

Fifth Semester B.E. Semester End Examination, JANUARY-MARCH 2023**FORMAL LANGUAGES AND AUTOMATA THEORY**

Time: 3 hrs.

Max. Marks :100

Instructions :1. Answer any FIVE full Question selecting at least ONE Question from Each Unit.

MODULE 1**L CO PO M**

1a. Elaborate the formal definition of DFA. Define transition diagram and transition table.

[1] [1] [1] [6]

1b. Design a DFA to accept all the strings with no more than 3 a's continuously. Each string in this language consists of a's and b's.

[3] [1] [2] [7]

1c. Convert the following Non-Deterministic Finite Automata (NFA) to Deterministic Finite Automata (DFA) using subset construction.

δ	a	b
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_0\}$
q_1	ϕ	$\{q_2\}$
$*q_2$	ϕ	ϕ

[3] [1] [2] [7]

OR

2a. Convert the following E-NFA to its equivalent DFA.

δ	a	b
$\rightarrow A$	B	ϕ
B	ϕ	C
$*C$	D	E
$*D$	D	E
$*E$	D	E

[3] [1] [1] [8]

2b. Indicate the ϵ -closure for all states of the following.

δ	ϵ	a	b	c
$\rightarrow p$	ϕ	$\{p\}$	$\{q\}$	$\{r\}$
q	$\{p\}$	$\{q\}$	$\{r\}$	ϕ
$*r$	$\{q\}$	$\{r\}$	ϕ	$\{p\}$

[2] [1] [1] [4]

2c. Design an NFA that accepts the language $L = \{wbb \mid w \in \Sigma(a,b)^*\}$.

Convert the resultant NFA to DFA.

[3] [1] [1] [8]

MODULE 2

3a. Define Regular expression. Obtain a Regular Expression for the following

1. $L = \{a^n b^m \mid n \geq 1, m \geq 1 \text{ and } nm \leq 3\}$
2. $L = \{vuv \mid v, u \in (a, b)^* \text{ and } |v| = 2\}$
3. Set of all strings that do not end with "01" over $\Sigma = \{0, 1\}$

[3] [2] [3] [12]

3b. Define Regular Expression. Apply state elimination method to obtain the Regular Expression

δ	0	1
*q0	q0	q1
*q1	q2	q1
q2	q2	q2

[3] [2] [3] [8]

OR

4a.

Define Distinguishable and Indistinguishable states. Apply Table Filling Algorithm to obtain a minimum state Automata

δ	0	1
$\rightarrow A$	B	C
B	C	E
*C	D	C
D	C	C
*E	B	E

[3] [2] [3] [12]

4b. Let R be a Regular Expression. Then Prove that there exists a finite automaton $M = (Q, \delta, q_0, A)$ which accepts $L(R)$.

[2] [2] [2] [8]

MODULE 3

5a. Define Context Free Grammar. Obtain a context free grammar to generate a language $L = \{a^n b^m \mid n \neq m\}$

[3] [3] [2] [6]

5b. Consider the context free grammar with productions.

- $$\begin{aligned} S &\rightarrow aB \mid bA \\ A &\rightarrow aS \mid bAA \mid a \\ B &\rightarrow bS \mid aBB \mid b \end{aligned}$$

Write leftmost derivation for the string aaabbabbba using the grammar

[3] [3] [1] [6]

5c. Eliminate unit productions from the grammar

- $$\begin{aligned} S &\rightarrow AB \\ A &\rightarrow a \\ B &\rightarrow C \mid b \\ C &\rightarrow D \\ D &\rightarrow E \mid bC \\ E &\rightarrow d \mid Ab \end{aligned}$$

[2] [3] [1] [8]

OR

6a. Show that the following grammar is ambiguous for the string aabbab

- $$\begin{aligned} S &\rightarrow aB \mid bA \\ A &\rightarrow aS \mid bAA \mid a \\ B &\rightarrow bS \mid aBB \mid b \end{aligned}$$

[3] [3] [2] [8]

6b. Define sentential form with an example.

[2] [3] [1] [4]

6c. Eliminate Useless symbols in the grammar.

$S \rightarrow aA \mid bB$

$A \rightarrow aA \mid a$

$B \rightarrow bB$

$D \rightarrow ab \mid Ea$

$E \rightarrow aC \mid d$

[3] [3] [2] [8]

MODULE 4

7a. Define PushDown Automata. Design a PDA to accept the following Language by final state $L = \{ na(w) = nb(w), \text{ where } n \geq 1 \}$

[3] [4] [3] [10]

7b. Define Turing machine. With a neat diagram explain the working model of Turing machine.

[2] [4] [2] [5]

7c. Design a Turing Machine to accept the language containing strings of 0's and 1's ending with 011.

[3] [4] [3] [5]

OR

8a. Design a Turing Machine to accept the following language and show the sequence of moves made by the Turing machine for the string "aaabbb" $L = \{ a^n b^n, \text{ where } n \geq 1 \}$

[3] [4] [3] [10]

8b. Design a PDA to accept the following language $L = \{ a^n b^m c^n, \text{ where } n, m \geq 1 \}$

[3] [4] [3] [10]

MODULE 5

9a. Explain the structure of Lex program with an example.

[2] [5] [1] [7]

9b. Design a lex program to count the number of words.

[3] [5] [1] [7]

9c. Explain yacc parser with an example.

[2] [5] [1] [6]

OR

10a. Summarize lexer parser communication

[2] [5] [1] [5]

10b. Define regular expression. Explain characters that form a regular expression

[2] [5] [1] [8]

10c. Develop a yacc program to recognize a valid arithmetic expression that uses operators +, -, * and /.

[3] [5] [1] [7]