

CONSIDERING WHAT IS BEING ASKED FOR, VISUALLY INSPECT THE FBD FOR A LOCATION TO SUM MOMENTS, YIELDING AN EFFICIENT EQUATION OF EQUILIBRIUM.

FOR THE FBD ABOVE,  
HERE ARE THE BEST

OPTIONS TO START YOUR ANALYSIS.

EQUATION

UNKNOWN

$$\sum M_{\text{AT PT. B}} = 0$$

$F_3$

$$\sum M_{\text{AT PT C}} = 0$$

$F_2$

$$\sum F_y = 0$$

$F_1$

INEFFICIENT STARTING OPTIONS

$$\sum F_x = 0$$

$F_2 \dotplus F_3$

$$\sum M_{\text{AT PT A}} = 0$$

$F_1 \dotplus F_3$

$$\sum M_{\substack{\text{2 FT ABOVE} \\ \text{PT B}}} = 0$$

$F_2 \dotplus F_3$

$$\sum F_{45^\circ} = 0$$

$F_1, F_2 \dotplus F_3$

$$\sum M_{\substack{\text{3 feet BELOW} \\ \text{PT A}}} = 0$$

$F_1, F_2 \dotplus F_3$

The equations of equilibrium can be thought of as a “transformer” to move from a picture to an equation. The picture (the FBD) must be transformed through a set of rules to yield an equation that will give us insights into the FBD. The insights may give us answers for the unknowns on the FBD or an affirmation of equilibrium - an independent statics check - confirming that indeed the object is in a state of equilibrium.

The “transformer” must specifically express the quantity being considered (force or moment). If a force, it must declare the direction of the forces and if a moment, it must declare the location that the moment is being calculated. Both forces and moments must state the sense of the direction for positive.

$$\rightarrow \sum F_x$$

$$+ \rightarrow \sum F_{x'}$$

$$+ \downarrow \sum F_y$$

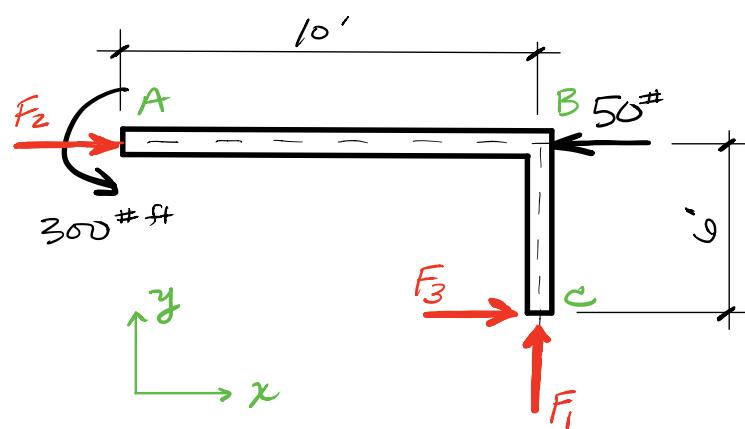
$$+ \sum M_{\text{AT PTA}}$$

$$+ \sum M_{z\text{-axis}} \\ \text{Thru pt B}$$

$$+ \sum M_{\text{AT 3 feet left of pt B}}$$

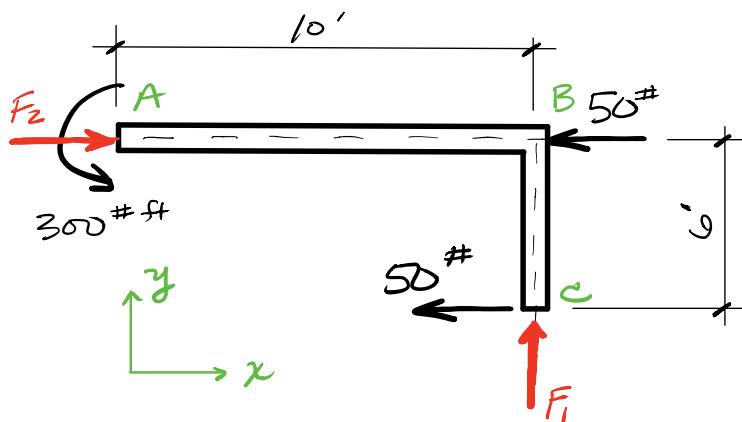
$$+ \downarrow \sum M_{y\text{-axis}} \\ \text{Thru pt C}$$

With this clear declaration, the FBD is now represented in equation form as a means to solve for the unknowns present on the diagram. **ANY NUMERICAL ANSWER RELATES TO THE FBD DRAWING.** The numerical answers, specifically if they are positive or negative, relates to the direction of the force or moment as it is drawn on the FBD. To maintain order and clarity in the calculations, you will often see the FBD redrawn with the unknowns solved for (“turned black”) The red arrows, orange arrows or purple arrows are just place holders for the numbers and senses that will replace the unknowns in due time.



$$\begin{array}{l} \text{---} \\ (+\sum M_{\text{AT PT B}} = 0) \quad -\text{OR-} \quad (+\sum M_{\text{AT PT B}} = 0) \\ -300^{\#'} - F_3 \times 6' = 0 \quad | \quad +300^{\#'} + F_3 \times 6' = 0 \\ F_3 = -50^{\#} \quad | \quad F_3 = -50^{\#} \\ \text{or } 50^{\#} \leftarrow \quad | \quad \text{or } 50^{\#} \leftarrow \end{array}$$

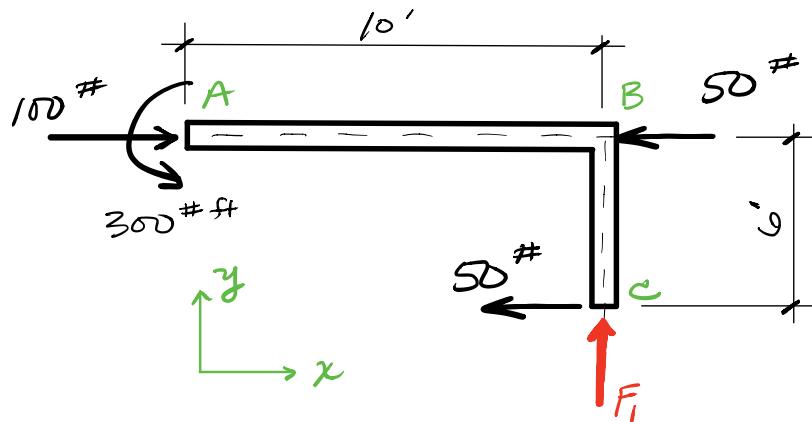
- SAME ANSWER -  
Now THE FBD LOOKS LIKE



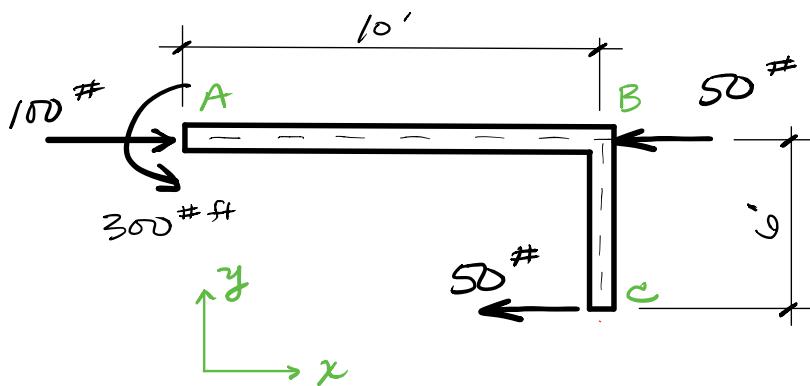
$$\begin{array}{l} (+\sum M_{\text{AT PT C}} = 0) \\ -300^{\#'} - 50^{\#} \cdot 6' + F_2 \cdot 6' = 0 \\ F_2 = +100^{\#} \text{ or } 100^{\#} \rightarrow \end{array}$$

- OR -

$$\begin{array}{l} (+\sum M_{\text{AT PT C}} = 0) \\ +300^{\#'} + 50^{\#} \cdot 6' - F_2 \cdot 6' = 0 \\ F_2 = +100^{\#} \text{ or } 100^{\#} \rightarrow \end{array}$$



$$\begin{aligned}
 & \text{(+} \sum M \text{ at pt A)} = 0 \\
 & +300\# \cdot 6' - 50\# \cdot 6' + F_I \cdot 10' = 0 \\
 & F_I \cdot 10' = 0 \\
 & F_I = 0
 \end{aligned}$$



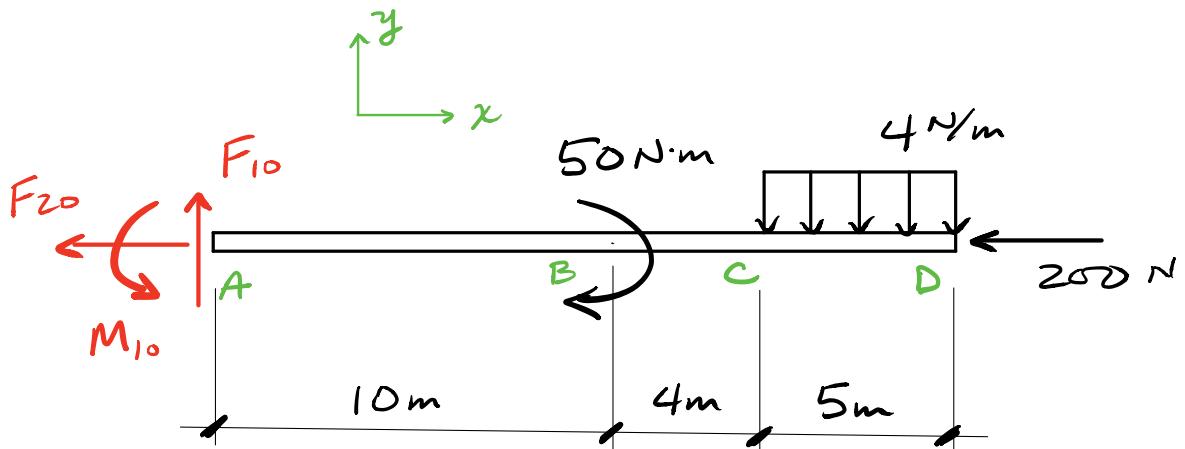
To get to this point, we have used three equations. We have summed moments at pt A, pt B and pt C. Each equation has been efficient - yielding a single unknown. We now have a solved FBD. However, we still have an infinite number of equations that will be satisfied if the solved FBD is in equilibrium. Let's choose any equation that has not already been used. The best equations to use here are ones that involve every force present on the FBD. For instance, if we sum moments halfway between points A and B, the 50# force at B and the 100# force at point A will not be present in the equation as they have a zero lever arm. But, summing moments 3 feet above the halfway point between A and B involves every force on the FBD and since they are all black arrows, that is good. The independent statics check will be thorough.

$$\begin{aligned}
 & \text{(+} \sum M \text{ } 6' \text{ ABOVE MIDWAY SEGMENT)} = 0 \\
 & -300\# \cdot AB - 100\# \cdot 3' + 50\# \cdot 3' + 50\# \cdot 9' = 0 \\
 & -300\# \cdot 3' - 300\# \cdot 150\# \cdot 450\# = 0
 \end{aligned}$$

$$O = O \quad \checkmark$$

$\Rightarrow$  EQUILIBRIUM  
CONFIRMED!

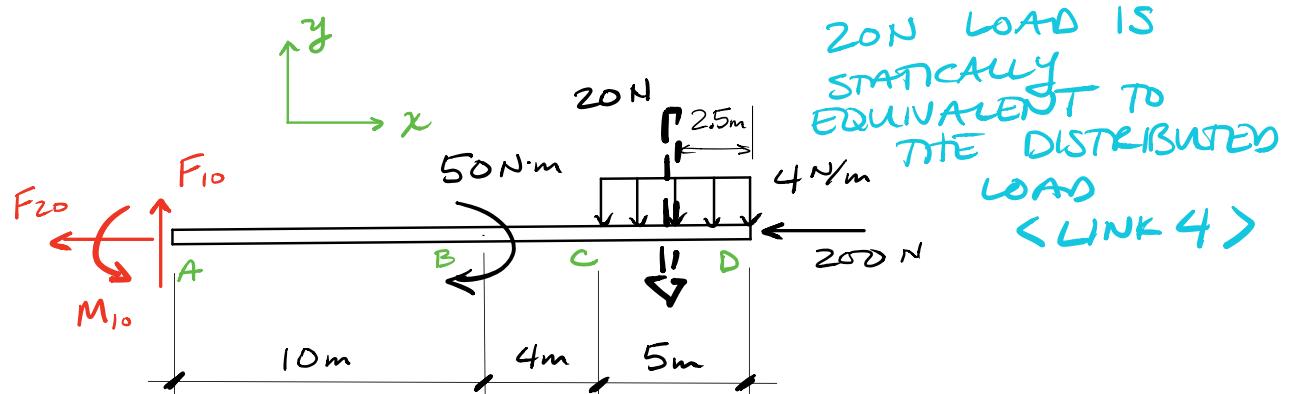
ANOTHER EXAMPLE



$$\sum M_{\text{AT PT A}} = 0 \quad M_{10}$$

$$\sum F_x = 0 \quad F_{20}$$

$$\sum F_y = 0 \quad F_{10}$$



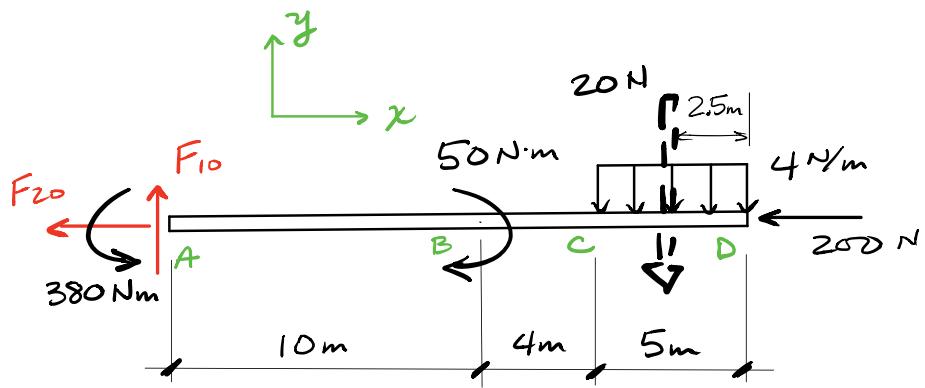
$$(\rightarrow \sum M_{\text{AT PT A}} = 0$$

$$-M_{10} + 50\text{ N}\cdot\text{m} + 20\text{ N} \cdot (14\text{ m} + 2.5\text{ m}) = 0$$

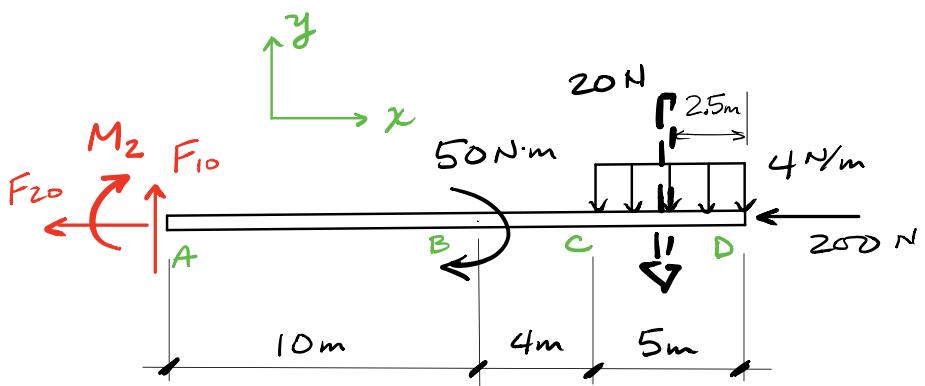
$$-M_{10} = -380\text{ N}\cdot\text{m}$$

$$M_{10} = 380\text{ N}\cdot\text{m}$$

$$\approx 380\text{ N}\cdot\text{m} \checkmark$$



ASIDE : IF THE INITIAL FBD WAS DRAWN DIFFERENT - BUT CORRECT :



$$\zeta + \sum M_{\text{AT PT } A} = 0$$

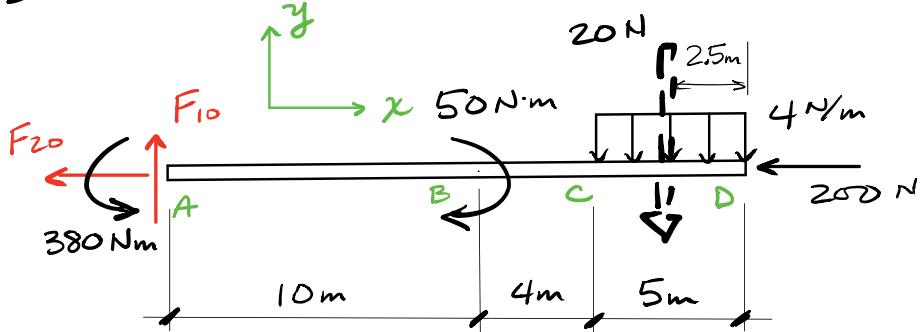
$$-M_2 - 50 \text{ N·m} - 20 \text{ N}(14 \text{ m} + 2.5 \text{ m}) = 0$$

$$-M_2 = +380 \text{ N·m}$$

$$M_2 = -380 \text{ N·m}$$

or  $380 \text{ N·m} \curvearrowleft$

FBD LOOKS THE SAME :



$$(\rightarrow \sum M \text{ AT PT B}) = 0$$

$$-380 \text{ Nm} + 50 \text{ Nm} + F_{10} \cdot 10 \text{ m} + 20 \text{ N} \cdot (4 \text{ m} + 2.5 \text{ m}) = 0$$

$$F_{10} \cdot 10 \text{ m} = 200 \text{ Nm}$$

$$F_{10} = 20 \text{ N}$$

or  $20 \text{ N} \uparrow$

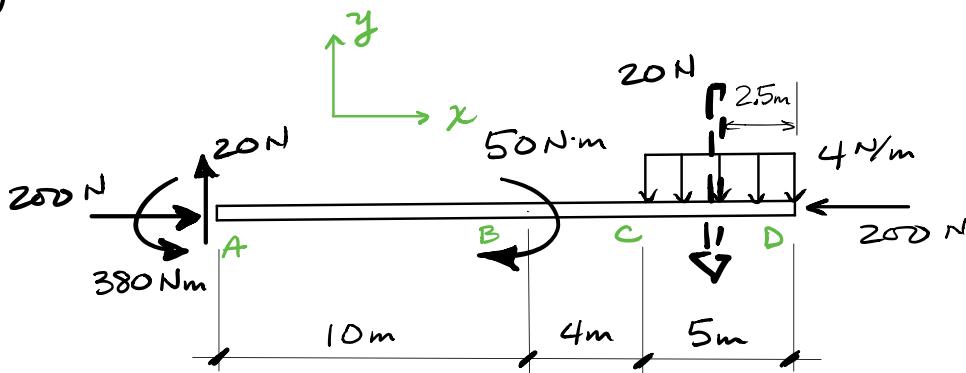
$$\leftarrow \sum F_x = 0$$

$$F_{20} + 200 \text{ N} = 0$$

$$F_{20} = -200 \text{ N}$$

or  $200 \text{ N} \rightarrow$

YIELDING A SOLVED FBD :



INDEPENDENT STATICS CHECK :

$$(\rightarrow \sum M_{2 \text{ m BELOW PT. D}} = 0)$$

$$+ 200 \text{ N} \cdot 2 \text{ m} + 20 \text{ N} \cdot 19 \text{ m} - 380 \text{ Nm} + 50 \text{ Nm}$$

$$- 20 \text{ N} \cdot 2.5 \text{ m} - 200 \text{ N} \cdot 2 \text{ m} = 0$$

$$0 = 0$$

$\Rightarrow$  EQUILIBRIUM  
CONFIRMED