

Constrained text generation through discrete & continuous inference

Sean Welleck | 03.11.2022



Neural text generation

- **Large-scale language models** drive state-of-the-art performance in text generation tasks:

The image displays five examples of neural text generation:

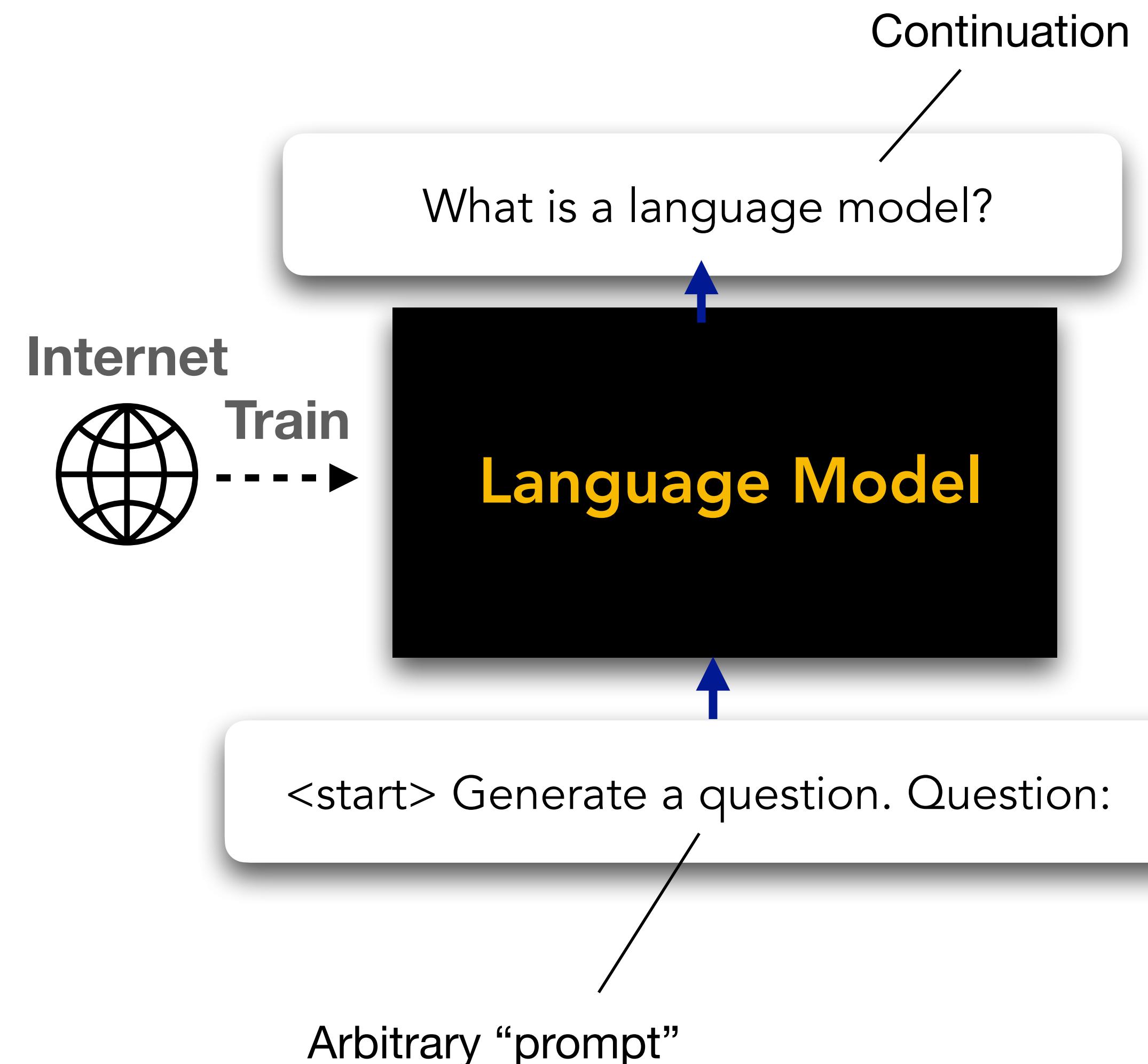
- Open-Ended Generation:** A screenshot from the OpenAI API landing page showing the text: "Build next-gen apps with OpenAI's powerful models." Below it, a snippet of text reads: "OpenAI's API provides access to GPT-3, which performs a wide variety of natural language tasks, and Codex, which translates natural language to code."
- Long-form QA:** A screenshot from a search interface showing the query: "How has technological growth increased so exponentially in the last 50 years?" Below it, a snippet of text reads: "There are many explanations for the exponential growth in technology in the last century. One explanation is that the pace of technological progress speeds up exponentially over time because of a common force pushing it forward^[3]. Another explanation is that each new generation of technology stands on the shoulders of its predecessors, allowing for improvements that lead to the next generation of even better..."
- Program Synthesis:** A screenshot of the GitHub Copilot interface titled "Your AI pair programmer". It shows a "prompt" box with Python code to "Write a python function that takes a number and returns one less than twice its value if it satisfies these tests:" and a "model" box with the generated code:

```
def check(n):
    if n == 2*int(str(n)[::-1]):
        return True
    else:
        return False
```
- Machine Translation:** A screenshot of the Google Translate interface showing the text "Machine Translation" in the input field.
- Dialogue:** A screenshot of a dialogue model interface. A user message says: "Hi! Hello, I am a friendly dialog model. What do you want to talk about?". A response message says: "What's a good topic for a new blog?". Another user message says: "Well there are so many! How about something about a new food item that you just tried." The interface includes like and dislike buttons.

[Austin et al 2021] [GitHub Copilot Chen et al 2021] [Thoppilan et al 2022]

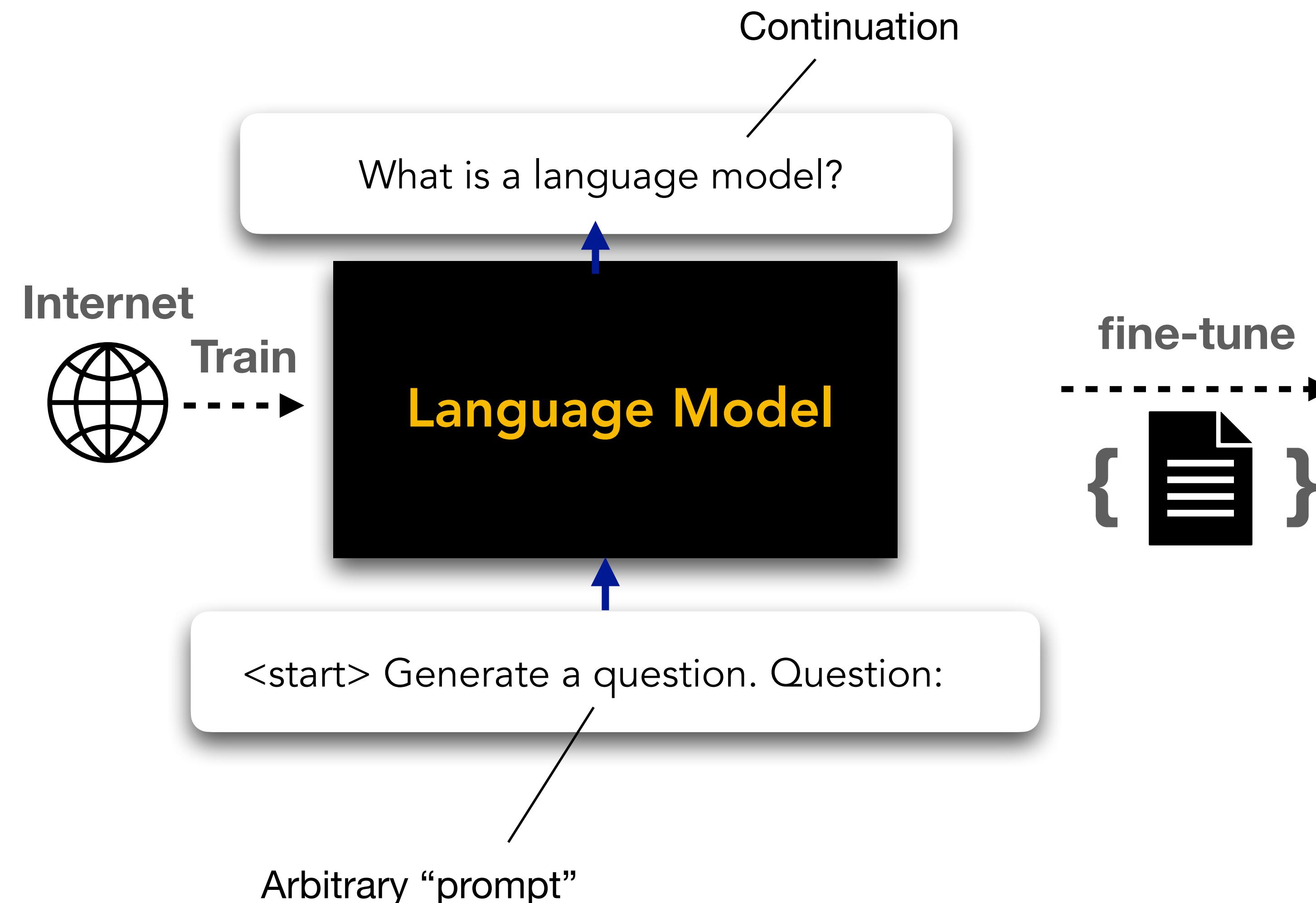
Neural text generation

- General purpose:

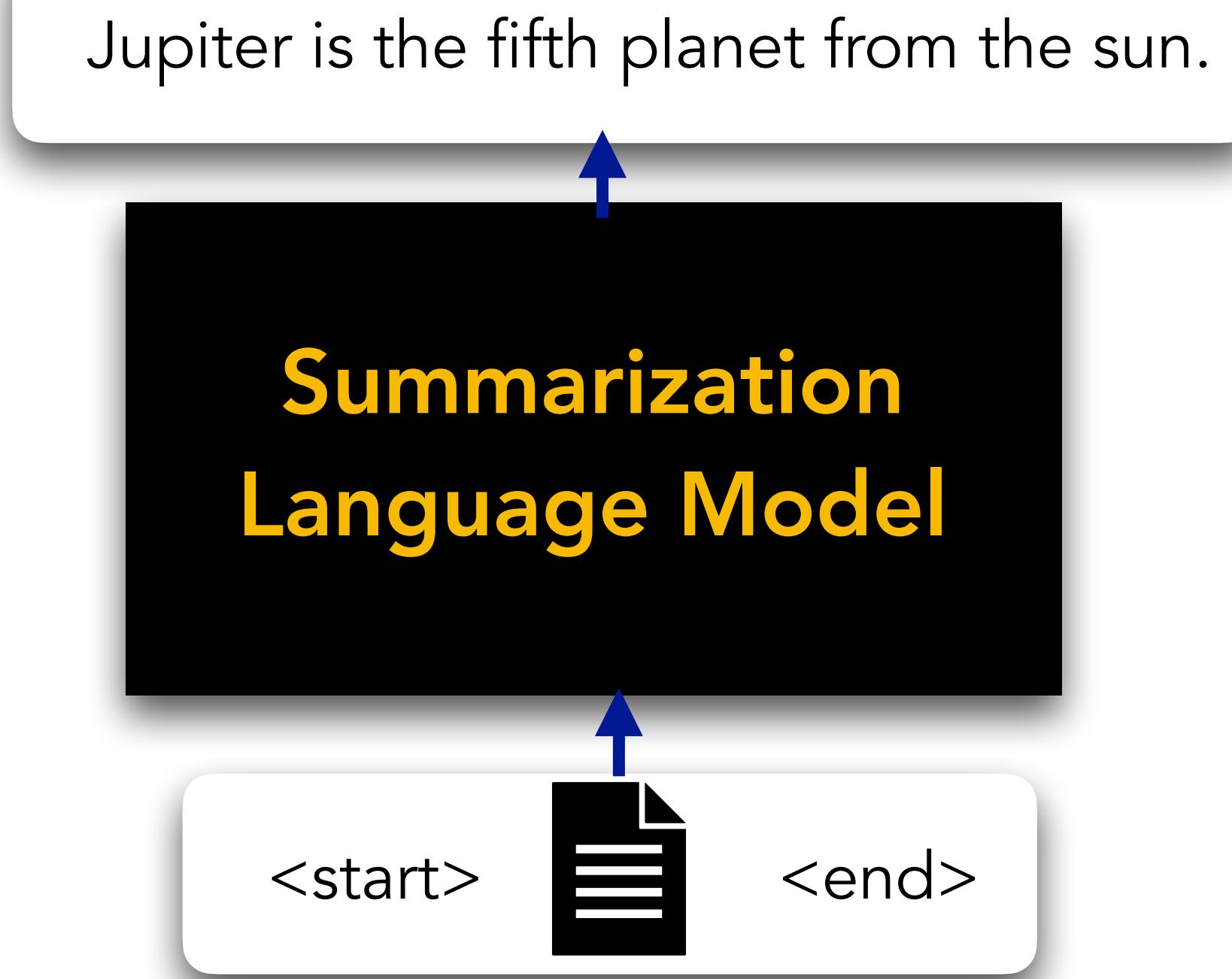


Neural text generation

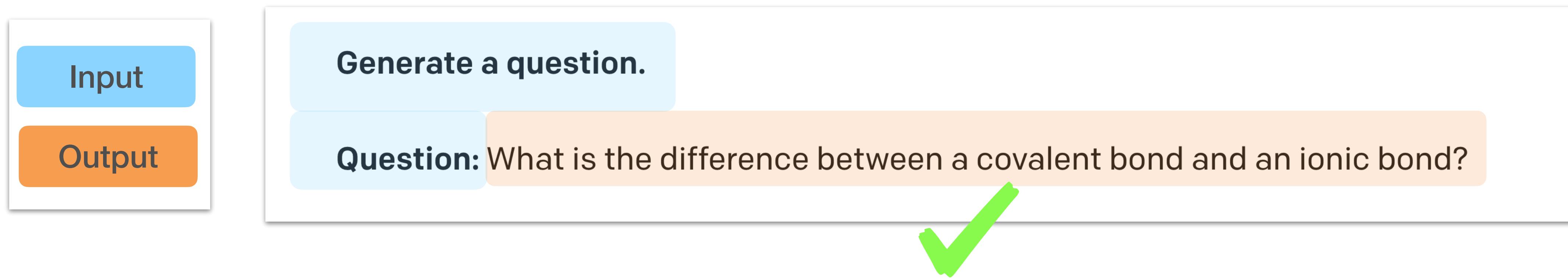
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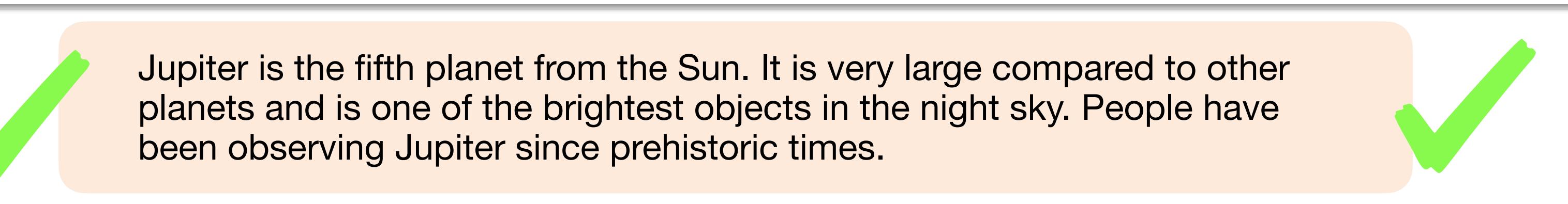
- Task-specific:



- **GPT-3: a general purpose 175B parameter language model:**

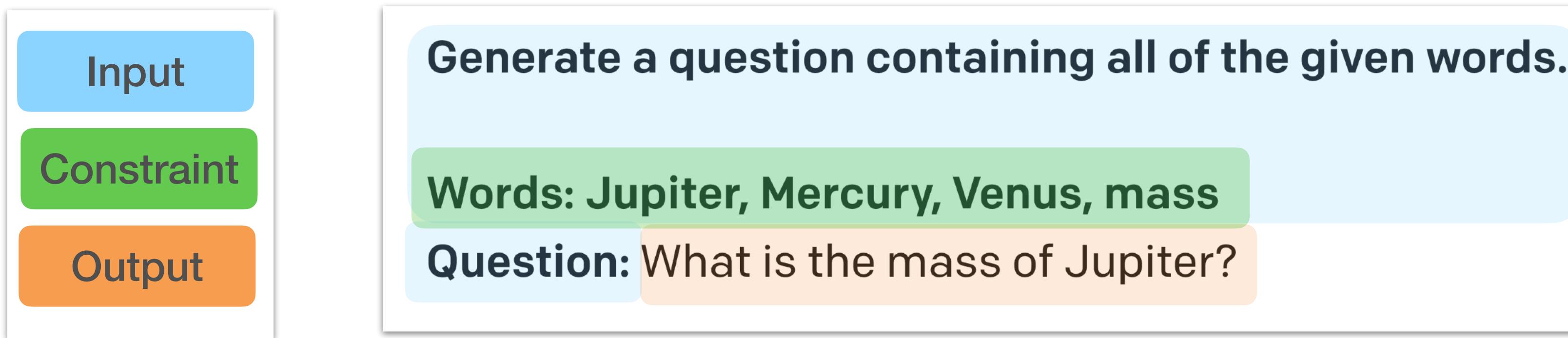


- **GPT-3: a general purpose 175B parameter language model:**

Input	Summarize this for a second-grade student: <h2>Jupiter</h2> <p>From Wikipedia, the free encyclopedia</p> <p><i>This article is about the planet. For the Roman god, see Jupiter (mythology). For other uses, see Jupiter (disambiguation).</i></p> <p>Jupiter is the fifth planet from the Sun and the largest in the Solar System. It is a gas giant with a mass more than two and a half times that of all the other planets in the Solar System combined, but slightly less than one-thousandth the mass of the Sun. Jupiter is the third brightest natural object in the Earth's night sky after the Moon and Venus. People have been observing it since prehistoric times; it was named after the Roman god Jupiter, the king of the gods, because of its observed size.</p>
Output	Jupiter is the fifth planet from the Sun. It is very large compared to other planets and is one of the brightest objects in the night sky. People have been observing Jupiter since prehistoric times.  

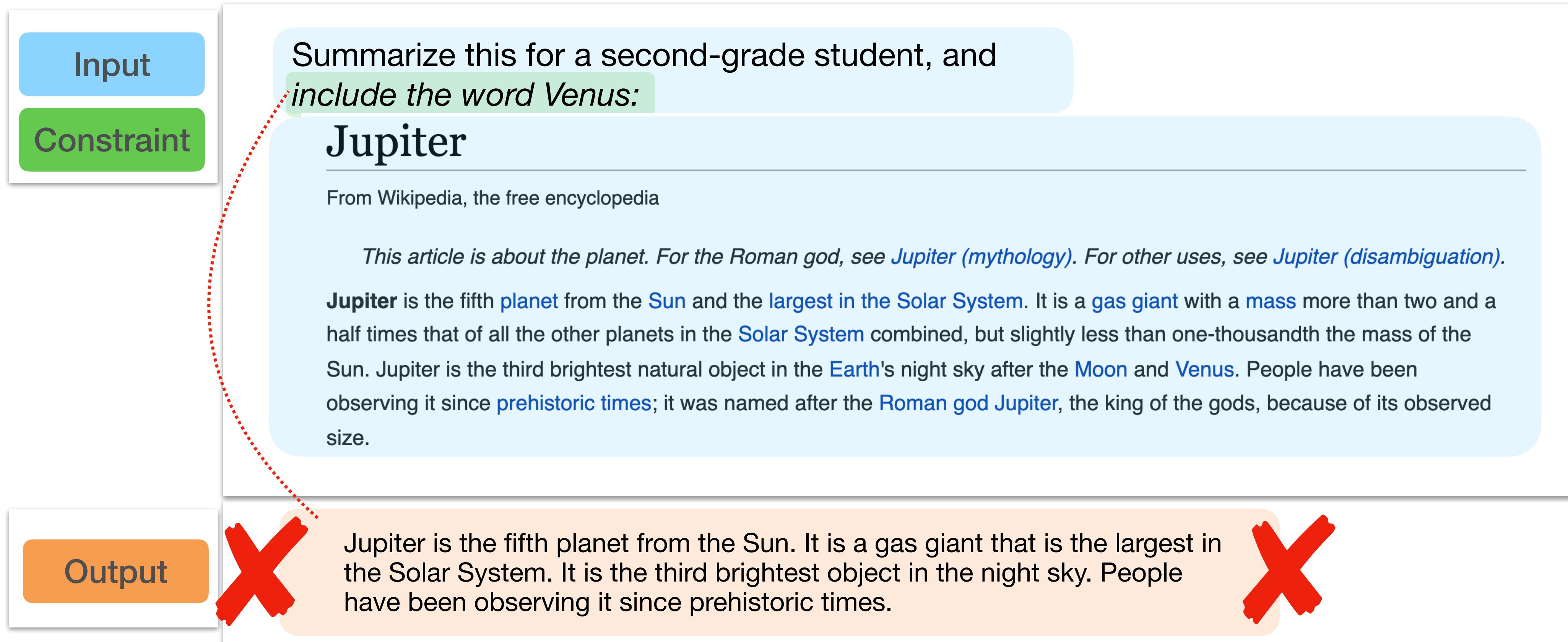
Controlling neural text generation

- Controlling the syntax, semantics, or style of generated text is difficult
 - Lexical content



Controlling neural text generation

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Controlling neural text generation

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Input

Summarize this for a second-grade student, and
include the word Venus:

Jupiter

From Wikipedia, the free encyclopedia

This article is about the planet. For the Roman god, see Jupiter (mythology). For other uses, see Jupiter (disambiguation).

Jupiter is the fifth [planet](#) from the [Sun](#) and the [largest in the Solar System](#). It is a [gas giant](#) with a [mass](#) more than two and a half times that of all the other planets in the [Solar System](#) combined, but slightly less than one-thousandth the mass of the Sun. Jupiter is the third brightest natural object in the [Earth's night sky](#) after the [Moon](#) and [Venus](#). People have been observing it since [prehistoric times](#); it was named after the [Roman god Jupiter](#), the king of the gods, because of its observed

- For a task specific model: how do we even **specify** the control words?

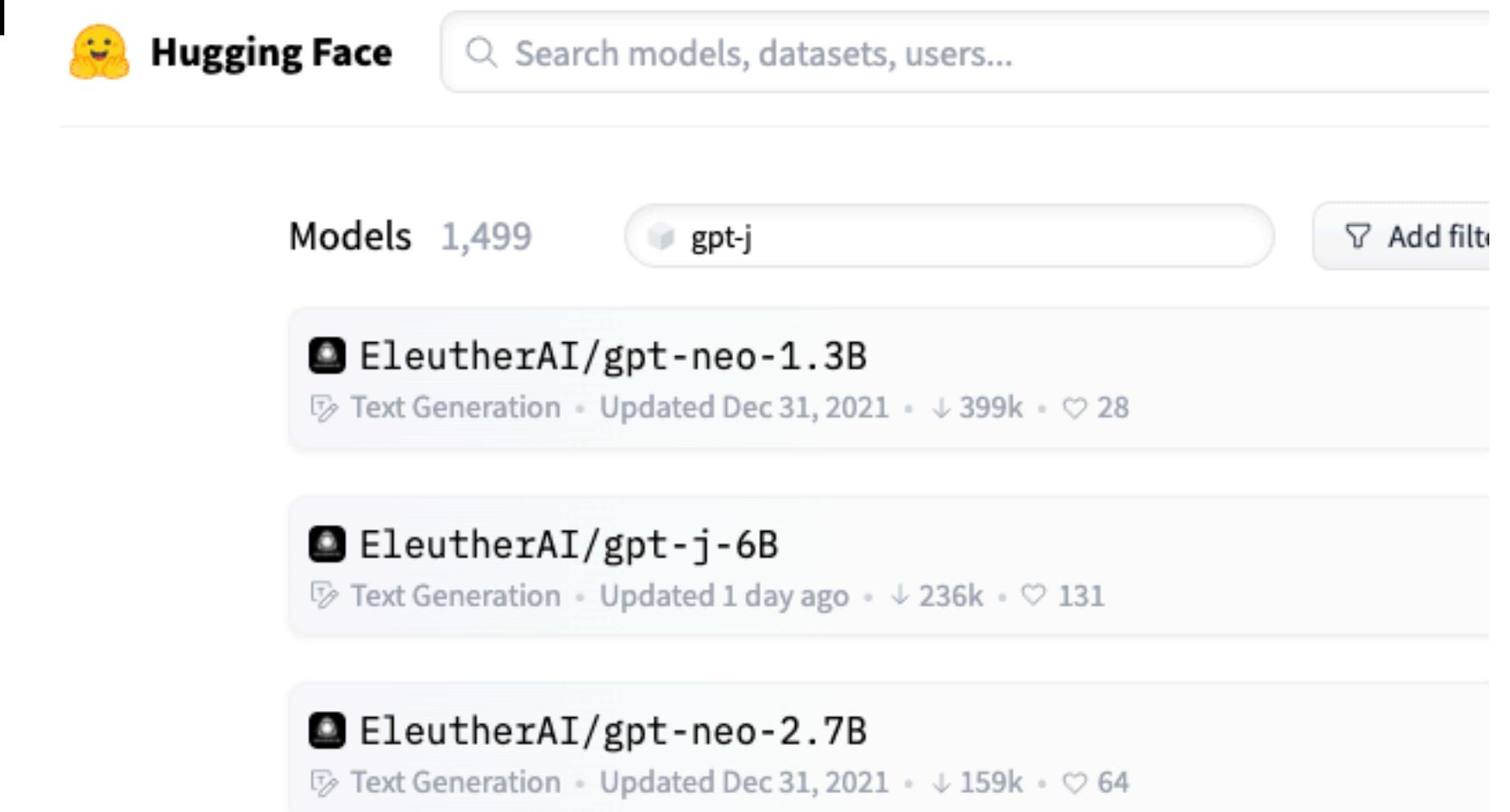
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X Jupiter is the fifth planet from the Sun. It is a gas giant that is the largest in the Solar System. It is the third brightest object in the night sky. People have been observing it since prehistoric times.

X

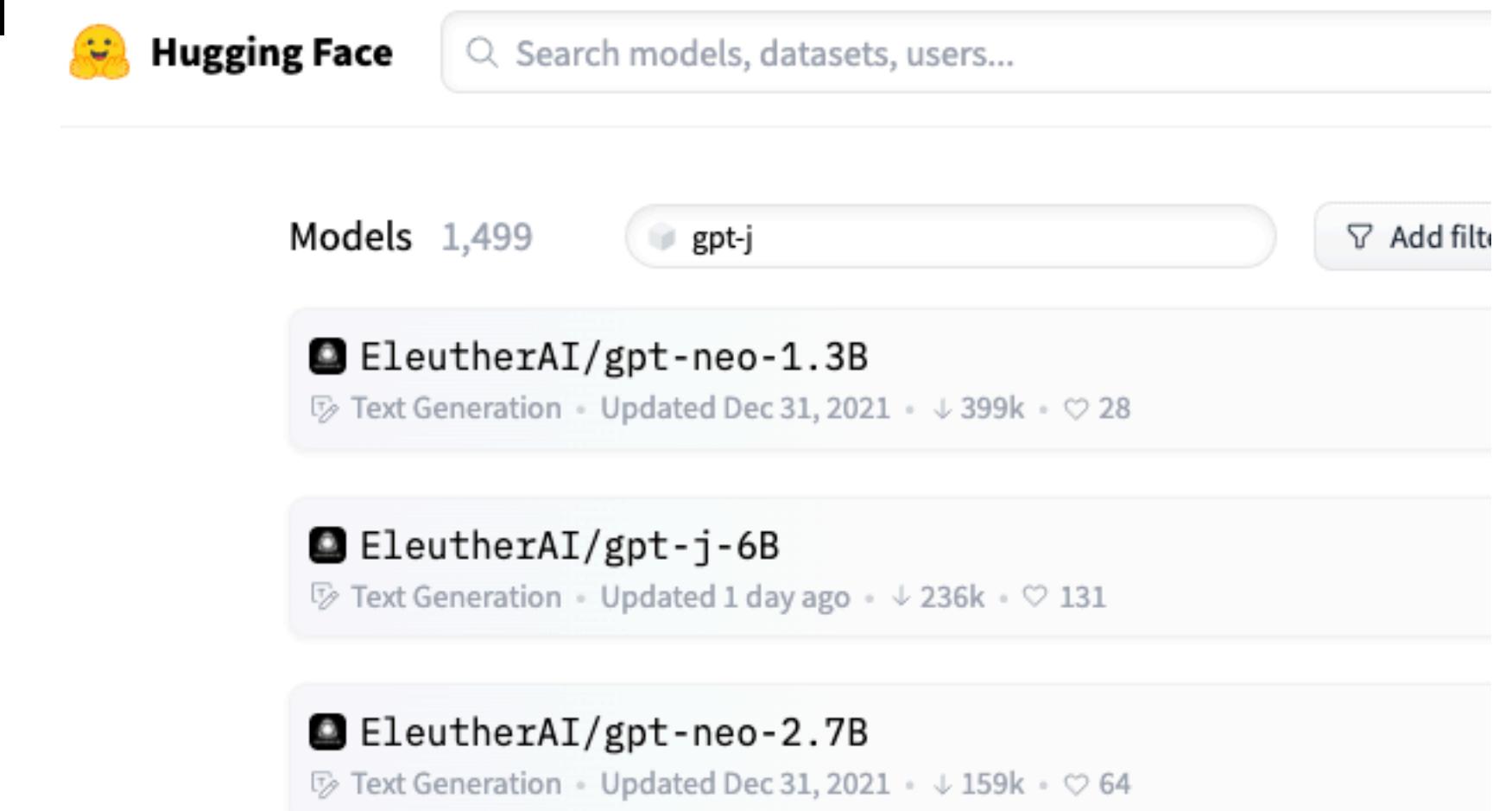
Controlling neural text generation

- Typical usage pattern: use an “off-the-shelf” model to generate text



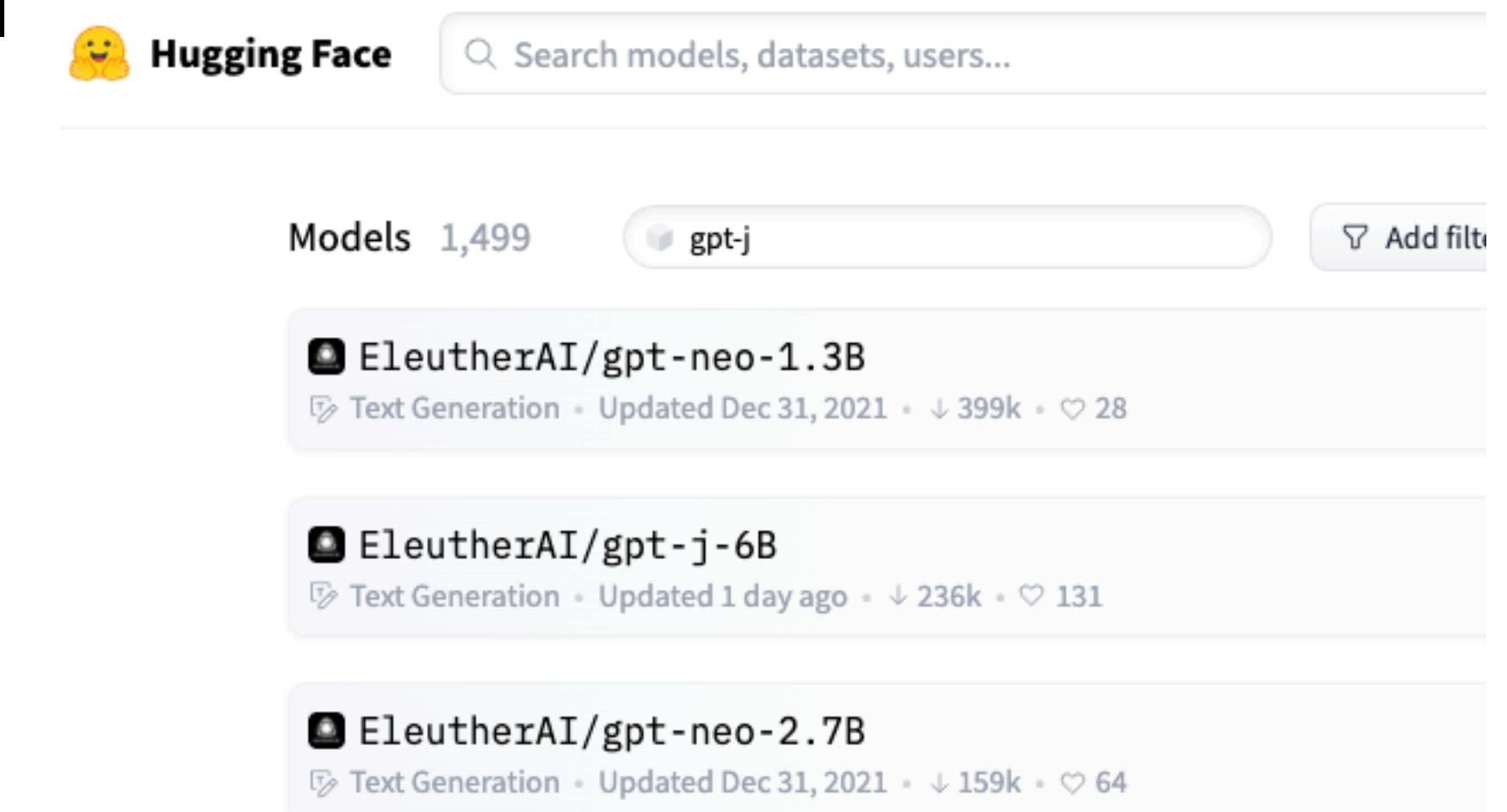
Controlling neural text generation

- Typical usage pattern: use an “off-the-shelf” model to generate text
 - Hard to get data for desired control outcomes



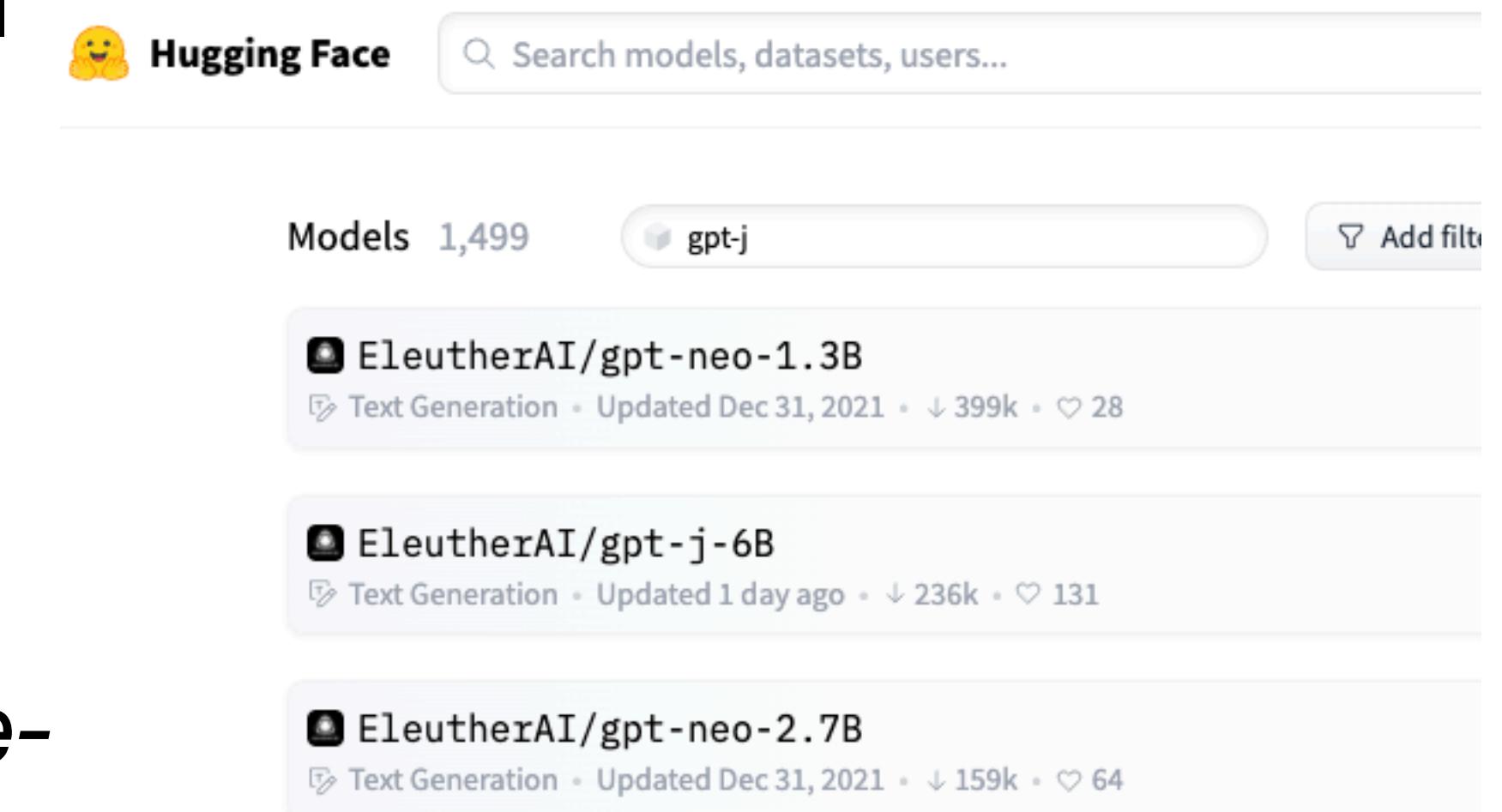
Controlling neural text generation

- Typical usage pattern: use an “off-the-shelf” model to generate text
 - Hard to get data for desired control outcomes
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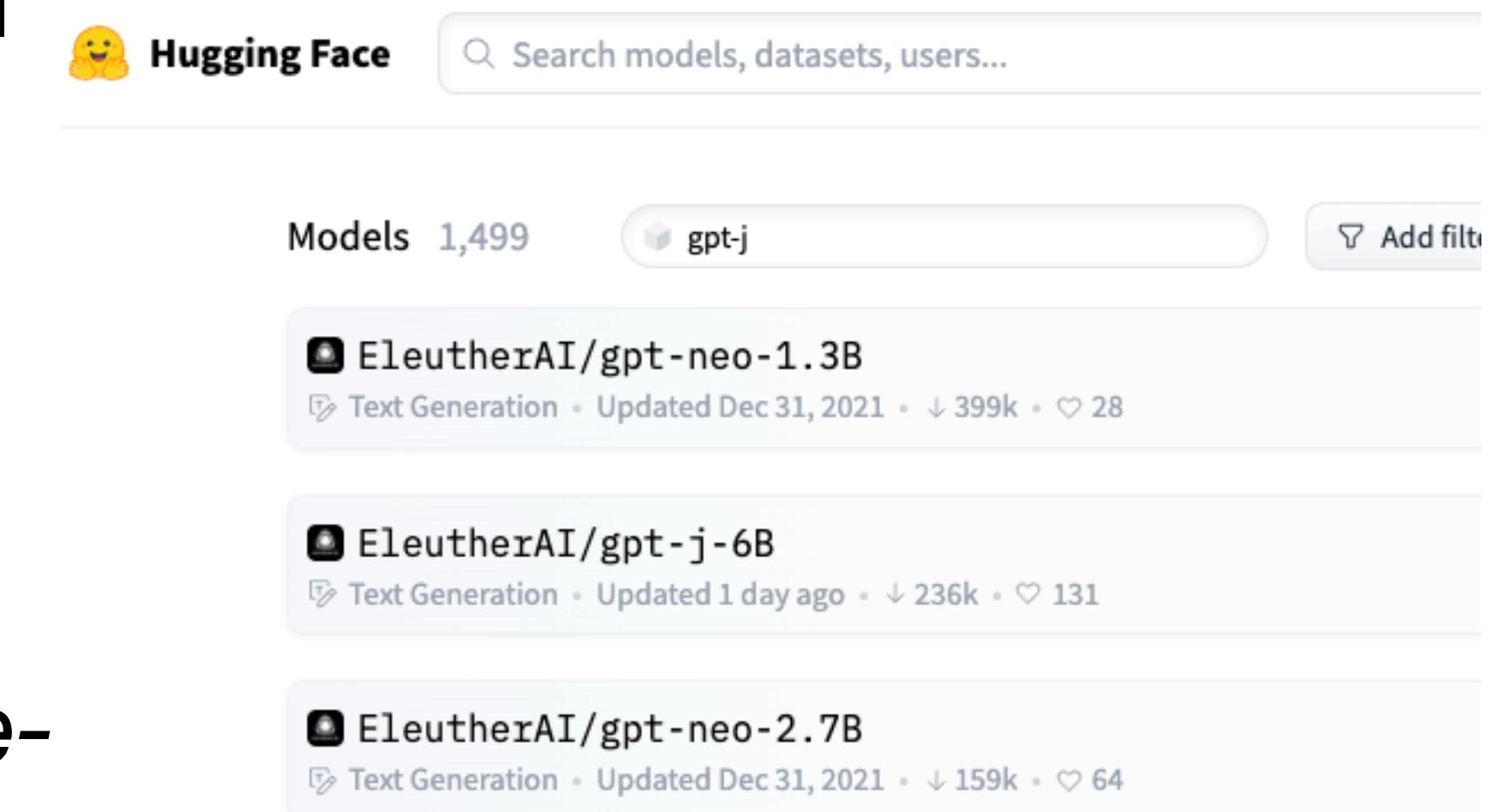
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Controlling neural text generation

- Typical usage pattern: use an “off-the-shelf” model to generate text
 - Hard to get data for desired control outcomes
 - Expensive to fine-tune & store a new model
- *How do we enable controlled generation for off-the-shelf models?*
 - *General-purpose or task-specific*



Control through inference

Model + decoding

Control through inference

Model + decoding

- Text generation involves two steps:

Control through inference

Model + decoding

- Text generation involves two steps:
- Learn a **model** from data (or download one...)

$$\bullet \quad p_{\theta}(\mathbf{y} \mid \mathbf{x}) = \prod_{t=1}^T p_{\theta}(y_t \mid y_{<t}, \mathbf{x})$$

Language Model

Control through inference

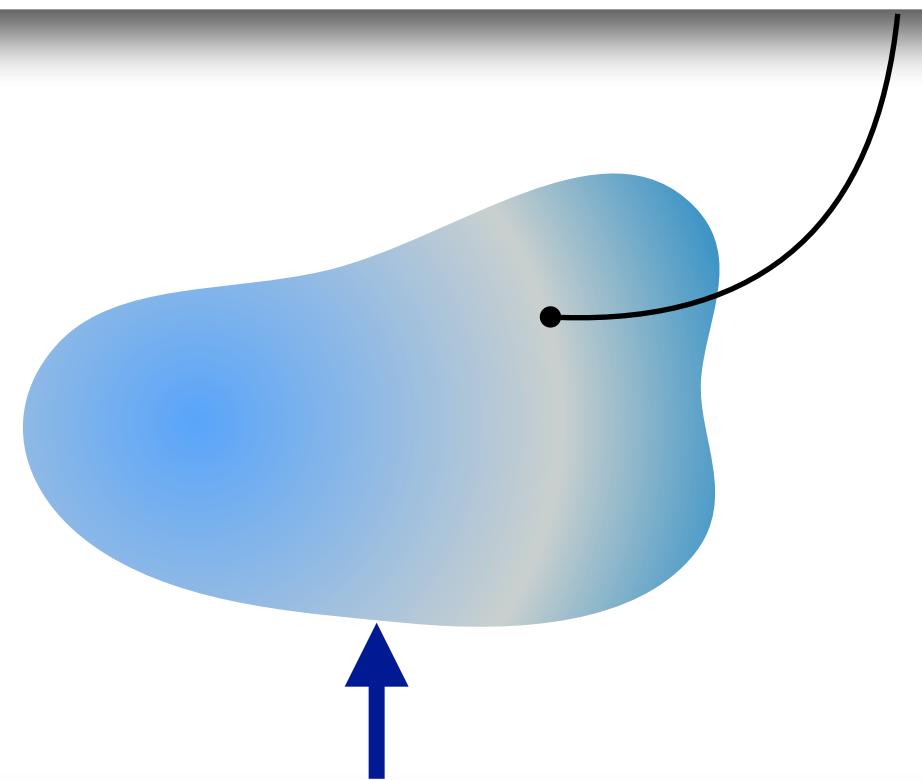
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$$\bullet \quad p_{\theta}(\mathbf{y} | \mathbf{x}) = \prod_{t=1}^T p_{\theta}(y_t | y_{<t}, \mathbf{x})$$

- Use an **inference/decoding** algorithm to generate text
 - $\hat{\mathbf{y}} = \text{decode}(p_{\theta}(\cdot | \mathbf{x}))$

What is the mass of Jupiter?



Decoding Algorithm

Language Model

<start>

Control through inference

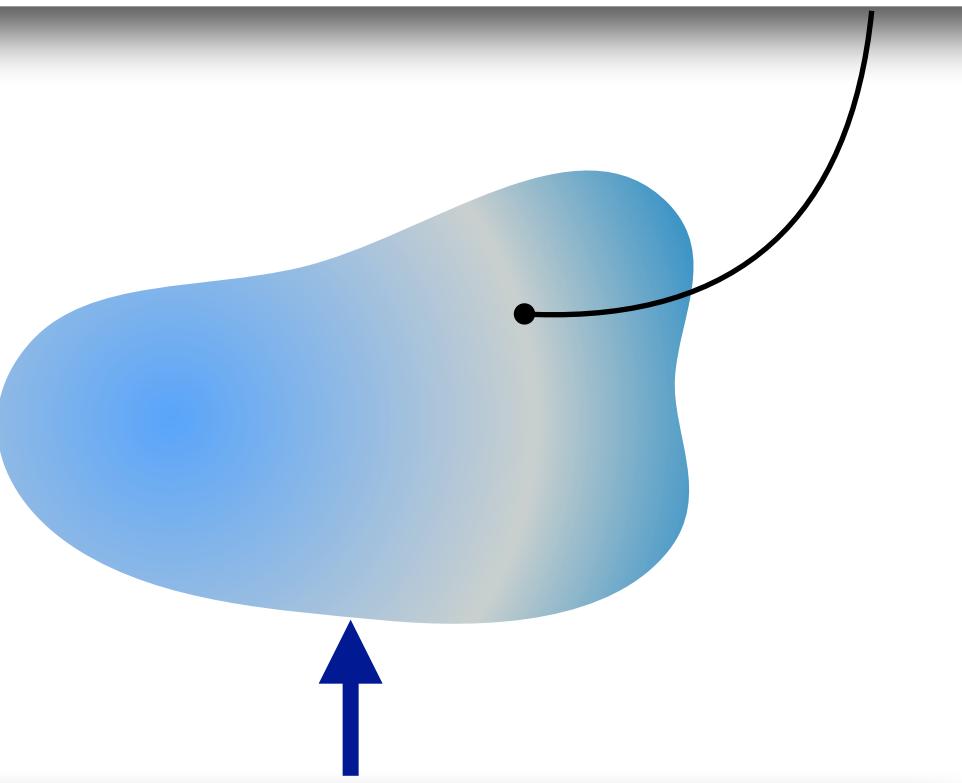
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Decoding Algorithm

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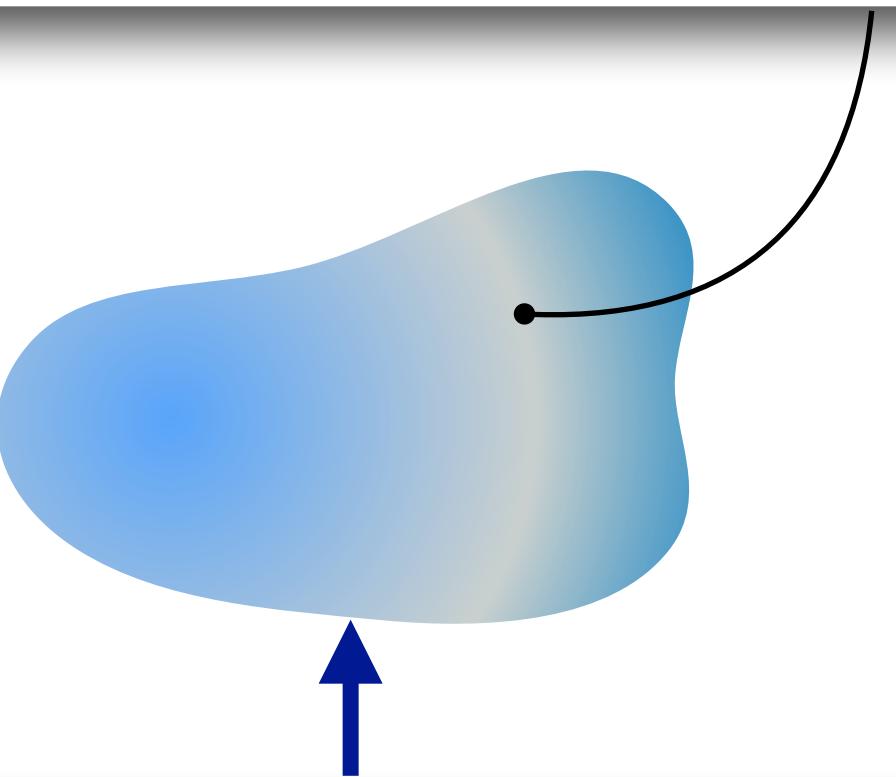
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 - e.g. sampling, $\mathbf{y}_t \sim p_{\theta}(y_t | y_{<t}, \mathbf{x})$
 - e.g. maximization $y_t = \arg \max_{y_t} p_{\theta}(y_t | y_{<t}, \mathbf{x})$

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Decoding Algorithm

Language Model

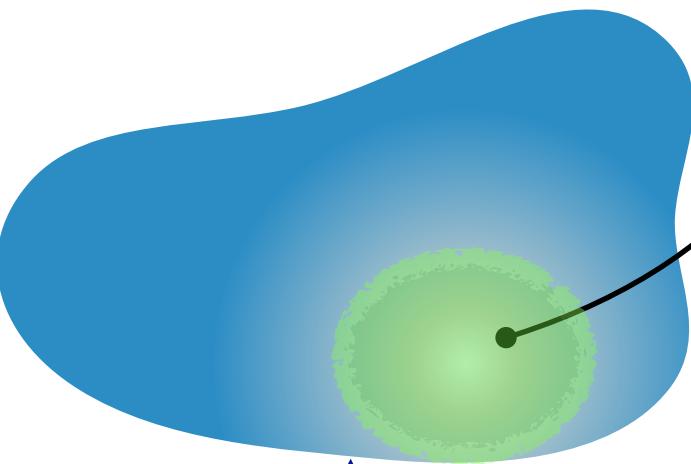
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Constraints through inference

Model + decoding

- Control: **constraints** on the generation distribution

Which has the most mass:
Mercury, Venus, or Jupiter?



Decoding Algorithm

Language Model

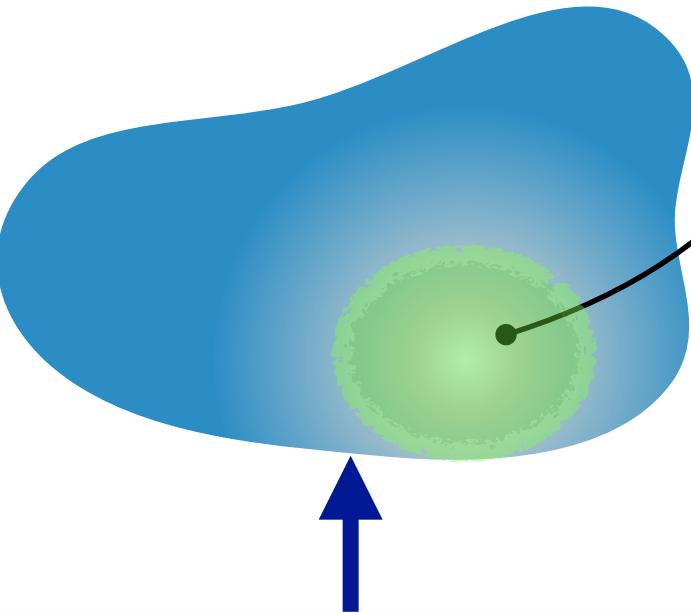
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Constraints through inference

Model + decoding

- Control: **constraints** on the generation distribution
- Goal: **decoding** algorithms that enable constraints
 - $\hat{y} = \text{decode}(p_\theta(\cdot | x), \text{constraints})$
 - Underlying model remains unchanged!

Which has the most **mass**:
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Constrained
Decoding

Language Model

<start>

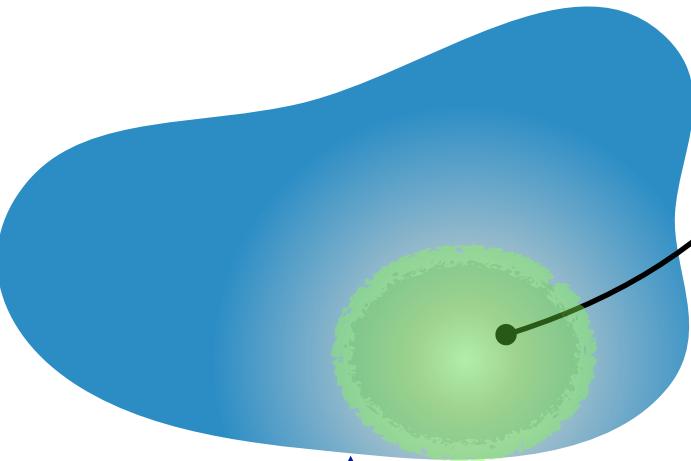
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- Which *classes* of constraints?
- How to specify and enforce them?

Which has the most **mass**:
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Constrained
Decoding

Language Model



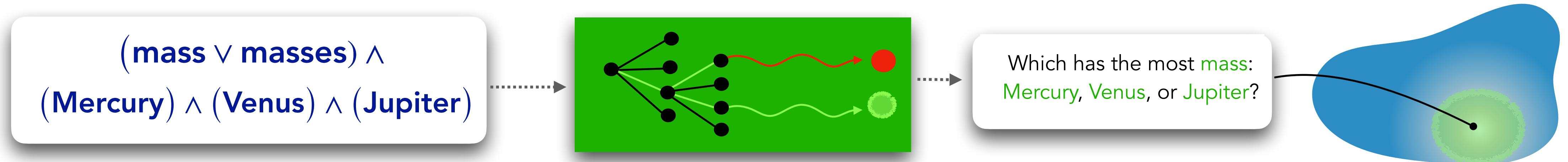
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Constrained generation through inference

- Today: decoding algorithms for constrained generation from two perspectives

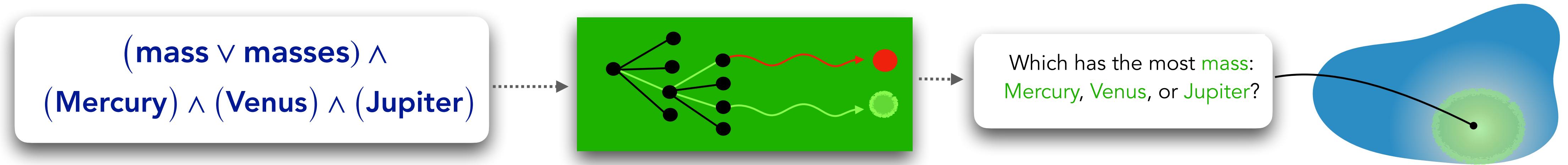
Constrained generation through inference

- Today: decoding algorithms for constrained generation from two perspectives
 - **Logical lexical constraints enforced through discrete inference**

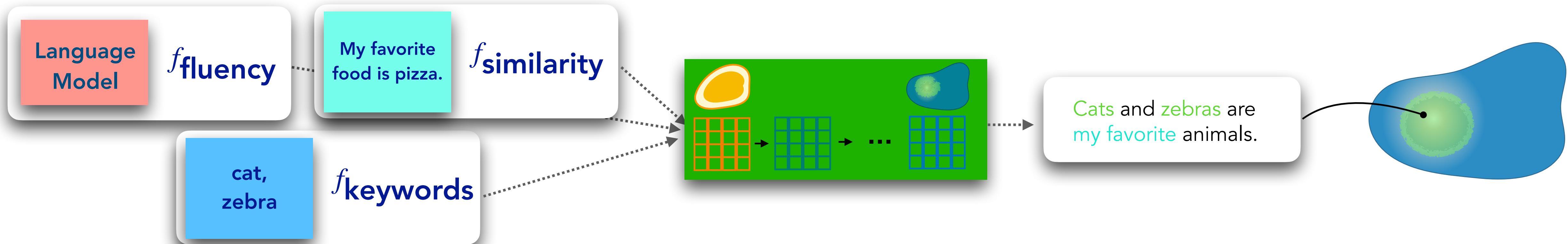


Constrained generation through inference

- Today: decoding algorithms for constrained generation from two perspectives
 - **Logical lexical constraints** enforced through **discrete inference**



- **Differentiable constraints** enforced through **continuous inference**



Constrained generation through *discrete* inference

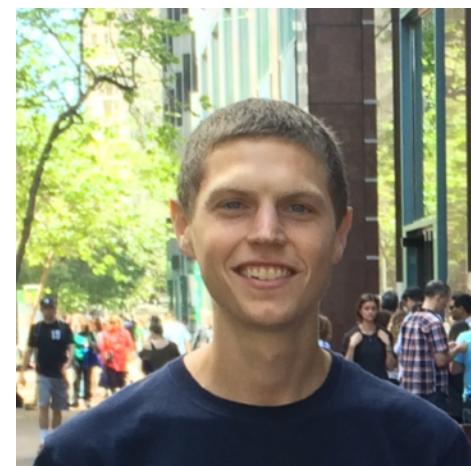
**NeuroLogic A*esque Decoding:
Constrained Text Generation with Lookahead Heuristics**

In Submission, [arxiv:2112.08726](https://arxiv.org/abs/2112.08726)

Ximing Lu



Sean Welleck



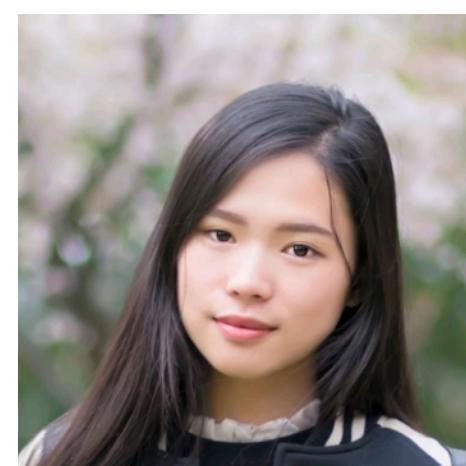
Peter West



Liwei Jiang



Lianhui Qin



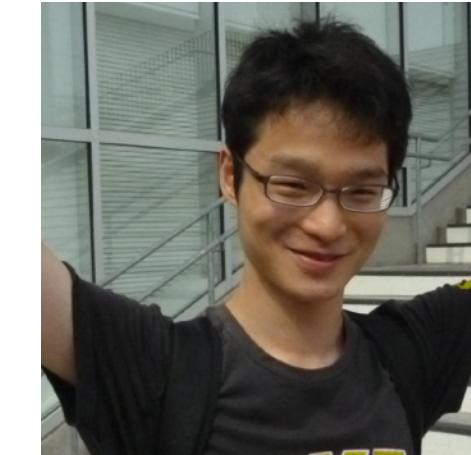
Youngjae Yu



Yejin Choi



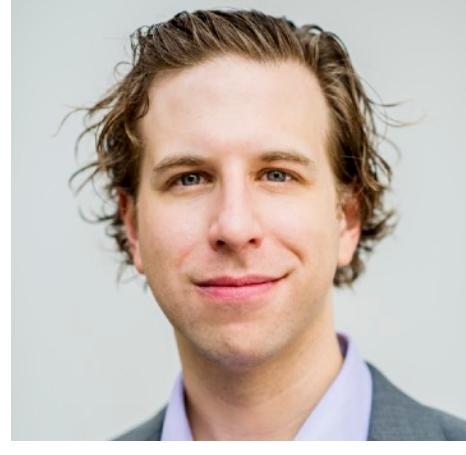
Daniel Khashabi Jungo Kasai



Ronan Le Bras Rowan Zellers



Noah Smith



Logical lexical constraints

- Ensure certain words **appear** or **do not appear**

Generate a sentence using
cat and fish, but not dog

Logical Constraints
 $(\text{cat} \vee \text{cats}) \wedge (\text{fish}) \wedge (\neg\text{dog})$

C

The cat jumped on the table and saw a fish.

A*-NeuroLogic

Off-the-shelf
Language Model

<start>

Decoding Objective

- Goal: $\mathbf{y}_* = \arg \max_{\mathbf{y} \in \mathcal{Y}} \underbrace{\log p_\theta(\mathbf{y})}_{\text{fluency}} + \underbrace{C(\mathbf{y})}_{\text{constraints}}$
- Logical Constraints**
 $(\text{cat} \vee \text{cats}) \wedge (\text{fish}) \wedge (\neg \text{dog})$

Standard decoding

Beam search

Standard decoding

Beam search

- $\mathbf{y}_* \approx \arg \max_{\mathbf{y} \in \mathcal{Y}} \underbrace{\log p_\theta(\mathbf{y})}_{\text{fluency}} + \underbrace{0}_{\text{constraints}}$

Standard decoding

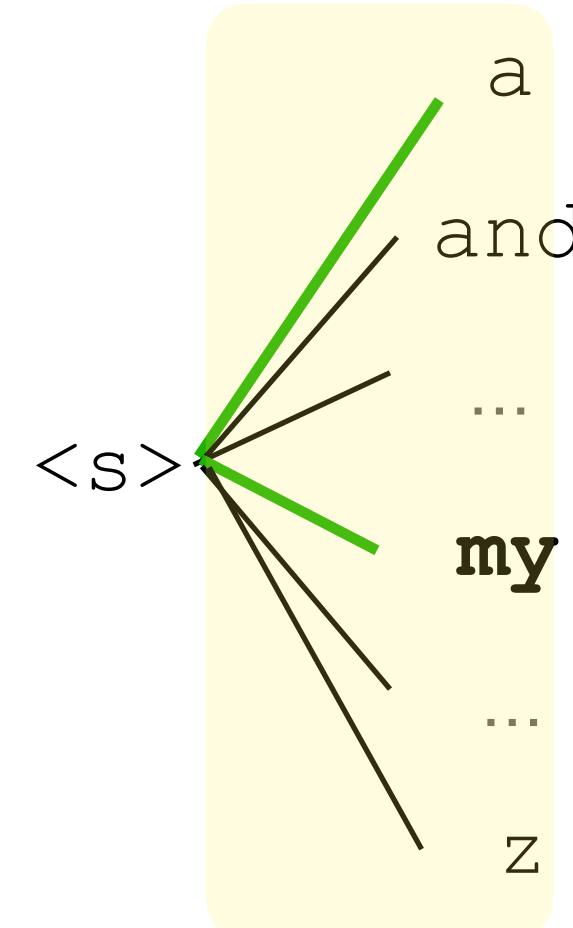
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Standard decoding

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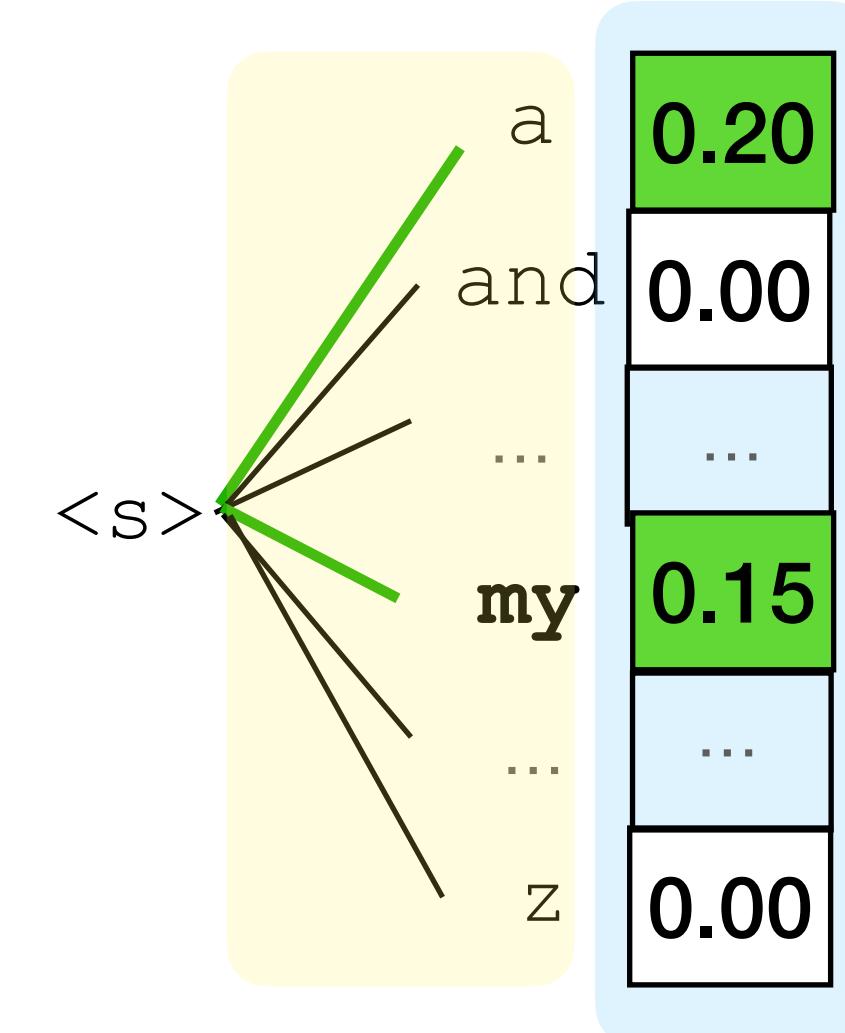
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Score each using
$$\underbrace{\log p_\theta(y_t | y_{<t})}_{\text{fluency}}$$



Standard decoding

Beam search

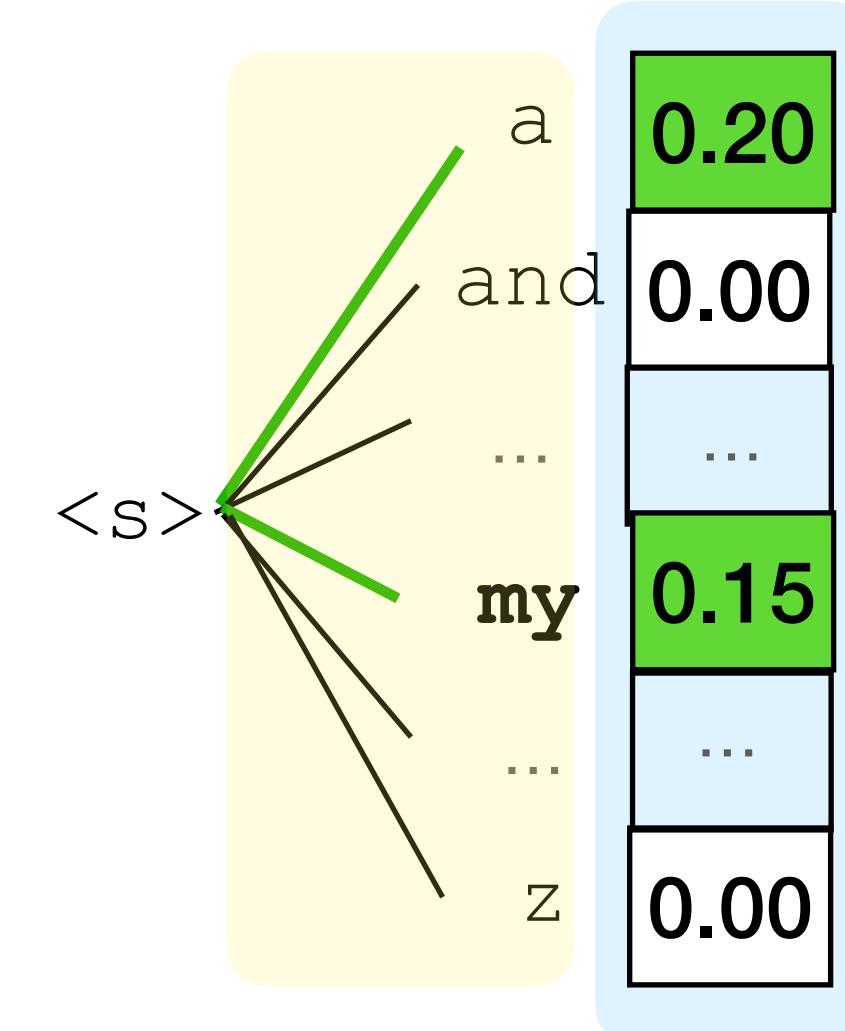
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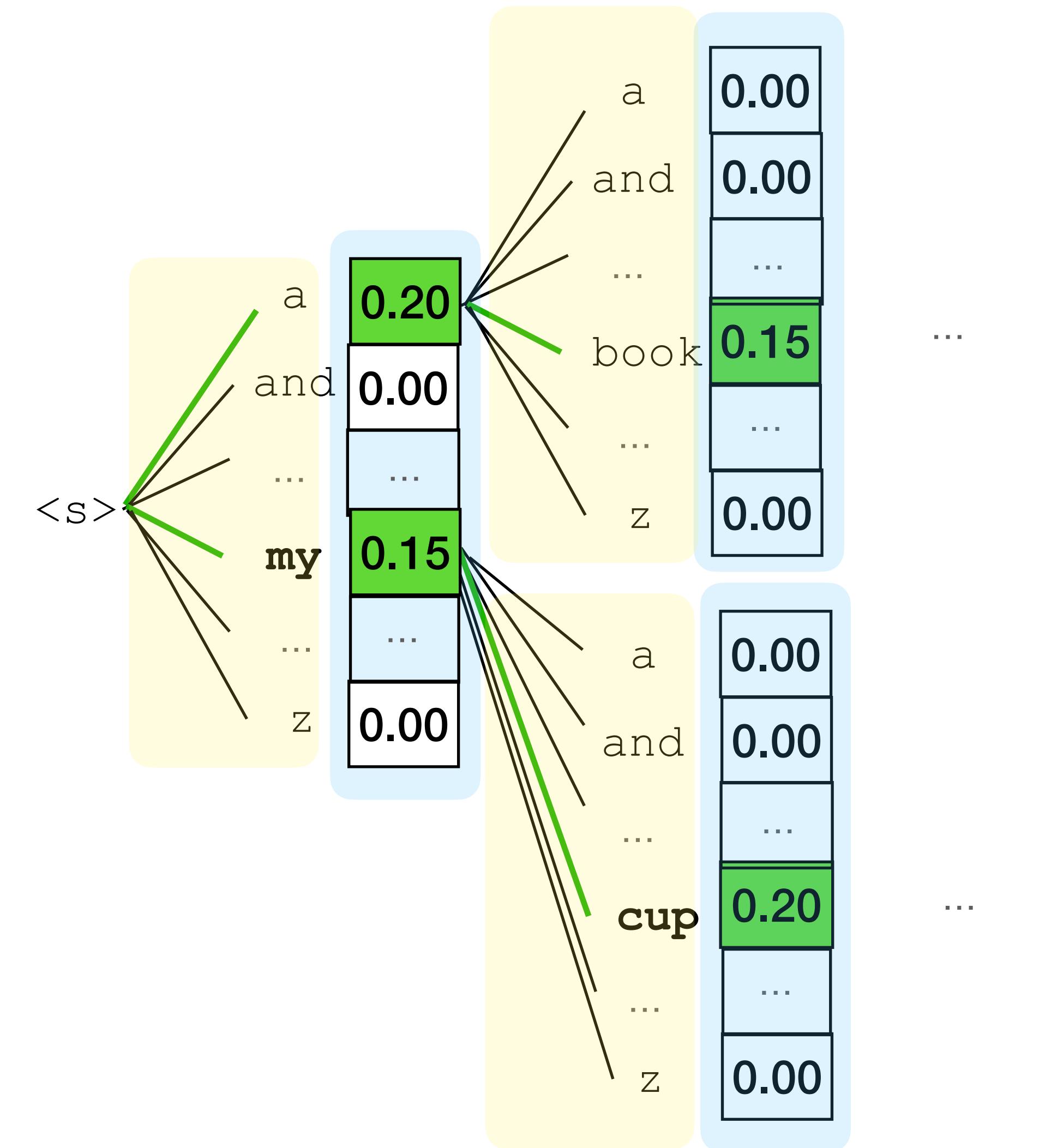
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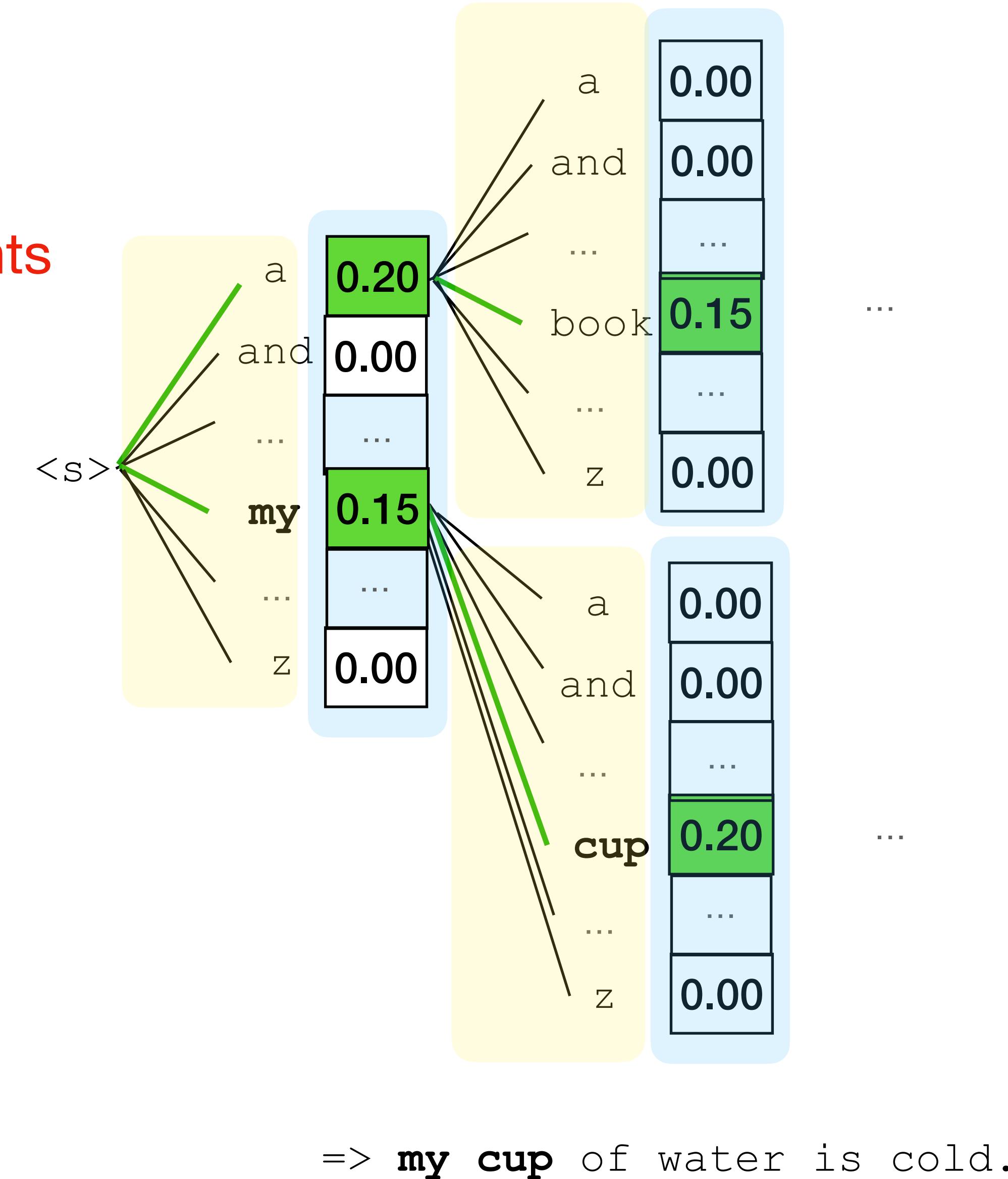


=> **my cup** of water is cold.

Standard decoding

Beam search

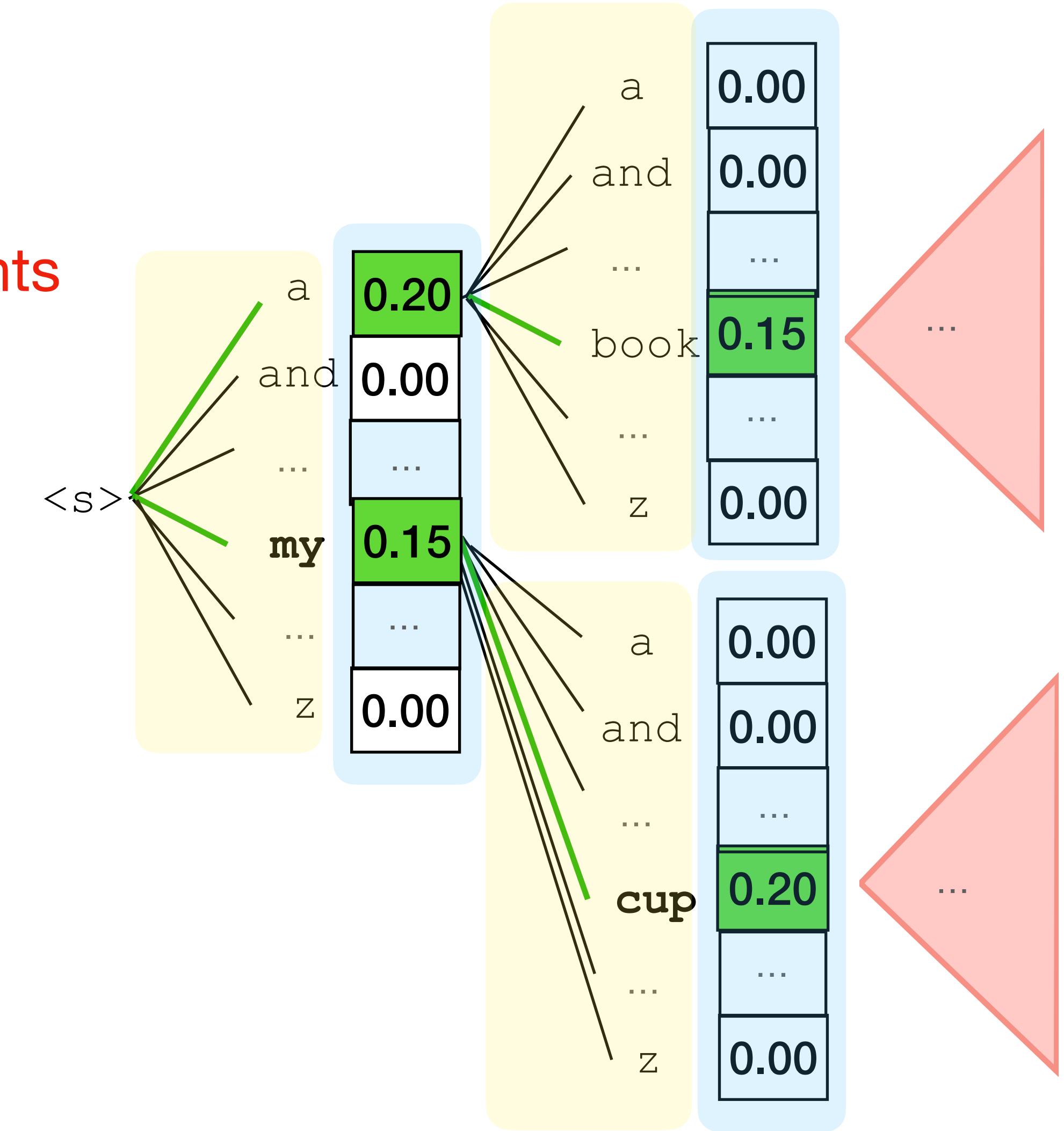
- $\mathbf{y}_* \approx \arg \max_{\mathbf{y} \in \mathcal{Y}} \underbrace{\log p_\theta(\mathbf{y})}_{\text{fluency}} + \underbrace{0}_{\text{constraints}}$ Ignores constraints
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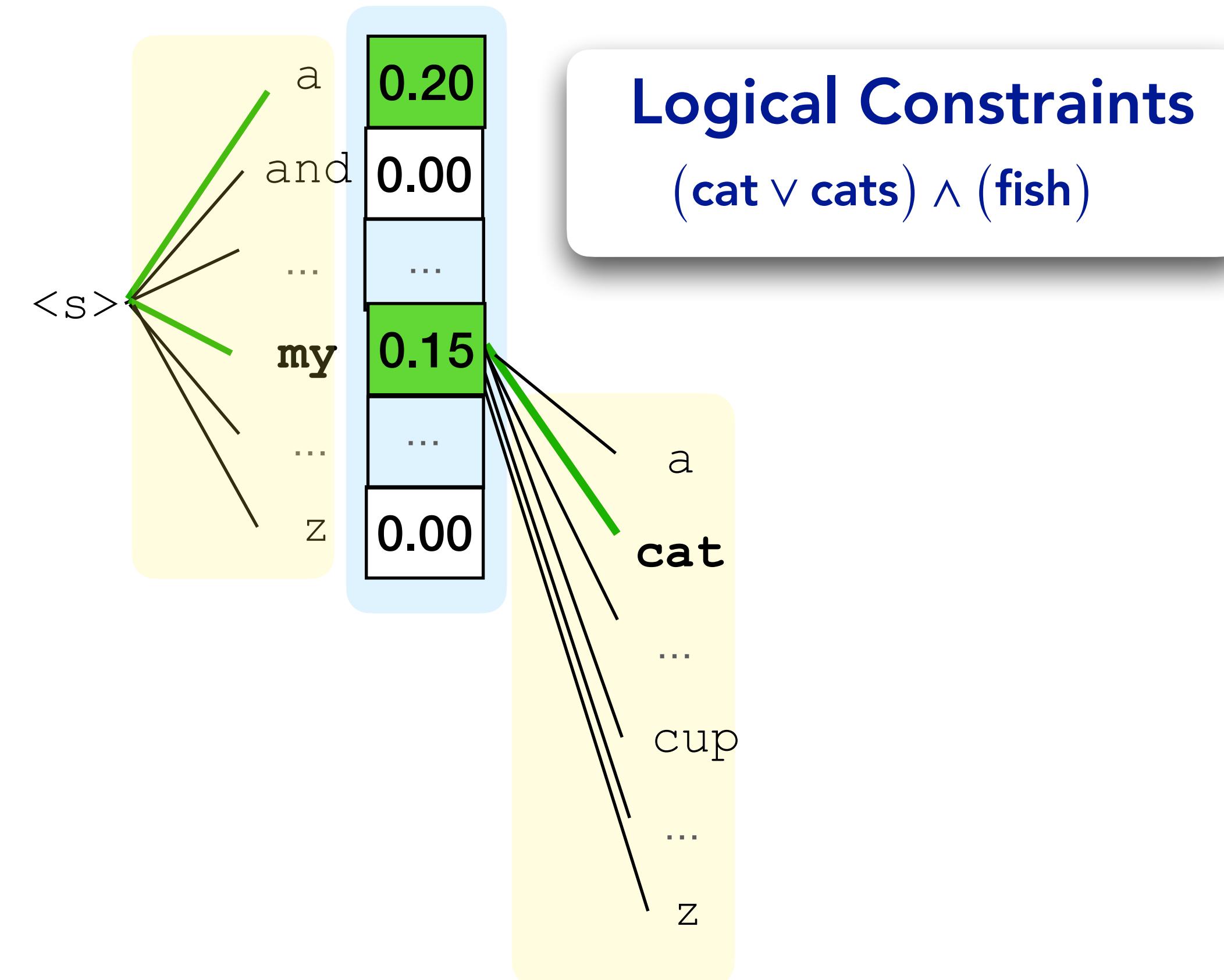
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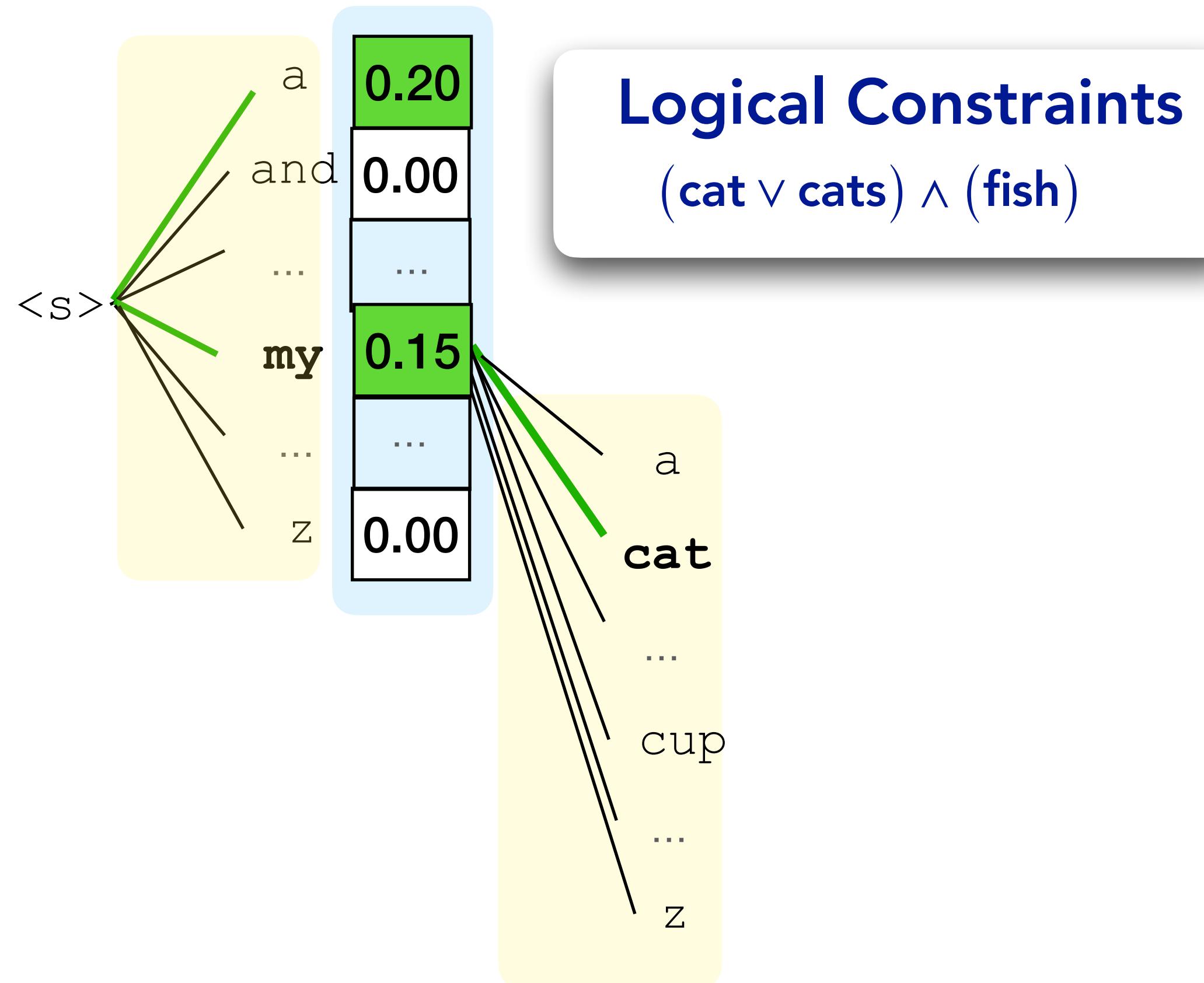
NeuroLogic decoding [Lu et al 2021]

- + favor tokens that [partially] satisfy constraints



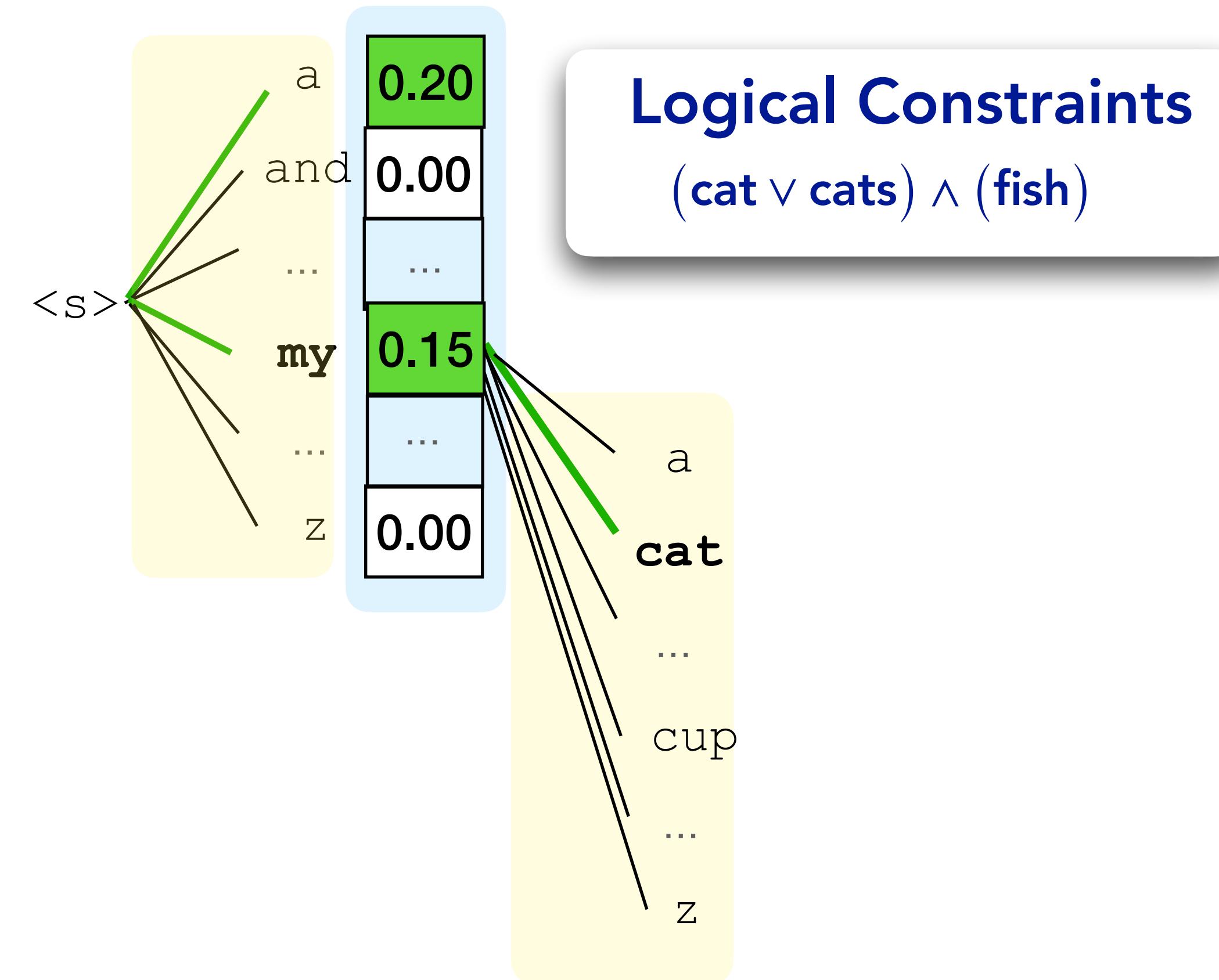
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Not trivial!

Details & other features
out of scope for this talk

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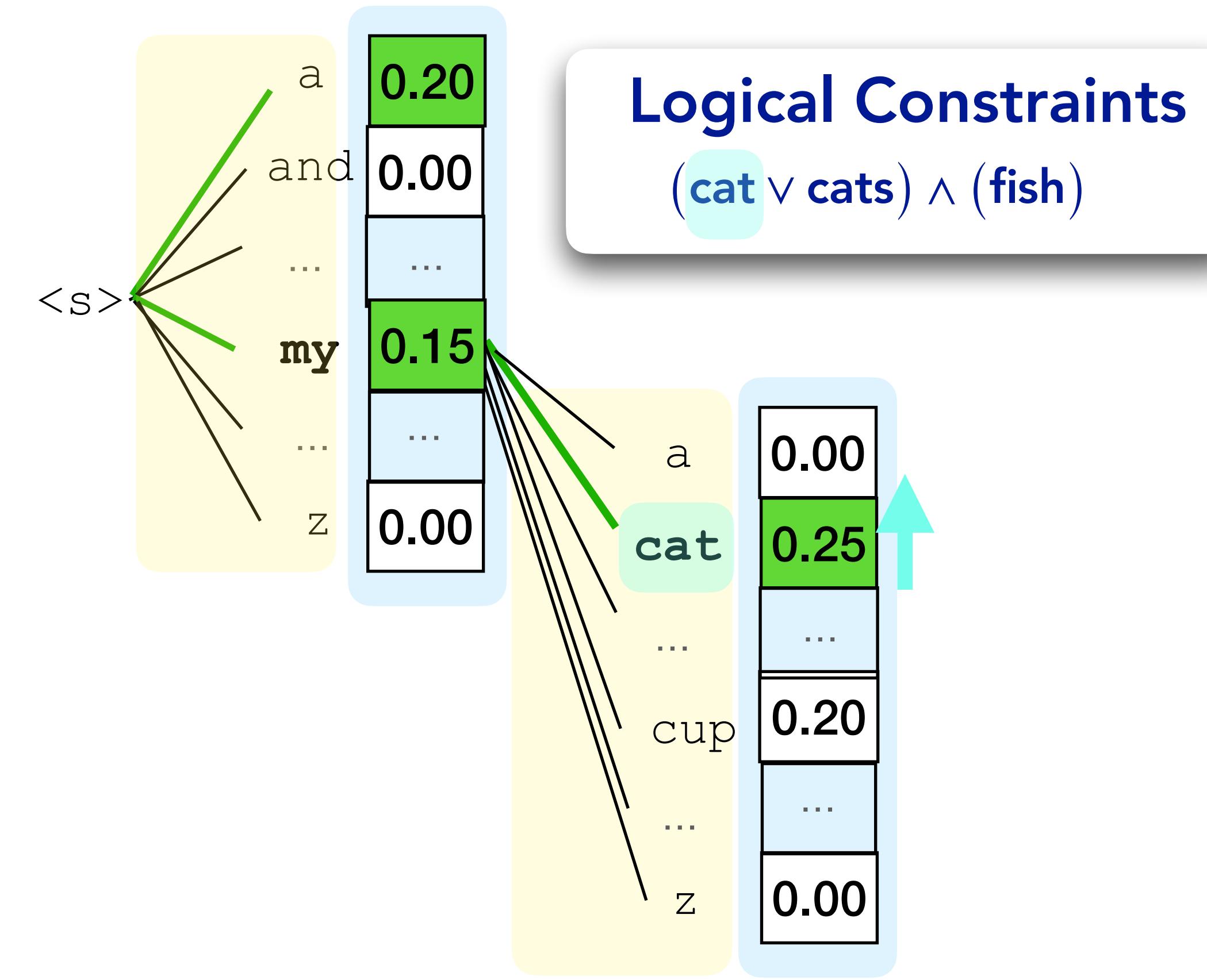
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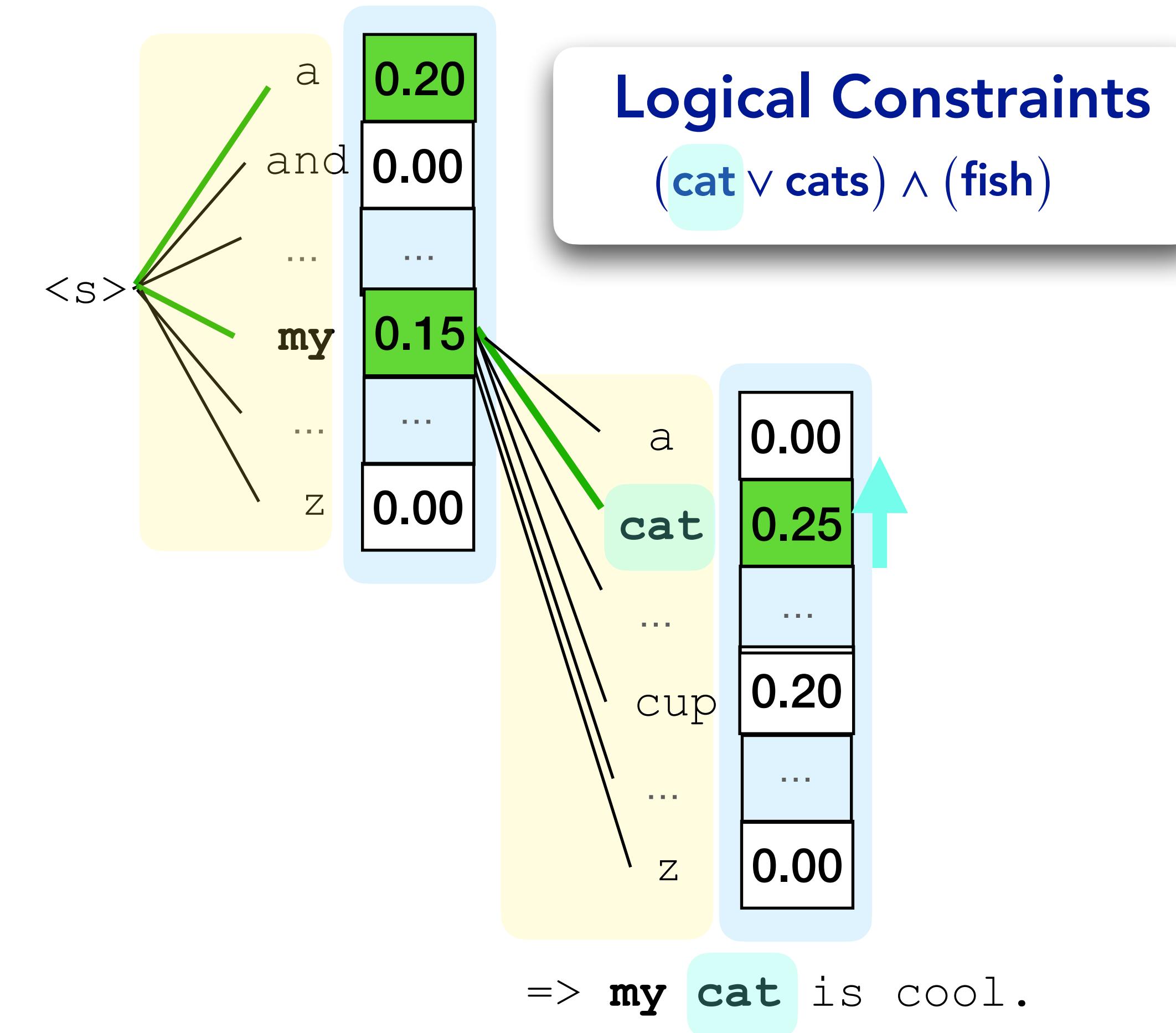
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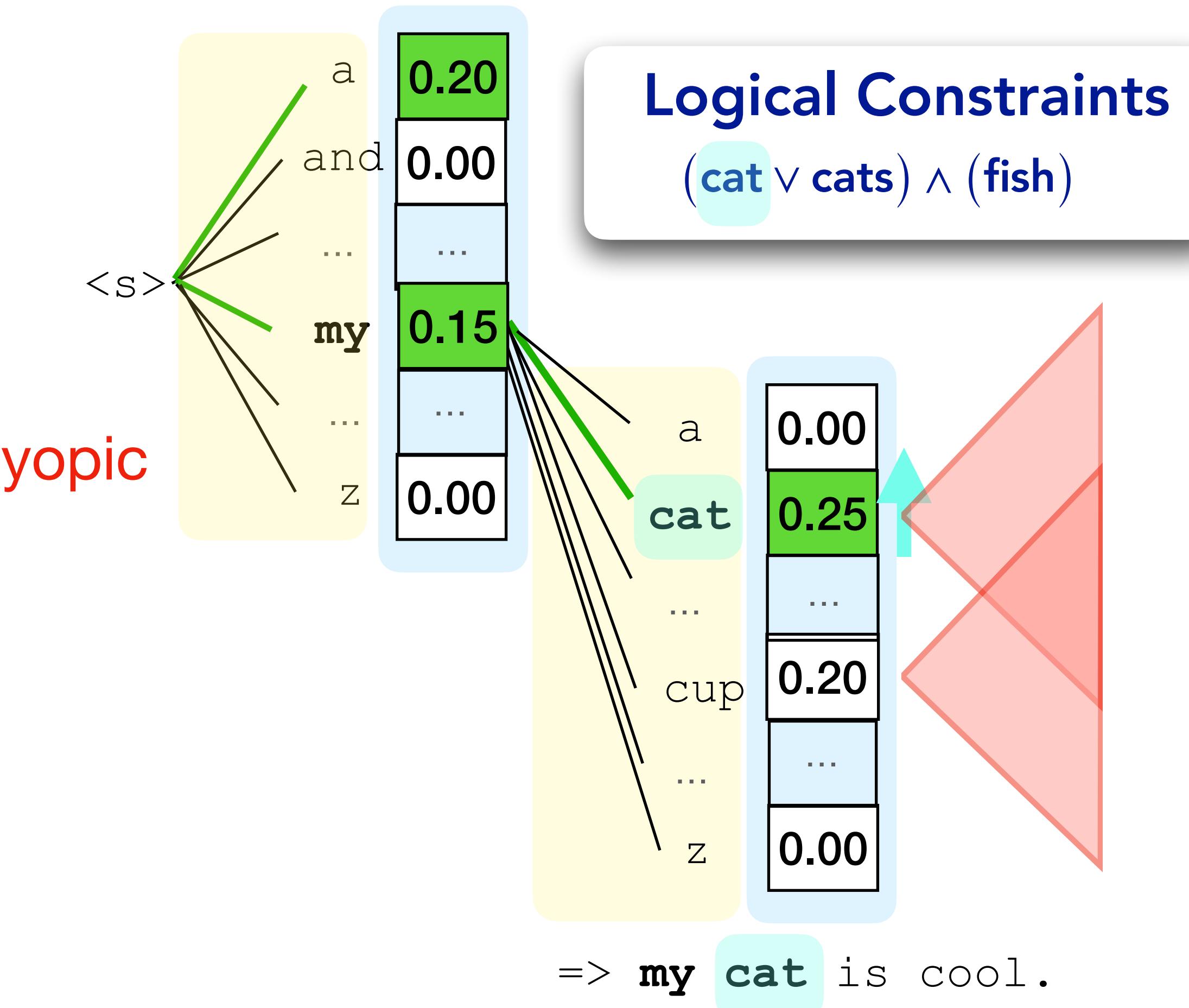
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NeuroLogic A*esque decoding

- Ideally, we want to select next-token candidates on optimal trajectories:

- $\text{argtopk}_{y_t} \left(\max_{\mathbf{y}_{>t}} F(\mathbf{y}_{, y_t, \mathbf{y}_{>t}}) \right), F = \text{fluency} + \text{constraints}$

NeuroLogic A*esque decoding

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The diagram illustrates the computation of the next-token candidate. It shows the expression $\text{argtopk}_{y_t} \left(\max_{\mathbf{y}_{>t}} F(\mathbf{y}_{<t}, y_t, \mathbf{y}_{>t}) \right)$. The term $\max_{\mathbf{y}_{>t}}$ is highlighted with a pink rounded rectangle. Two lines point from this highlighted term to the text "Intractable" located below the expression.

NeuroLogic A*esque decoding

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Intractable

- A* Search: best-first search with future heuristics

- $f(a) = \underbrace{s(a)}_{\text{score so-far}} + \underbrace{h(a)}_{\text{future heuristic}}$

score so-far future heuristic



NeuroLogic A*esque decoding

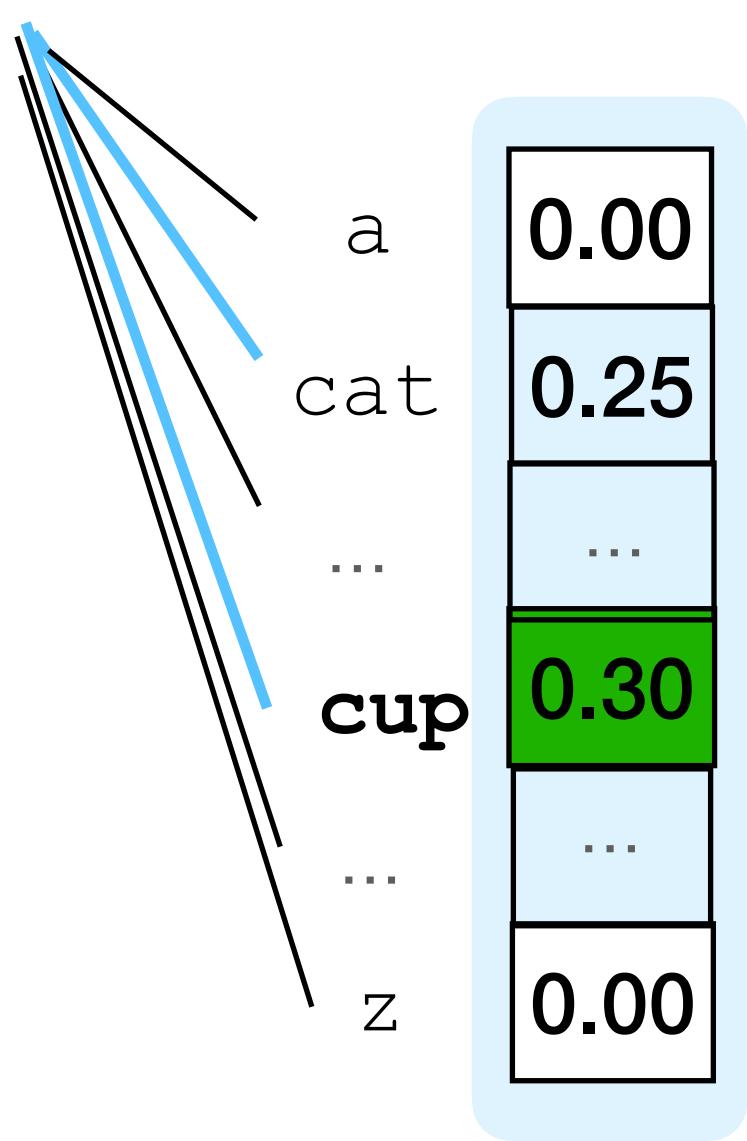
- Approximate with a *lookahead heuristic*:

$$\cdot \text{argtopk}_{y_t} \left(s(\mathbf{y}_{\leq t}) +$$

Fluency + constraints-so-far

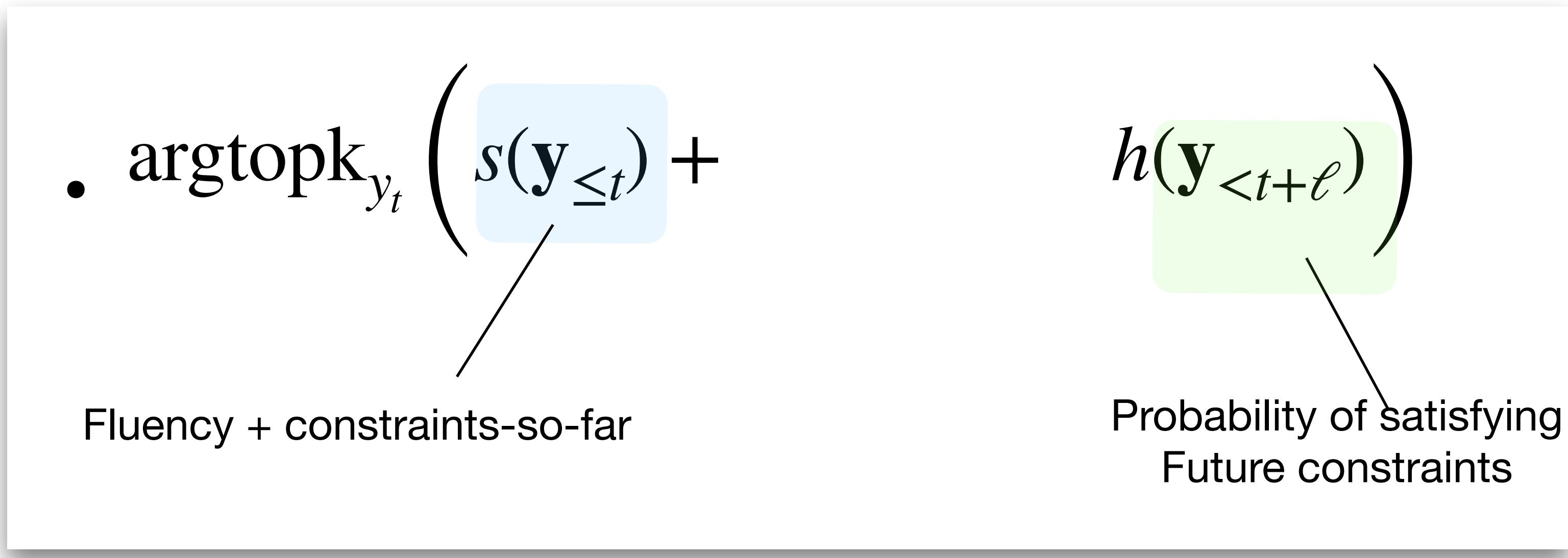
Logical Constraints

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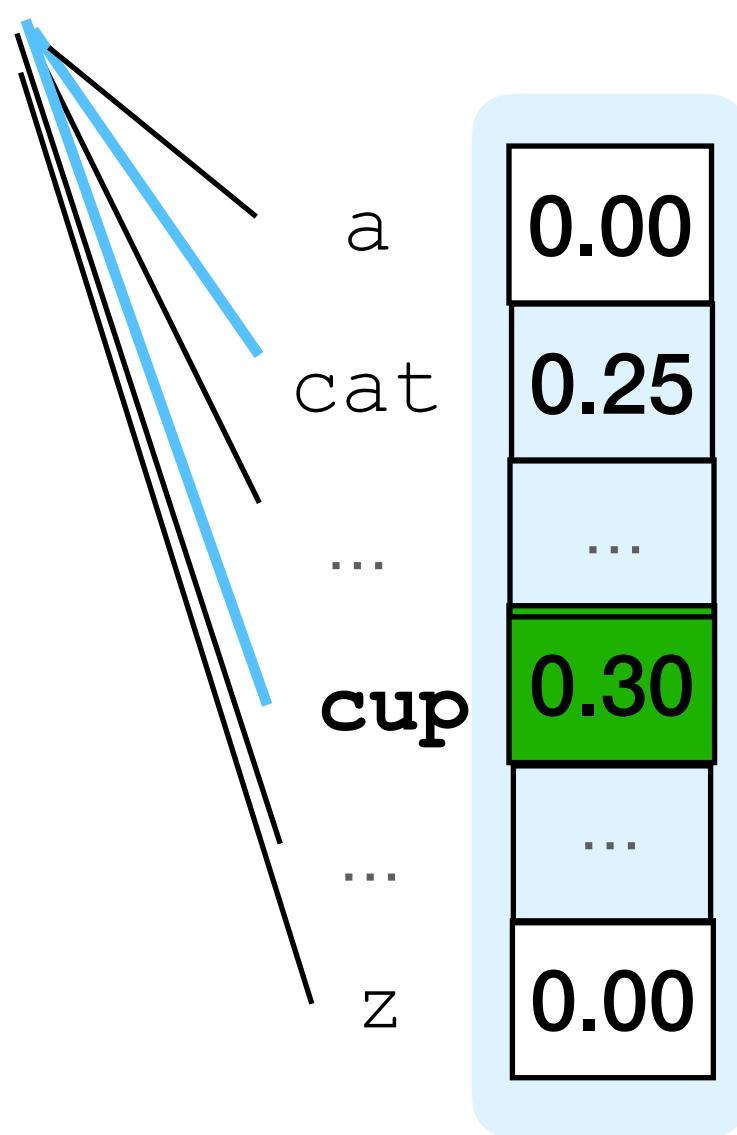


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 $(\text{cat} \vee \text{cats}) \wedge (\text{fish})$



NeuroLogic A*esque decoding

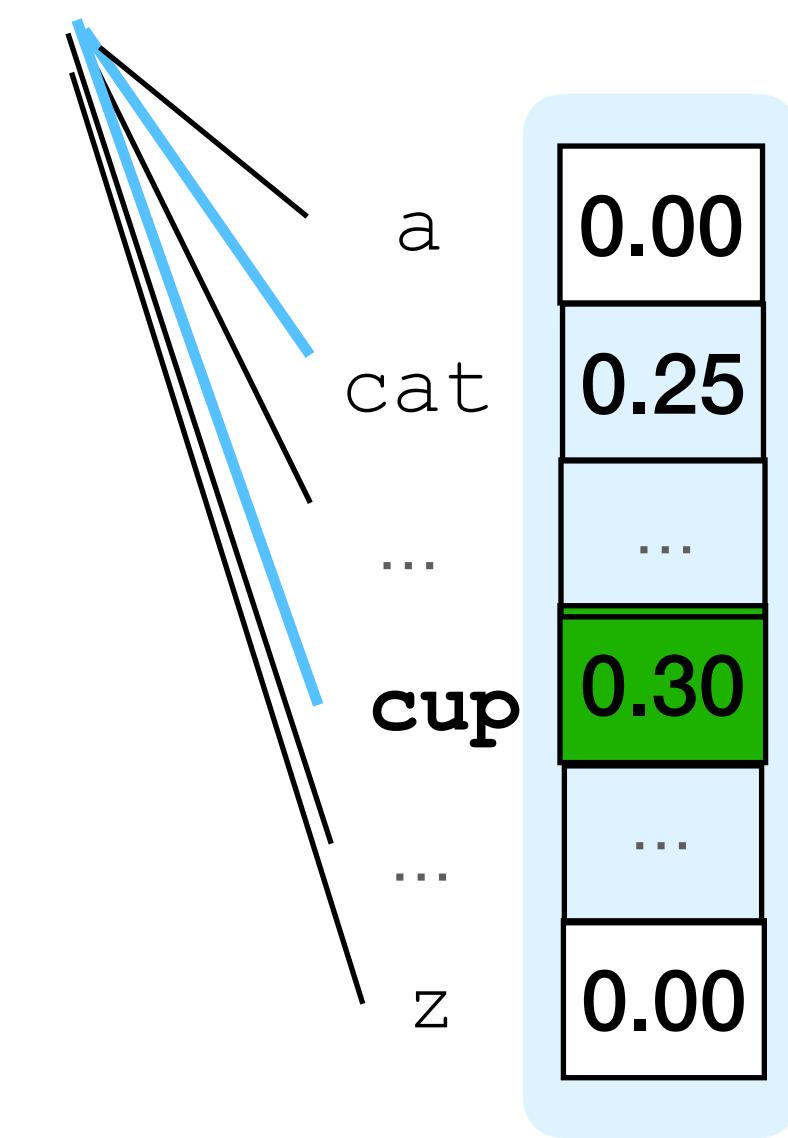
- Approximate with a *lookahead heuristic*:

$$\bullet \text{ argtopk}_{y_t} \left(s(\mathbf{y}_{\leq t}) + \max_{\text{Lookaheads}} h(\mathbf{y}_{<t+\ell}) \right)$$

Fluency + constraints-so-far

E.g. single greedy lookahead

Probability of satisfying Future constraints



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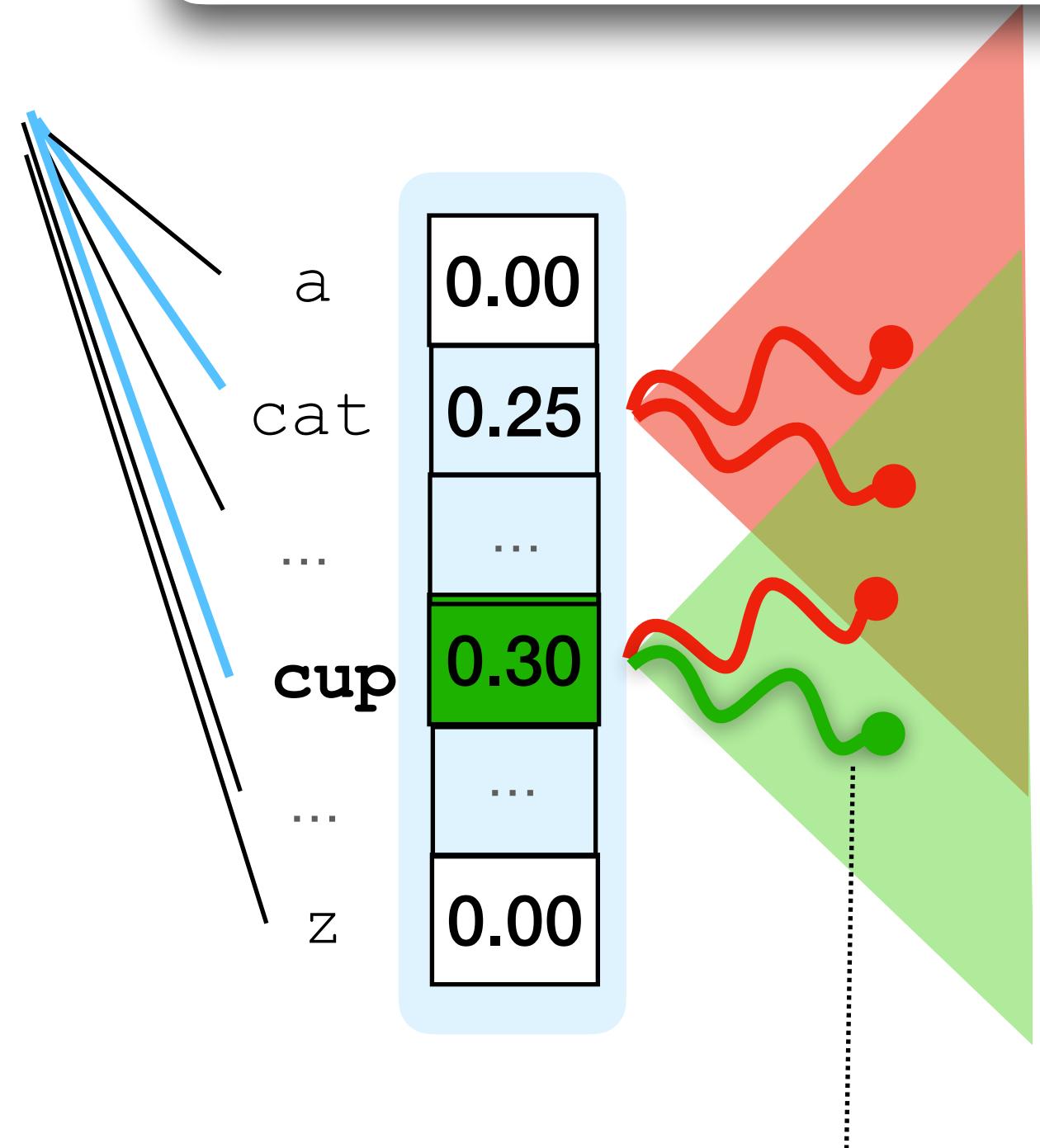
Fluency + constraints-so-far

E.g. single greedy lookahead

Probability of satisfying Future constraints

Logical Constraints

$$(\text{cat} \vee \text{cats}) \wedge (\text{fish})$$



NeuroLogic A*esque decoding

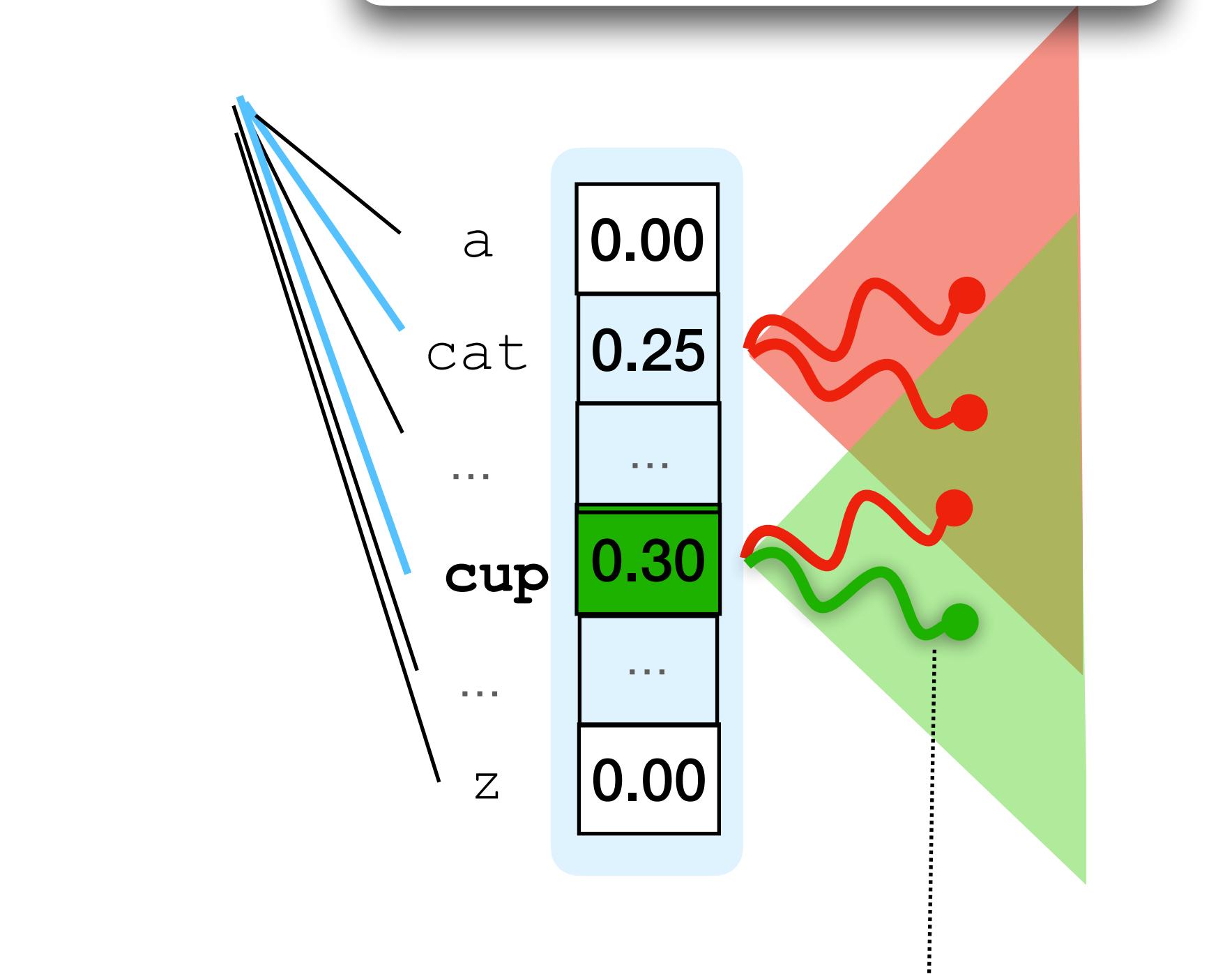
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Fluency + constraints-so-far

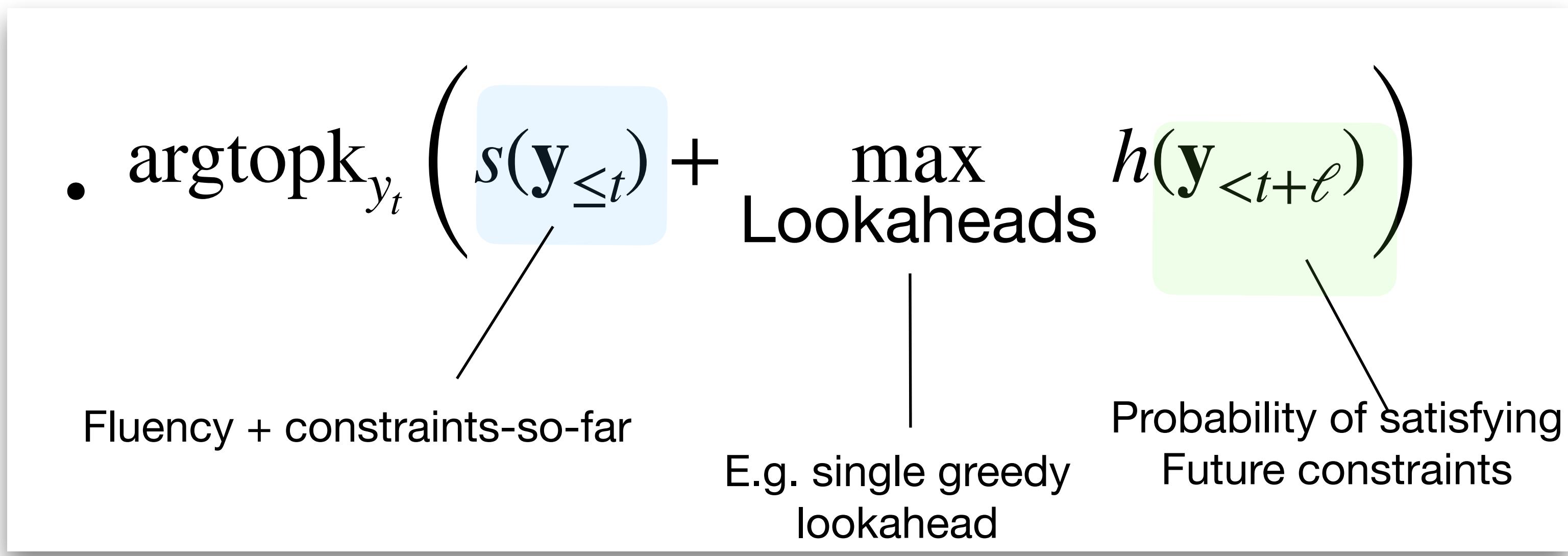
E.g. single greedy lookahead

Probability of satisfying Future constraints

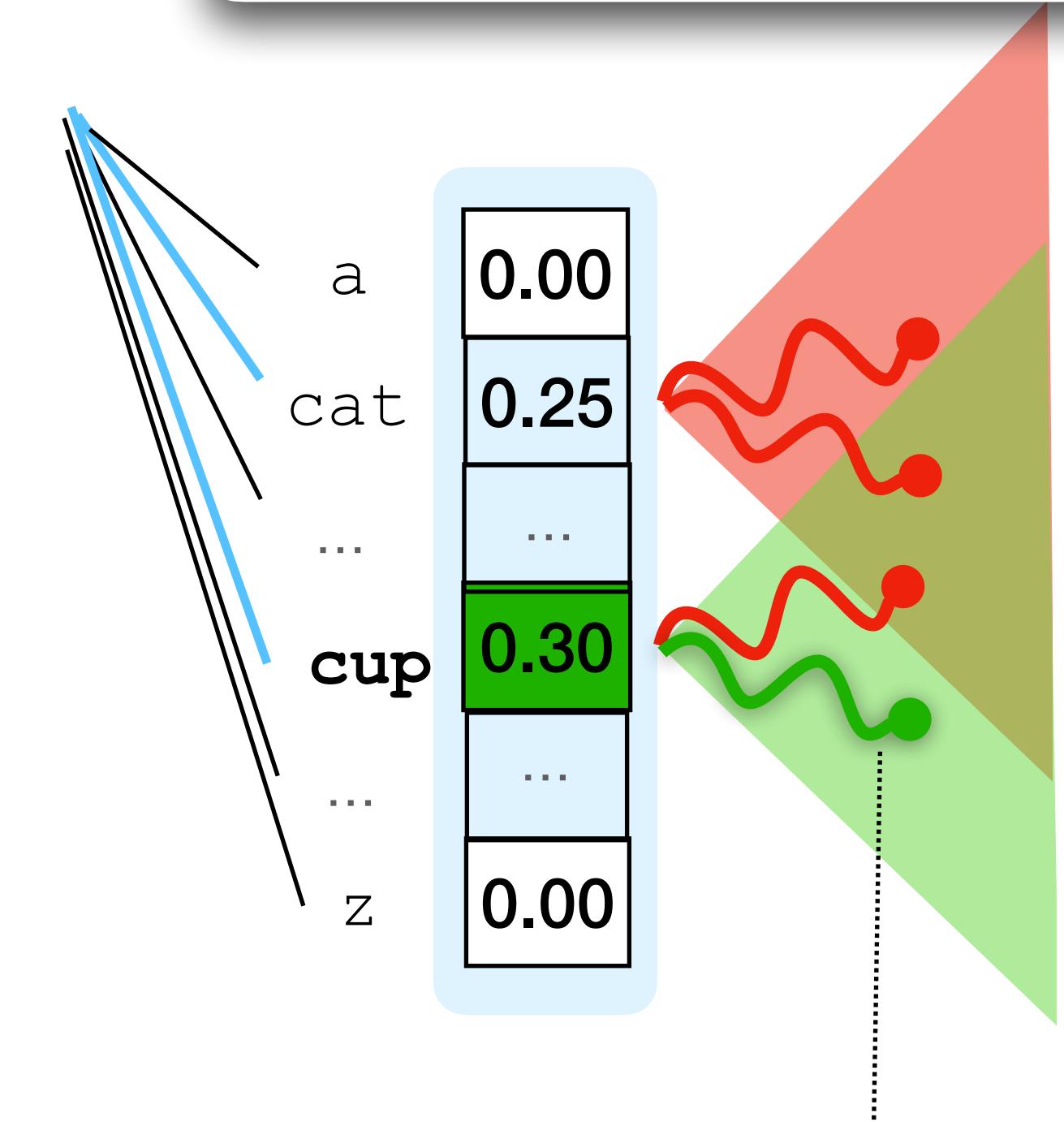


NeuroLogic A*esque decoding

- Approximate with a *lookahead heuristic*:



Logical Constraints
 $(\text{cat} \vee \text{cats}) \wedge (\text{fish})$

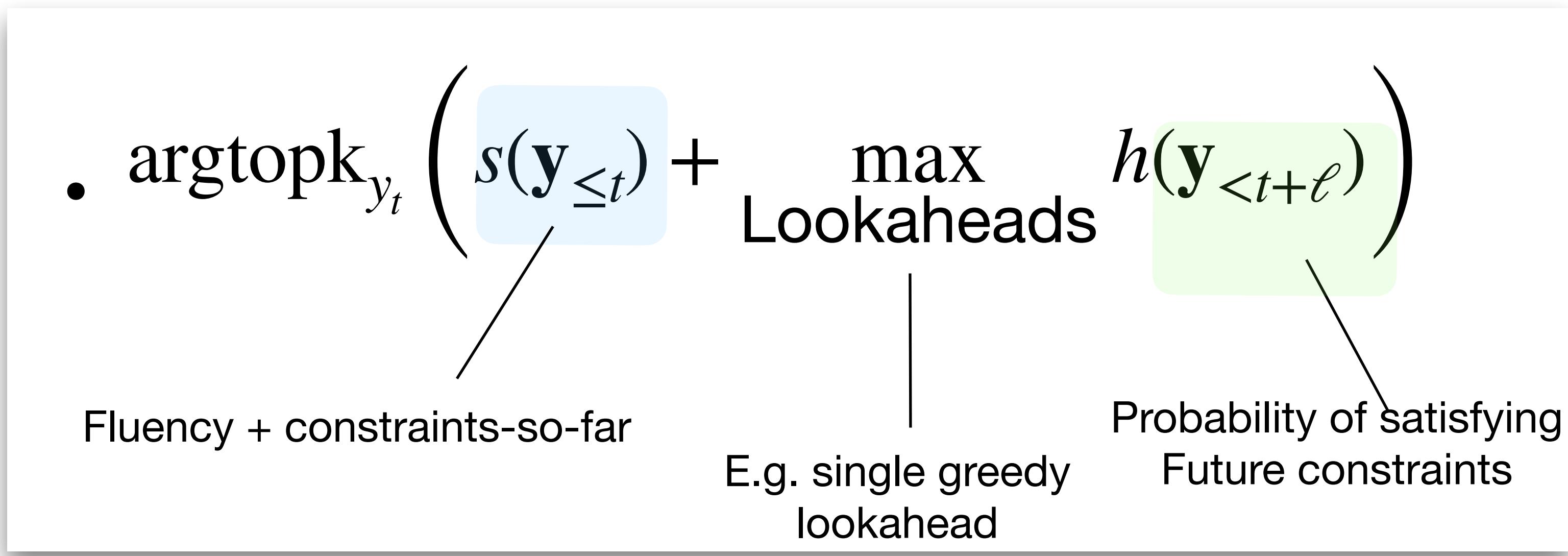


=> my cup has a **fish** and **cat** on it.



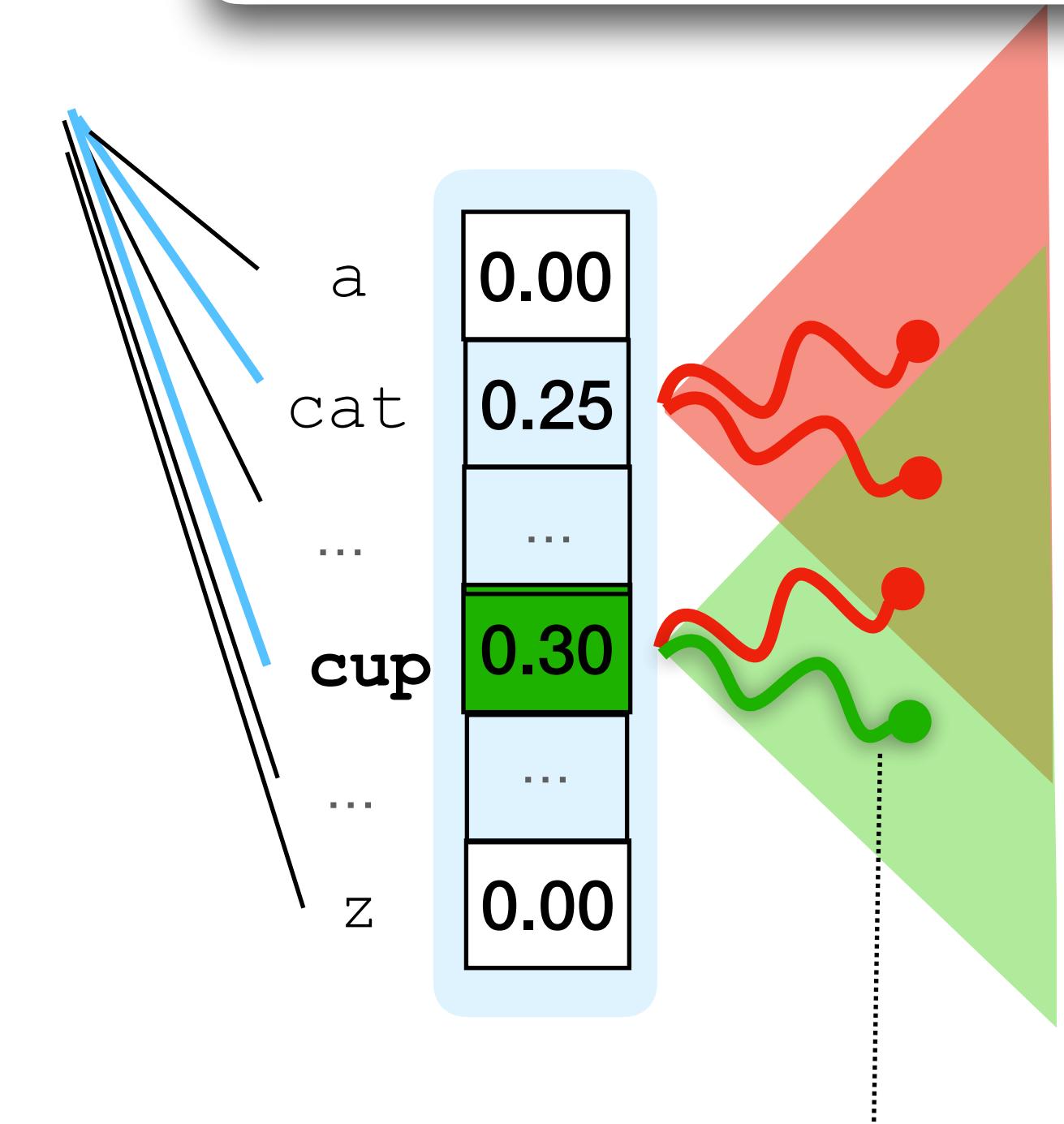
NeuroLogic A*esque decoding

- Approximate with a *lookahead heuristic*:



Logical Constraints

$$(\text{cat} \vee \text{cats}) \wedge (\text{fish})$$



=> my cup has a **fish** and **cat** on it.



- “A*esque”: beam instead of best-first

CommonGen

(Lin et al., 2020)

- Standard constrained generation benchmark:
~60k train, ~7k test

Constraints: {sponge, pour, pool, side, clean}

Example output: Pour water on a sponge and use it
to clean the side of the pool.

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beam search

The woman, whose name has
not been released, was taken to
a local hospital, where she was
listed in stable condition,
according to the sheriff's office.

completely irrelevant

CommonGen

(Lin et al., 2020)

- Standard constrained generation benchmark:
~60k train, ~7k test

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(sponge \vee sponges) \wedge (pour \vee
pours \vee pouring \vee poured) \wedge
(pool \vee pools) \wedge (side \vee sides) \wedge
(clean \vee clean \vee cleans \vee cleaning)

beam search

The woman, whose name has
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completely irrelevant

NeuroLogic

The man **cleans** a **sponge** in
a **pouring pool** at the **side**
of the road.

slightly awkward

C

CommonGen

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- Standard constrained generation benchmark:
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completely irrelevant

NeuroLogic

The man **cleans** a **sponge** in
a **pouring pool** at the **side**
of the road.

slightly awkward

C

A* NeuroLogic

The boy **cleaned** the **side** of the
pool with a **sponge**, and **poured**
water over it .

Human evaluation | CommonGen

(Lin et al., 2020)

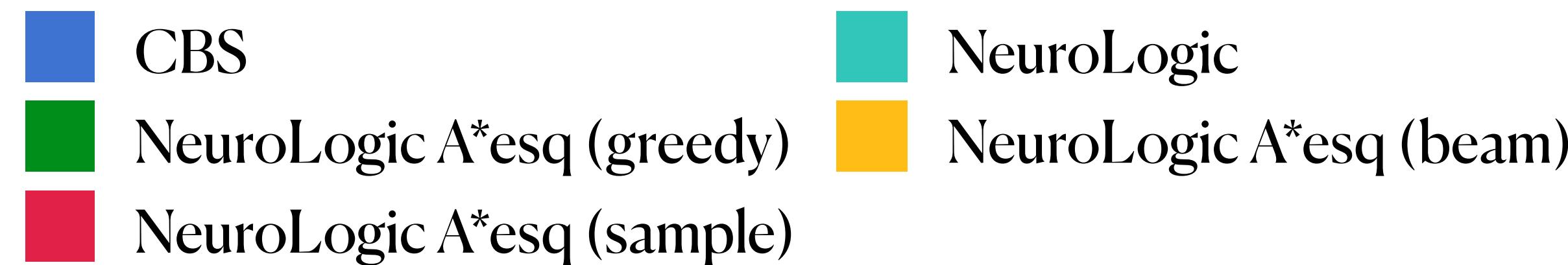
Fine-tuned GPT-2

Off-the-shelf GPT-2

Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2



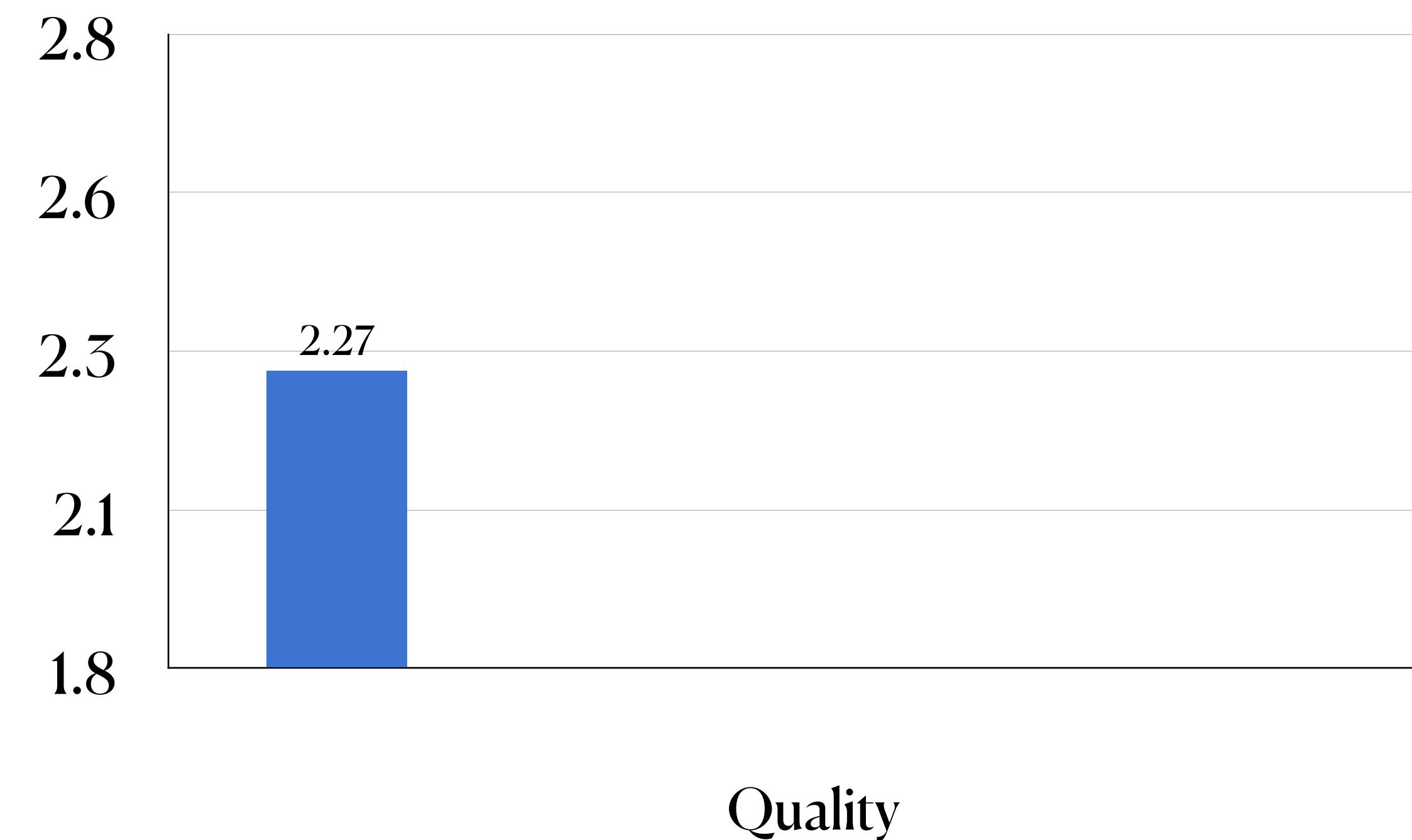
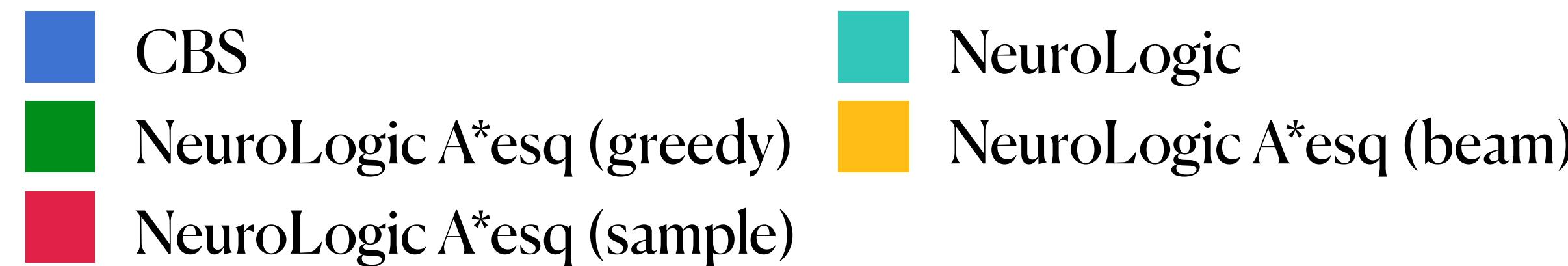
Off-the-shelf GPT-2



Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2

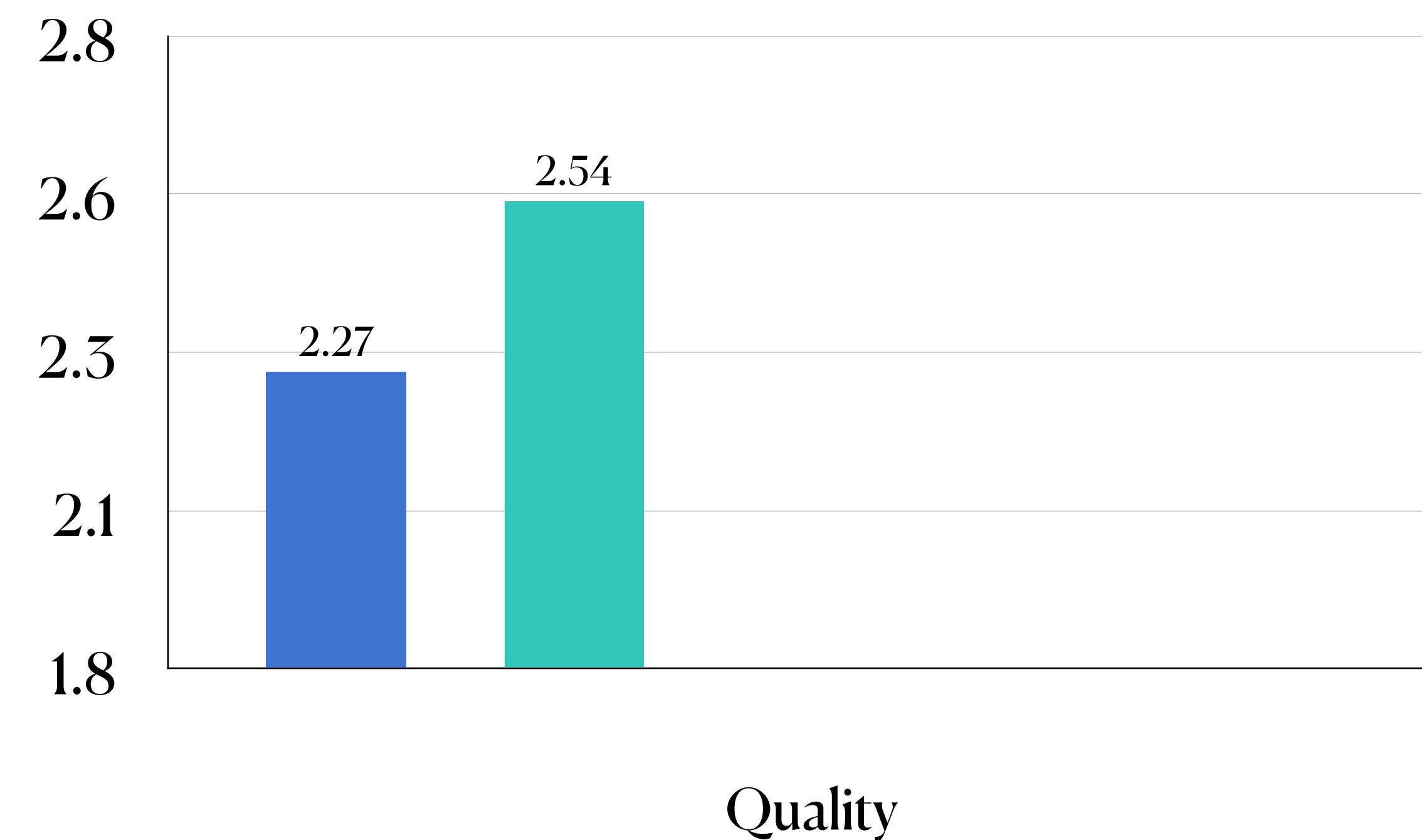
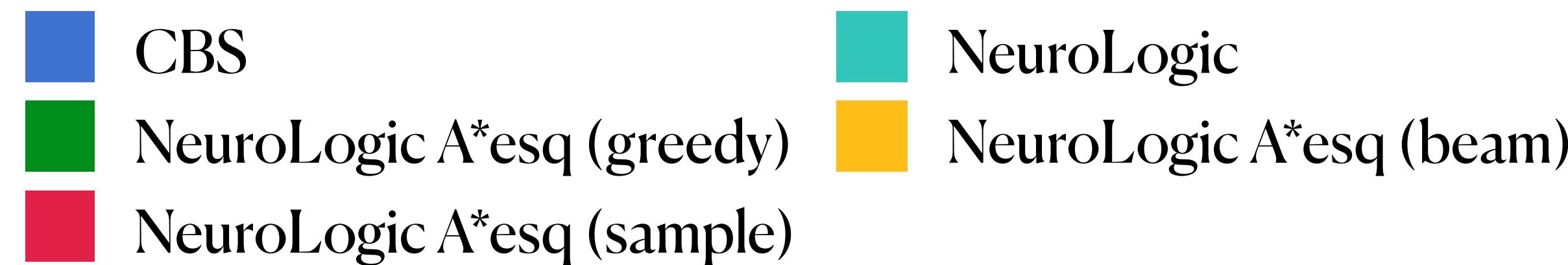


Off-the-shelf GPT-2

Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2

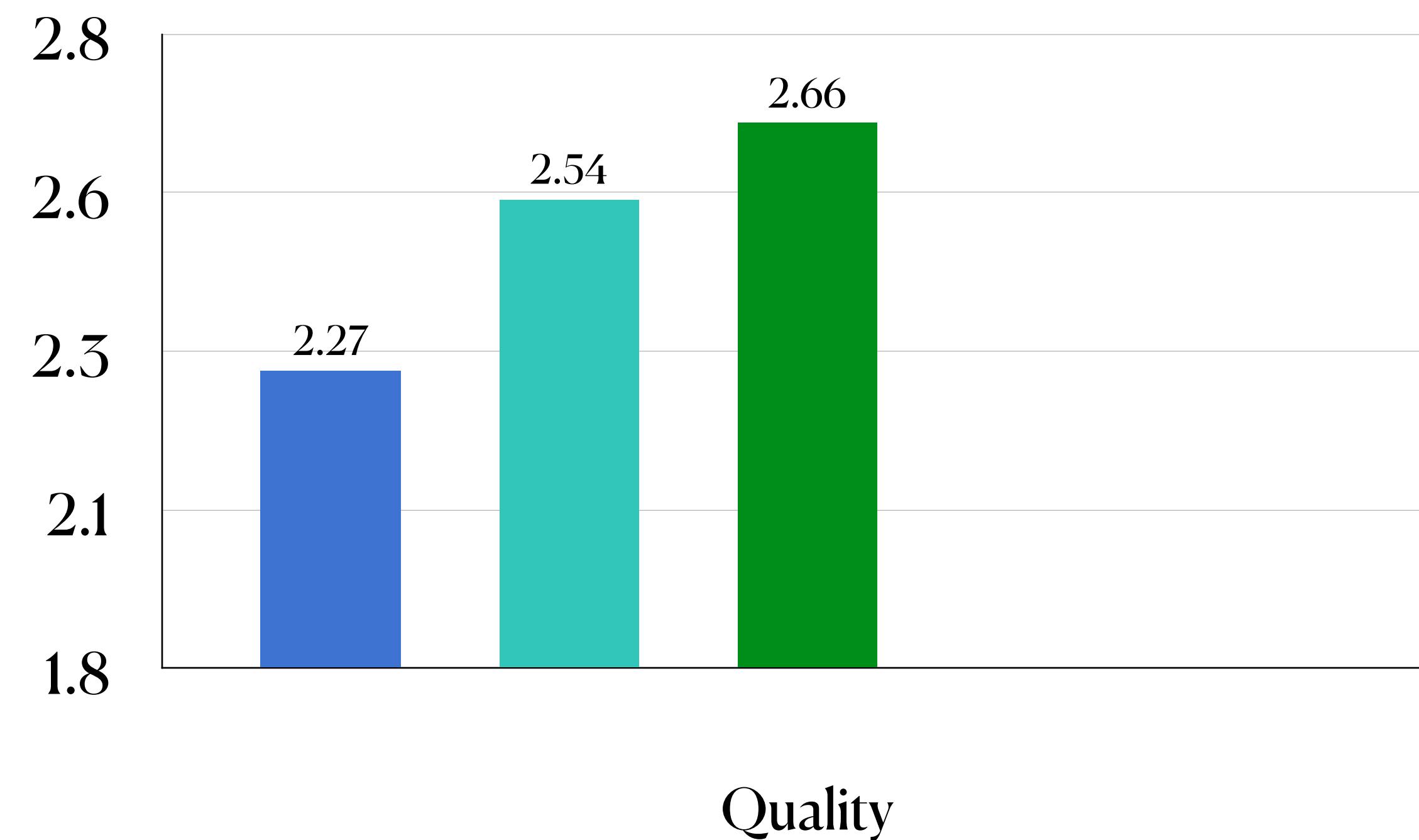
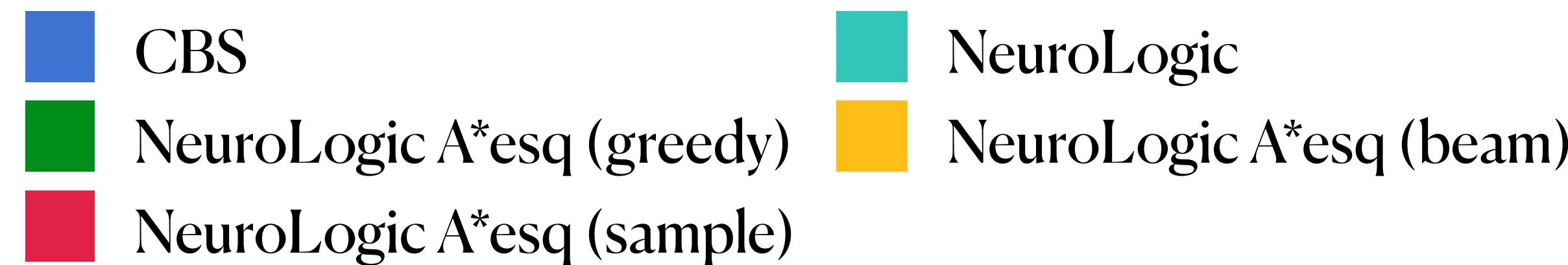


Off-the-shelf GPT-2

Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2

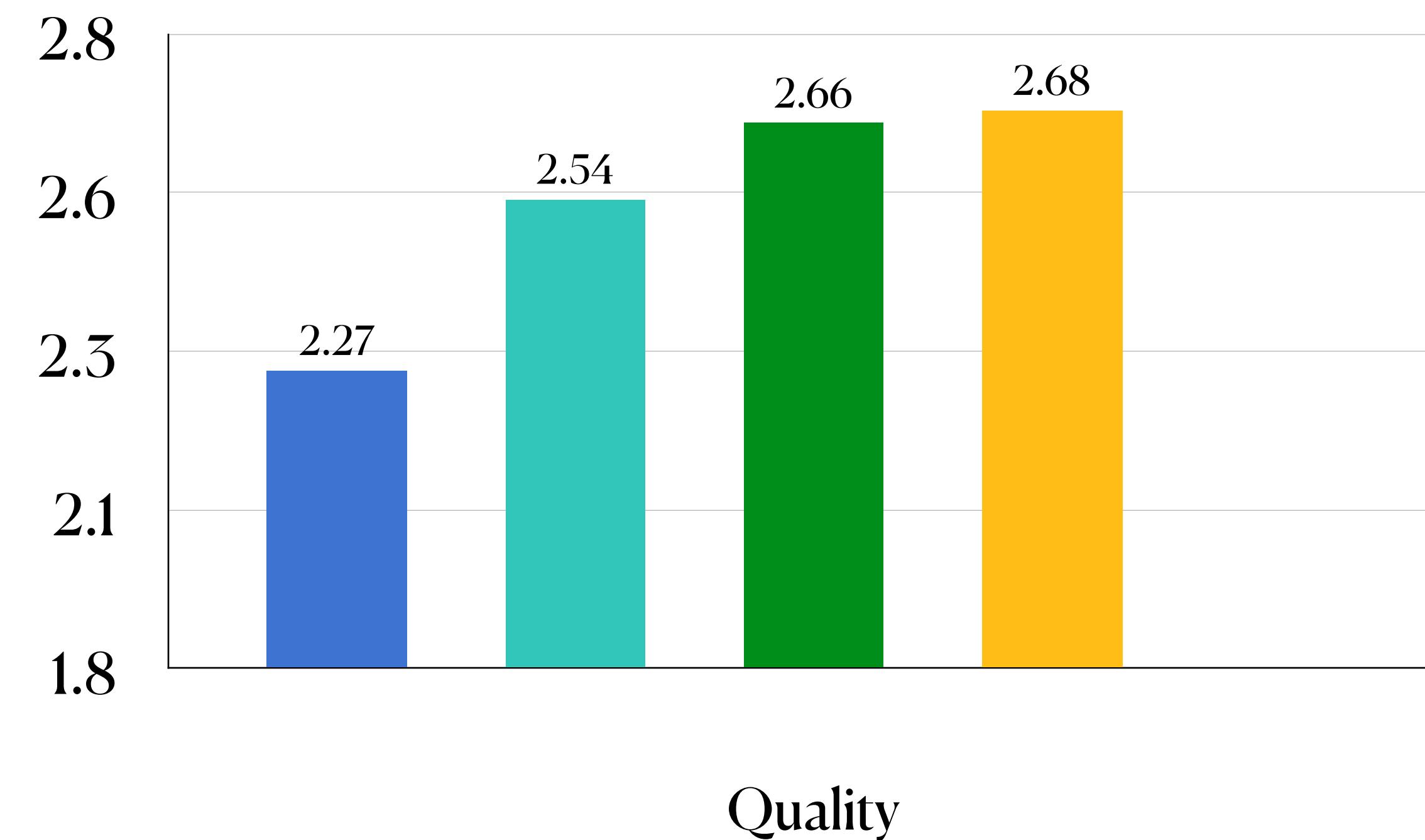
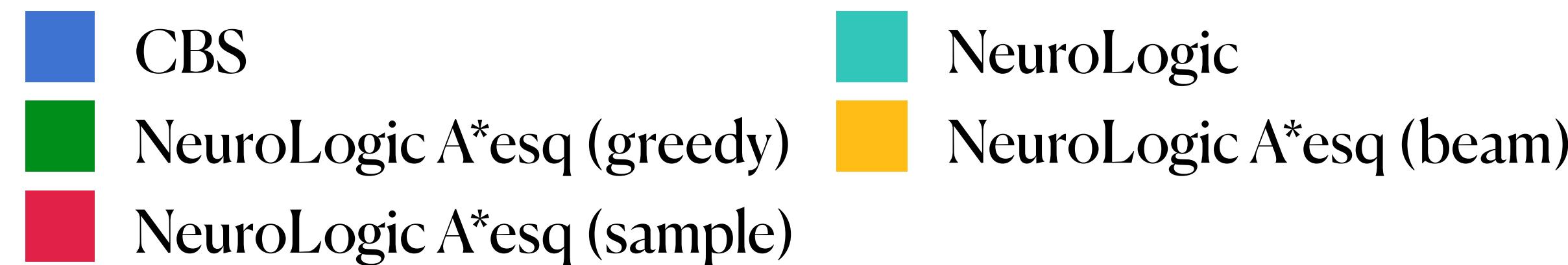


Off-the-shelf GPT-2

Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2

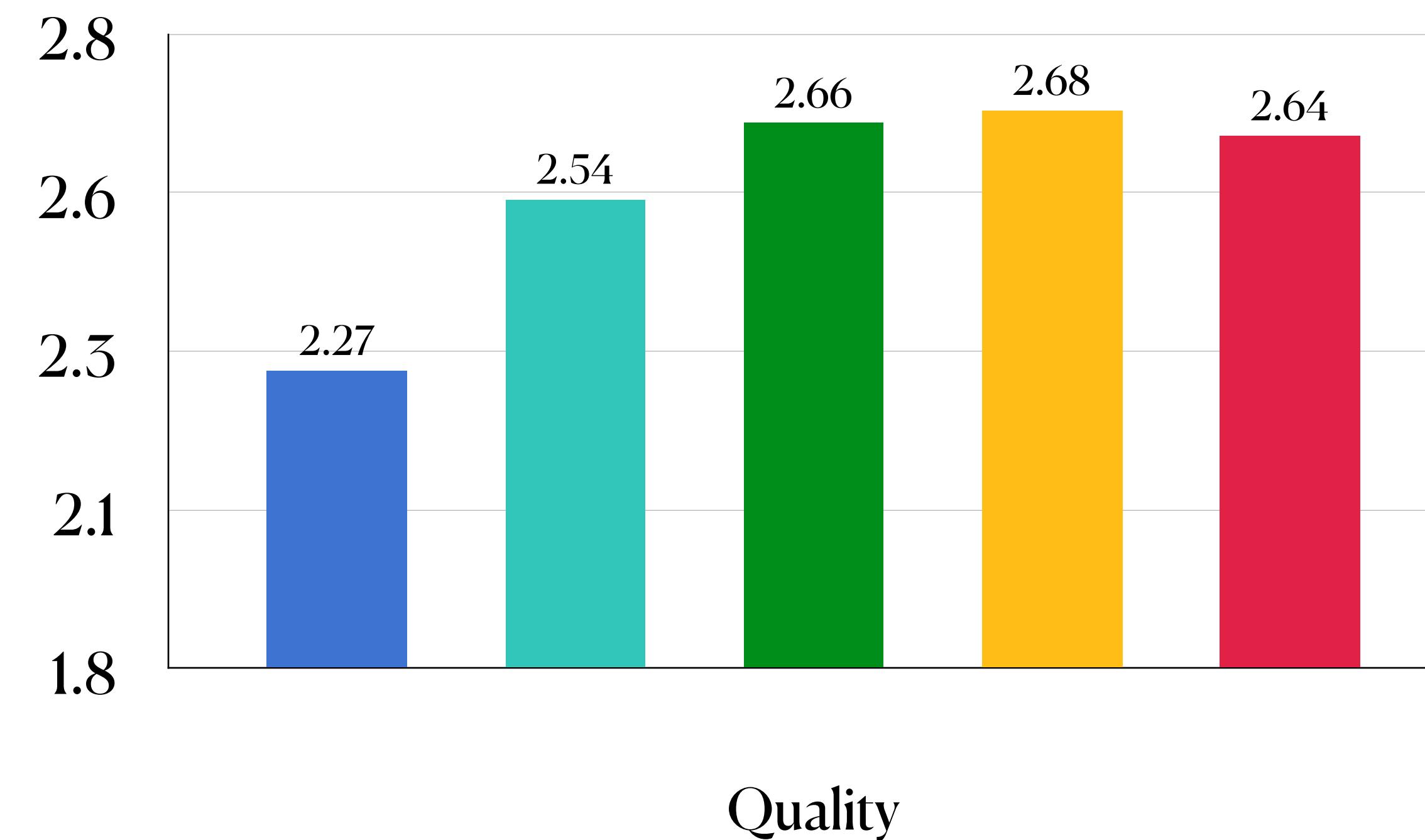
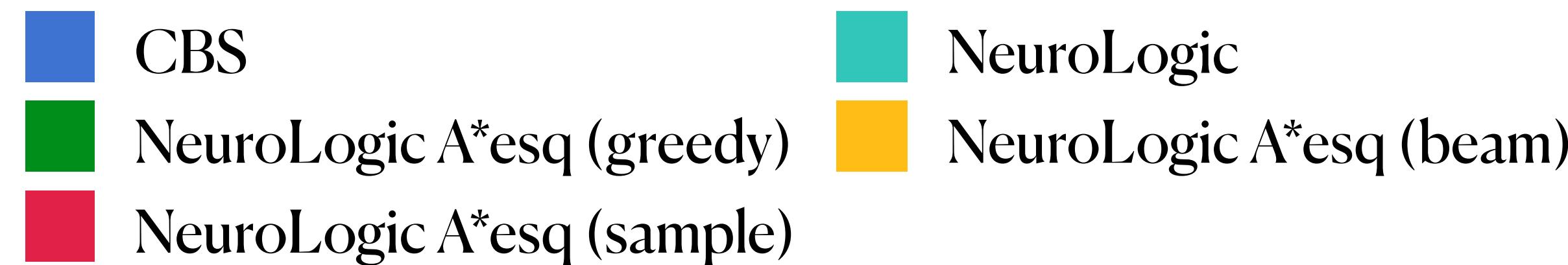


Off-the-shelf GPT-2

Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2

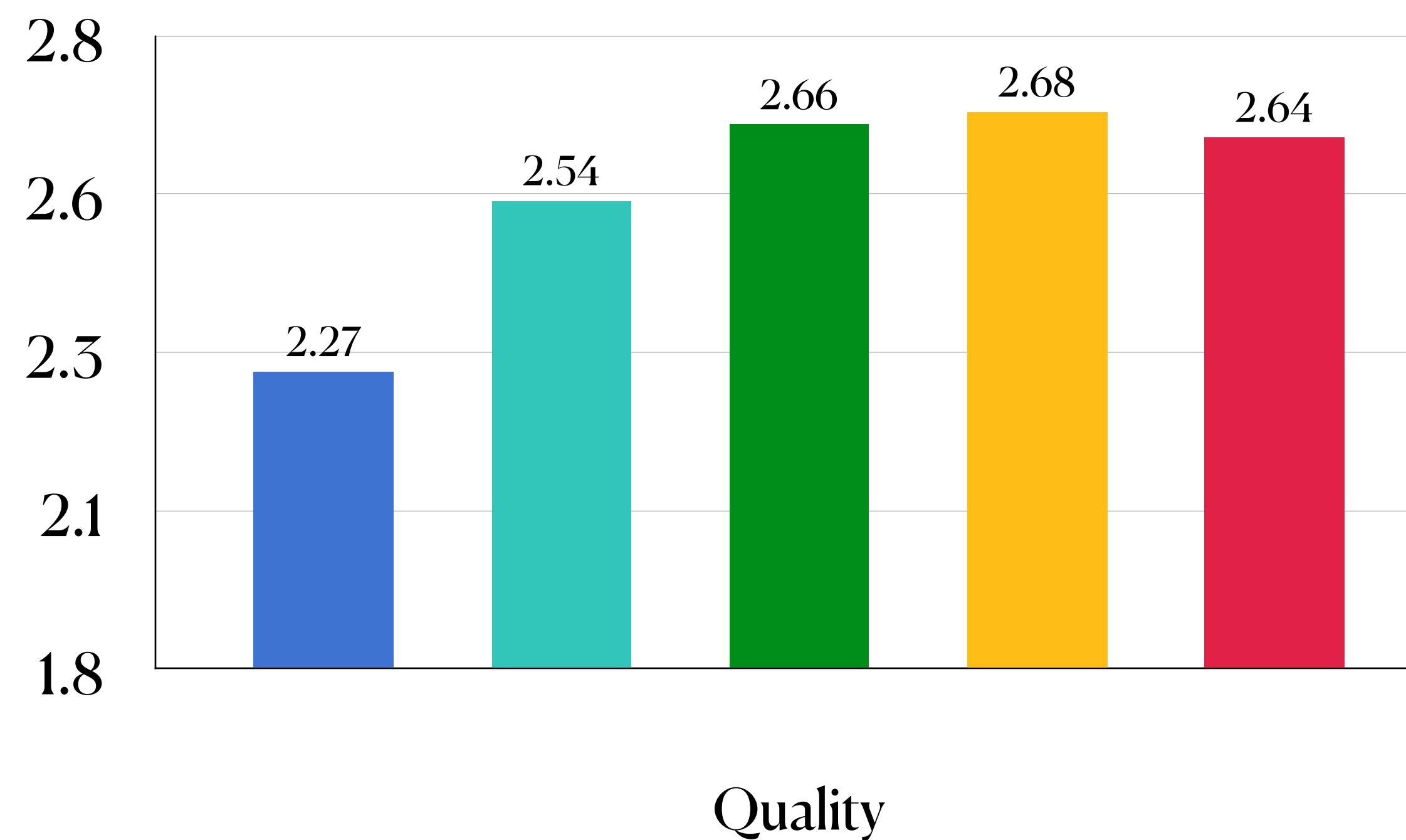
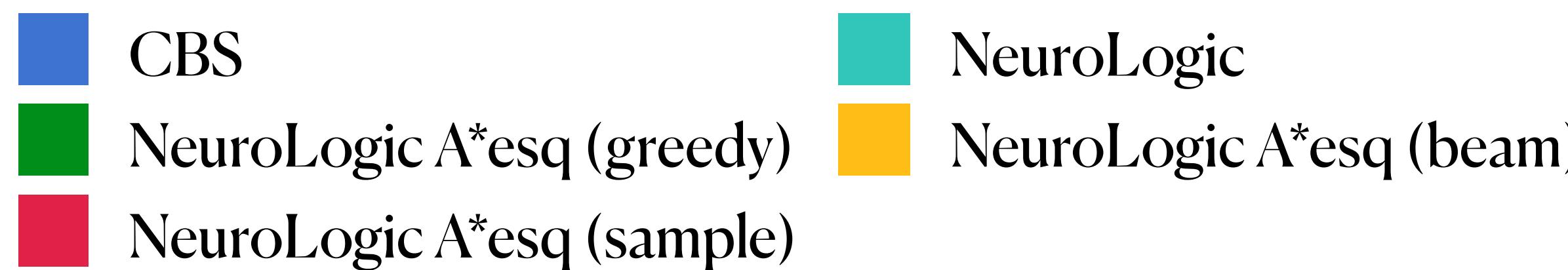


Off-the-shelf GPT-2

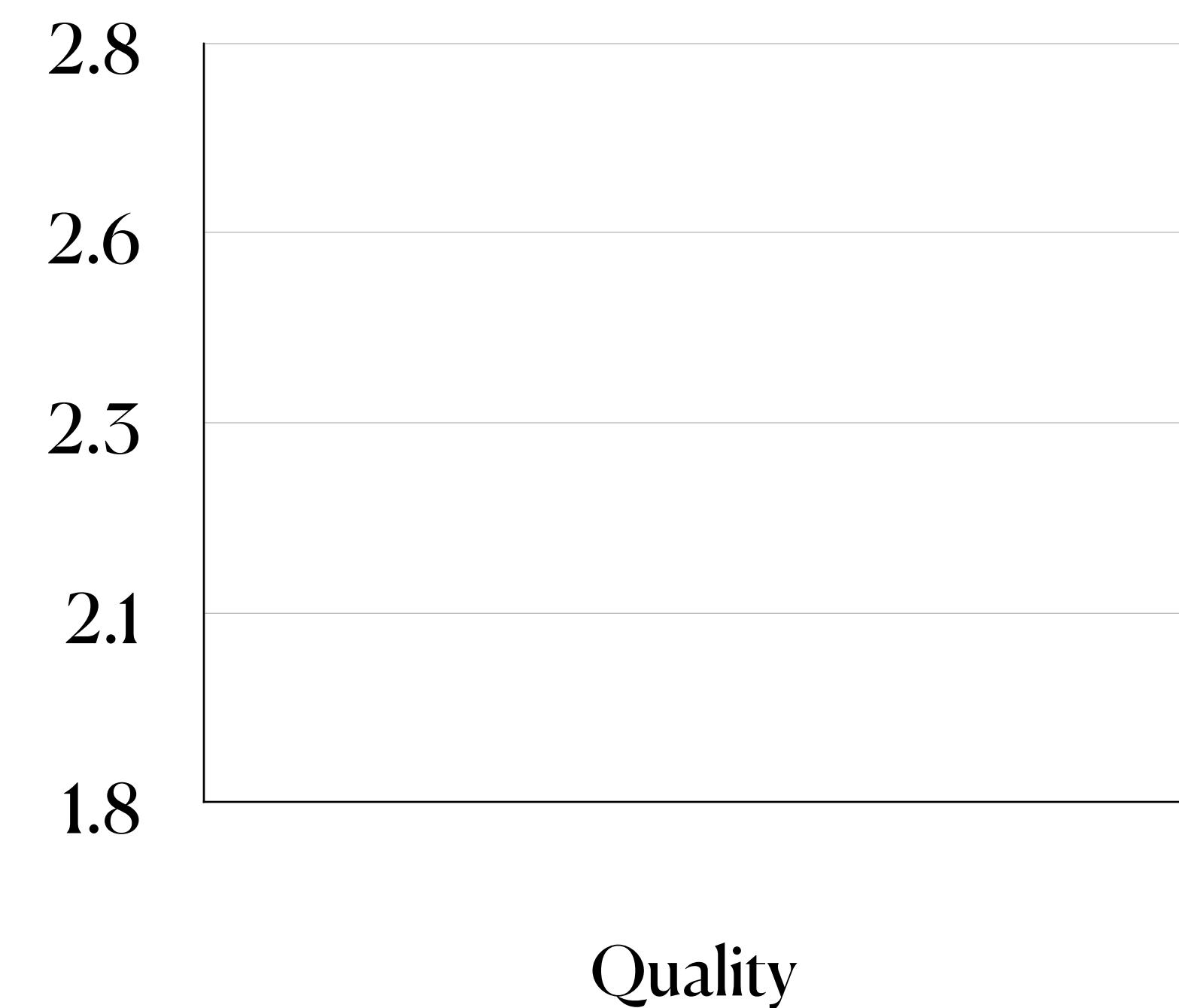
Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2



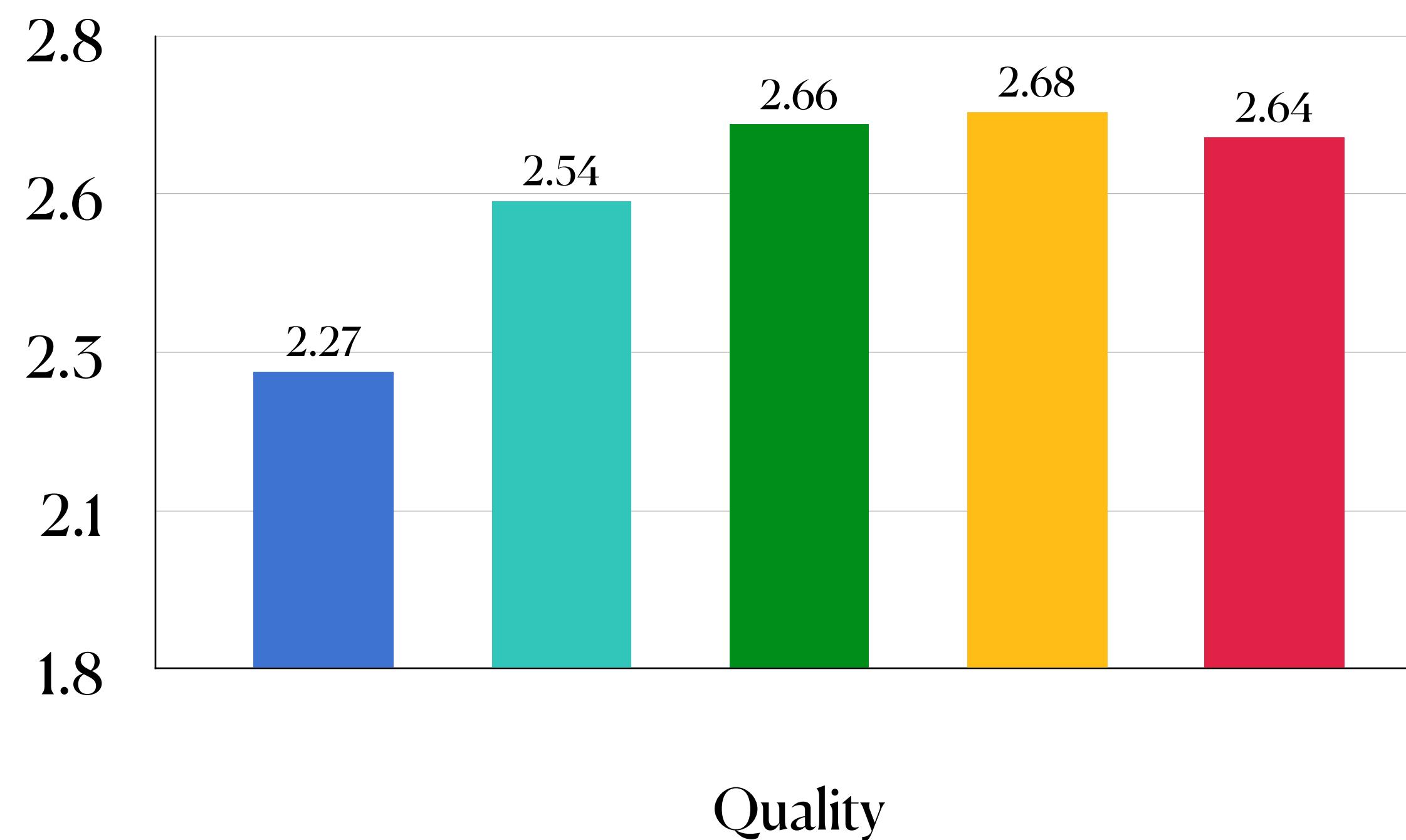
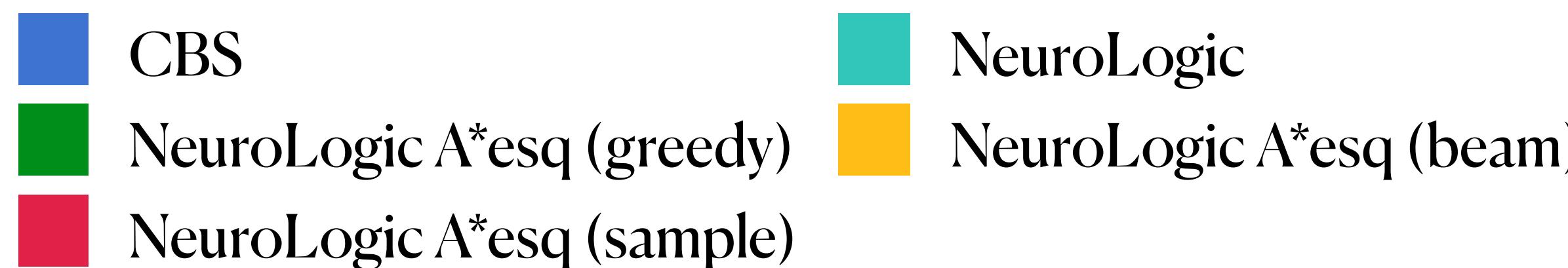
Off-the-shelf GPT-2



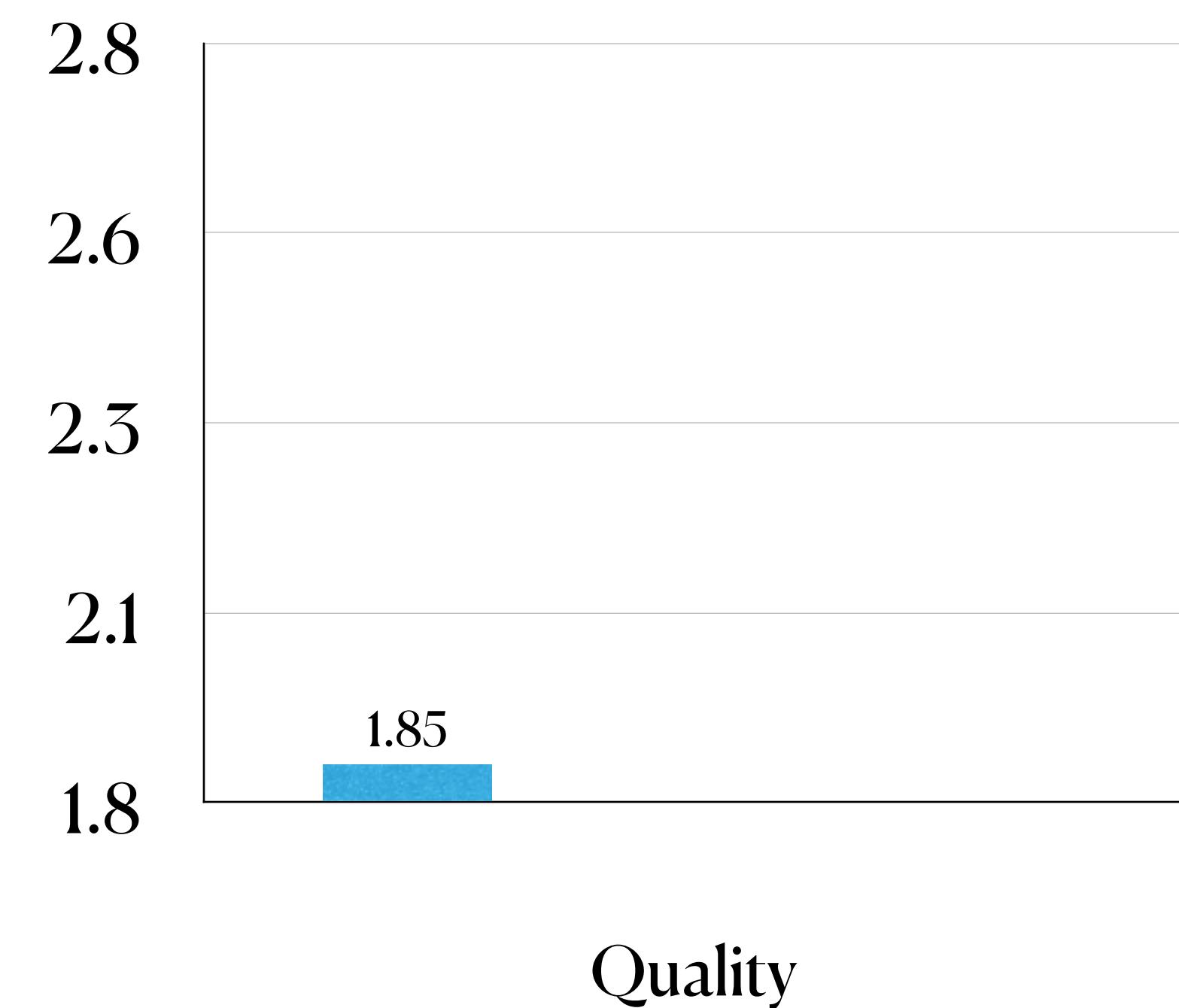
Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2



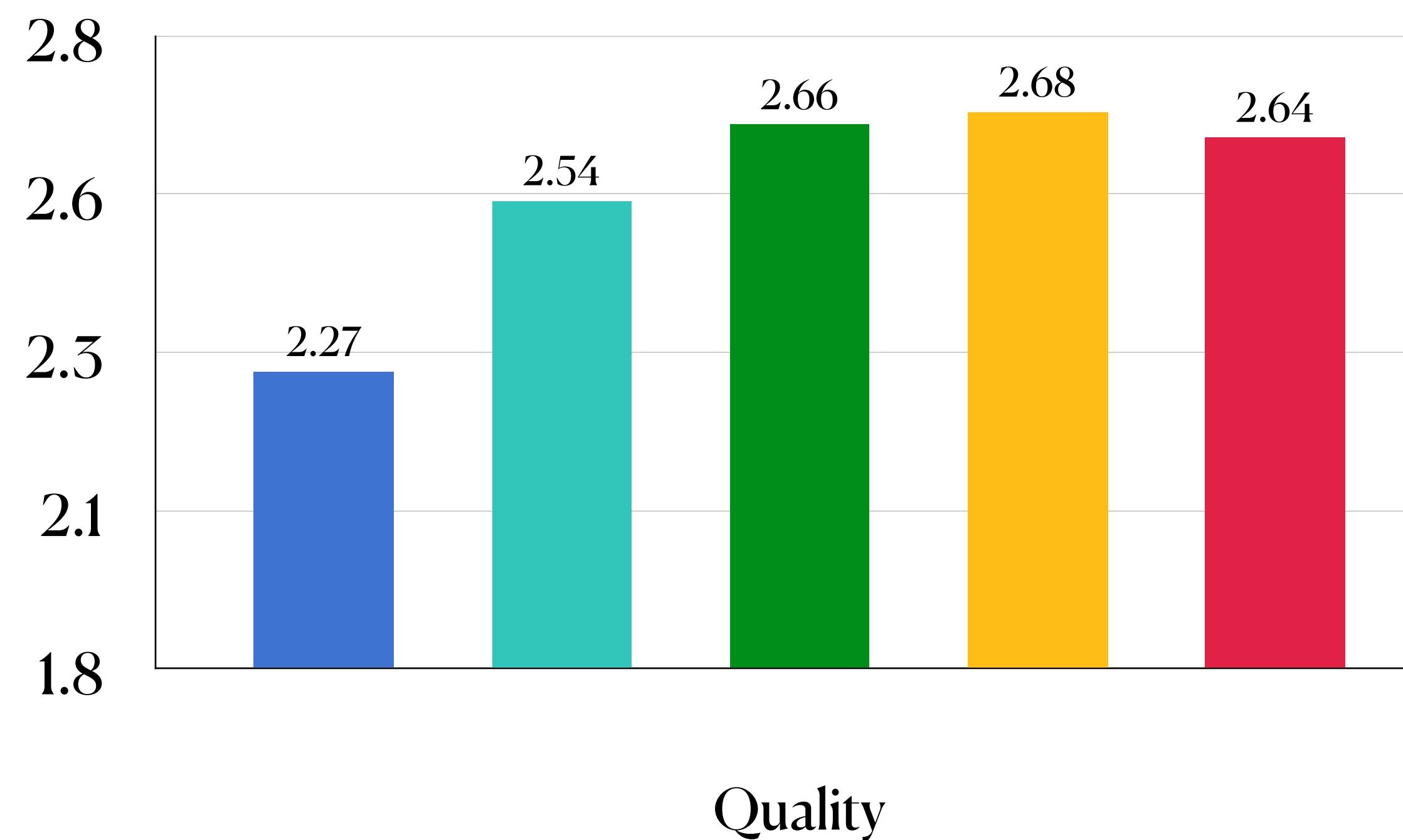
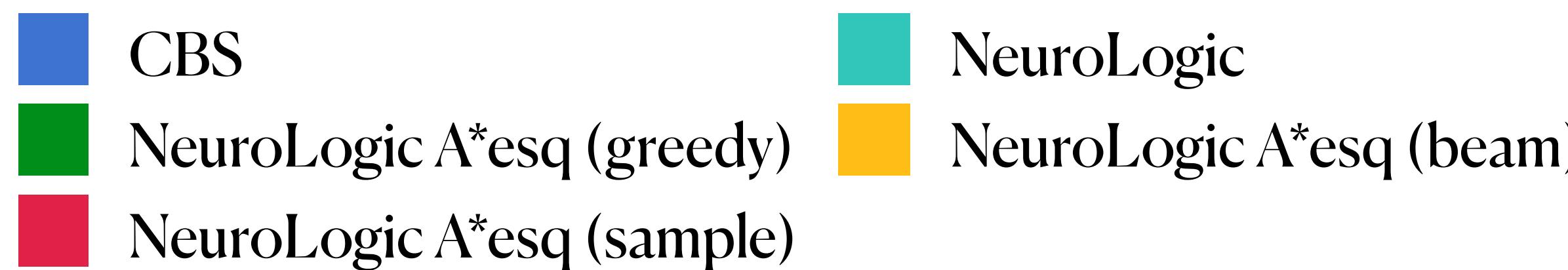
Off-the-shelf GPT-2



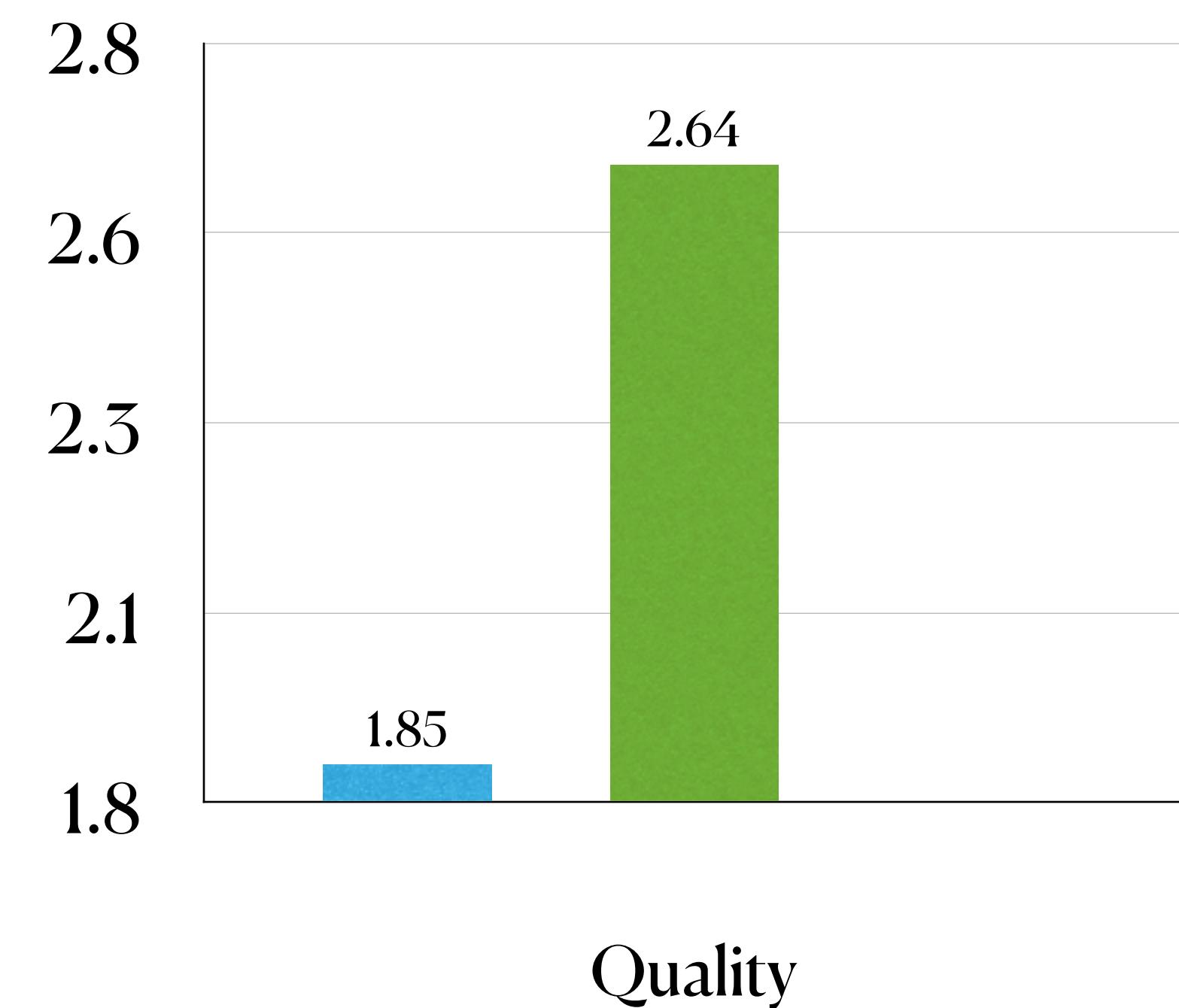
Human evaluation | CommonGen

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Fine-tuned GPT-2



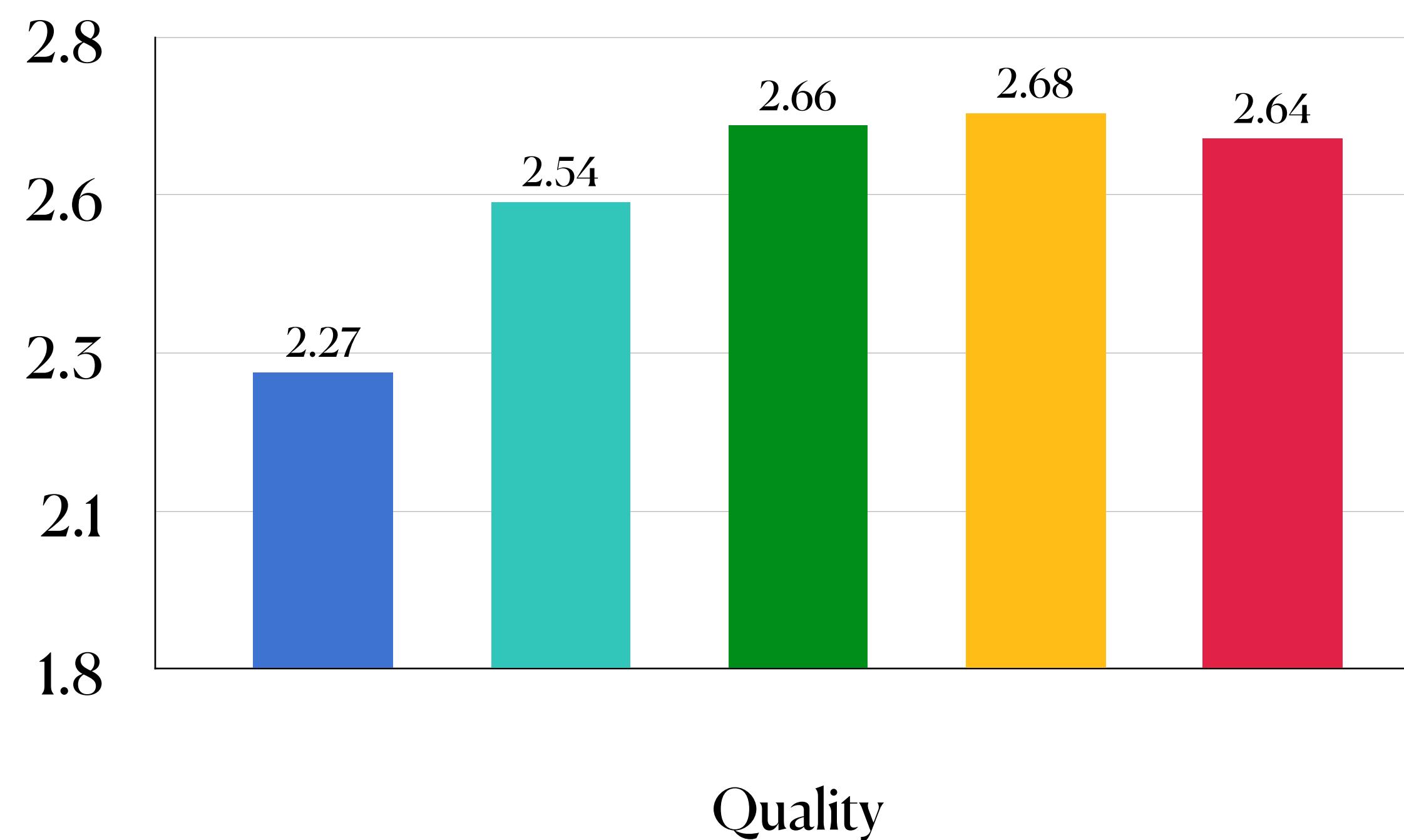
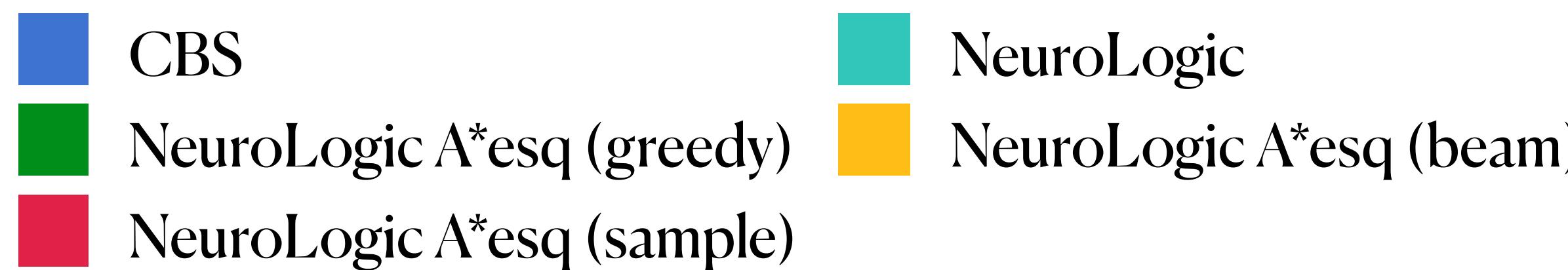
Off-the-shelf GPT-2



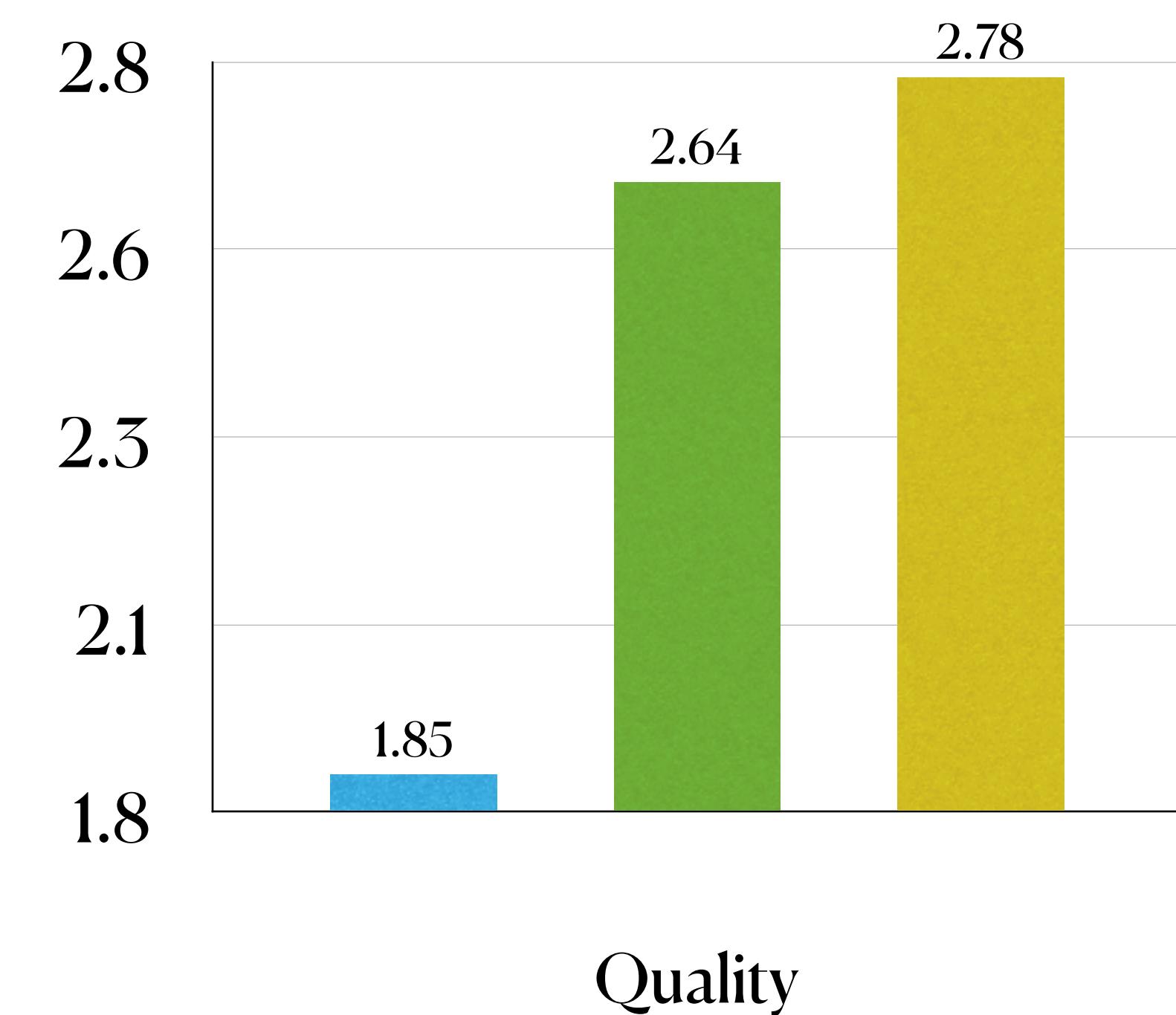
Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2



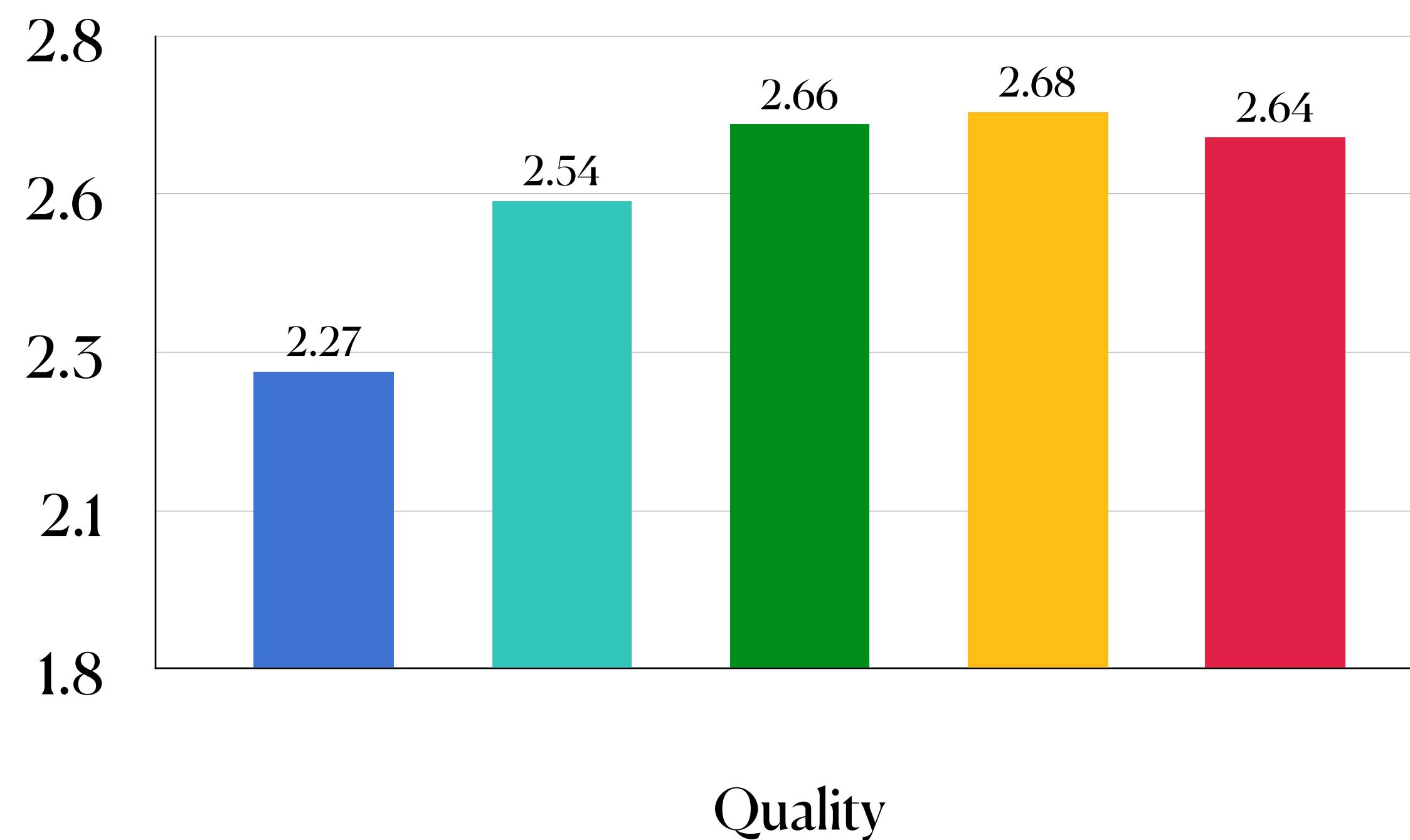
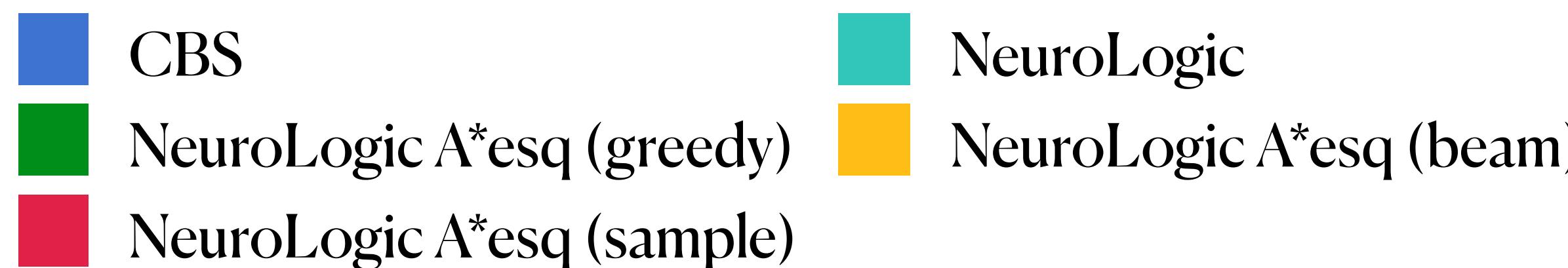
Off-the-shelf GPT-2



Human evaluation | CommonGen

(Lin et al., 2020)

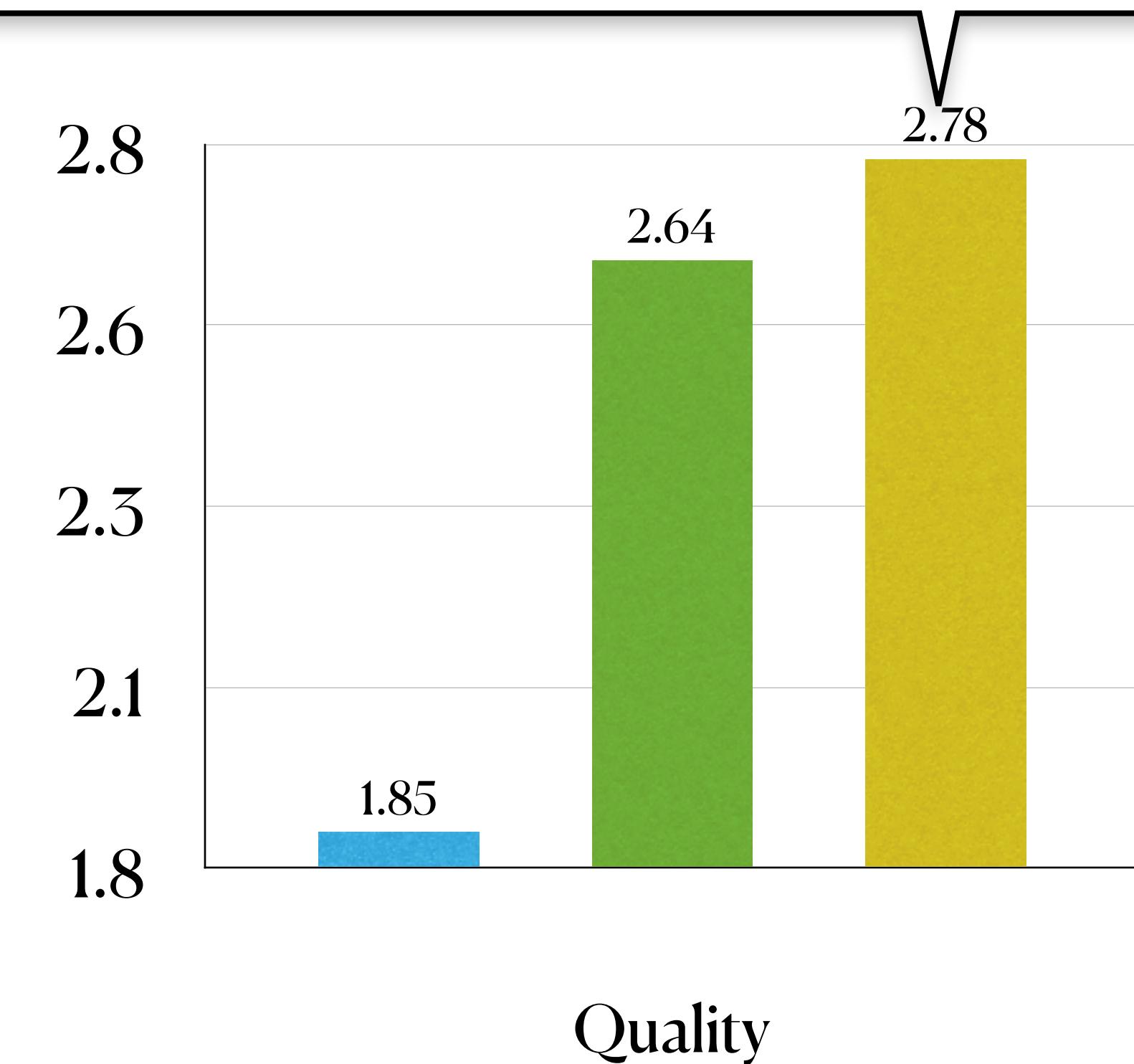
Fine-tuned GPT-2



Off-the-shelf GPT-2



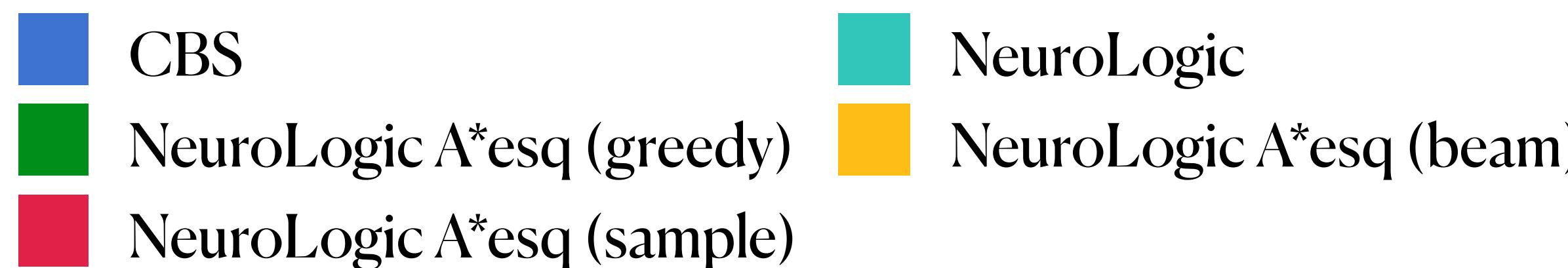
Off-the-shelf A* outperforms all fine-tuned methods



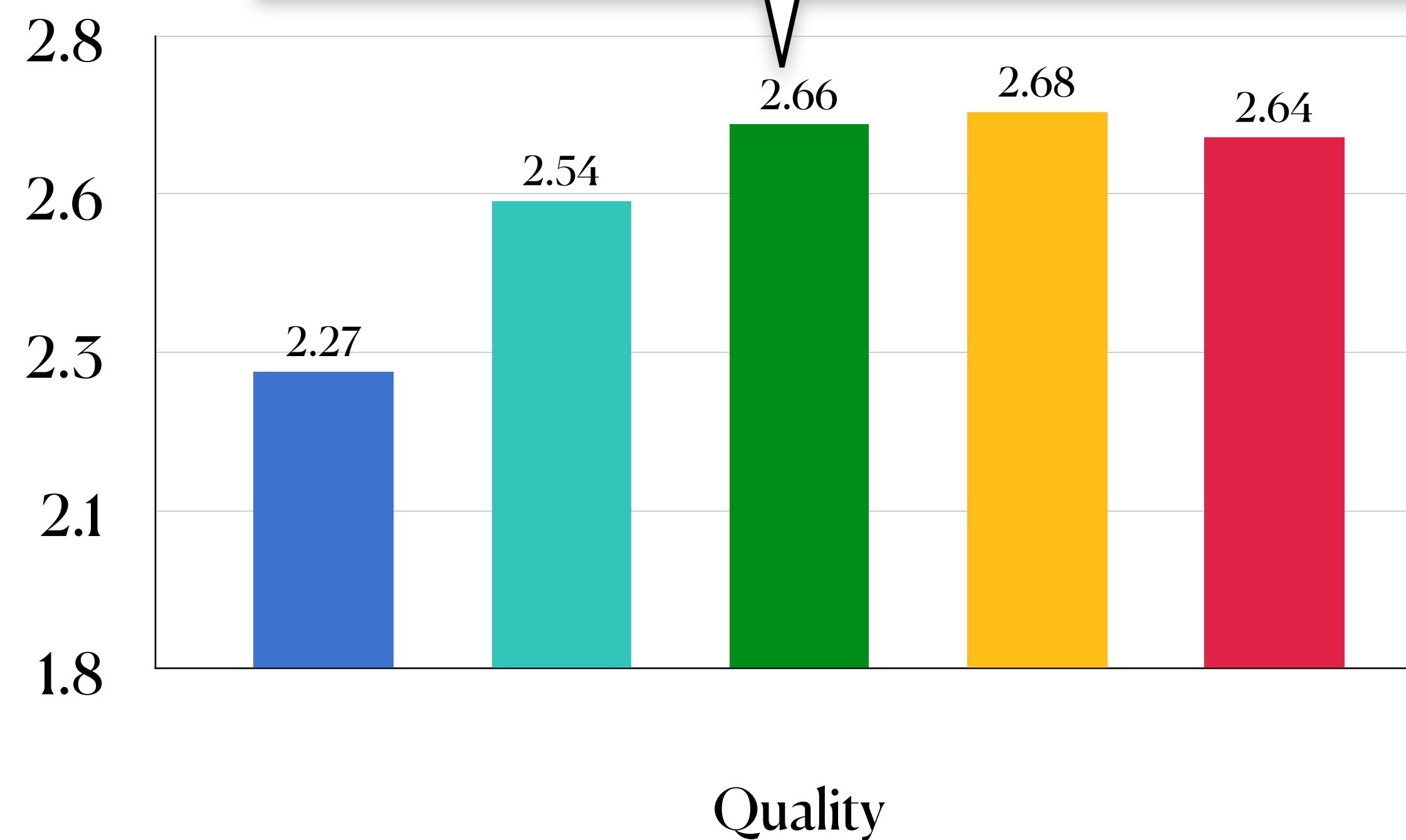
Human evaluation | CommonGen

(Lin et al., 2020)

Fine-tuned GPT-2



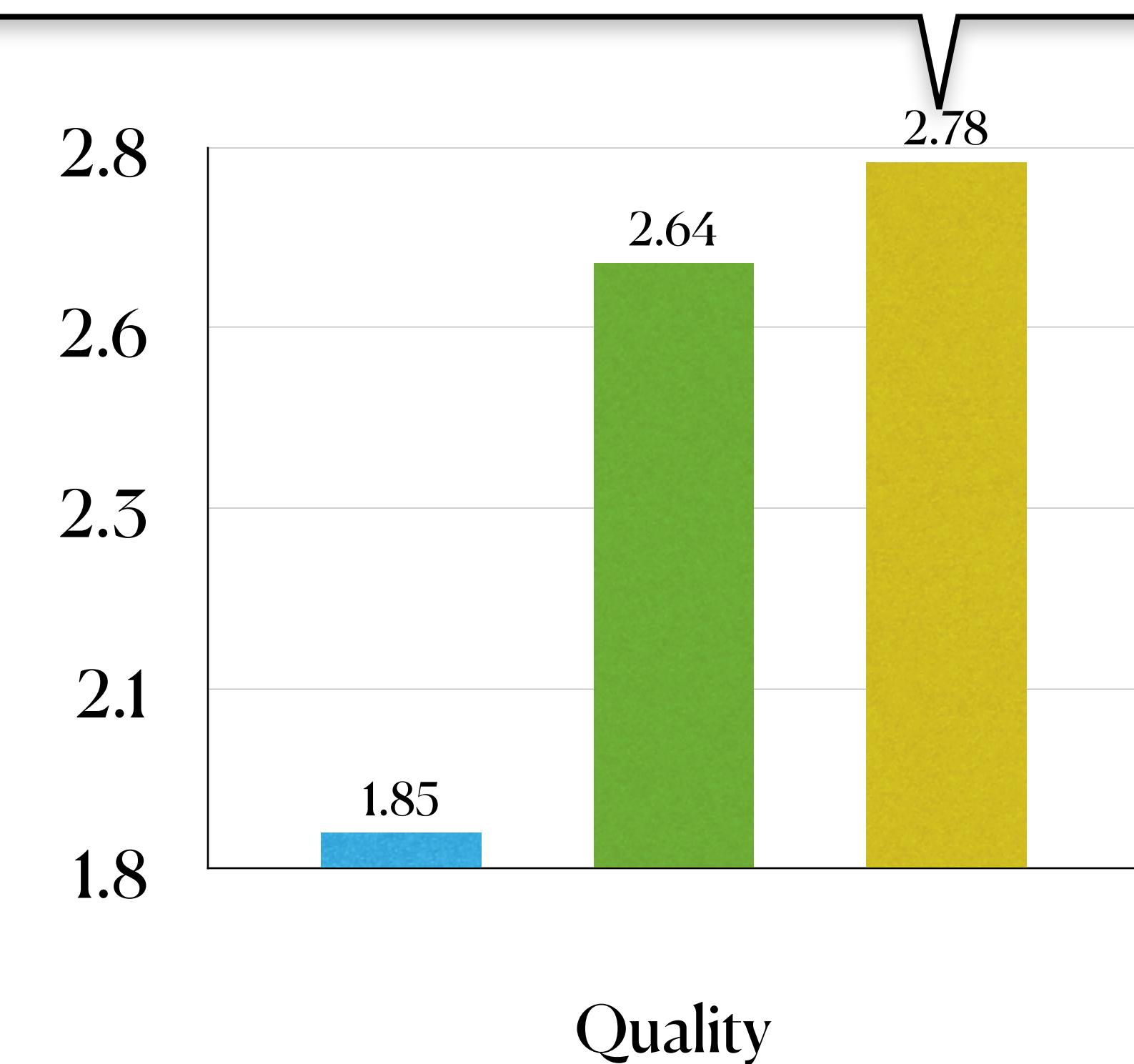
A* NeuroLogic with greedy lookahead:
efficient & performant



Off-the-shelf GPT-2



Off-the-shelf A* outperforms all fine-tuned methods



Enables many constrained generation tasks

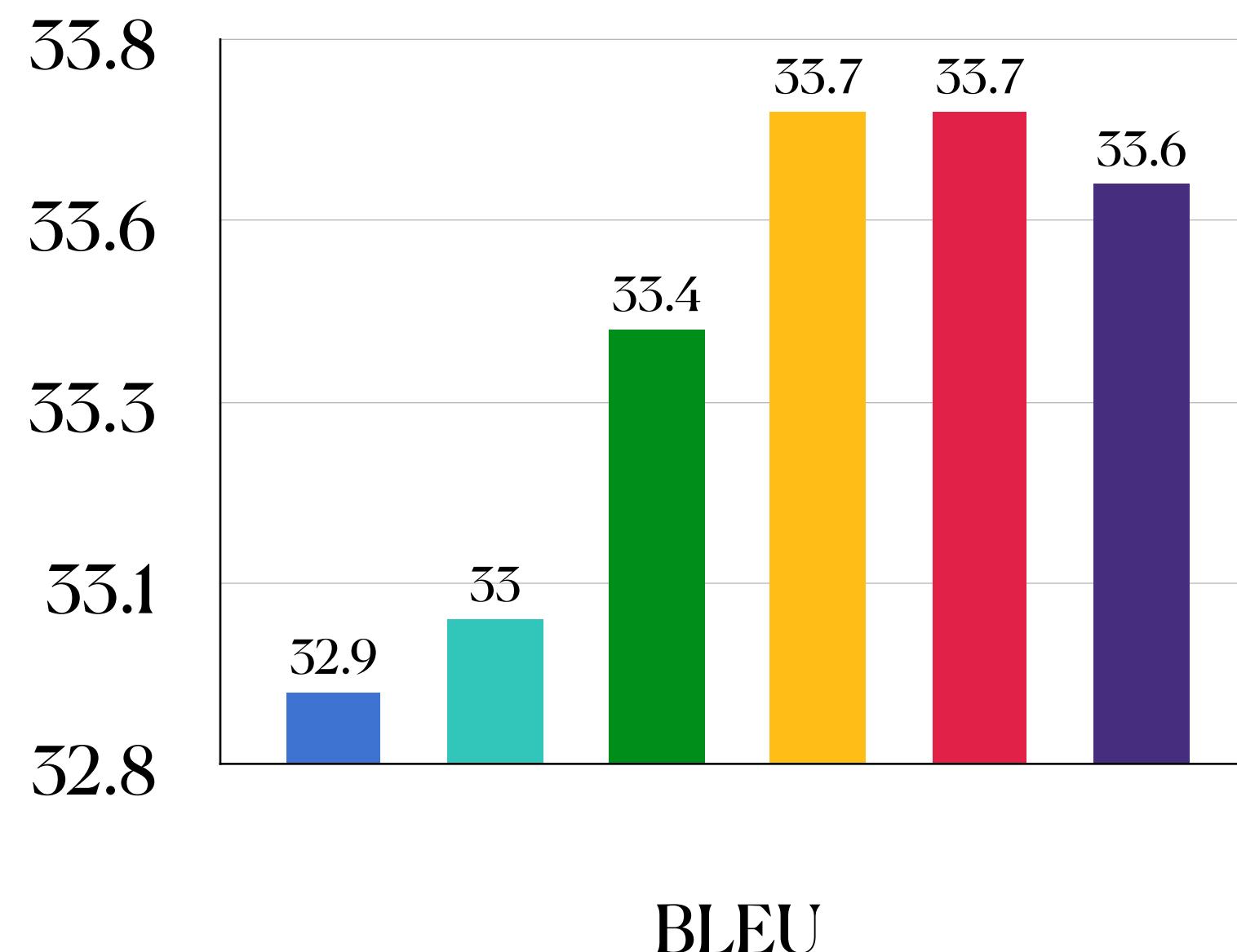


Enables many constrained generation tasks

Constrained MT

(Dinu et al., 2019)

- MarianMT
- Post and Vilar (2018)
- NeuroLogic
- NeuroLogic A*esq (greedy)
- NeuroLogic A*esq (beam)
- NeuroLogic A*esq (sample)

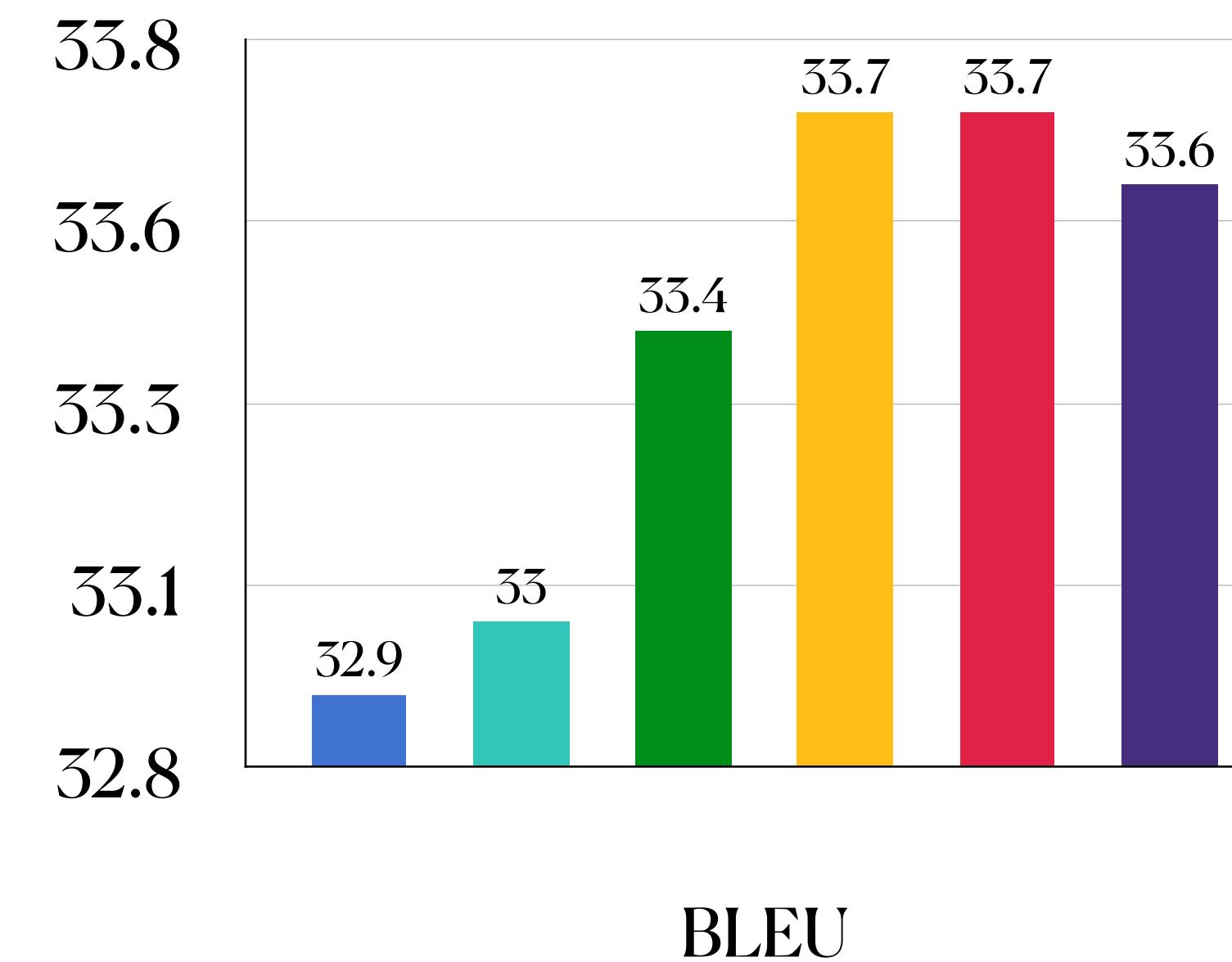


Enables many constrained generation tasks

Constrained MT

(Dinu et al., 2019)

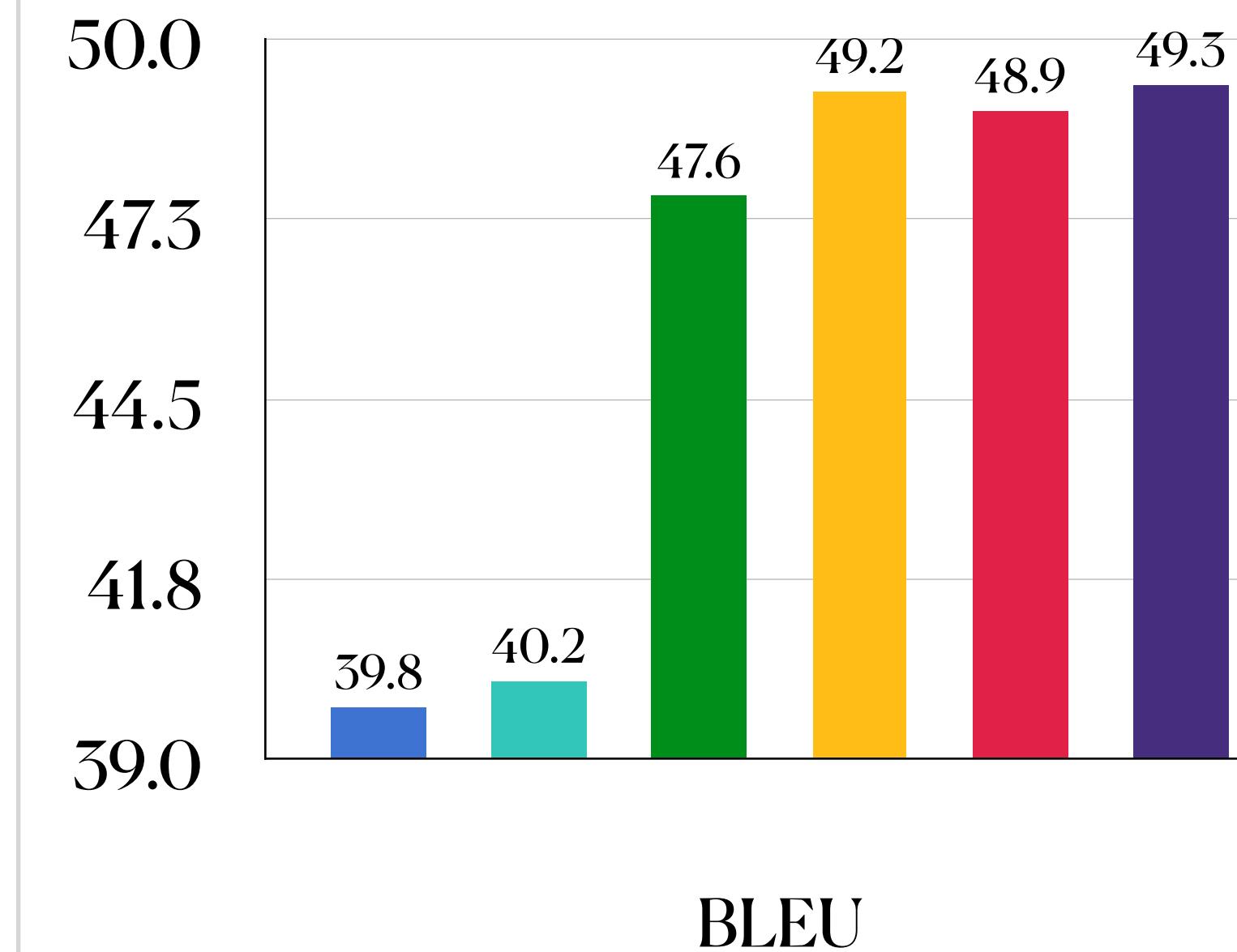
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- NeuroLogic A*esq (sample)



Few-Shot E2ENLG

(Chen et al., 2020)

- KGPT-Graph
- KGPT-Seq
- NeuroLogic
- NeuroLogic A*esq (greedy)
- NeuroLogic A*esq (beam)
- NeuroLogic A*esq (sample)

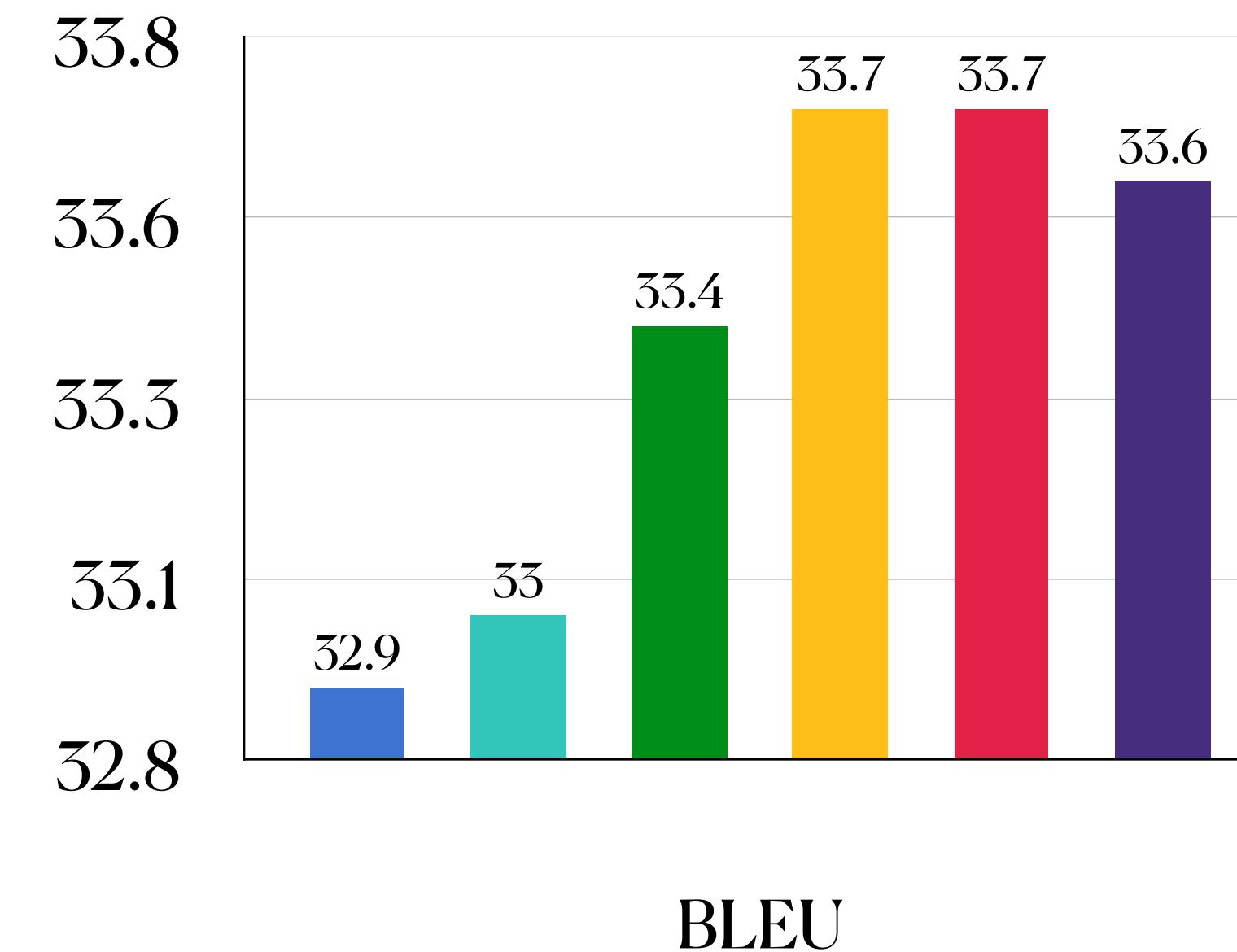


Enables many constrained generation tasks

Constrained MT

(Dinu et al., 2019)

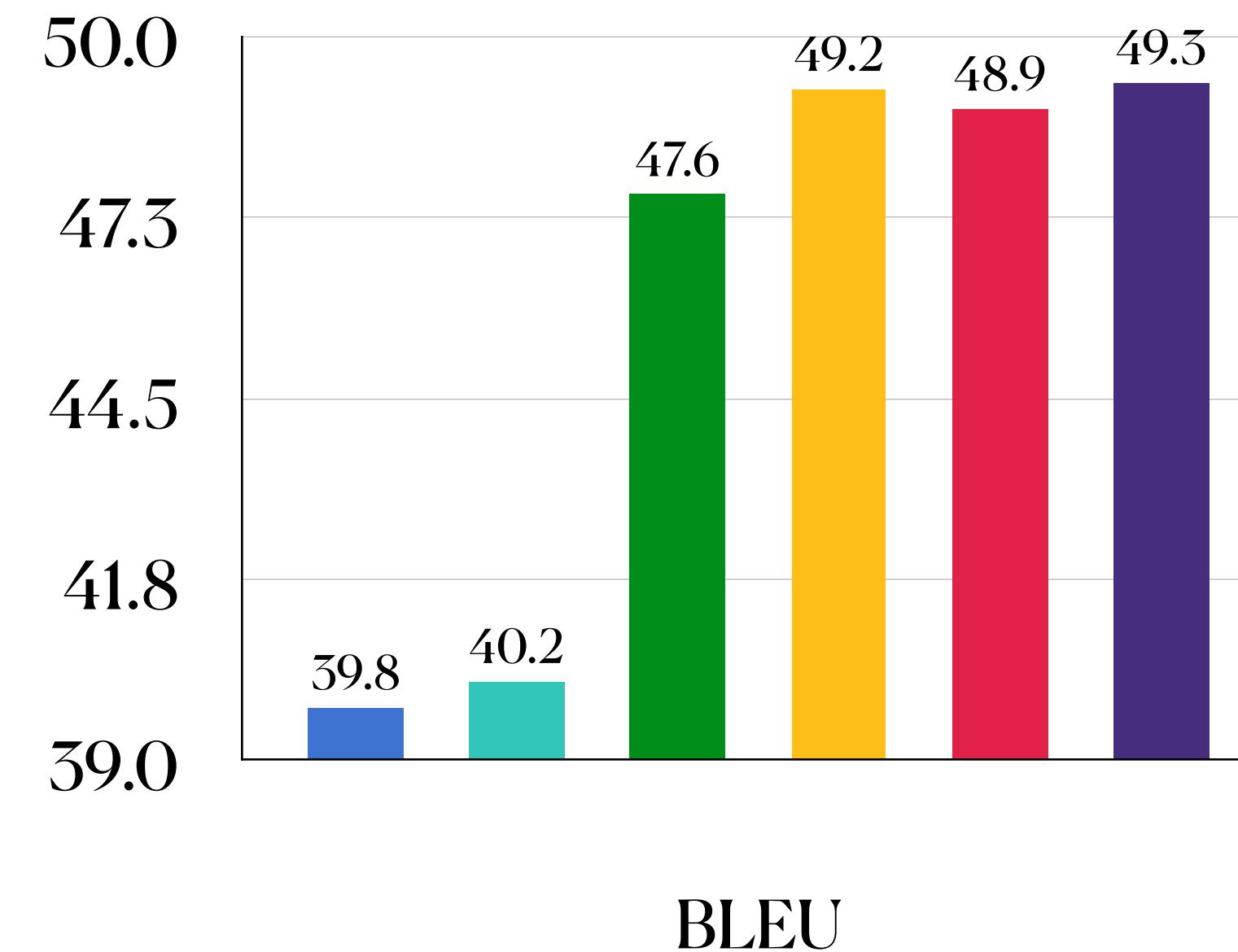
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Few-Shot E2ENLG

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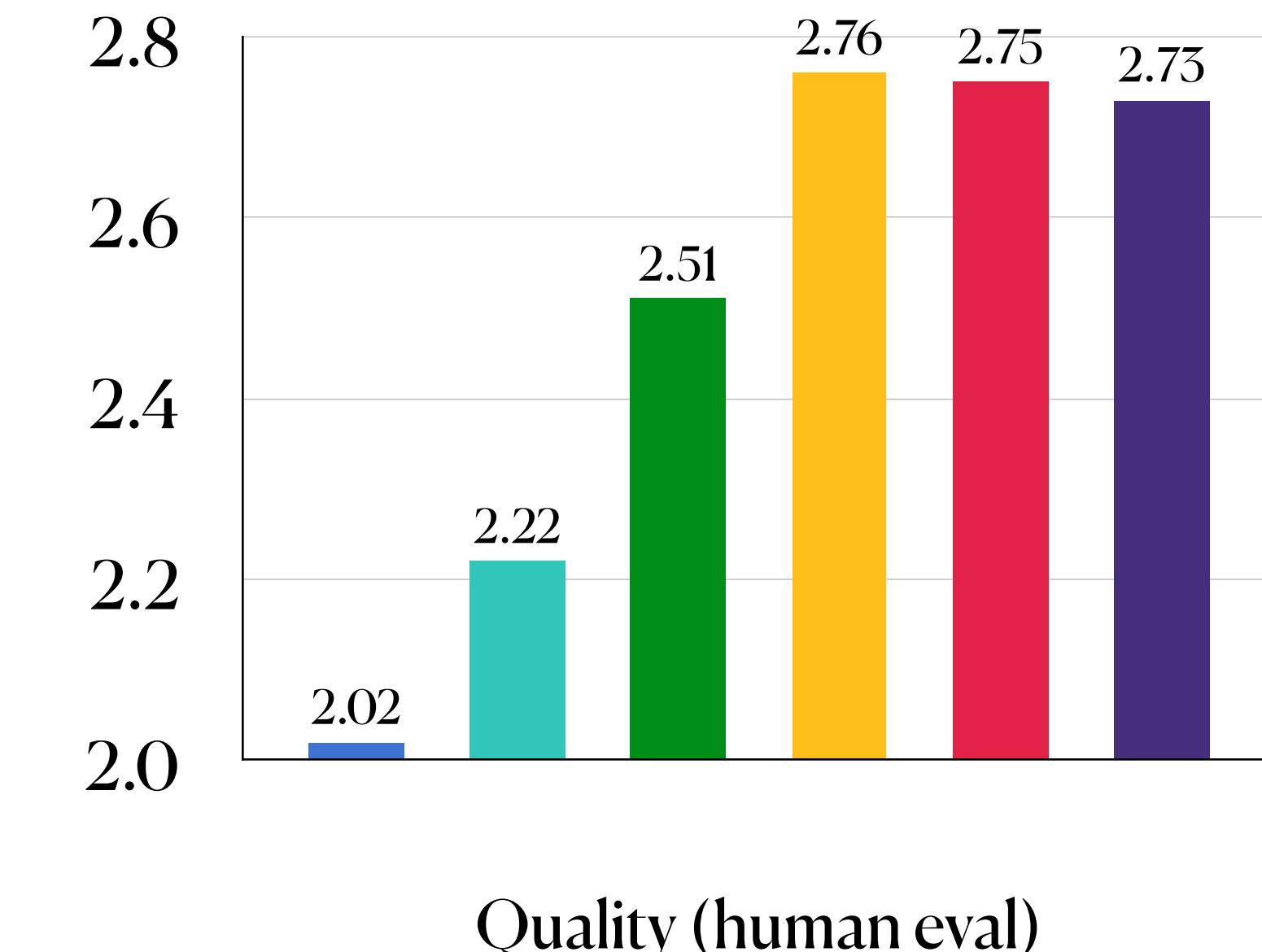
- KGPT-Graph
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- NeuroLogic A*esq (greedy)
- NeuroLogic A*esq (beam)
- NeuroLogic A*esq (sample)



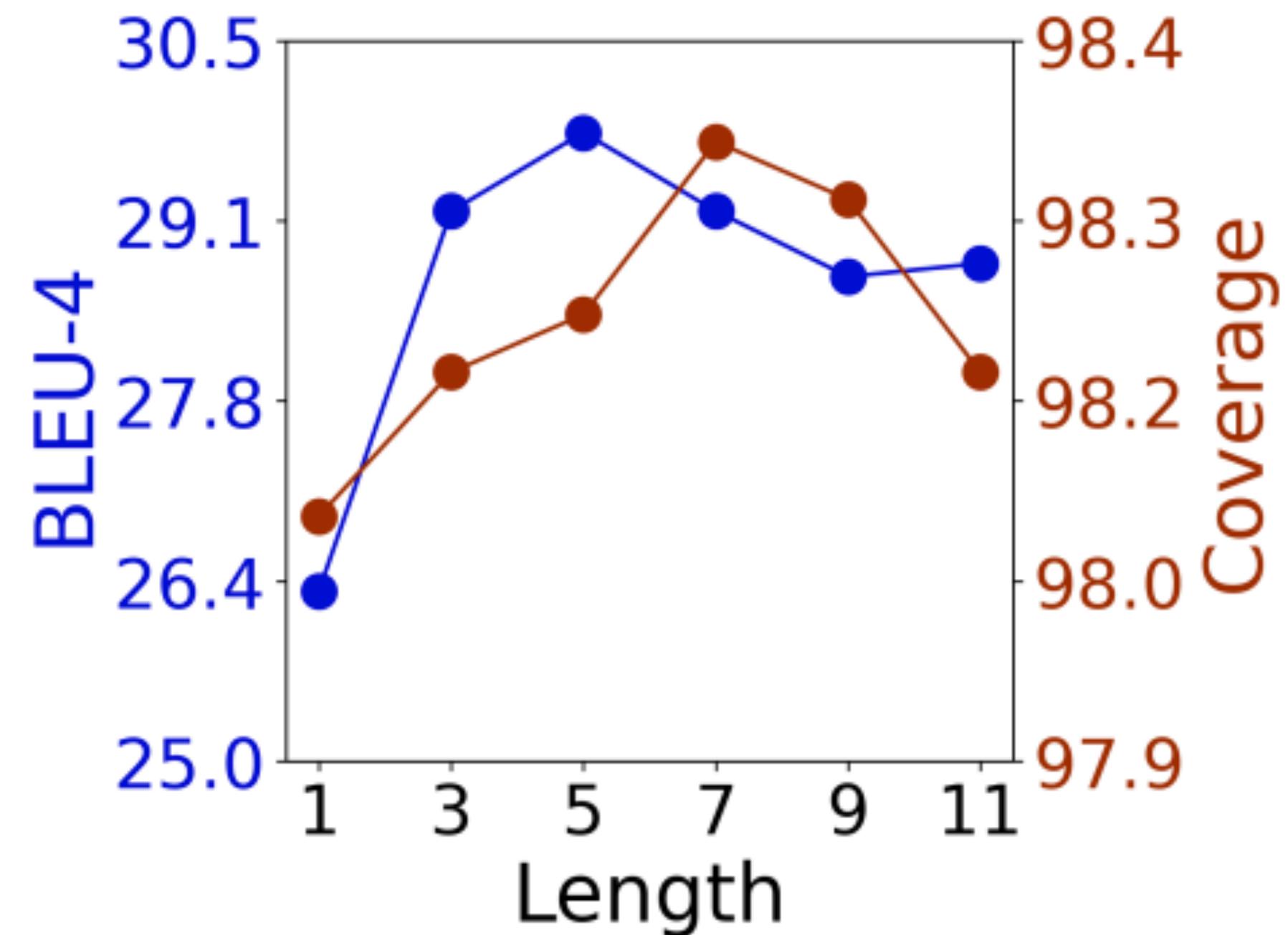
Question Generation

(Zhang et al., 2020)

- CGMH
- TSMH
- NeuroLogic
- NeuroLogic A*esq (greedy)
- NeuroLogic A*esq (beam)
- NeuroLogic A*esq (sample)



- Greedy lookahead length (CommonGen)



- Improves at varying amounts of training data

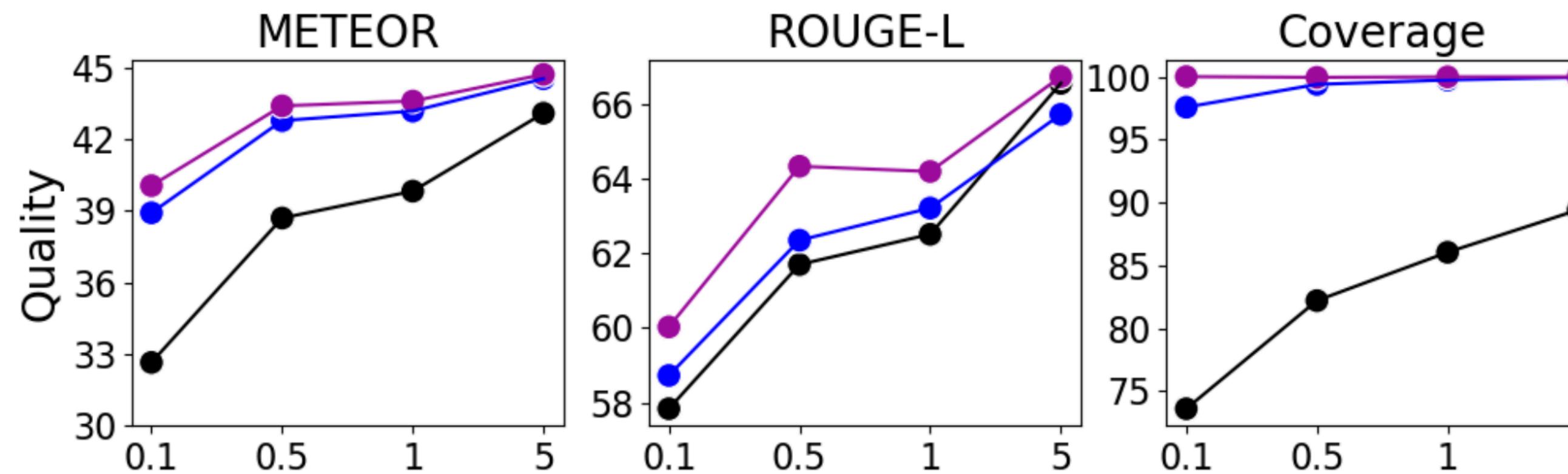
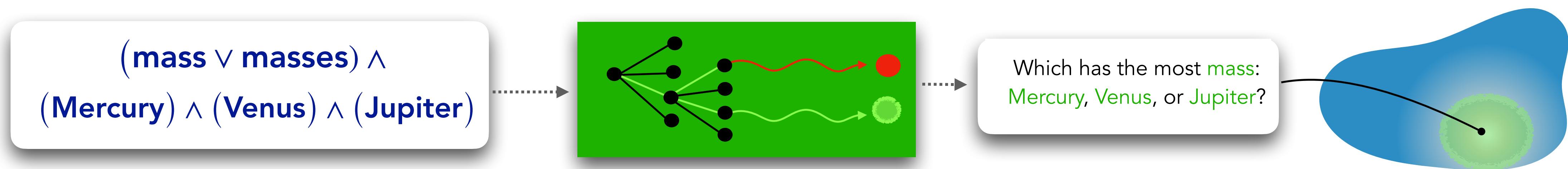


Figure 3: Performance (y-axis) of supervised GPT-2 on E2ENLG, with a varying amount of training data for supervision (x-axis). The **purple**, **blue**, and **black** line denote decoding with NEUROLOGIC★, NEUROLOGIC and conventional beam search respectively.

Constrained generation through *discrete* inference

A* Neurologic

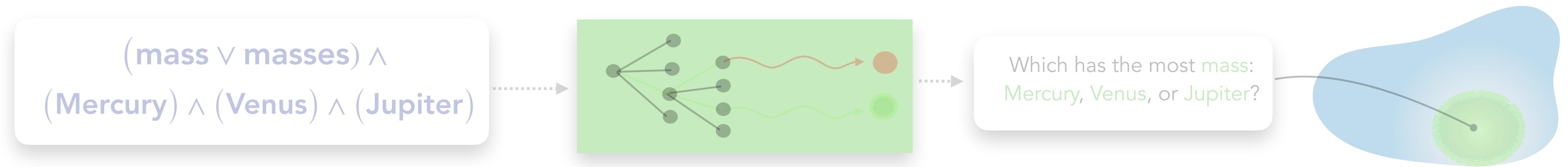
- **Constraints:** expressive class of lexical constraints
- **Search:** discrete with future approximation
- **Enables:** constraints without fine-tuning, better fine-tuned performance



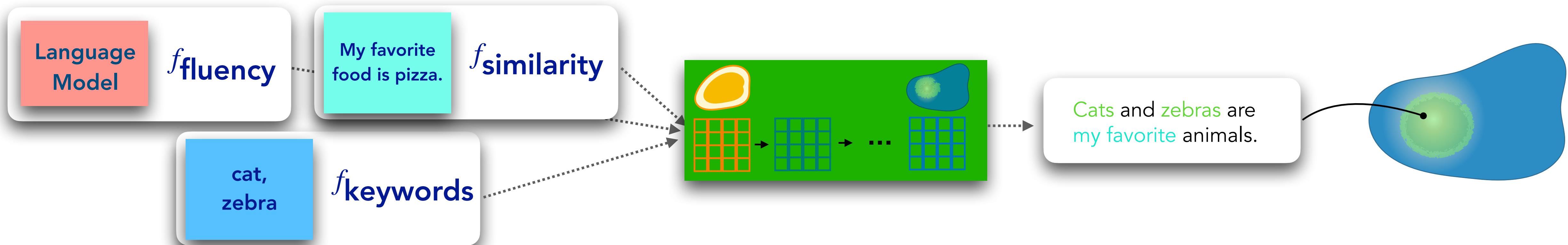
**NeuroLogic A*esque Decoding:
Constrained Text Generation with Lookahead Heuristics**
[arxiv:2112.08726](https://arxiv.org/abs/2112.08726)
[github.com/GloriaXimingLu/star neurologic](https://github.com/GloriaXimingLu/star_neurologic)

Constrained generation through inference

- Today: algorithms for constrained generation from two perspectives
 - **Logical lexical constraints** enforced through **discrete inference**



- **Differentiable constraints** enforced through **continuous inference**



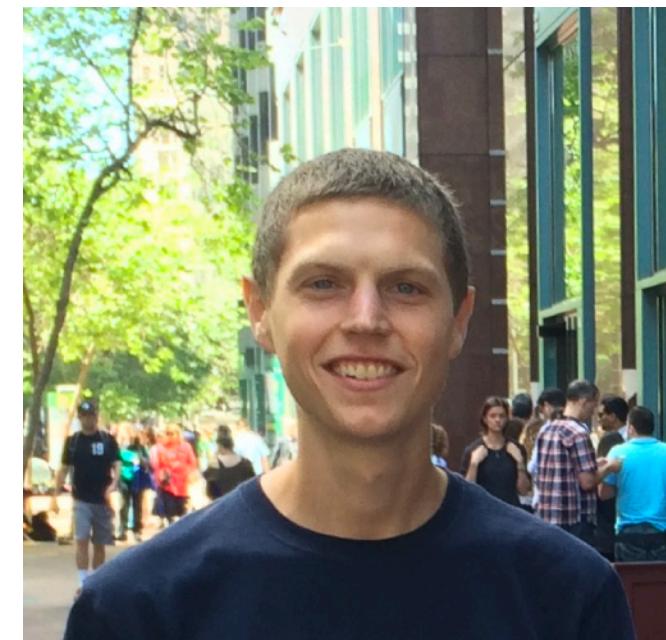
Constrained generation through *continuous* inference

COLD Decoding:
Constrained Decoding with Langevin Dynamics

In Submission, [arxiv:2202.11705](https://arxiv.org/abs/2202.11705)



Lianhui Qin



Sean Welleck



Daniel Khashabi

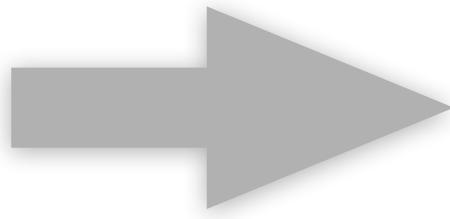


Yejin Choi

Lexically Constrained Generation

Keywords

{ mass, Mercury, Jupiter }



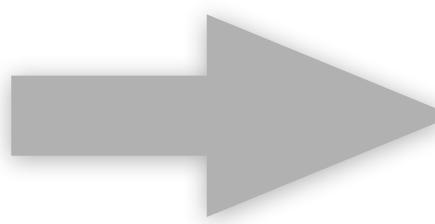
Generation

Jupiter has more mass than
Mercury.

Lexically Constrained Generation

Keywords

{ mass, Mercury, Jupiter }



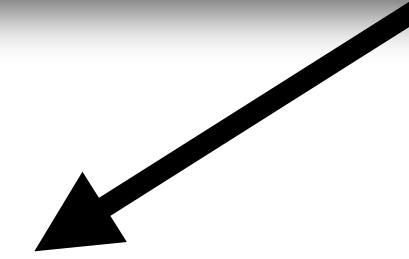
Generation

Jupiter has more mass than
Mercury.

Constraints:

Language
Model

$f_{fluency}(y)$

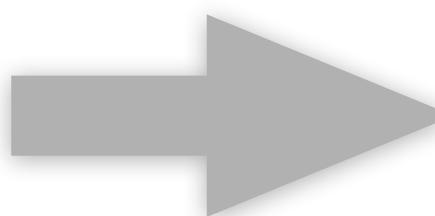


Fluency constraint

Lexically Constrained Generation

Keywords

{ mass, Mercury, Jupiter }



Generation

Jupiter has more mass than
Mercury.

Constraints:

Language
Model

$f_{fluency}(y)$

Mass,
Jupiter,
Mercury

$f_{keywords}(y)$

Fluency constraint

Task-specific constraints

Text infilling / abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

Left context

She went to practice everyday.

Text infilling / abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

Left context

She went to practice everyday.

Right context

She won a gold medal in the
Olympic marathon.

Text infilling / abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

Left context

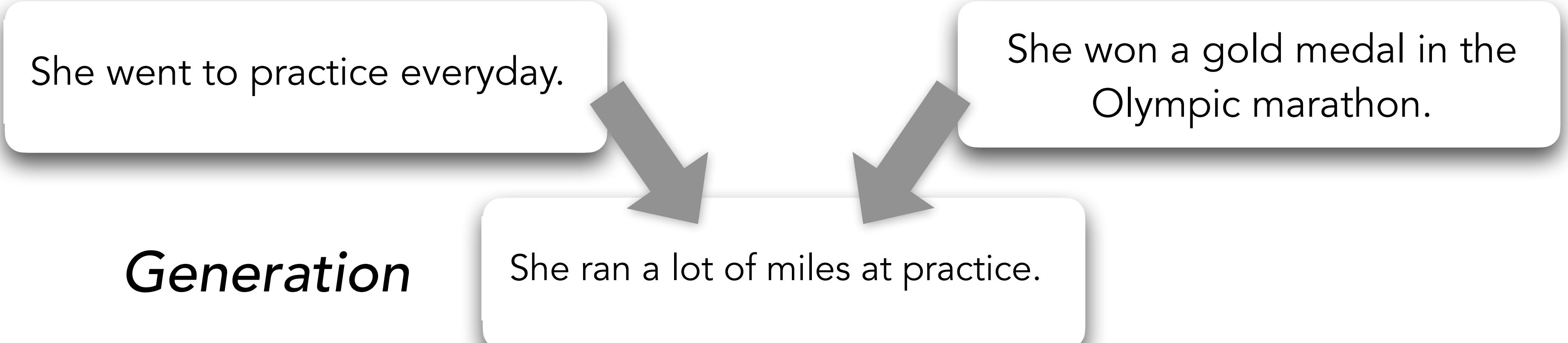
She went to practice everyday.

Right context

She won a gold medal in the
Olympic marathon.

Generation

She ran a lot of miles at practice.



Text infilling / abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

Left context

She went to practice everyday.

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She won a gold medal in the
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Generation

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Constraints:

Language
Model

$f_{fluency}(y)$

Fluency constraint

Text infilling / abductive reasoning

AbductiveNLG

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Left context

She went to practice everyday.

Right context

She won a gold medal in the
Olympic marathon.

Generation

She ran a lot of miles at practice.

Constraints:

Language
Model

$f_{fluency}(y)$

She went to
practice ...

$f_{coherence-left}(y)$

Fluency constraint

Task-specific constraints

Text infilling / abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

Left context

She went to practice everyday.

Right context

She won a gold medal in the Olympic marathon.

Generation

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Constraints:

Language Model

$f_{fluency}(y)$

She went to practice ...

$f_{coherence-left}(y)$

She won a gold ...

$f_{coherence-right}(y)$

Fluency constraint

Task-specific constraints

Text similarity / counterfactual reasoning

TimeTravel

(Qin et al., 2019)

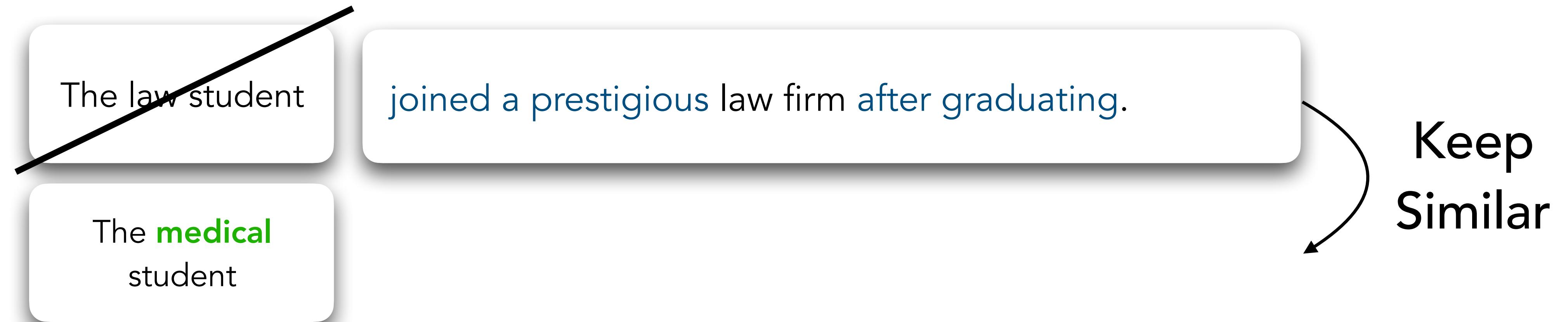
The law student

joined a prestigious law firm *after* graduating.

Text similarity / counterfactual reasoning

TimeTravel

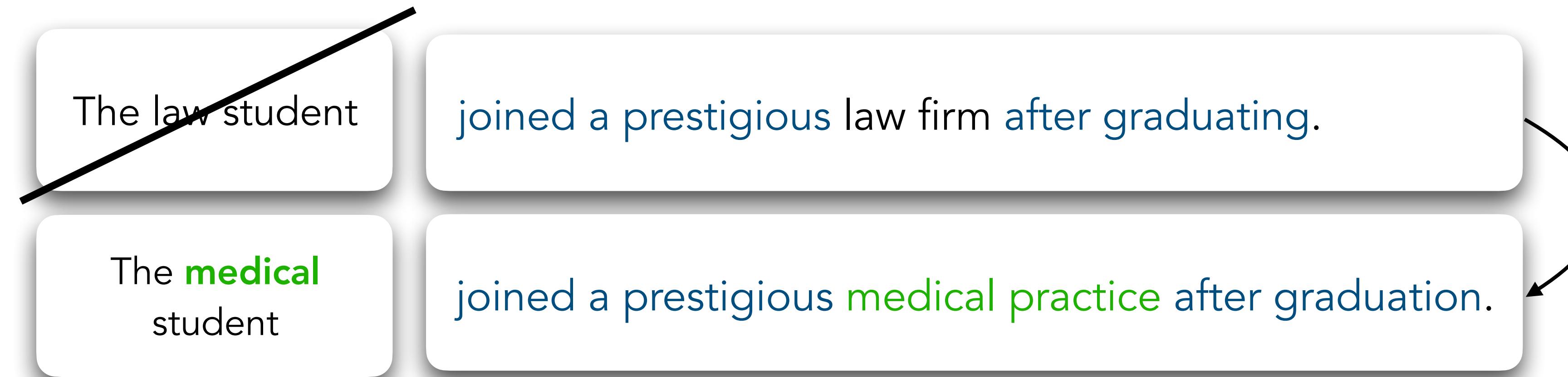
(Qin et al., 2019)



Text similarity / counterfactual reasoning

TimeTravel

(Qin et al., 2019)

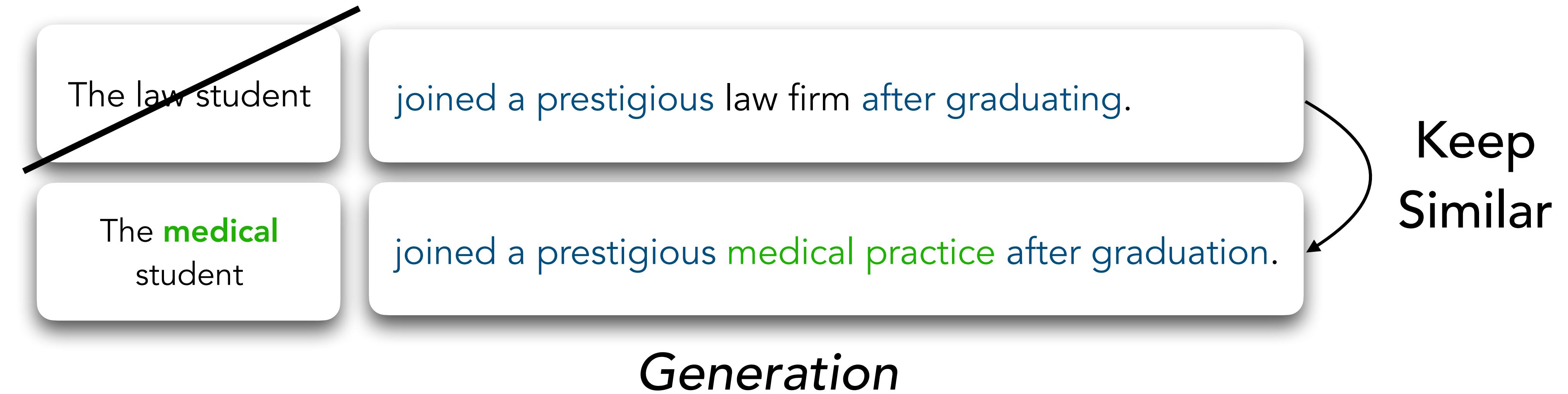


Generation

Text similarity / counterfactual reasoning

TimeTravel

(Qin et al., 2019)

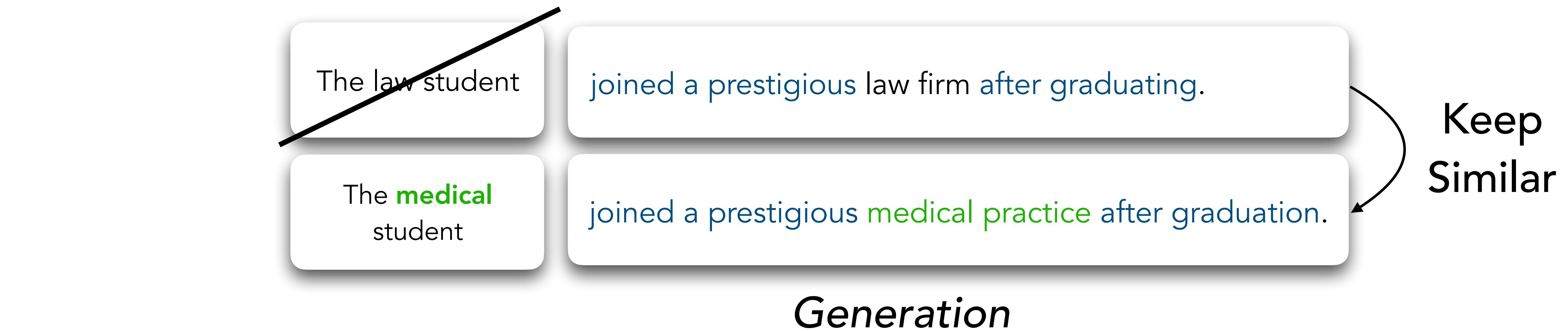


Fluency constraint

Text similarity / counterfactual reasoning

TimeTravel

(Qin et al., 2019)



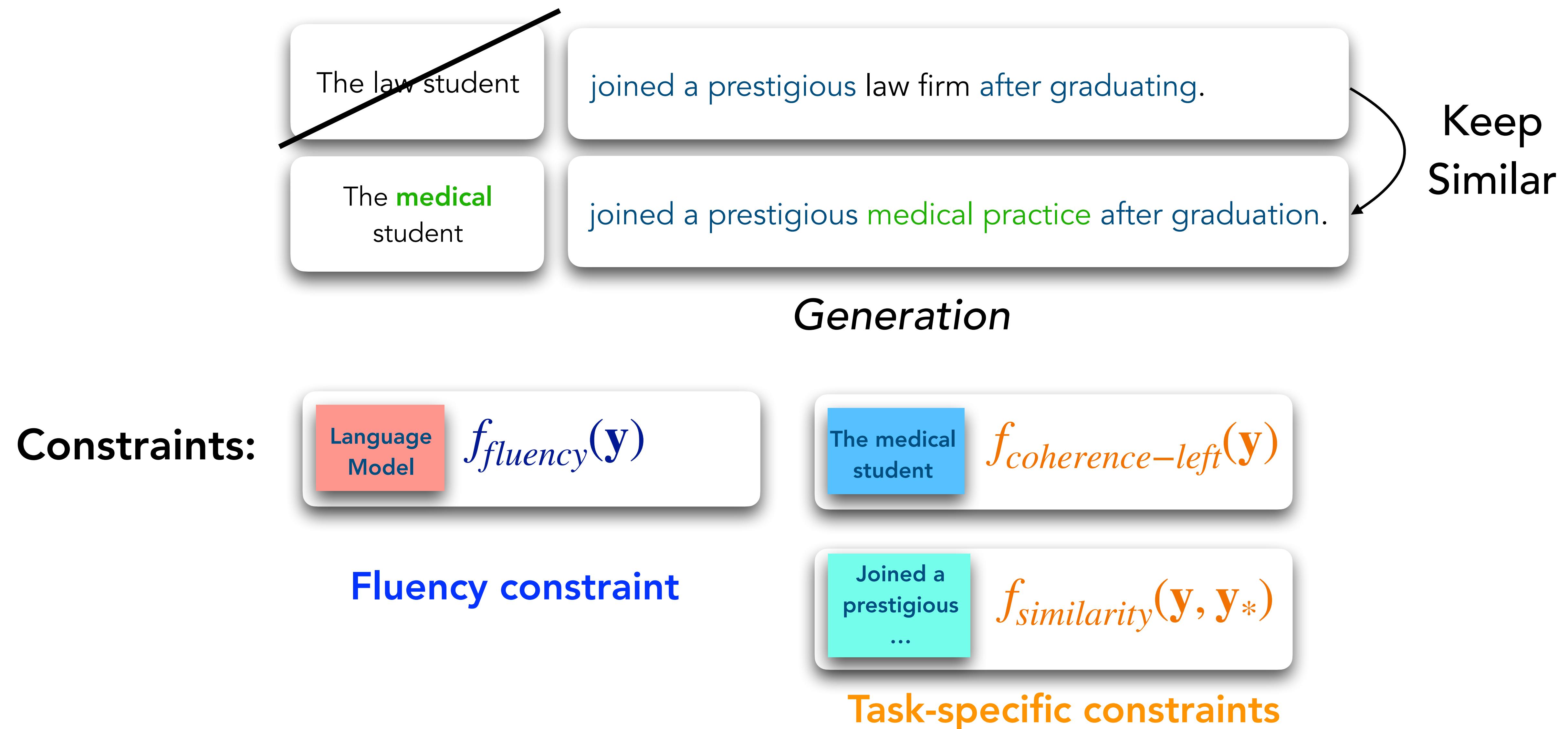
Fluency constraint

Task-specific constraints

Text similarity / counterfactual reasoning

TimeTravel

(Qin et al., 2019)

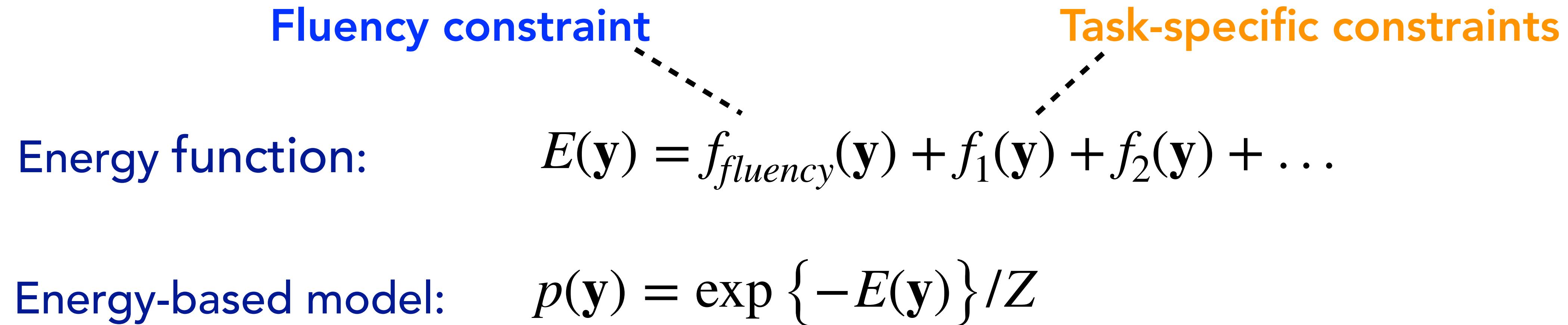


Constrained generation as sampling from an energy-based model

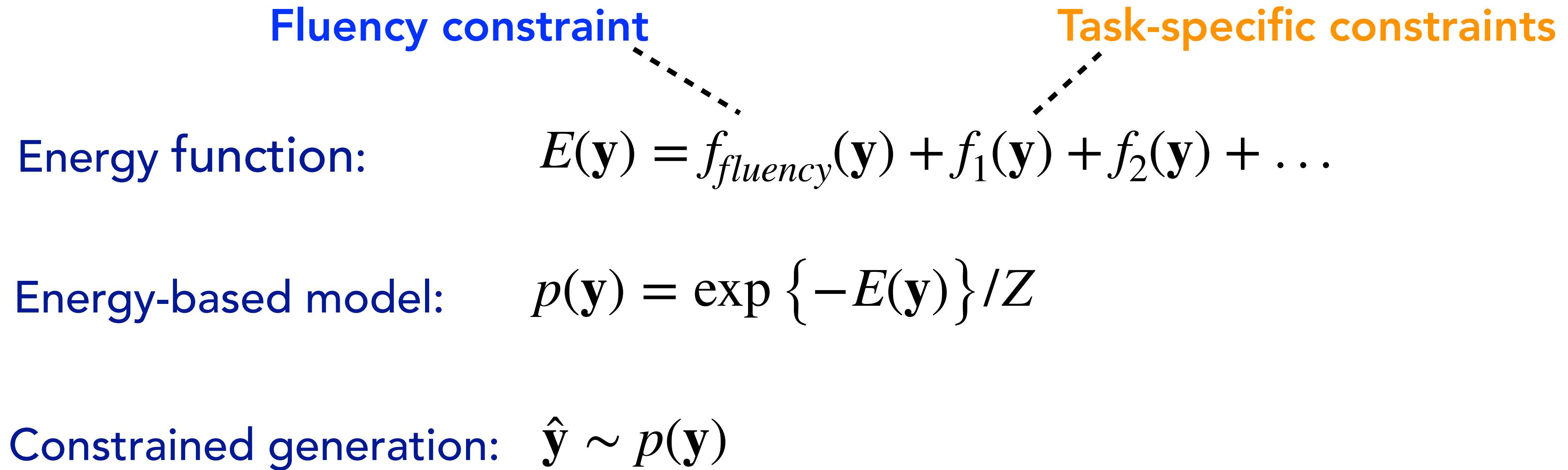
Fluency constraint **Task-specific constraints**

Energy function: $E(\mathbf{y}) = f_{fluency}(\mathbf{y}) + f_1(\mathbf{y}) + f_2(\mathbf{y}) + \dots$

Constrained generation as sampling from an energy-based model



Constrained generation as sampling from an energy-based model



Sampling from an energy-based model

Constrained generation: $\hat{\mathbf{y}} \sim \exp\{-E(\mathbf{y})\}/Z$

- Gradient-free MCMC (e.g. Gibbs sampling [Bishop & Nasrabadi 2006]): **slow**

Sampling from an energy-based model

Constrained generation: $\hat{\mathbf{y}} \sim \exp\{-E(\mathbf{y})\}/Z$

- *Gradient based MCMC, e.g. Langevin dynamics* [Welling & Teh, 2011; Du & Mordatch, 2019]

$$\tilde{\mathbf{y}}^{(n)} = \tilde{\mathbf{y}}^{(n-1)} - \eta \boxed{\nabla_{\tilde{\mathbf{y}}} E(\tilde{\mathbf{y}})} + \epsilon \quad \epsilon \sim N(0, 1)$$

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More efficient sampling by using the gradient of $E(\tilde{\mathbf{y}})$

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$\nabla_{\mathbf{y}} E(\mathbf{y})$ not defined for discrete \mathbf{y}

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Constrained generation: $\hat{\mathbf{y}} \sim \exp\{-E(\mathbf{y})\}/Z$

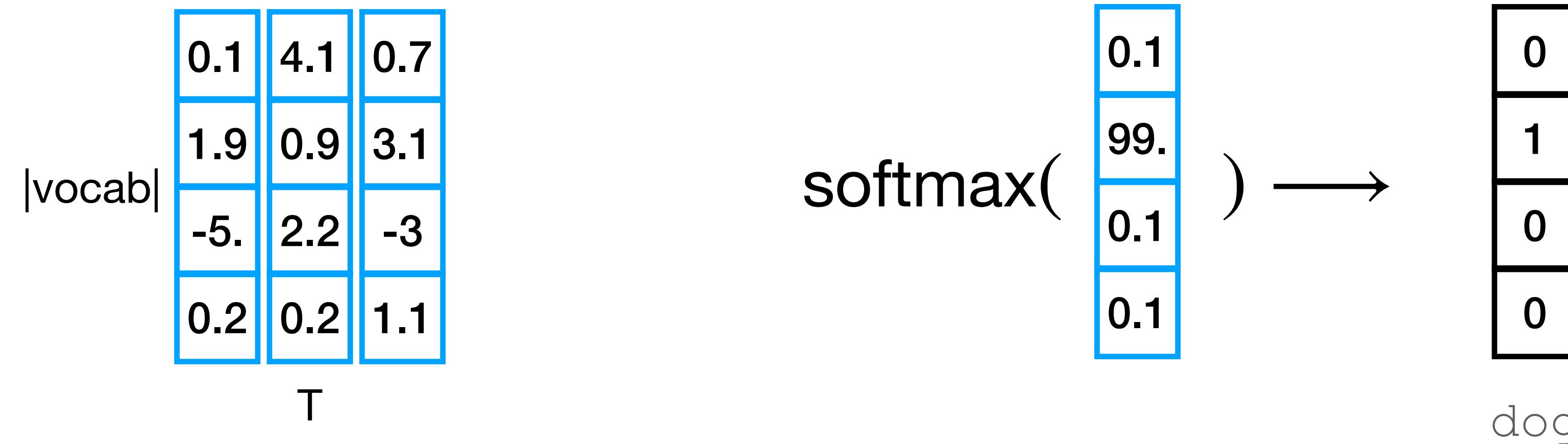
- Define energy over “**soft sequence**” of continuous vectors:
- $\tilde{\mathbf{y}} = (\tilde{\mathbf{y}}_1, \dots, \tilde{\mathbf{y}}_T)$, where $\tilde{\mathbf{y}}_t \in \mathbf{R}^{vocab}$

	0.1	4.1	0.7
vocab	1.9	0.9	3.1
	-5.	2.2	-3
T	0.2	0.2	1.1

Sampling from an energy-based model

Constrained generation: $\hat{\mathbf{y}} \sim \exp\{-E(\mathbf{y})\}/Z$

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- Discrete token: $\text{softmax}(\tilde{\mathbf{y}}_t/\tau)$ as $\tau \rightarrow 0$

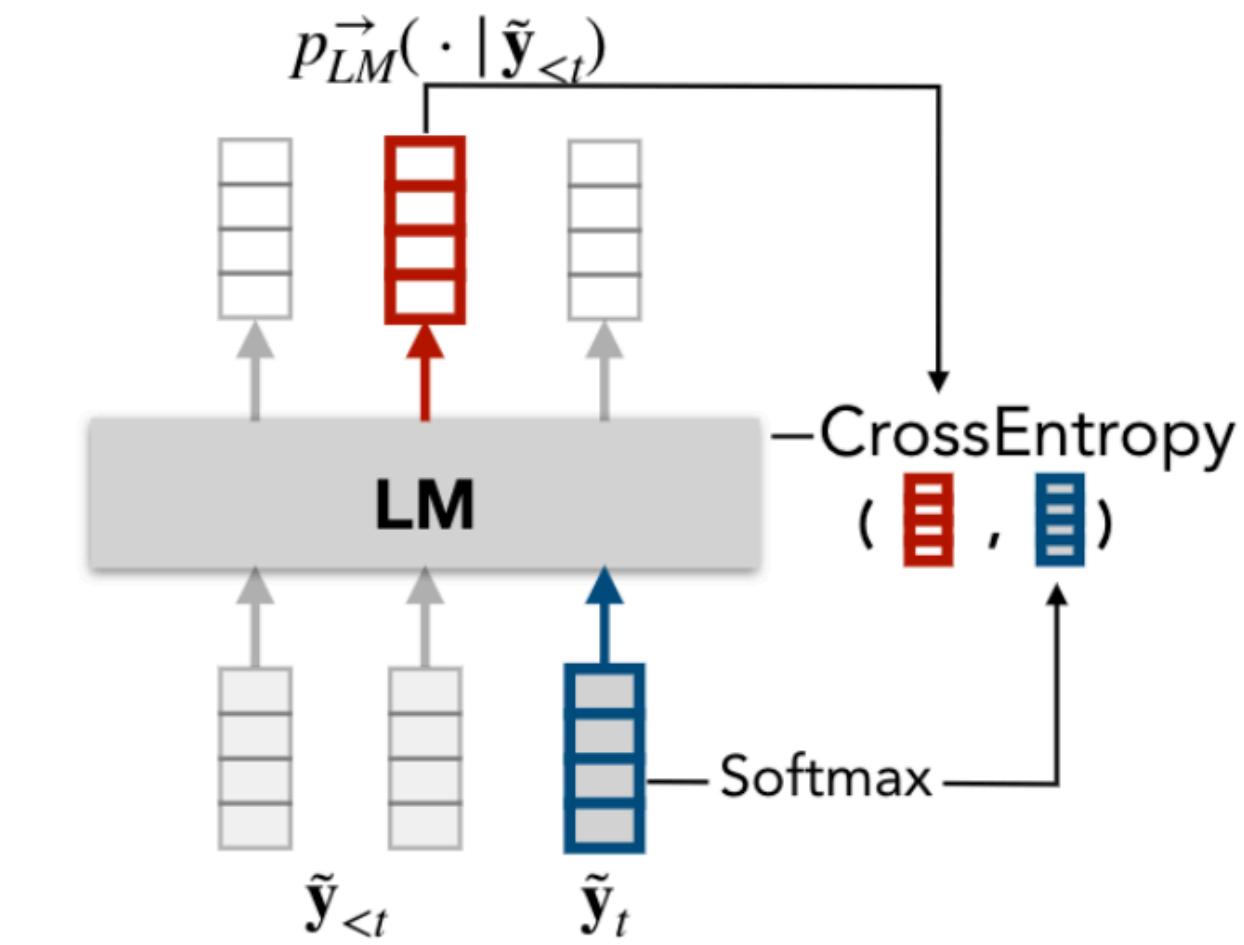
Sampling from an energy-based model

Constrained generation: $\hat{\mathbf{y}} \sim \exp \{-E(\mathbf{y})\}/Z$

- Constraints as differentiable functions



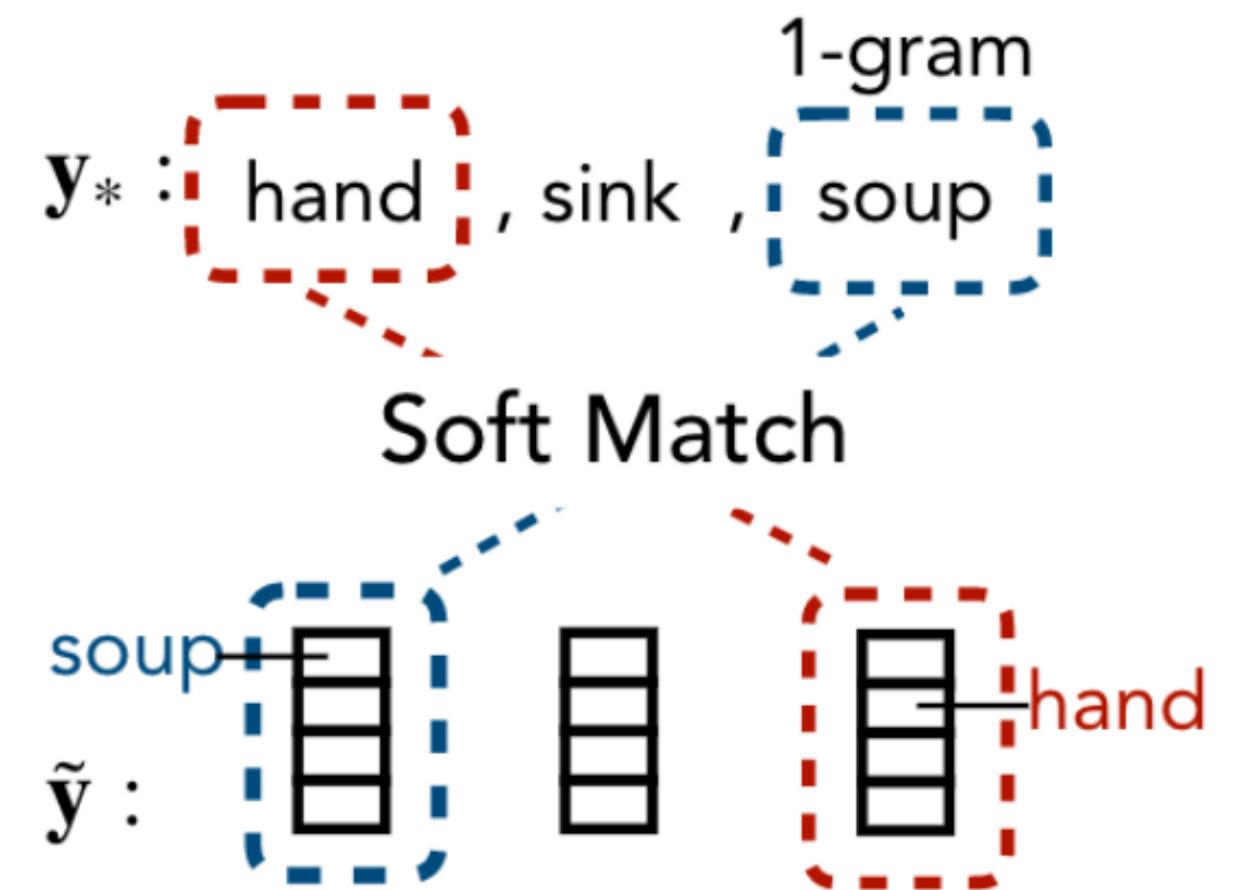
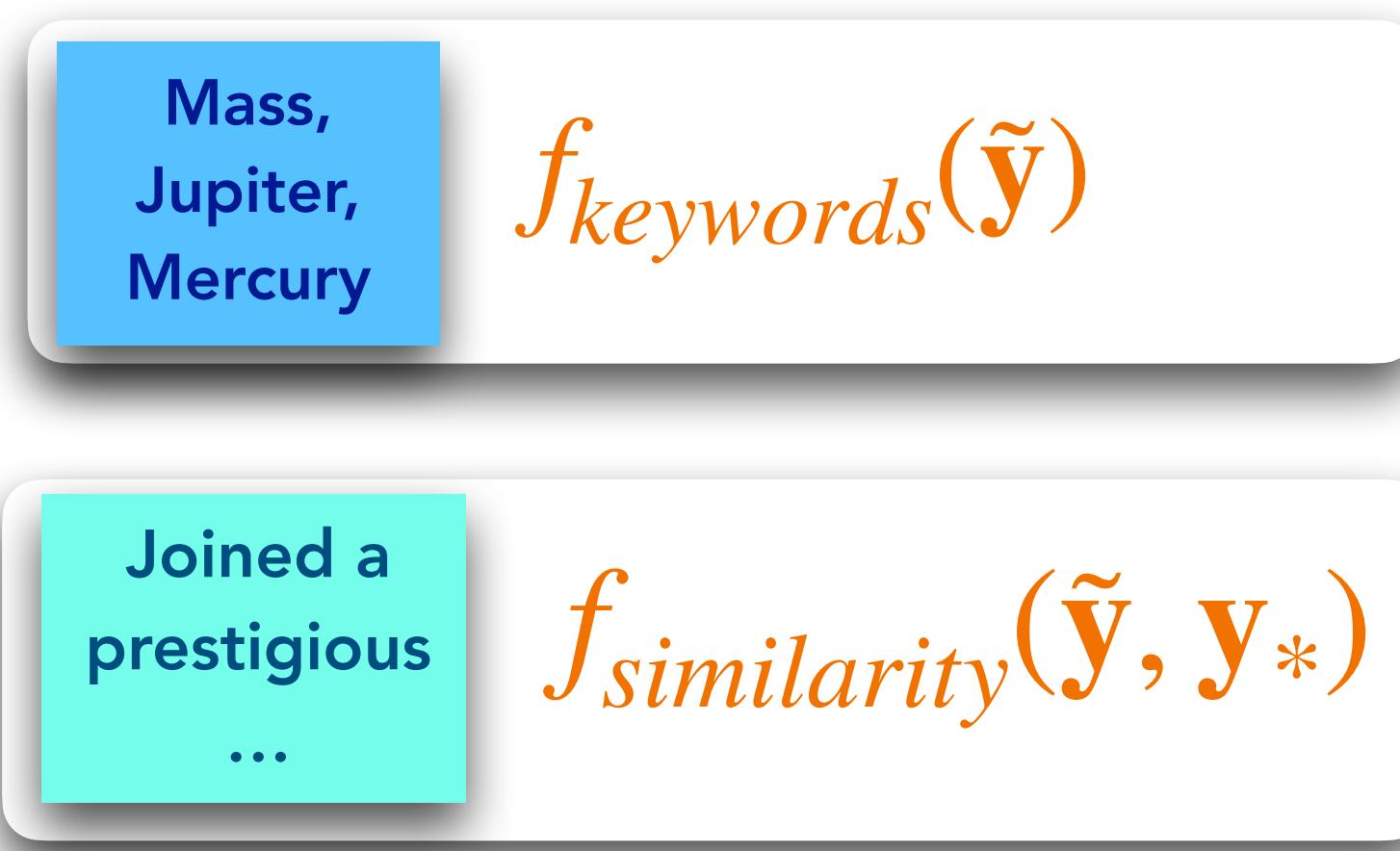
$$f_{LM}^{\rightarrow}(\tilde{\mathbf{y}}) = \sum_{t=1}^T \sum_{v \in \mathcal{V}} p_{LM}^{\rightarrow}(v | \tilde{\mathbf{y}}_{<t}) \log \text{softmax}(\tilde{\mathbf{y}}_t(v))$$



Sampling from an energy-based model

Constrained generation: $\hat{\mathbf{y}} \sim \exp\{-E(\mathbf{y})\}/Z$

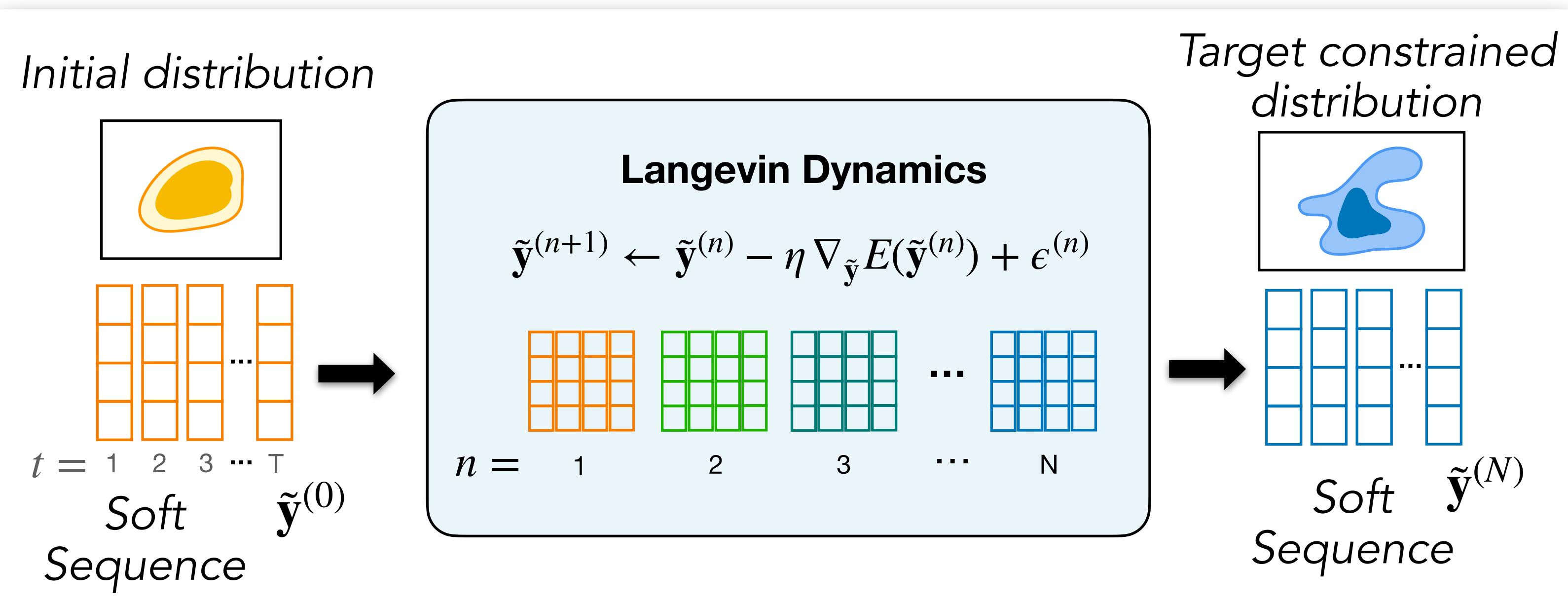
- Constraints as **differentiable functions**



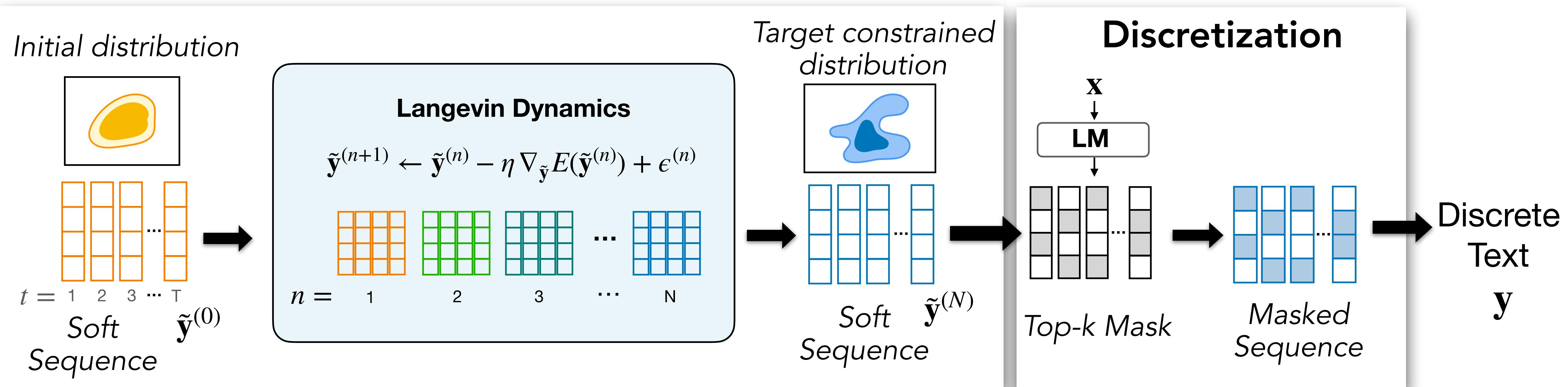
$$f_{\text{sim}}(\tilde{\mathbf{y}}; \mathbf{y}_*) = \text{ngram-match}(\tilde{\mathbf{y}}, \mathbf{y}_*) \quad (\text{Liu et al., 2021})$$

Specify energy $E(\tilde{\mathbf{y}}) = \sum_i f_i(\tilde{\mathbf{y}})$, then:

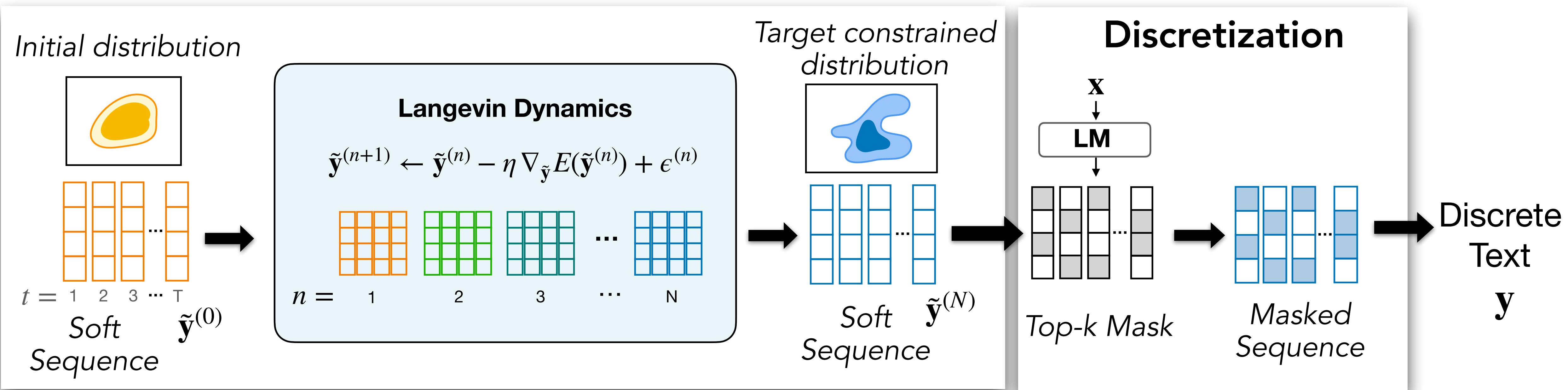
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Apply directly to **off-the-shelf** left-to-right language models
without the need for any task-specific fine-tuning

Lexically constrained generation

CommonGen

(Lin et al., 2020)

We specify an energy function of the following form:

$$E(\tilde{\mathbf{y}}) = \lambda_a^{lr} f_{LM}^{\rightarrow}(\tilde{\mathbf{y}}) + \lambda_a^{rl} f_{LM}^{\leftarrow}(\tilde{\mathbf{y}}) + \lambda_b f_{\text{sim}}(\tilde{\mathbf{y}}; \mathcal{W}) + \lambda_c f_{\text{pred}}(\tilde{\mathbf{y}}; c(\mathcal{W})).$$

Models	Coverage		Fluency	
	Count	Percent	PPL	Human
TSMH	2.72	71.27	1545.15	1.72
NEUROLOGIC	3.30	91.00	28.61	2.53
COLD (ours)	4.24	94.50	54.98	2.07

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- Good constraint coverage
- Competitive fluency with lexical-specific NeuroLogic

Abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

- Enables **left** and **right** coherence while staying **fluent**

$$E(\tilde{\mathbf{y}}) = \lambda_a^{lr} f_{LM}^{\rightarrow}(\tilde{\mathbf{y}}; \mathbf{x}_l) + \lambda_a^{rl} f_{LM}^{\leftarrow}(\tilde{\mathbf{y}}; \mathbf{x}_r) + \lambda_b f_{\text{pred}}(\tilde{\mathbf{y}}; \mathbf{x}_r) \\ + \lambda_c f_{\text{sim}}(\tilde{\mathbf{y}}; \text{kw}(\mathbf{x}_r) - \text{kw}(\mathbf{x}_l)).$$

Begin. \mathbf{x}_l	Tim wanted to learn astronomy.
End. \mathbf{x}_r	Tim worked hard in school to become one.
LEFT-ONLY	He was a good student.
DELOREAN	So he bought a telescope.
COLD (ours)	He wanted to become a professional astronomer.

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Models	Automatic Eval				Human Eval			
	BLEU ₄	ROUGE-L	CIDEr	BERTScore	Grammar	Left-coherence ($\mathbf{x}_l\mathbf{y}$)	Right-coherence ($\mathbf{y}\mathbf{x}_r$)	Overall-coherence ($\mathbf{x}_l\mathbf{y}\mathbf{x}_r$)
LEFT-ONLY	0.88	16.26	3.49	38.48	4.57	3.95	2.68	2.70
DELOREAN	1.60	19.06	7.88	41.74	4.30	4.23	2.83	2.87
COLD (ours)	1.79	19.50	10.68	42.67	4.44	4.00	3.06	2.96

Abductive reasoning

AbductiveNLG

(Bhagavatula et al., 2020)

top- k	Grammar	Left-coher. (x-y)	Right-coher. (y-z)	Overall-coher. (x-y-z)
2	4.38	3.99	2.88	2.92
5	4.27	3.71	3.04	2.87
10	4.09	3.84	3.09	2.94
50	3.95	3.62	3.07	2.87
100	3.80	3.54	3.03	2.84

Table 6. Ablation for the effect of k in top- k filtering mechanism (§3.3). We use the same setting as Table 5.

- Discretization step important: low fluency with large k

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Table 6. Ablation for the effect of k in top- k filtering mechanism (§3.3). We use the same setting as Table 5.

- **Discretization step important:** low fluency with large k
- **COLD sampling important:** low right-coherence with small k

Abductive reasoning

AbductiveNLG

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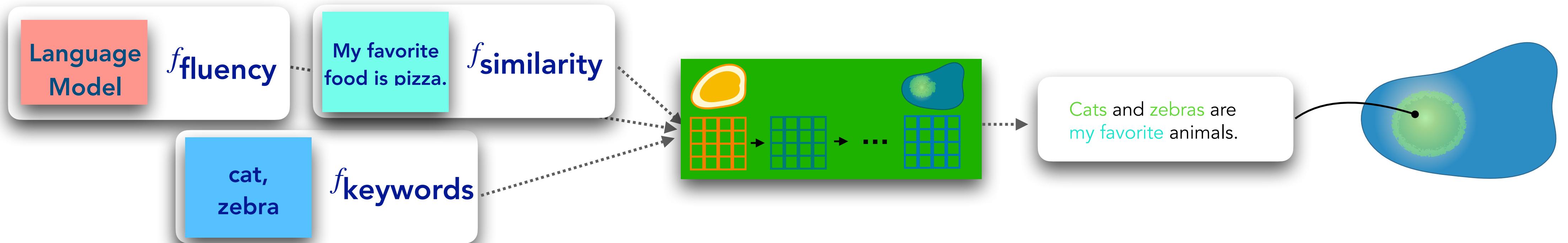
Models	Gram- mar	Left- coher. (x-y)	Right- coher. (y-z)	Overall- coher. (x-y-z)
COLD (Full)	4.17	3.96	2.88	2.83
COLD - f_{sim}	4.54	3.82	2.73	2.69
COLD - $f_{\text{LM}}^{\leftarrow}$	4.35	3.97	2.84	2.80
COLD - f_{pred}	4.61	4.07	2.75	2.77

Table 5. Ablation for the effect of different constraints in Eq. (7). We use the abductive reasoning task as a case study, with human evaluation on 125 test examples. The best overall coherence is achieved when all the constraints are present.

- Right-hand constraints are important for right-hand coherence!

Constrained generation through *continuous* inference

- **Constraints:** differentiable constraints; fluency, keywords, similarity
- **Search:** Langevin dynamics + discretization
- **Enables:** constraints without additional fine-tuning



COLD Decoding:
Constrained Decoding with Langevin Dynamics

[arxiv:2202.11705](https://arxiv.org/abs/2202.11705)

[github.com/qkaren/COLD decoding](https://github.com/qkaren/COLD_decoding)

Constrained generation

Looking ahead

Constrained generation

Looking ahead

- **Grounded generation**

Theorem

Let $M = (A, d)$ be a metric space.

Then M is a perfectly normal space.

Gold Proof

By definition, a topological space is perfectly normal space if and only if it is:

a perfectly T_4 space
a T_1 (Fréchet) space.

We have that:

a Metric Space is Perfectly T_4
a Metric Space is T_2 (Hausdorff)
a T_2 (Hausdorff) Space is a T_1 (Fréchet) Space.

Computer-Generated Proof

From:

Metric Space is Hausdorff
 T_2 (Hausdorff) Space is T_1 Space
Metric Space is Perfectly T_4

it follows that M is a topological space which is perfectly normal.

■
[NaturalProofs: Mathematical Theorem Proving in Natural Language](#)

[Towards Grounded Natural Language Proof Generation \(Work in Progress\)](#)

Constrained generation

Looking ahead

- **Grounded generation**

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Computer-Generated Proof

From:

Metric Space is Hausdorff

T_2 (Hausdorff) Space is T_1 Space

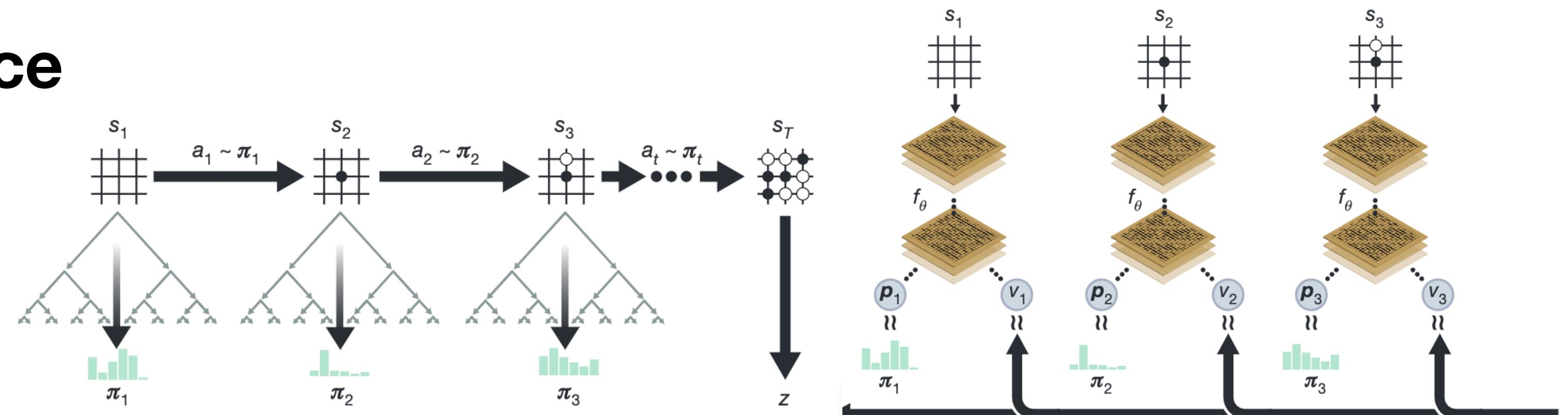
Metric Space is Perfectly T_4

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- **Joint learning & inference**



Thanks for your attention!