STREAM 3D project

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Overview

- Introduction
- Mathematical model
- Numerical Plattofrm
- 4 Conclusion

Introduction

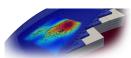
Background and Motivations

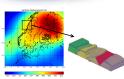
Key processes of sedimentary basin evolution:

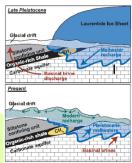
- geomechanics and dynamic evolution of stress and deformations;
- transport of dissolved chemicals;
- geochemical reactive processes.

The effects of glaciations on the subsurface:

- the mechanical compaction due to the load of ice sheets;
- the deformation of the lithosphere by isostasy;
- the subglacial meltwater;







Mathematical model

Poromechanics

$$-\nabla \cdot (2\mu\varepsilon(\mathbf{u}) + \nabla \cdot \mathbf{u}) + \alpha\nabla p = \rho \mathbf{g},$$

$$\partial_t \left(\frac{p}{M} + \alpha\nabla \cdot \mathbf{u}\right) + \nabla \cdot \mathbf{u_d} = S_f,$$

$$\mathbf{K}^{-1}\mathbf{u_d} + \nabla p = \rho_f \mathbf{g},$$

Temperature Dynamics

$$C_T \frac{\partial T}{\partial t} + (\phi \rho_l c_l \mathbf{v_l} + (1 - \phi) \rho_s c_s \mathbf{v_s}) \cdot \nabla T - K_T \nabla^2 T = Q.$$

Chemical transport

$$C_T \frac{\partial C}{\partial t} + \mathbf{u_D} \cdot \nabla C - D\nabla^2 T = Q_c.$$

Coupled model

Poromechanics - Temperature Dynamics - Chemical transport

$$-\nabla \cdot (2\mu\varepsilon(\mathbf{u}) + \nabla \cdot \mathbf{u}) + \alpha \nabla p = \rho \mathbf{g},$$

$$\partial_t \left(\frac{p}{M} + \alpha \nabla \cdot \mathbf{u} \right) + \nabla \cdot \mathbf{u_d} = S_f,$$

$$\mathbf{K}^{-1} \mathbf{u_d} + \nabla p = \rho_f \mathbf{g},$$

$$C_T \frac{\partial T}{\partial t} + (\phi \rho_l c_l \mathbf{v_l} + (1 - \phi) \rho_s c_s \mathbf{v_s}) \cdot \nabla T - K_T \nabla^2 T = Q.$$

$$C_T \frac{\partial C}{\partial t} + \mathbf{u_D} \cdot \nabla C - D \nabla^2 T = Q_c.$$

Constitutive law

$$\mu = 1.002 \, 10^{-3} \left(1 + \alpha_1(T) + \alpha_2(C_M) \right) \tag{1}$$

$$\rho_l = \rho_0 (1 + \beta_1(T) + \beta_2(C_M)). \tag{2}$$

Ice fraction

$$S_{i} = \begin{cases} 1 & T > T_{L}, \\ (1 - S_{lres}) \exp\left[-\left(\frac{T - T_{L}}{w}\right)^{2}\right] + S_{lres} & T_{L} > T > T_{lres}, \\ S_{lres} & T < T_{lres}, \end{cases}$$

$$(3)$$

Numerical Plattofrm

Numerical platform



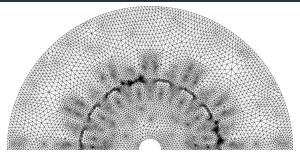
GetFem

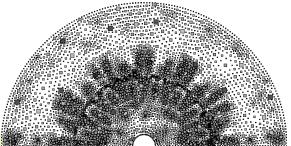
- c++ finite element platform
- Generic assembly language
- Level-set and finite element cut by one or several level-set (Xfem).

SAMG library Algebraic Multigrid Methods for Systems

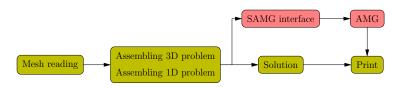
- solution of large linear systems
- higly scalable
- easy to integrate

Geometric VS Algebraic





Integration



- Simple interface (CSR matrix)
- Same programming language

Conclusion