

MAXimal

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Finding power divider

Given two numbers n and k , find the largest x such that $n!$ is divided into k^x .
 Required to calculate with any degree of the divisor k is one $n!$, ie find the largest x such that $n!$ is divided into k^x .



Original text

MAXimal

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:55

○ Solution for the case of composite k

Solution for the case of simple k

Consider first the case when k simple.

We write down the expression for the factorial explicitly:

$$n! = 1 \cdot 2 \cdot 3 \cdot \dots \cdot (n-1) \cdot n$$

Note that each k member of the $n!$ is divided into k , ie allows one to answer; the number of such members of the same $\lfloor n/k \rfloor$.

Further, we note that each k^2 th term of this series is divided into k^2 , ie gives one more to the answer (given that k in the first degree has already been considered before); the number of such members of the same $\lfloor n/k^2 \rfloor$.

And so on, every k^i th term of the series gives one to answer, and the number of members equal $\lfloor n/k^i \rfloor$.

Thus, the magnitude of response is:

$$\frac{n}{k} + \frac{n}{k^2} + \dots + \frac{n}{k^i} + \dots$$

This amount, of course, is not infinite, because only the first about $\log_k n$ members are non-zero. Consequently, the asymptotic behavior of the algorithm is $O(\log_k n)$.

Implementation:

```
int fact_pow (int n, int k) {
    int res = 0;
    while (n) {
        n /= k;
        res += n;
    }
    return res;
}
```

}

Solution for the case of composite k

The same idea is applied directly anymore.

But we can factor k , solve the problem for each of its prime divisors, and then select the minimum of the answers.

More formally, let k_i – this is i th factor of the number k belongs to him in power p_i . We solve the problem for k_i using the above formula for $O(\log n)$; though we got an answer Ans_i . Then the answer for the composite k will be a minimum of values Ans_i/p_i .

Given that the factorization is performed in the simplest way $O(\sqrt{k})$, we obtain the asymptotic behavior of the final $O(\sqrt{k})$.

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В конце, наверное, асимптотика \sqrt{k} , а не из N ?

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