

26/12/22

Theory of Approximate Reasoning

Rules:- 1) If \rightarrow then

2) If \rightarrow then else

1) If \rightarrow then

if x is A then y is B where $x \in Y$ are
the universes and $A \in X$ & $B \in Y$ are fuzzy sets on
the given universes respectively.

Here if part is called as Antecedent &
then part is called as Consequent.

The above rule is expressed in terms of fuzzy
logic as,

$$R = (A \times B) \cup (\bar{A} \times Y) \quad \text{where } Y \text{ is universe}$$

e.g.: - If temperature is high then speed is high.

2) If \rightarrow then else :-

if x is A then y is B else y is C
Antecedent consequent consequent

In the above rule

$$R = (A \times B) \cup (\bar{A} \times C)$$

The above consist of two antecedents, thus
consequents i.e. (x is A) acts as Antecedent
for consequent y (y is B) is executed
if Antecedent (x is A) is not executed

e.g.: - If tomatoes are red then they are ripe
else they are not ripe.

①

$$A = \left\{ \frac{0.1}{x_1} + \frac{0.2}{x_2} + \frac{0.5}{x_3} \right\} \in X$$

$$B = \left\{ \frac{0.6}{y_1} + \frac{0.3}{y_2} + \frac{0.1}{y_3} \right\} \in Y$$

find "if x is A then y is B"

$$\text{soln: } R = (A \times B) \cup (\bar{A} \times C)$$

$$Y = \left\{ \begin{array}{l} 1 \\ 1 \\ 1 \end{array} \right\} \quad (\text{max of max is } 1)$$

$$A \times B \subset Y \quad \bar{A} = \left\{ \frac{0.9}{x_1} + \frac{0.8}{x_2} + \frac{0.5}{x_3} \right\}$$

$$A \times B = \begin{bmatrix} 0.1 & 0.1 & 0.1 \\ 0.2 & 0.2 & 0.1 \\ 0.5 & 0.3 & 0.1 \end{bmatrix}$$

$$\bar{A} \times Y = \begin{bmatrix} 1 & 1 & 1 \\ 0.9 & 0.9 & 0.9 \\ 0.8 & 0.8 & 0.8 \\ 0.5 & 0.5 & 0.5 \end{bmatrix}$$

$$R = \begin{bmatrix} 0.9 & 0.9 & 0.9 \\ 0.8 & 0.8 & 0.8 \\ 0.5 & 0.5 & 0.5 \end{bmatrix}$$

$$C = \left\{ \frac{0.6}{y_1} + \frac{0.1}{y_2} + \frac{1}{y_3} \right\} \in Y$$

find "if x is A then y is B & else y is C"

$$R = (A \times B) \cup (\bar{A} \times C)$$

$$\bar{A} \times C = \begin{bmatrix} 0.6 & 0.1 & 0.9 \\ 0.6 & 0.1 & 0.8 \\ 0.5 & 0.1 & 0.5 \end{bmatrix}$$

$$R = \begin{bmatrix} 0.6 & 0.1 & 0.9 \\ 0.6 & 0.2 & 0.8 \\ 0.5 & 0.3 & 0.5 \end{bmatrix}$$

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Suppose we are evaluating a new issue innovation to determine its commercial protection. We will use a matrix R . Uniqueness of innovation denoted by the universe novelty skills.

$x = [1, 2, 3, 4]$ & the market size of innovation commercial market denoted by the universal market size.

$y = [1, 2, 3, 4, 5, 6]$ In both universe lowest numbers are with highest uniqueness and highest market size new innovation is the group say compressible liquid or very useful temp air the and viscosity.

has just received score of medium uniqueness denoted by A and medium market size B . We wish to determine implication that is if medium uniqueness and "medium market size" following on the given fuzzy set also find if medium uniqueness than medium market size like different market size.

Suppose the fuzzy relation are developed using if then rule, describe the \rightarrow innovation potential. We wish to know what market size would be associated with a b uniqueness almost high uniqueness with new anticipated a find the consequent B' using max min composition

$$A' = \text{almost high uniqueness} = \left\{ \frac{0.5}{1} + \frac{1}{2} + \frac{0.3}{3} + \frac{0}{4} \right\}$$

$$A = \text{medium uniqueness} = \left\{ \frac{0.6}{2} + \frac{1}{3} + \frac{0.2}{4} \right\}$$

$$B = \text{medium market size} = \left\{ \frac{0.4}{1} + \frac{0.5}{2} + \frac{0.6}{3} + \frac{0.6}{4} + \frac{0.6}{5} + \frac{0.3}{6} \right\}$$

$$B = \text{medium market size} = \left\{ \frac{0.4}{2} + \frac{1}{3} + \frac{0.8}{4} + \frac{0.3}{5} \right\}$$

$$C = \text{diffuse market size} = \left\{ \frac{0.3}{1} + \frac{0.5}{2} + \frac{0.6}{3} + \frac{0.6}{4} + \frac{0.6}{5} \right\} + 0.39$$

$$y = \left\{ \frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \frac{1}{6} \right\}$$

$A \times B$

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	0.4	0.6	0.6	0.3	0
3	0	0.4	1	0.8	0.3	0
4	0	0.2	0.2	0.2	0.2	0

$$\bar{A} = \left\{ \frac{1}{1} + \frac{0.4}{2} + \frac{0}{3} + \frac{0.8}{4} \right\}$$

$\bar{A} \times y$

	1	2	3	4	5	6
1	1	1	1	1	1	1
2	0.4	0.4	0.4	0.4	0.4	0.4
3	0	0	0	0	0	0
4	0.8	0.8	0.8	0.8	0.8	0.8

$$R = (A \times B) \cup (\bar{A} \times y)$$

	1	2	3	4	5	6
1	1	1	1	1	1	1
2	0.4	0.4	0.6	0.6	0.4	0.4
3	0	0.4	1	0.8	0.3	0
4	0.8	0.8	0.8	0.8	0.8	0.8

$$I_2 - \text{then} - \text{else} \quad R = (A \times B) \cup (\bar{A} \times C)$$

Q2

$$\bar{A} \times C = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 \end{bmatrix}$$

1	0.3	0.5	0.6	0.6	0.5	0.3
2	0.3	0.4	0.4	0.4	0.4	0.3
3	0	0	0	0	0	0
4	0.3	0.5	0.6	0.6	0.5	0.3

$$R = (A \times B) \cup (\bar{A} \times C)$$

1	2	3	4	5	6	
1	0.3	0.5	0.6	0.6	0.5	0.3
2	0.3	0.4	0.6	0.6	0.4	0.3
3	0	0.4	1	0.8	0.3	0
4	0.3	0.5	0.6	0.6	0.5	0

By using principle of cylindrical extension principle
extending A on y domain

$$A' = \left\{ \frac{0.5}{1}, \frac{1}{2}, \frac{0.3}{3}, \frac{0}{4} \right\} \rightarrow \text{convert to matrix}$$

$$B' = A' \cdot R$$

	1	2	3	4	5	6
1	0.5	1	0.3	0		
2		0.4	0.4	0.6	0.6	0.4
3		0	0.4	1	0.8	0.3
4		0.8	0.8	0.8	0.8	0.8

$$B' = [0.5, 0.5, 0.6, 0.6, 0.5, 0.5]$$

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①

$$W = \text{weak stimulus} = \left\{ \frac{1}{0} + \frac{0.9}{50} + \frac{0.3}{100} + \frac{10}{150} + \frac{0}{200} \right\} \text{Ex}$$

$$M = \text{medium stimulus} = \left\{ \frac{0}{0} + \frac{0.4}{50} + \frac{1}{100} + \frac{0.4}{150} + \frac{0}{200} \right\} \text{Ex}$$

$$S = \text{desire response} = \left\{ \frac{0}{0} + \frac{0}{50} + \frac{0.5}{100} + \frac{0.9}{150} + \frac{1}{200} \right\} \text{Ey}$$

- find if weak stimulus then net desire response.

$$\text{net desire} = \bar{S} = \left\{ \frac{1}{0} + \frac{1}{50} + \frac{0.5}{100} + \frac{0.1}{150} + \frac{0}{200} \right\} \text{Ey}$$

$$\text{if } x \in A \text{ then } y \in \bar{B} = (A \times \bar{B}) \cup (\bar{A} \times y) \\ = (w \times \bar{s}) \cup (\bar{w} \times y)$$

$$\bar{w} = \left\{ \frac{0}{0} + \frac{0.1}{50} + \frac{0.7}{100} + \frac{1}{150} + \frac{1}{200} \right\} \text{Ex}$$

$$w \times \bar{s} = \left\{ \frac{0}{0}, \frac{0}{50}, \frac{0.3}{100}, \frac{0}{150}, \frac{0}{200} \right\} \text{Ey}$$

$$y = \left\{ \frac{1}{0} + \frac{1}{50} + \frac{1}{100} + \frac{1}{150} + \frac{1}{200} \right\}$$

$$w \times \bar{s} = \begin{matrix} 0 & 1 & 1 & 0.5 & 0.1 & 0 \\ 50 & 0.9 & 0.4 & 0.5 & 0.1 & 0 \\ 100 & 0.3 & 0.3 & 0.3 & 0.1 & 0 \\ 150 & 0 & 0 & 0 & 0 & 0 \\ 200 & 0 & 0 & 0 & 0 & 0 \end{matrix}$$

$$\bar{w} \times y = \begin{matrix} 0 & 0 & 0 & 0 & 0 \\ 50 & 0.1 & 0.1 & 0.1 & 0.1 & 0.1 \\ 100 & 0.7 & 0.7 & 0.7 & 0.7 & 0.7 \\ 150 & 1 & 1 & 1 & 1 & 1 \\ 200 & 1 & 1 & 1 & 1 & 1 \end{matrix}$$

	0	50	100	150	200
0	1	1	0.5	0.1	0
50	0.9	0.9	0.5	0.1	0.1
100	0.7	0.7	0.7	0.7	0.7
150	1	1	1	1	1
200	1	1	1	1	1

Find the response B' , if medium stimulus i.e.
find $B' = S \cdot R$ using max min & comp

$$S = \left\{ \frac{0}{0} + \frac{0}{50} + \frac{0.5}{100} + \frac{0.1}{150} + \frac{1}{200} \right\}$$

$$\boxed{B' = A' \cdot R}$$

$$(1 \times 5) \begin{bmatrix} 0 & 0.4 & 1 & 0.4 & 0 \end{bmatrix} \begin{bmatrix} 1 & 1 & 0.5 & 0.1 & 0 \\ 0.9 & 0.9 & 0.5 & 0.1 & 0.1 \\ 0.7 & 0.7 & 0.7 & 0.7 & 0.7 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$

max min Comp

$$B' = [0.7 \quad 0.7 \quad 0.7 \quad 0.7 \quad 0.7]$$

(7)

weight of:

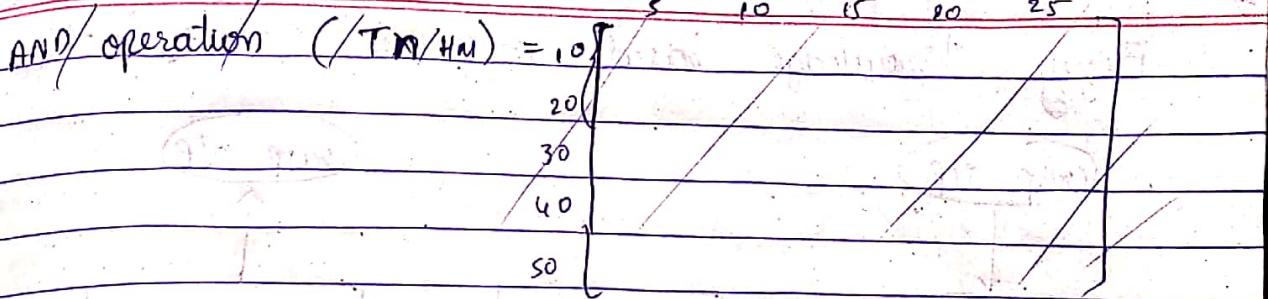
$$\textcircled{2} \quad T = \text{Heat Temp} \left\{ \frac{0.1}{10} + \frac{0.2}{20} + \frac{0.5}{30} + \frac{0.8}{40} + \frac{0.9}{50} \right\} \text{C}$$

$$H_m = \text{moderate humidity} = \left\{ \frac{0.4}{5} + \frac{0.6}{10} + \frac{0.8}{15} + \frac{0.9}{20} + \frac{1}{25} \right\} \text{ft}$$

$$N_H = \text{high speed fan} = \left\{ \frac{1}{1000} + \frac{2}{1500} + \frac{6}{2000} + \frac{8}{2500} + \frac{9}{3000} \right\} \text{ft}$$

"if temp is hot & humidity then speed is high"

$$y = \left\{ \frac{1}{1000} + \frac{1}{1500} + \frac{1}{2000} + \frac{1}{2500} + \frac{1}{3000} \right\} \text{g}$$



AND operation ($T_H \cap H_M$)

$$(i) T_H = \left\{ \begin{array}{l} 0.1 \\ (10, 5) \end{array}, \begin{array}{l} 0.2 \\ (20, 10) \end{array}, \begin{array}{l} 0.5 \\ (30, 15) \end{array}, \begin{array}{l} 0.8 \\ (40, 20) \end{array}, \begin{array}{l} 0.9 \\ (50, 25) \end{array} \right\}$$

	1000	1500	2000	2500	3000
x_1	0.1	0.1	0.1	0.1	0.1
x_2	0.1	0.2	0.2	0.2	0.2
x_3	0.1	0.3	0.5	0.5	0.5
x_4	0.1	0.3	0.6	0.8	0.8
x_5	0.1	0.3	0.6	0.8	0.9

$$\bar{T}_H = \left\{ \begin{array}{l} 0.9 \\ x_1 \end{array}, \begin{array}{l} 0.8 \\ x_2 \end{array}, \begin{array}{l} 0.5 \\ x_3 \end{array}, \begin{array}{l} 0.2 \\ x_4 \end{array}, \begin{array}{l} 0.1 \\ x_5 \end{array} \right\}$$

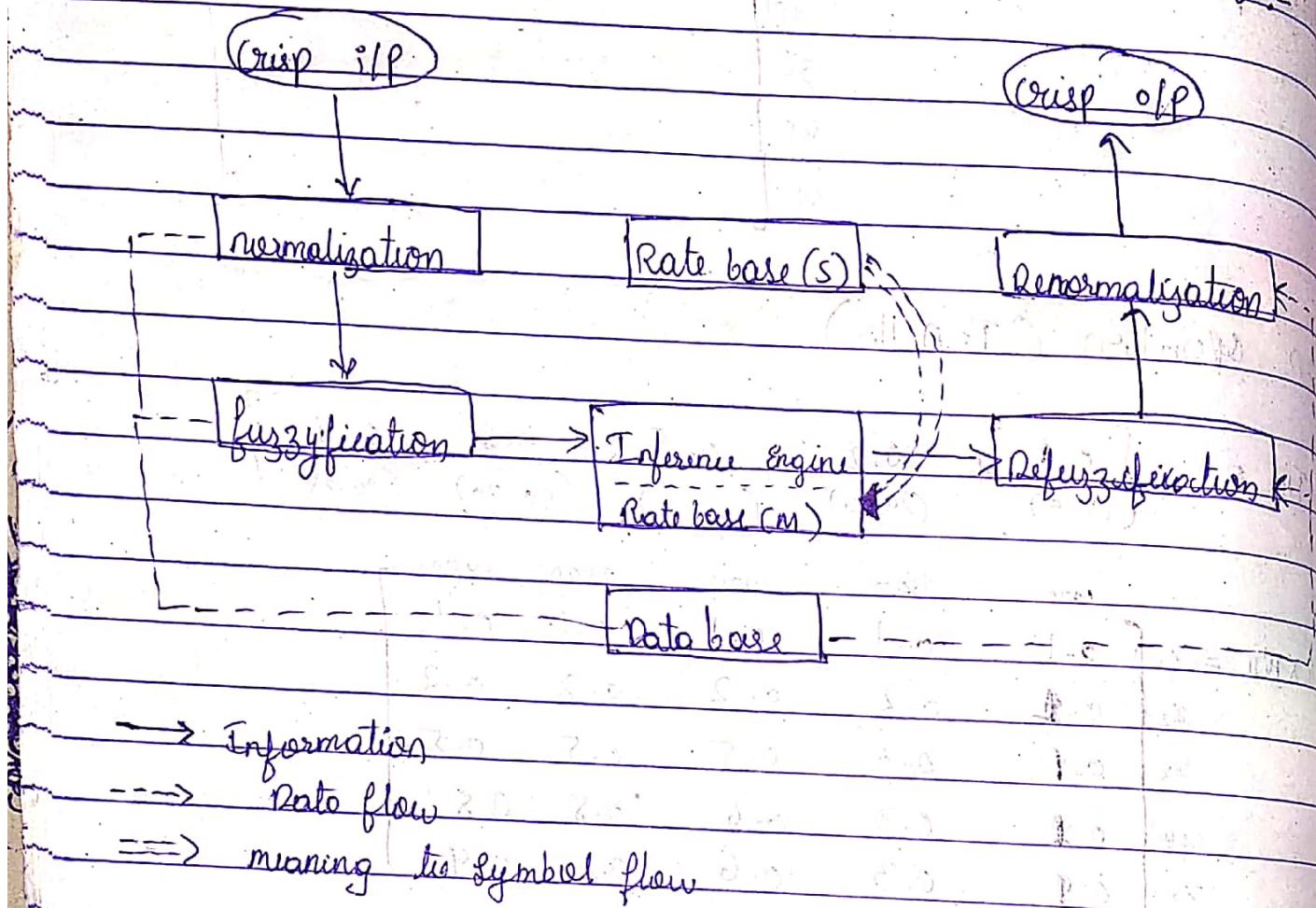
	1000	1500	2000	2500	3000
x_1	0.9	0.9	0.9	0.9	0.9
x_2	0.8	0.8	0.8	0.8	0.8
x_3	0.5	0.5	0.5	0.5	0.5
x_4	0.2	0.2	0.2	0.2	0.2
x_5	0.1	0.1	0.1	0.1	0.1

$$ii) (T_H \times N_H) \cup (\bar{T}_H \times Y)$$

	1000	1500	2000	2500	3000
x_1	0.9	0.9	0.9	0.9	0.9
x_2	0.8	0.8	0.8	0.8	0.8
x_3	0.5	0.5	0.5	0.5	0.5
x_4	0.2	0.3	0.6	0.8	0.8
x_5	0.1	0.3	0.6	0.8	0.9

21/1/2023

Fuzzy Knowledge based controller (FKBC)



* Fuzzification :- Convert crisp value into fuzzy value (both i/p & o/p).

i/p	P-L	P-M	P-H	o/p	Tank full washing
cut of ethyl (0 to 7 kg)	0-3	3-5	5-7	0-20	(0 - 60 min)
(0-3) (3-5) (5-7)	L	M	H	0-20 (20-40) (40-60)	L M H

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Select randomly the set

* There are two methods of choosing the scaling function:

① Heuristic method

② Analytical method

① Heuristic method :- This is a trial & error base method

choice :-

i) Select randomly the scaling function

ii) check for the performance of the controller

iii) if not satisfactory go to Step 1

iv) if satisfactory Select the scaling function.

② Analytical Method :- Here mathematical models are used to evaluate the scaling function.

* choice of membership function :-

1. higher computation efficiency

2. efficient use of memory

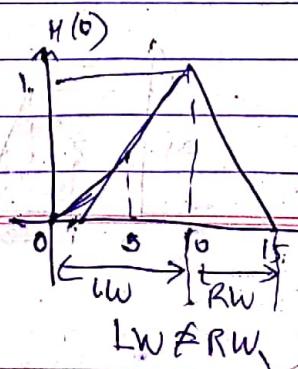
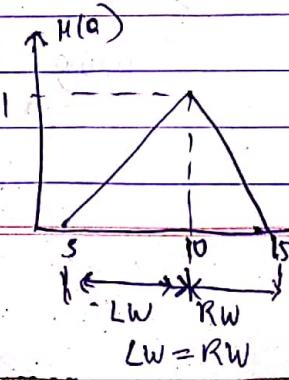
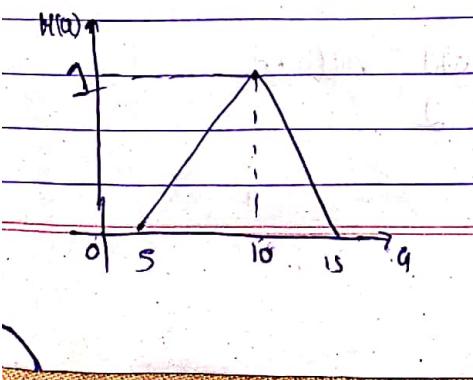
3. uniform representation

usefull choices are triangular, trapezoidal, Increment, decrement

4. The best choice is triangular function.

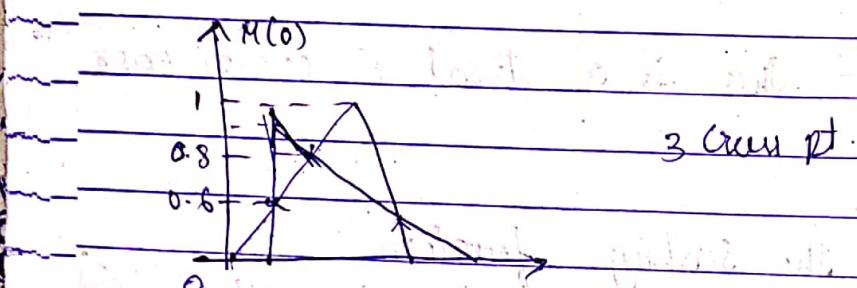
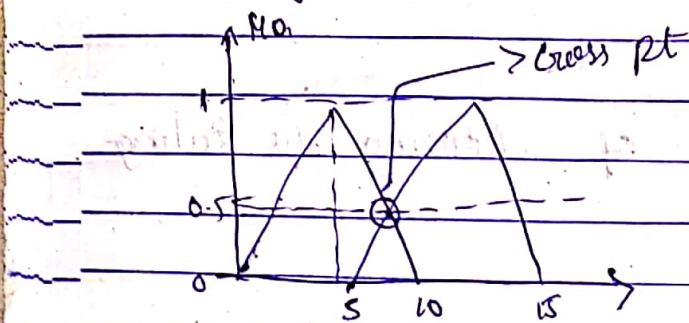
1) Peak functn:-

2) left & Right width



2)

- 1) Select a funct which has max cross pt.
 2) No. of cross point



The most optimal choice of M funct is one which as peak value = 1, & $LW = RW$ as no. of cross point = 1 E.g. cross point = 0.5.

* Defuzzification :-

① height method

2). weighted average method

3). middle of maximum (MOM)

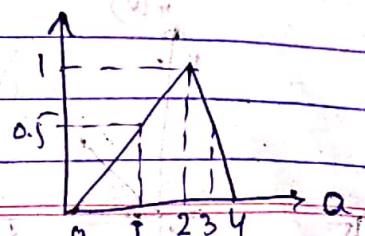
4) First of maximum (FOM)

5) last of maximum (LOM)

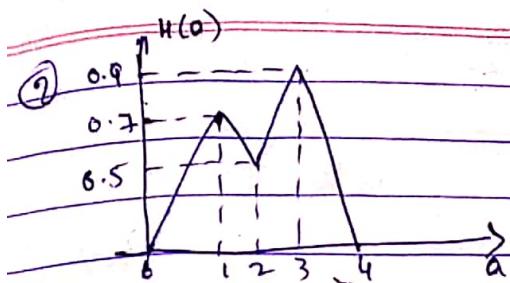
6.) centre of gravity (COG)

① height method:

① find the defuzzified value (Z^*)

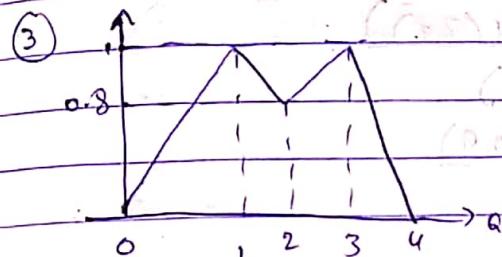


Using height method.
 $\therefore Z^* = 2$.



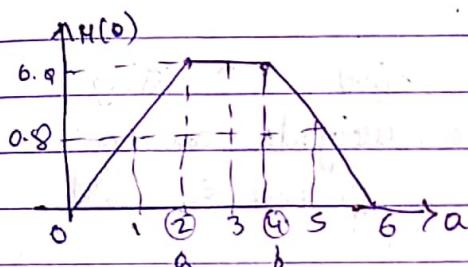
A "fuzzy" output whose membership value of max no. of members membership:

$$\therefore z^* = 3$$

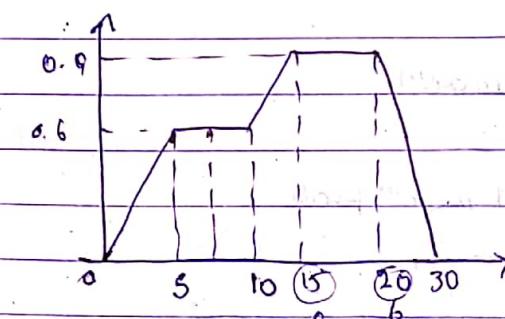


(c) Height method:

NA

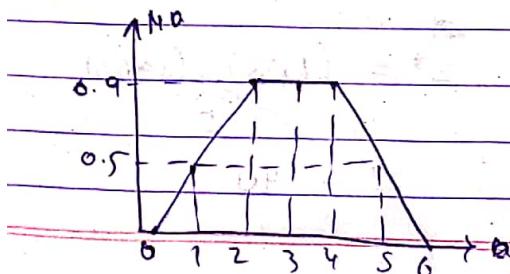


$$z^* = \frac{0+6}{2} = \frac{2+3}{2} = \frac{6}{2} = 3$$



$$z^* = \frac{0+6}{2} = \frac{15+20}{2} = \frac{35}{2} = 17.5$$

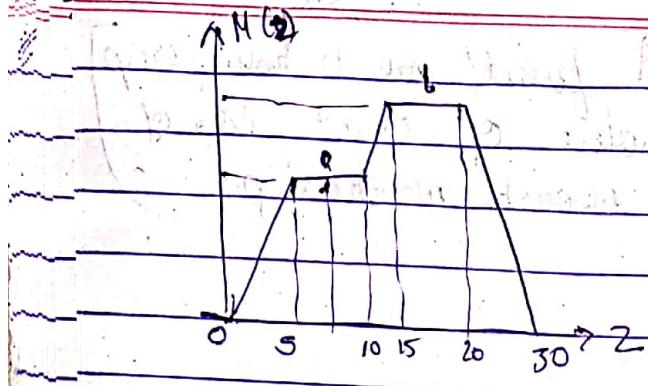
- (2) Weighted average value :- crisp value associated with a -



$$z^* = \sum_{a=1}^n (o \times \mu_H(a))$$

$$\sum_{a=1}^n \mu_H(a)$$

$$z^* = \frac{3 \times 0.9}{0.9} = 3$$

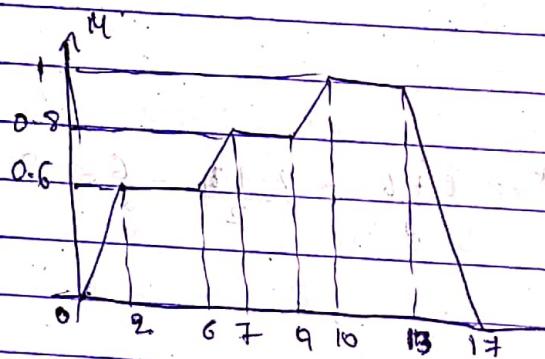


$$Z^* = (\alpha \times M(z_1)) + (\beta \times M(z_2))$$

$$\therefore M(z_1) + M(z_2)$$

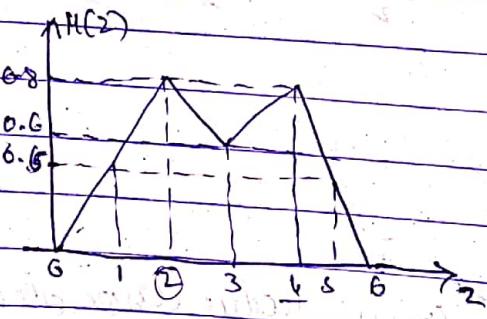
$$= (7.5 \times 0.6) + (17.5 \times 0.9)$$

$$= 0.9 \times 0.6$$



find Z^* using
weighted average
method E. Mom

(4,5) First of max^m & last of max^m

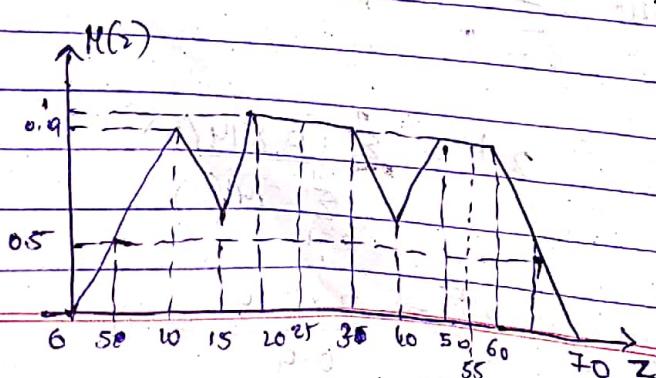


First max^m peak

$$Z^* = 2$$

Last max^m peak

$$Z^* = 4$$



Wet Mom

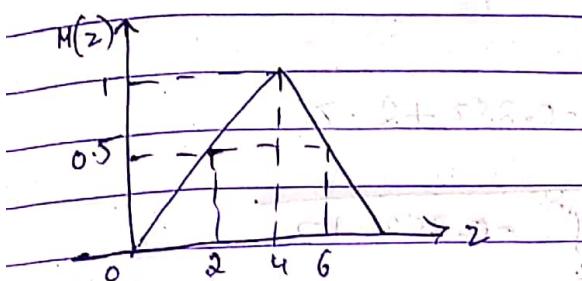
$$Z^* = \frac{(1 \times 25) + (1 \times 55)}{2}$$

$$Z^* = 40$$

Sush.

$$FOM = 20 \text{ cm}, LOM = 60.$$

6) Centre of gravity (COG) :-



Find z^* using applicable method.

Height method = 4

$$FOM = 14$$

$$LOM = 4$$

Centre of gravity :=

$$\text{For AB} = y = mx + c \quad m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 0}{4 - 0} = 0.25$$

$$\therefore y = 0.25x$$

$$1 = (0.25 \times 4) + c$$

$$\boxed{c = 0}$$

$$M(z_1) = m_1 z_1 + c = \frac{0.25 z_1 + 0}{\boxed{M(z_1) = 0.25 z_1}} \quad \text{--- (1)}$$

$$\text{For BC} = y = mx + c \quad m = \frac{0 - 1}{8 - 4} = \frac{-1}{4} = -0.25$$

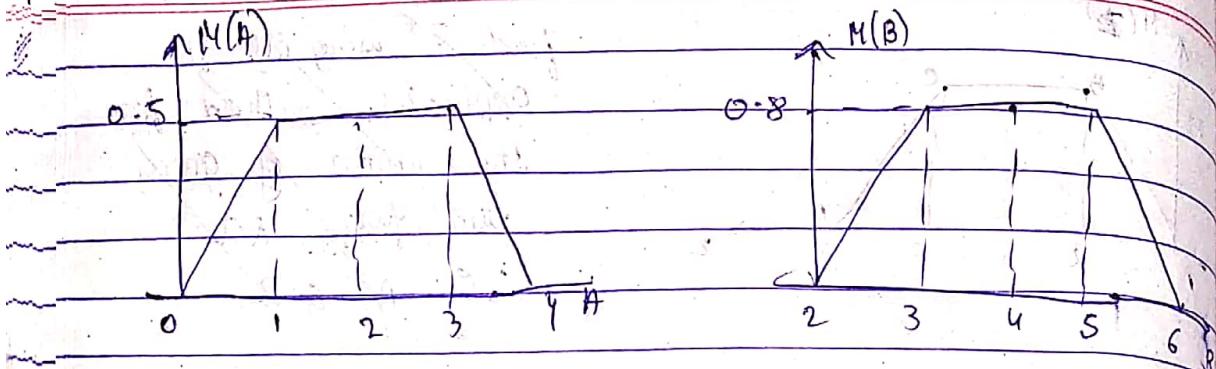
$$\text{here } y = 0, x = 8$$

$$0 = -0.25 \times 8 + c$$

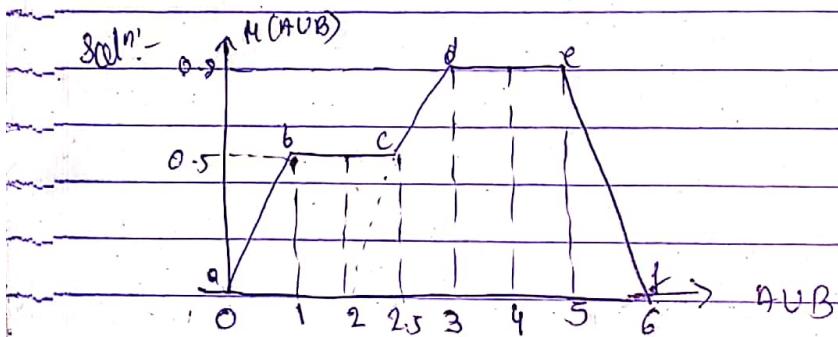
$$\boxed{c = 2}$$

$$M(z_2) = m_2 z_2 + c = \boxed{-0.25 z_2 + 2} \quad \text{--- (2)}$$

$$z^* = \frac{\int M(z) \cdot z \, dz}{\int M(z) \, dz}$$



find z^* using all the applicable methods for the union of given fuzzy sets i.e. $A \cup B$



$$\text{height avg} = z^* = \frac{\sum M(z) \cdot z}{\sum M(z)}$$

$$= \frac{(0.5 \times 1.75) + (0.8 \times 4)}{(0.5 + 0.8)} = \frac{3.134}{1.3} = 2.37$$

$$MOM = 4$$

$$LOM = z^* = 2.37$$

$$FOM = 2^* = 3$$

Centre of Gravity :

$$\text{for } ab = y = mx + c \quad m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0.5 - 0}{1 - 0} = 0.5$$

$$\text{here } y = 0.5, x = 1$$

$$\therefore 0.5 = (0.5 \times 1) + c$$

$$c = 0$$

$$M(z_1) = m_2 + c$$

$$\boxed{M(z_1) = 0.52} \quad -\textcircled{1}$$

$$\text{for } bc : \boxed{M(z_2) = 0.5} \quad -\textcircled{2}$$

$$\text{for } cd : y = m_2 x + c \quad m = \frac{0.8 - 0.5}{3 - 2.5} = 0.1266 \quad 0.6$$

$$\text{here } y = 0.8, x = 3$$

$$0.8 = (0.266 \times 3) + c$$

$$0.8 = 0.798 + c$$

$$c =$$

$$y = m_2 x + c$$

$$0.8 = 0.6 \times 3 + c$$

$$0.8 = 1.8 + c$$

$$c = -1$$

$$M(z_3) = m_2 + c$$

$$\boxed{M(z_3) = 0.62 - 1}, \quad -\textcircled{3}$$

$$\text{for } de = \boxed{M(z_4) = 0.8}, \quad -\textcircled{4}$$

$$\text{for } ef = y = m_2 x + c \quad m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - 0.8}{6 - 5} = \frac{-0.8}{1} = -0.8$$

$$y = 0, x = 6$$

$$0 = (-0.8 \times 6) + c$$

$$c = 4.8$$

$$M(z) = m_2 + c \quad \boxed{M(z_5) = -0.8 + 4.8} \quad -\textcircled{5}$$

$$\therefore \int_0^{1.5} M(z_1) z \, dz + \int_1^{2.5} M(z_2) z \, dz + \int_{2.5}^3 M(z_3) z \, dz + \int_3^5 M(z_4) z \, dz + \int_5^6 M(z_5) z \, dz$$

$$\therefore \int_0^{1.5} M(z_1) \, dz + \int_1^{2.5} M(z_2) \, dz + \int_{2.5}^3 M(z_3) \, dz + \int_3^5 M(z_4) \, dz + \int_5^6 M(z_5) \, dz$$

16/1/23

Unit 4

* Design a Fuzzy for a fully automatic washing m/c :-

1) Selection of input & o/p Parameters.

i/p

- 1) weight of cloths (W)
- 2) type of cloths (T_c)
- 3) dirt level (D)

o/p

- 1) time of washing (T)
- 2) qty of detergent (W_d)
- 3) " water (W_w)

2) Range selection :-

i/p

$$W = (0 \text{ to } 9 \text{ kg})$$

$$T_c = (s, c, w, n)$$

$$D = (0 \text{ to } 100\%)$$

o/p :

$$T (0 \text{ to } 60 \text{ min})$$

$$W_d = (0 \text{ to } 300 \text{ gms})$$

$$W_w = (0 \text{ to } 100 \text{ ltr})$$

For simplicity of calculation we will select only 2 i/p & one o/p for our further calculation :-

SIM Term Sets

$$\text{i/p } W = (0 \text{ to } 9 \text{ kg}) \Rightarrow [0-4.5] [2.25-6.75] [4.5-9]$$

low (L) medium (M) High (H)

$$D = (0 \text{ to } 100\%) \Rightarrow [0-50] [25-75] [50-100]$$

L M H

o/p (Time for washing):

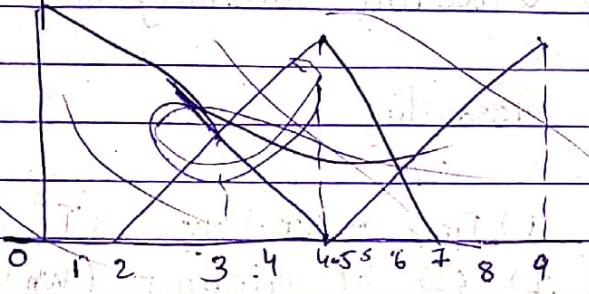
$$T = (0 \text{ to } 60 \text{ min}) \Rightarrow [0-30] [15-45] [30-60]$$

L M H

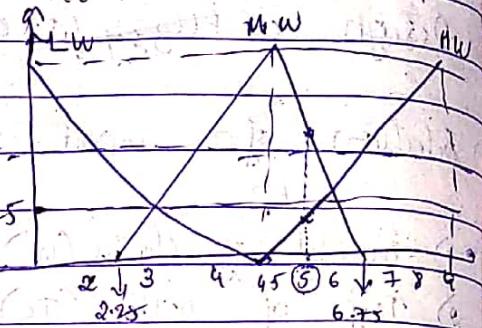
* Normalization :- as the values are small, normalization not reqd for i/p & o/p variables.

*

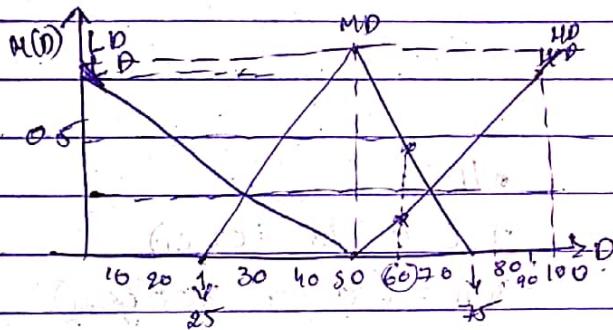
* Fuzzification :-



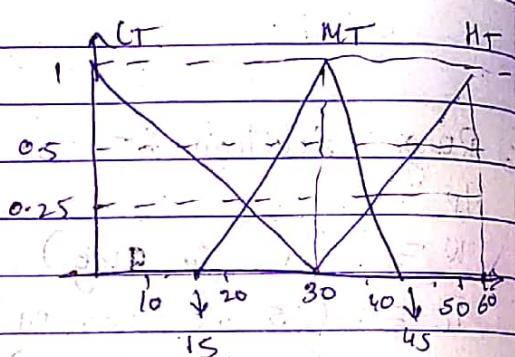
μ_{LW}



μ_M



μ_{HW}



* Rule base :-

e.g. if W is L & T is W then T is L .

W	L	M	H	T
L	L	M	H	L
M	M	M	H	M
H	M	H	H	H

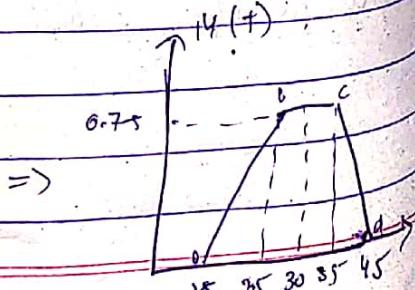
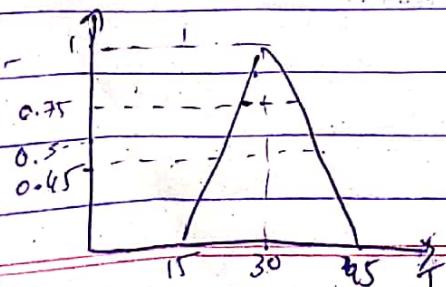
e.g. Assume $W=5\text{ kg}$, $T=60^\circ\text{C}$ find Time for washing

if W is M & T is M then T is M .

* Inference Engine :-

The above problem can be solved by Mamdani's clipped Inference engine.

* Defuzzification :-



$$d_{out}/d_{cut} = 0.75$$

1) Height = NA

2) Weight = $0.75 \times 30 = 30$
away 0.75

3) HOM = 30

4) FOM = 25

5) LOM = 35

6) COG

Traffic Signal



* Selection of i/p & o/p parameter -

i/p	o/p
V vertical in lane 1	Time of green signal for L1
V in L2	T _G for L ₂
V in L3	T _G for L ₃
V in L4	T _G for L ₄

* Terms like in Range:

i/p $V_{L_1} = [0 \text{ to } 15] \Rightarrow [0 - 7.5] [3.75 - 11.25] [7.5 - 10]$

$V_{L_3} = [0 \text{ to } 15] [0 - 7.5] [3.75 - 11.25] [7.5 - 15]$

o/p $T_{G1} = [0 \text{ to } 60 \text{ sec}]$

* Normalization :- Not required.

Fuzzification :-

$$\text{if } P \text{ } V_{L1} = [0.25 \text{ to } 0.5] \\ [0 \text{ - } 1.5] [0.75 \text{ - } 1.25] [1.5 \text{ - } 1.75]$$

$$\text{if } P @ V_{L2} = [6 \text{ to } 15] \\ [0 \text{ - } 7.5] [0.75 \text{ - } 11.25] [7.5 \text{ - } 15]$$

$$\text{if } P @ V_{L3} = [0 \text{ - } 6.0] \\ [0 \text{ - } 3.0] [15 \text{ - } 45] [30 \text{ - } 60]$$

Fuzzification :-

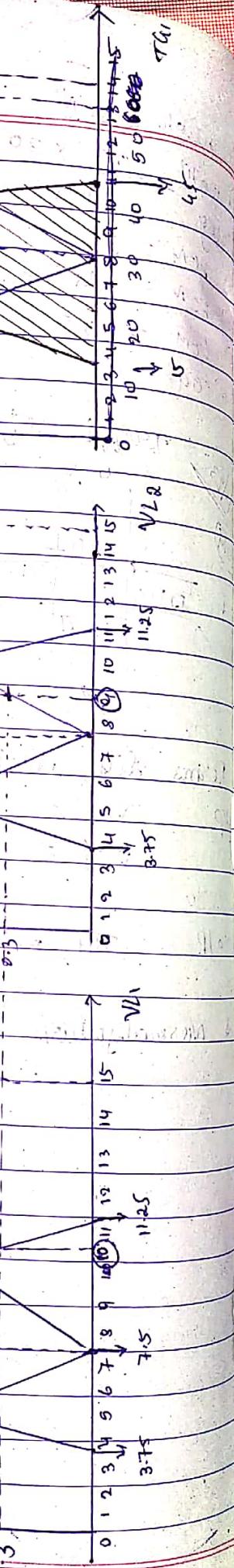
$m(V_{L1})$

$m(V_{L2})$

$m(V_{L3})$

m

0.5
0.4
0.3



Rule base:

	V_{L2}	L	M	H
VL1	L	L	L	
M	M	M	M	
H	H	M	M	

eg:-

Assume

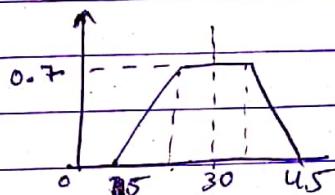
$$V_{L1} = 10$$

$$V_{L2} = 9$$

If V_{L1} is H & V_{L2} is M then T_{C1} is M

The above problem can be solved by mamdani clipped Inference engine.

Defuzzification



i) Height M = NA

2) weighted avg = $\frac{0.7 \times 30}{0.7} = 30$

3) MOM =

4) FOM =

5) LOM = 8