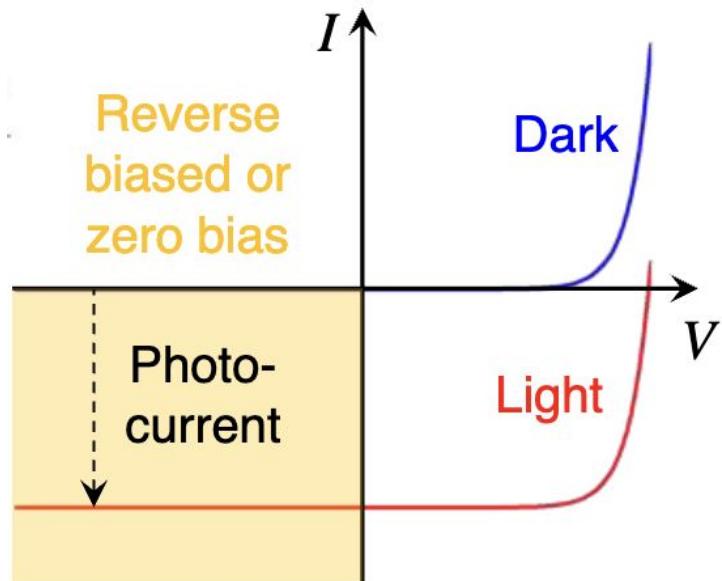
Use SimWindows to measure:

- Dark Current
- Photocurrent
- Absorption

PROBLEM: SimWindows does not model TMM (cannot simulate full RCE-PD)

To simulate, also need a reverse bias voltage

- Set to -3V



Carrier Collection Efficiency

SOLUTION: get carrier collection efficiency (ζ) of Si PIN setup

$$\eta(\lambda) = [1 - R_\lambda(\lambda)] \cdot \zeta \cdot [1 - e^{-\alpha(\lambda)d}]$$

ζ constant in setup, so we can apply this constant to the TMM model

Current Simulation Inputs:

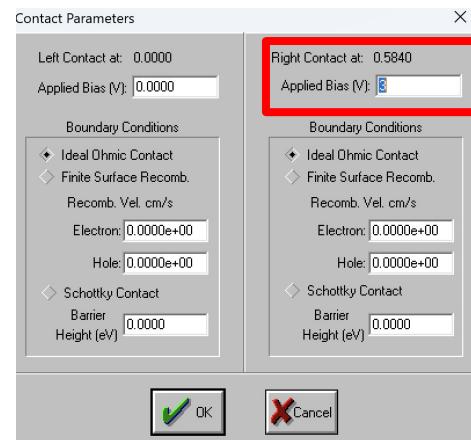
grid length=0.584 points=2500

structure material=si length=0.584

doping length=0.075 Na=1e18

doping length=0.434

doping length=0.075 Nd=1e18



Measurements

$$\eta(\lambda) = [1 - R_\lambda(\lambda)] \cdot \zeta \cdot [1 - e^{-\alpha(\lambda)d}]$$

$[1 - R_\lambda(\lambda)]$: Start Simulation in intrinsic layer (term goes to 1)

$[1 - e^{-\alpha(\lambda)d}]$: Plot “Total Poynting [mW/cm²]", calculate manually (~0.0334)

For Responsivity... $R = \frac{I_{photocurrent} - I_{dark}}{P_{in}} = \eta \cdot \frac{\lambda}{1.24}$

Power input: 100[mW/cm²]

Photocurrent at power input: $2.287 \cdot 10^{(-3)}$ [A/cm²]

Dark Counts: $8.05 \cdot 10^{(-16)}$ [A/cm²] (very negligible)

Relate **R** to ζ : $\zeta \sim 99.8\%$

$$\zeta = \frac{R \cdot 1.24}{\lambda \cdot [1 - e^{-\alpha(\lambda)d}]}$$

Quantum Efficiency Calculation

$$\eta(\lambda) = [1 - R_\lambda(\lambda)] \cdot \zeta \cdot [1 - e^{-\alpha(\lambda)d}]$$

$[1 - R_\lambda(\lambda)]$: TMM reflection (6%)

$[1 - e^{-\alpha(\lambda)d}]$: TMM absorption (93.9%)

Quantum Efficiency: 88%

Quantum Bit Error Rate (qBER)

Wanted qBER parameters:

- 50Gbps
- qBER > $10^{**}(-9)$ requested

Probability of received photons m given expected photons \bar{m} :

$$P(m) = \left(\bar{m}\right)^m \cdot \exp(-\bar{m}) / m!$$

Need to define:

- Expected photons
- Threshold for 0/1 distinguishing (base on dark current)

BER Calculation Method

From slides,... $\text{BER} = \frac{1}{2}(P_0 + P_1)$

- P_0 = probability of detecting 0 as a 1
- P_1 = probability of detecting 1 as 0

P_0 VERY small from measured dark current, threshold=1 works

$$P_0 = 1 - \frac{\bar{m}_{dark}^0 \exp(-\bar{m}_{dark})}{0!} \quad \bar{m}_{\text{dark}} = \frac{i_{\text{dark}} t_b}{q}$$

$$P_1 = \frac{\bar{m}_I^0 \exp(-\bar{m}_I)}{0!} \quad \bar{m}_I = \frac{\eta P \lambda_0}{hc \cdot \text{bps}}$$

Varying power P ,...

$P=2.89e-7[\text{W}] \rightarrow 1156[\text{mW/cm}^2]$ needed to reach BER requirement

SNR Considerations

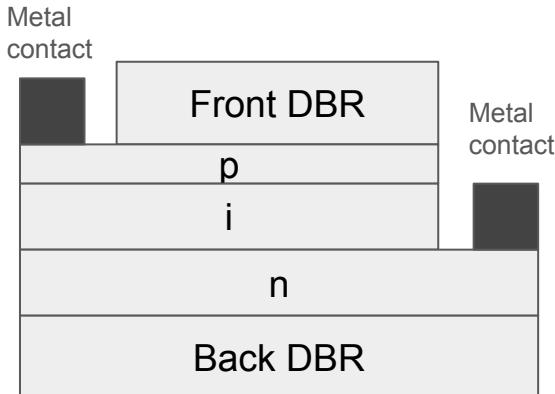
Assuming we operate at the power and bandwidth specified previously, define SNR as...

$$SNR = \left(\frac{\bar{i}}{\sigma_i} \right)^2$$

Using $\sigma_i^2 = 2e \cdot \bar{i} \cdot B$, $B \sim \frac{1}{2\tau_{int}}$, and $\bar{i} = \eta \cdot \frac{0.85}{1.24} P$, we get shot noise SNR=20dB obtained

Dark current contributes VERY little to shot noise

Final “Spec Sheet”



(not to scale)

Thickness: 2.7[um]

QE: 88%

f_3dB: 95[GHz]

Front DBR: 5um x 5um (light-receiving area)

Power for BER at 10e-9: 2.89e-7[W]

SNR at BER Power: 20dB

Reverse bias: -3[V]

Closing Thoughts

Improvements?

Cavity length could be increased

- Leeway with vertical stack thickness (I had 0.3[um] left)
- Still achieved req's, but could have been better...

Resistivity considerations

Use of AI:

- Early stages: finding relevant papers and articles on RCE-PDs
- Middle stages: Double-checking code, some erroneous assumptions
- End stages: Seeing if my values “made sense,” not very helpful...