

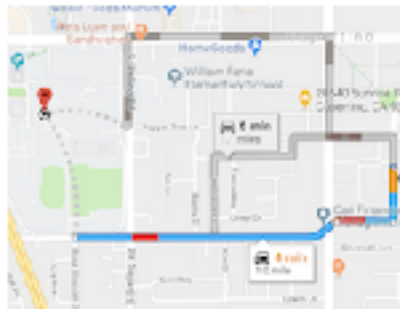
# Dijkstra's Algorithm

## A Deep Dive and Implementation

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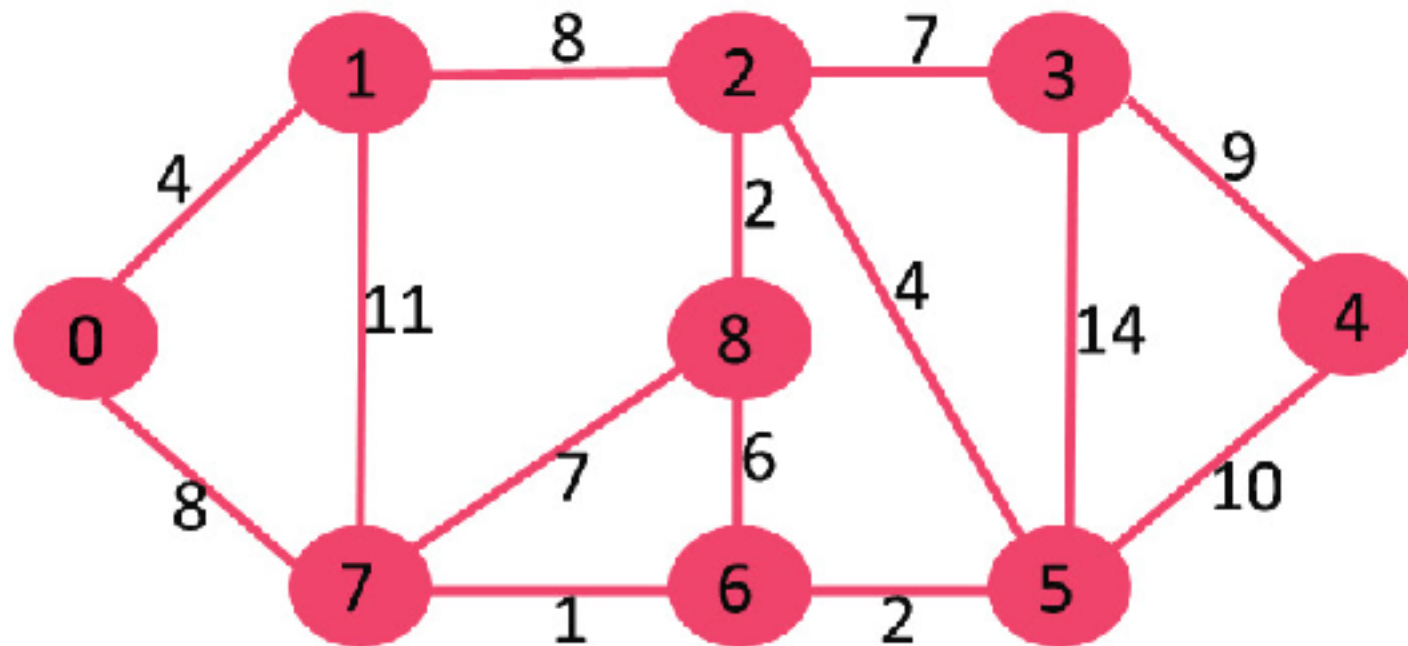
# Introduction

- "Simplicity is a prerequisite for reliability" - Edsger Dijkstra



- A search algorithm and graph data structure designed to find the shortest path between two nodes in a connected graph.
- Designed by Edsger Dijkstra in 1956

## Explanation



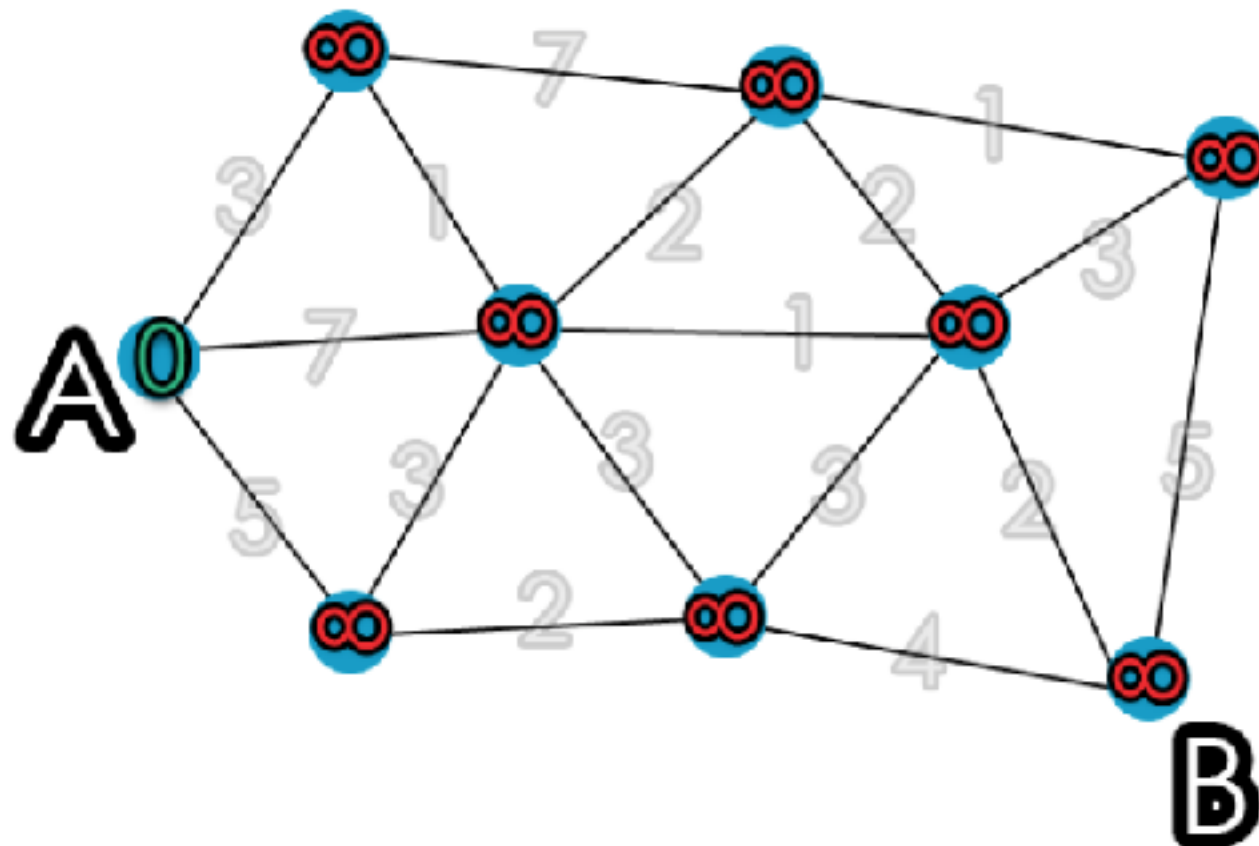
- There are nodes (or vertices)
- Weighted edges connect nodes

## Explanation Continued

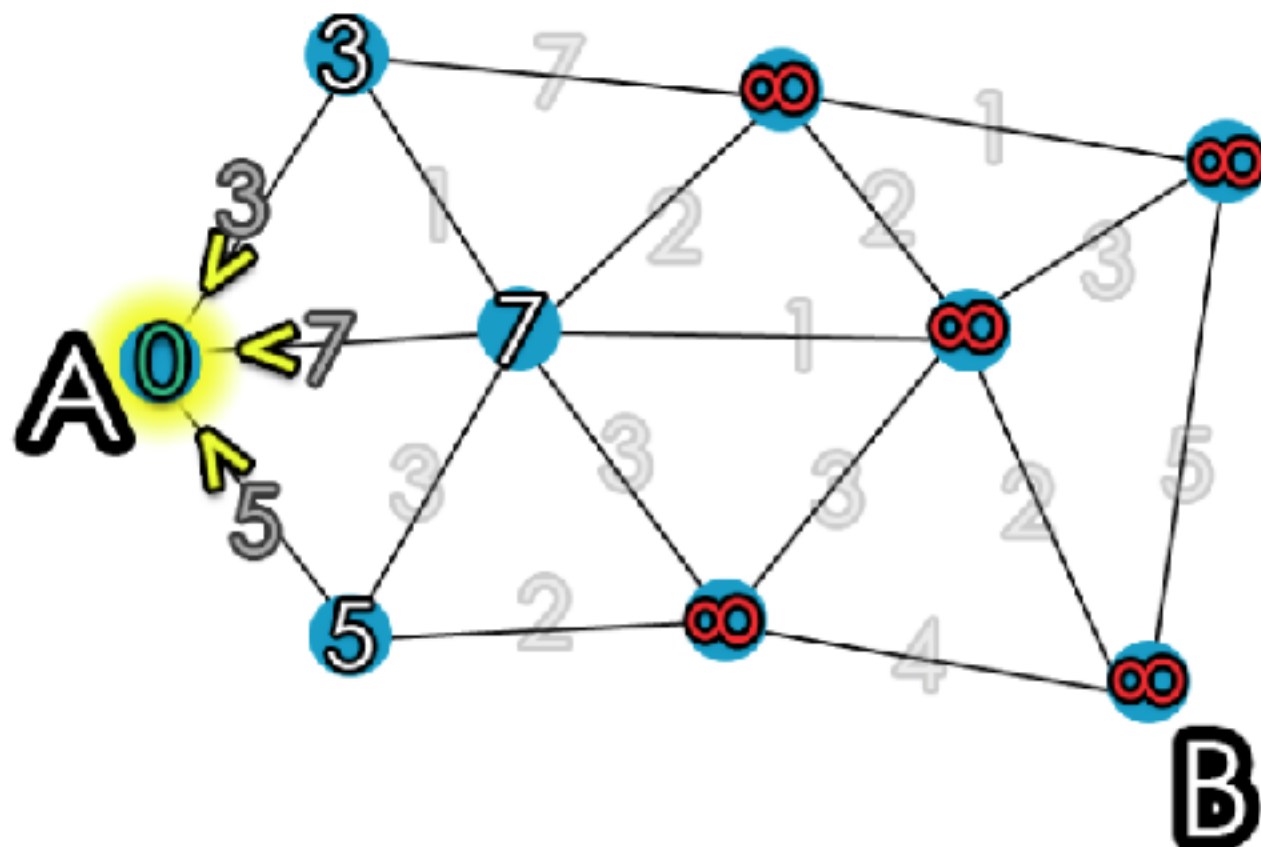
- `dist` initialized, an array to store distances from source node
  - `dist(s) = 0` since the distance from source node should be 0
  - `dist(v) = infinity` since distances to all other nodes are unknown
  - $Q$ , a queue is used to store all nodes in the graph,  $Q$  will be empty by the time the algorithm is done
  - $S$  represents the set of nodes the algorithm visited

# Pseudo-explanation

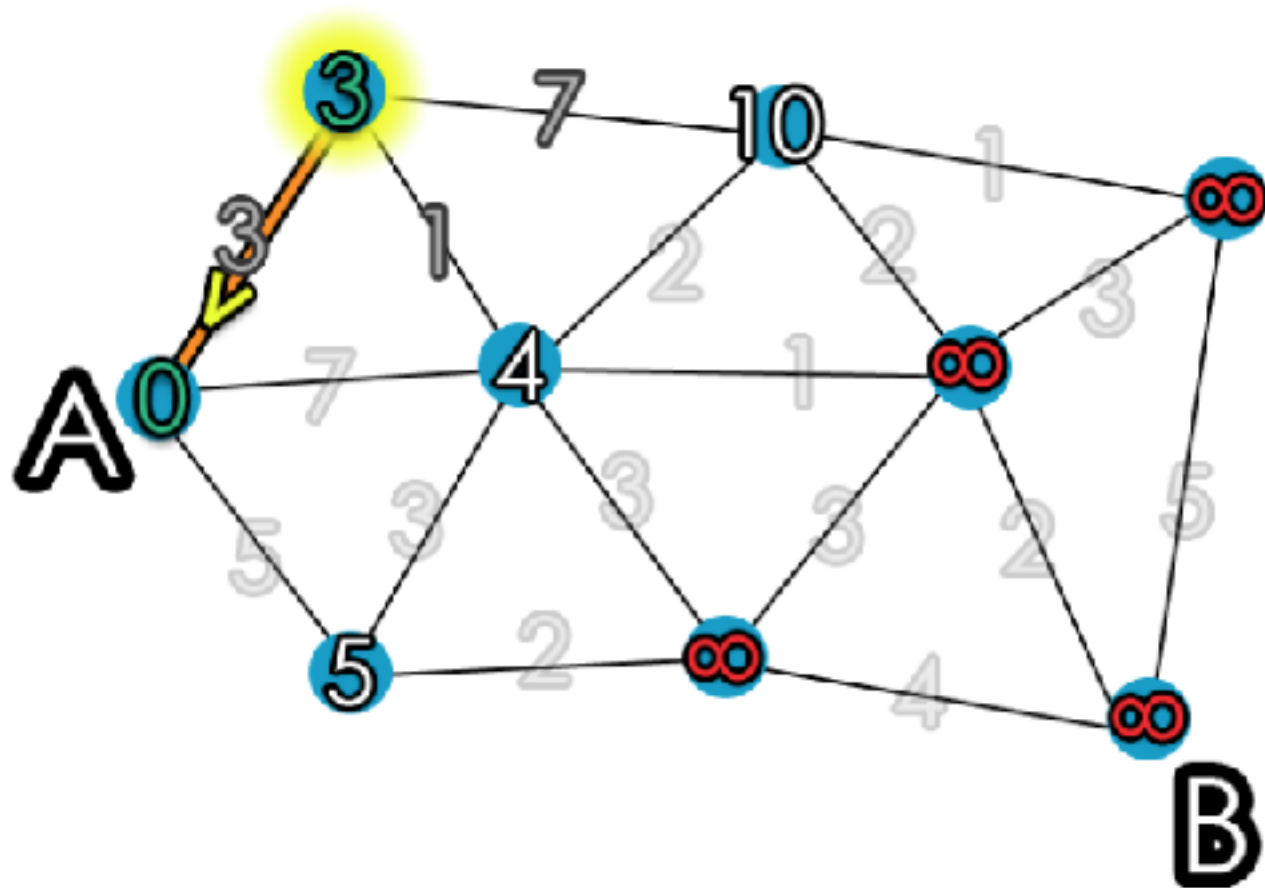
Suppose you have this connected graph:



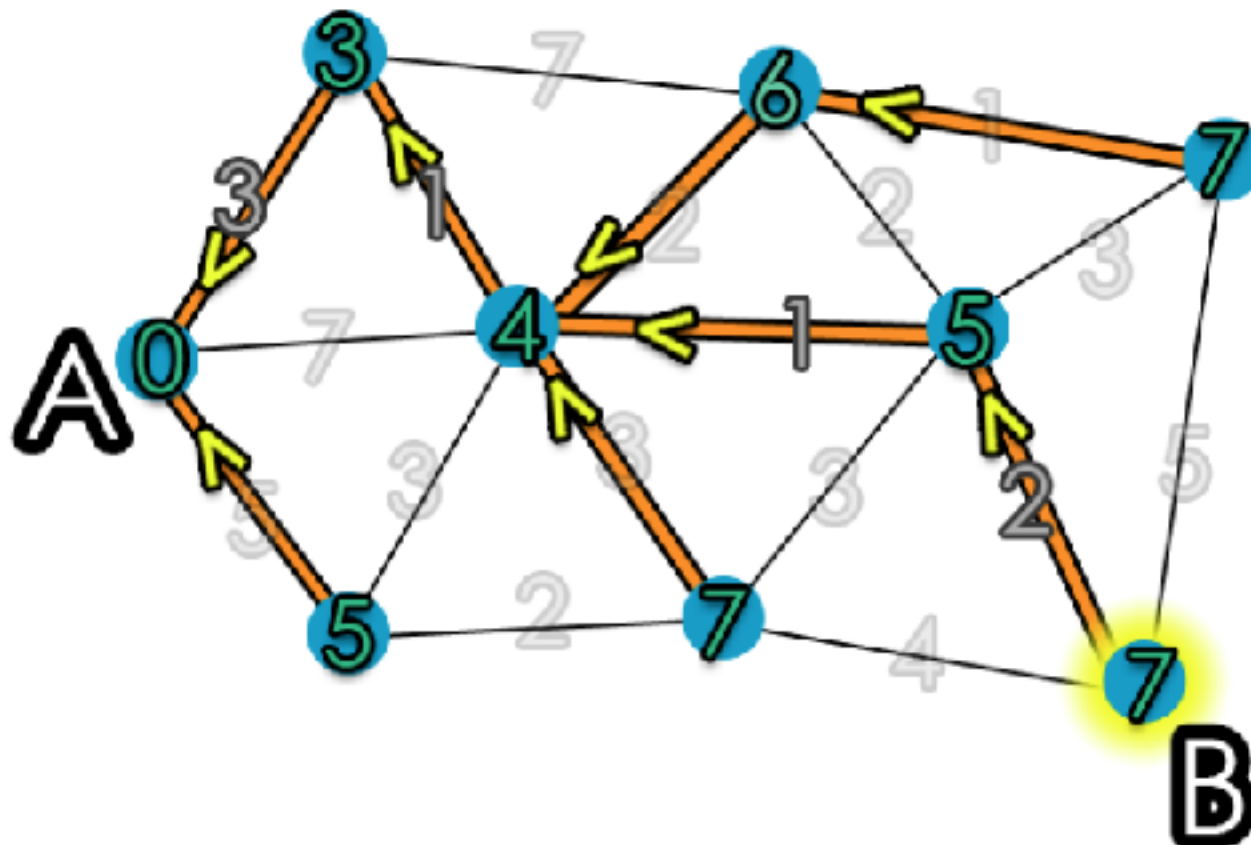
Calculate distances to adjacent nodes



Pick node closest to source node



Finally we get





# Psuedocode

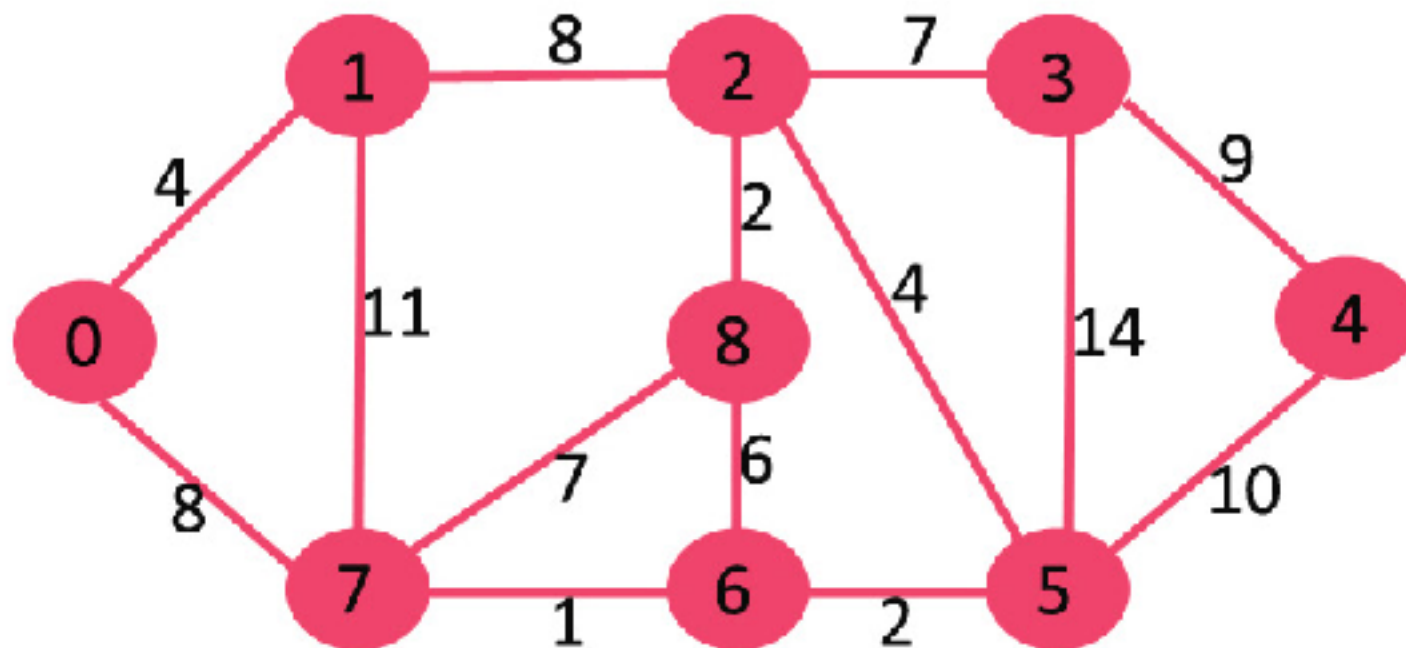
```
dist[s] = 0
for all other distances:
    dist[v] = infinity

S                                     #initialize
Q = V                               #initialize V

while Q not null:                    #initalize Q is not null
    do u = minDistance(Q) #select element u w/ min di.
    S = S union {u} # add u to list of visited vert.
    for all v in neighbors of {u}
        do if dist[v]>dist[u] + w(u,v)
            # if new shortest path found
            then d[v] = d[u]+w(u,v)
            #set value of shortest path
```

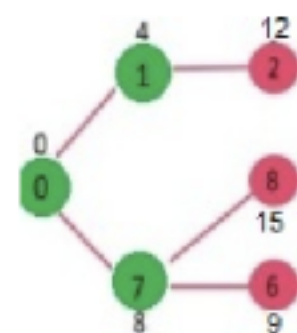
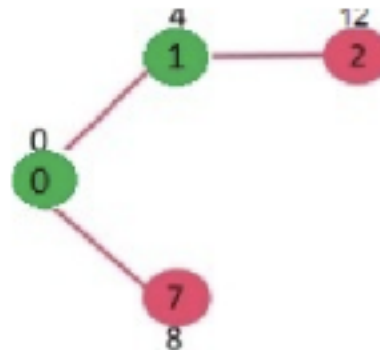
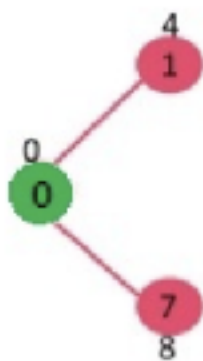
# Another Implementation

- Given a graph with weighted edges, construct a shortest-path "tree."
- Create a min heap and put in all the vertices.
  - Ordered by distance from source.
- Any node added into the SPT will be removed from this heap.



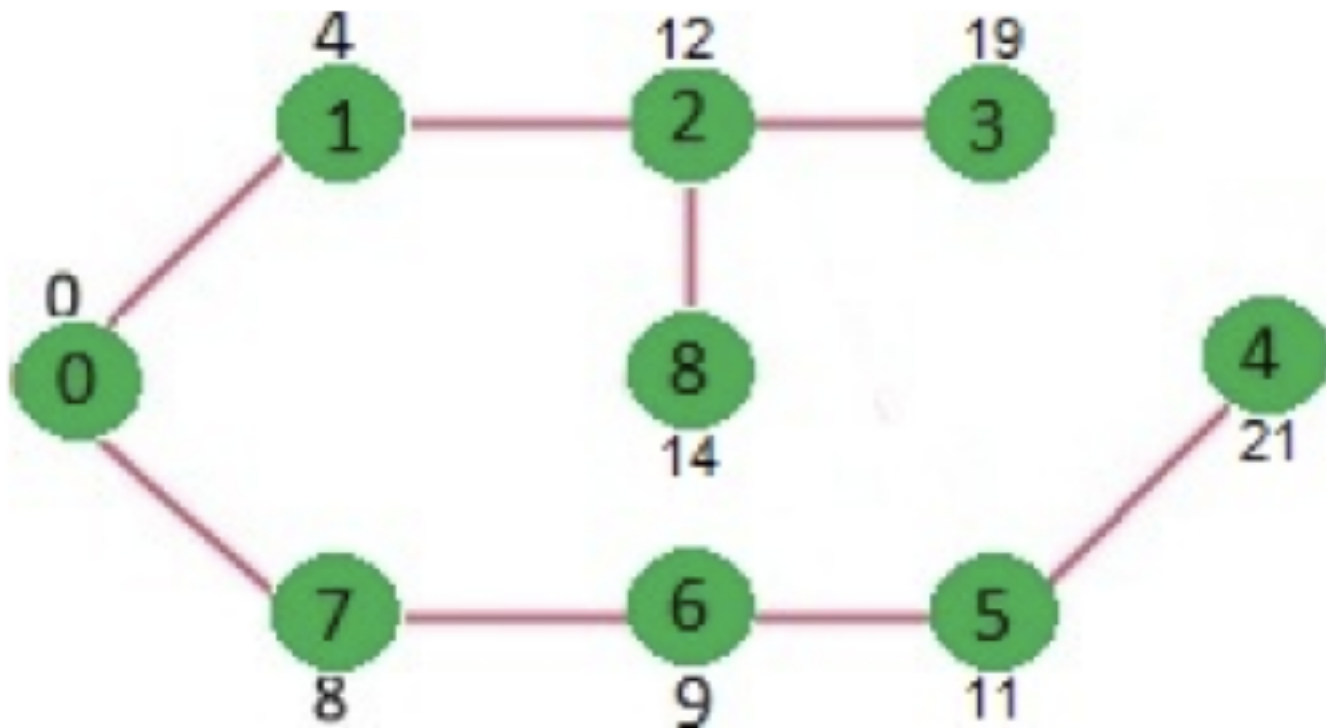
## Another Implementation Continued

- Start by adding the source node into the SPT.
- Retrieve the top of the heap (a.k.a. the node closest to the source) and add it to the SPT.
- Update distances of nodes adjacent to the picked node.
- Repeat above two steps until every node is in the SPT/nothing left in the heap.



## Another Implementation Extended

- Completed SPT:



# Data Structures Used

- Adjacency Matrix
  - Used to store the graph.
- Arrays
  - Min heap and adjacency matrix implementation uses this.
  - ArrayLists/Vectors could have been used, but that would be excessively complicated.
- Heaps
  - Used to determine the node closest to the source to add to the SPT.
- Linked Lists
  - Used as adjacency lists for each vertex.

## Big O Analysis

- Our implementation:  $O(n^2)$
- Can be improved by simply storing the edges instead of the entire graph to  $O(E \log V)$ 
  - $E$  - Number of edges.
  - $V$  - Number of vertices.

# Implementation

**Have a nice day!**