

## 8. Birthday attack.

There are 365 possible birth days. when there's only one person, that person can born on any day out of 365 days so  $\frac{365}{365} = 1.00$ .

How about when there are two students?

The first student A can be born on any day  $\frac{365}{365}$   
But the second student B can only be born on any day other than the day that student A was born so  $\frac{364}{365}$

Probability that both of them were born on different days

$$P = \frac{365}{365} \cdot \frac{364}{365} \quad \text{---} \quad 364 = 365 - (2-1)$$

Suppose there are  $n$  student that we want to know this type of probability of. the denominator won't change from 365 but numerator seem to change for  $n$  students

365,  $365(2-1)$ ,  $365-(3-1)$ , ...,  $365-((n-1)-1)$ ,  $365-(n-1)$

And we are thinking about 40 students for this problem so

$$P(40 \text{ students born on different day}) = \frac{365}{365} \cdot \frac{364}{365} \cdot \frac{363}{365} \cdot \frac{362}{365} \cdots \frac{327}{365} \cdot \frac{326}{365}$$

$$= 0.10876819$$