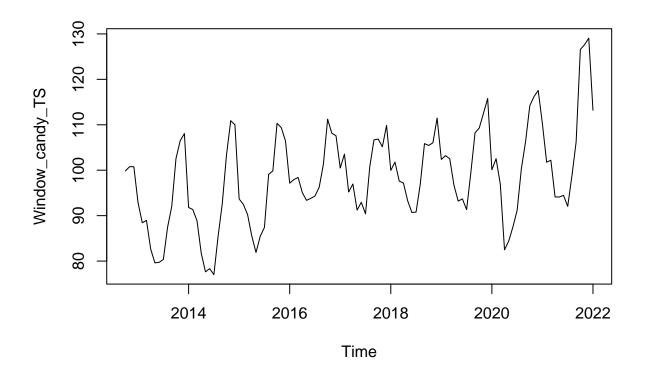
## Final Candy

#### 2022-12-06

```
library(forecast)
## Registered S3 method overwritten by 'quantmod':
##
    method
     as.zoo.data.frame zoo
##
library(readr)
library(tseries)
IPG3113N <- read_csv("/Users/danieltamayo/Desktop/CandyFinal.csv")</pre>
## Rows: 121 Columns: 2
## -- Column specification ------
## Delimiter: ","
## dbl (1): IPG3113N
## date (1): DATE
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
candy_ts <- ts(IPG3113N$IPG3113N,frequency = 12,start=c(2012,10))</pre>
Window_candy_TS <-window(candy_ts, start = 2012, end = 2022)</pre>
## Warning in window.default(x, \dots): 'start' value not changed
## Plot and Inference
plot(Window_candy_TS)
```



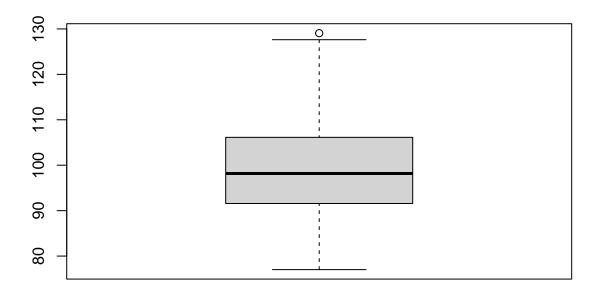
From this plot, we can see that over time from 2012 to 2022 there appears to be a seasonal component of candy production in the US. There appears to be an element of seasonality as well. This element of seasonality appears to happen once a year.

```
#Central Tendency
summary(Window_candy_TS)

## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 77.02 91.69 98.18 98.50 106.09 129.06
```

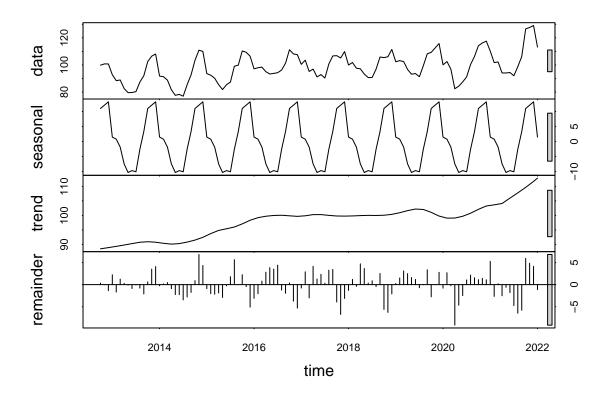
#### **Including Plots**

```
boxplot(Window_candy_TS)
```



FRom this we can see that the Data seems to be pretty unifromly distributed; The mean and the median are about the same. However most of the data lies between the min and the median/mean.

```
#Decomposition
stl_decomp <- stl(Window_candy_TS,s.window ="periodic")
plot(stl_decomp)</pre>
```



From the decomposition, we can see that there is quite a strong element of seasonality in the Candy Time Series.

## Since the variation of seasonality(widths and heights) does not change over time, we can see that this decomposition is in fact additive.

```
#Decomposition
Window_candy_TS
##
              Jan
                       Feb
                                 Mar
                                          Apr
                                                    May
                                                             Jun
                                                                       Jul
                                                                                 Aug
## 2012
## 2013
                                                                   80.3623
                                                                            87.3990
         92.8393
                   88.4378
                            88.9572
                                      82.6418
                                                79.6009
                                                         79.7216
         91.8045
                   91.3464
                            88.8527
                                      81.7442
                                                77.6292
                                                         78.3359
                                                                   77.0192
                                                                            85.4452
  2014
   2015
         93.6676
                   92.4733
                            90.2388
                                      85.5111
                                                81.8907
                                                         85.4442
                                                                   87.4143
                                                                            99.0757
  2016
         97.1509
                   97.9475
                                      95.0657
                                                93.3682
                                                         93.8015
                                                                   94.3271
                            98.4111
                                                                            96.2487
   2017 100.4828 103.5407
                            95.2095
                                      96.9654
                                                91.2276
                                                         92.9268
                                                                   90.3917
                                                                           100.6988
  2018
         99.9651 101.7932
                            97.6257
                                      97.1776
                                                93.2973
                                                         90.7030
                                                                   90.7825
                                                                            96.9555
## 2019 102.3790 103.2079
                                      96.6862
                                                93.2061
                                                         93.6885
                                                                   91.3219
                                                                            99.4256
## 2020 100.1032 102.5297
                            96.9412
                                      82.4777
                                                84.4155
                                                         87.5411
                                                                   91.2016 100.3417
## 2021 110.1841 101.7558 102.2030
                                      94.1243
                                               94.0966
                                                         94.4684
                                                                   92.0391
                                                                            98.7301
## 2022 113.1828
##
                       Oct
                                Nov
                                          Dec
             Sep
## 2012
                   99.8541 100.7874 100.7643
```

```
## 2013 92.0523 102.5585 106.4783 108.0668
## 2014 92.7103 103.4097 110.9082 109.9962
## 2015 99.8525 110.3226 109.3626 106.4516
## 2016 101.3271 111.2323 108.1348 107.5859
## 2017 106.6639 106.8689 105.1628 109.8611
## 2018 105.8597 105.4468 106.0408 111.4674
## 2019 108.2320 109.2961 112.5268 115.7811
## 2020 106.3095 114.2083 116.2062 117.5581
## 2021 106.2289 126.5753 127.6255 129.0640
## 2022
```

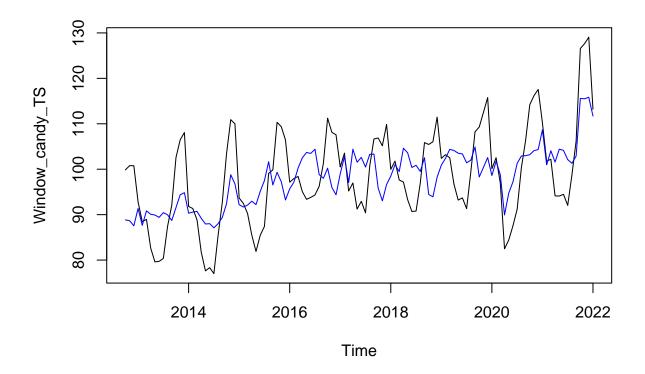
Here are the values of the seasonal monthly indices.

```
#Decomposition
tapply(Window_candy_TS,cycle(Window_candy_TS),mean)
##
                     2
                                3
                                                     5
                                                               6
           1
## 100.17593
              98.11470
                        95.66139
                                   90.26600
                                             87.63690
                                                       88.51456
                    10
                               11
## 102.13736 108.97726 110.32334 111.65965
```

These are the average values for the months from our Time Series. From this, we can see that based on the average, The most Candy is produced in December and the least amount of Candy is produced in May.

##I believe the most Candy is produced in December for Holiday season and in May there is not that much because there are not that many known festivities in May that involve candy.

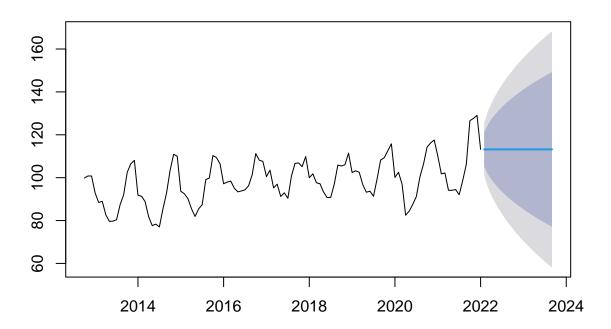
```
#Decomposition
plot(Window_candy_TS)
lines(seasadj(stl_decomp), col="blue")
```



## This is the graph of our regular TS and our seasonaly adjusted Time Series in Blue over that.

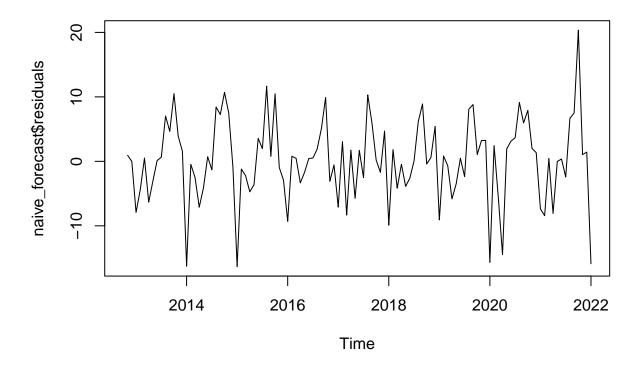
```
#Naive Method
naive_forecast <- naive(Window_candy_TS,20)
plot(naive_forecast)</pre>
```

## **Forecasts from Naive method**



#Naive Method

plot(naive\_forecast\$residuals)

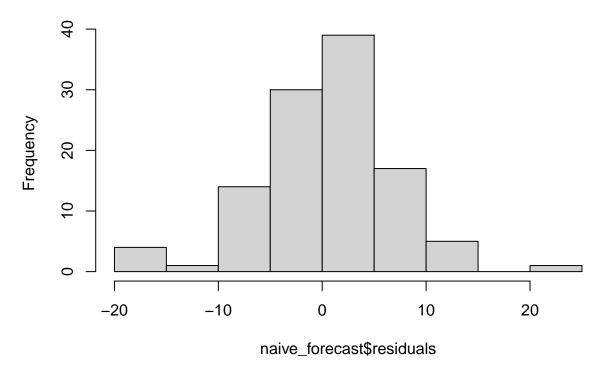


##Since there appears to be season laity and a trend in the resiudals. This shows that the naive forecast is not a good fit for this data set.

#### #Naive Method

hist(naive\_forecast\$residuals)

## Histogram of naive\_forecast\$residuals

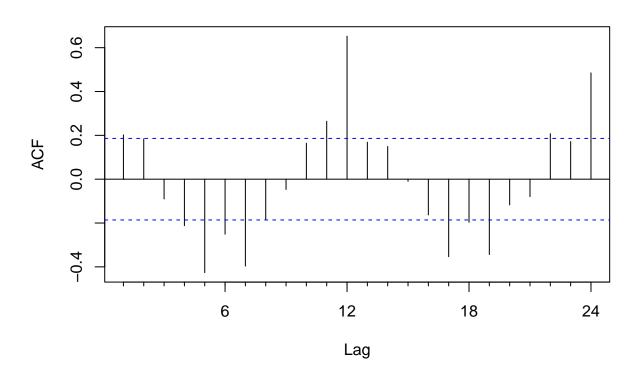


 $\#\#\mathrm{This}$  shows that he data is pretty normally distributed.

#Naive Method

Acf(naive\_forecast\$residuals)

#### Series naive\_forecast\$residuals

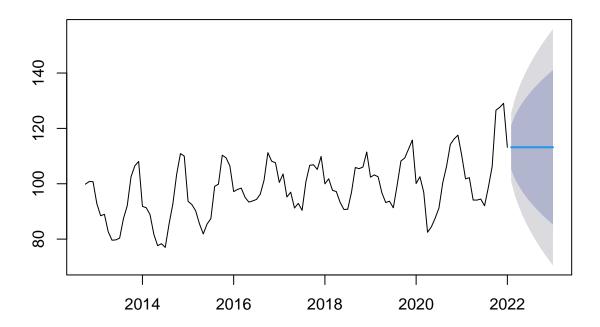


##This indicates that there seems to be a seasonal component, there are also some values in the residuals which are statistically significant.

```
#Naive Method
accuracy(naive_forecast)
##
                       ME
                              RMSE
                                        MAE
                                                     MPE
                                                             MAPE
                                                                      MASE
## Training set 0.1200784 6.290507 4.634619 -0.08377488 4.696548 1.195201
                     ACF1
## Training set 0.2019946
#Naive Method
naive_forecast_12 <- naive(Window_candy_TS,12)</pre>
naive_forecast_12
            Point Forecast
                               Lo 80
                                        Hi 80
                                                   Lo 95
                                                            Hi 95
## Feb 2022
                  113.1828 105.12119 121.2444 100.85363 125.5120
## Mar 2022
                  113.1828 101.78196 124.5836
                                               95.74672 130.6189
## Apr 2022
                           99.21968 127.1459
                  113.1828
                                               91.82805 134.5375
## May 2022
                  113.1828
                            97.05958 129.3060
                                               88.52446 137.8411
## Jun 2022
                  113.1828 95.15649 131.2091
                                               85.61394 140.7517
## Jul 2022
                  113.1828 93.43597 132.9296 82.98263 143.3830
## Aug 2022
                  113.1828 91.85379 134.5118 80.56289 145.8027
```

```
## Sep 2022
                 113.1828 90.38112 135.9845 78.31065 148.0550
## Oct 2022
                  113.1828
                           88.99797 137.3676 76.19530 150.1703
## Nov 2022
                  113.1828
                           87.68975 138.6758 74.19455 152.1711
## Dec 2022
                           86.44547 139.9201 72.29158 154.0740
                  113.1828
## Jan 2023
                  113.1828
                           85.25657 141.1090
                                              70.47331 155.8923
#Naive Method
plot(naive_forecast_12)
```

#### **Forecasts from Naive method**

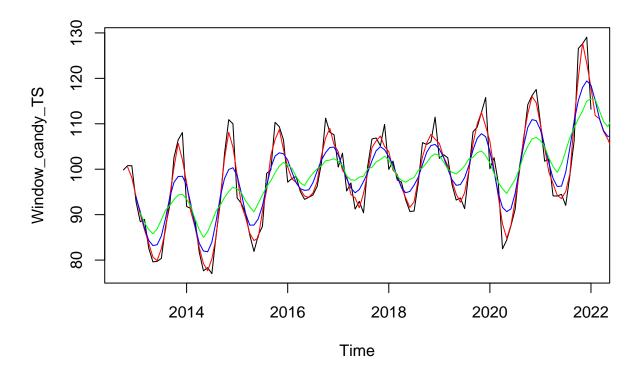


##Overall, the Naive forecast is not the best since it does not take into account seasonality and teh trend. It says the value will be 113.

```
#Simple Moving Averages

MA3_forecast <- ma(candy_ts,order=3)
MA6_forecast <- ma(candy_ts,order=6)
MA9_forecast <- ma(candy_ts,order=9)

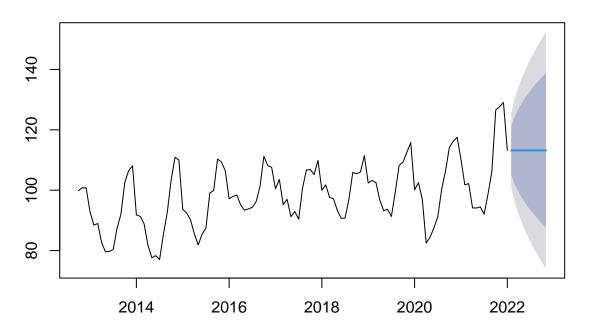
plot(Window_candy_TS)
lines(MA3_forecast,col="Red")
lines(MA6_forecast,col="Blue")
lines(MA9_forecast,col="Green")</pre>
```



## As the moving average goes up we can see that the seasonality is less wide. Overall, this smooths the graph out.

```
#Simple Smoothing
SES_candy <- ses(Window_candy_TS)
SES_candy_forecast <- forecast(SES_candy)
plot(SES_candy_forecast)</pre>
```

#### Forecasts from Simple exponential smoothing



#### #Simple Smoothing

SES\_candy

```
##
           Point Forecast
                              Lo 80
                                       Hi 80
                                                 Lo 95
                                                          Hi 95
## Feb 2022
                 113.1844 105.08605 121.2827 100.79905 125.5697
## Mar 2022
                                              95.66976 130.6990
                 113.1844 101.73219 124.6366
## Apr 2022
                 113.1844 99.15860 127.2102
                                              91.73379 134.6350
## May 2022
                 113.1844 96.98893 129.3798
                                              88.41558 137.9532
## Jun 2022
                 113.1844 95.07741 131.2914
                                              85.49216 140.8766
## Jul 2022
                 113.1844 93.34925 133.0195 82.84917 143.5196
## Aug 2022
                 113.1844 91.76005 134.6087 80.41868 145.9501
## Sep 2022
                 113.1844 90.28084 136.0879 78.15644 148.2123
## Oct 2022
                 113.1844 88.89155 137.4772 76.03169 150.3371
## Nov 2022
                 113.1844 87.57751 138.7913 74.02205 152.3467
```

#### #Simple Smoothing

SES\_candy\$alpha

## NULL

#### #Simple Smoothing

SES\_candy\$beta

#### ## NULL

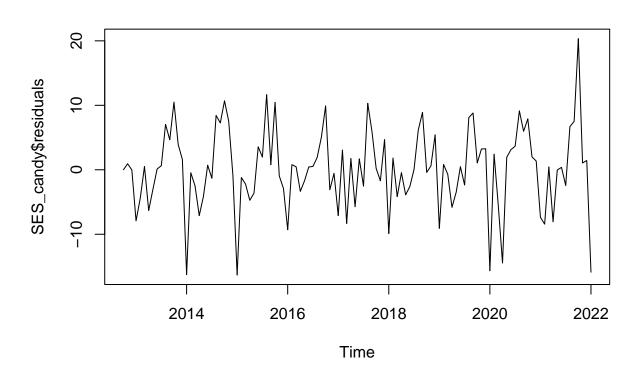
#### #Simple Smoothing

SES\_candy\$gamma

#### ## NULL

#### #Simple Smoothing

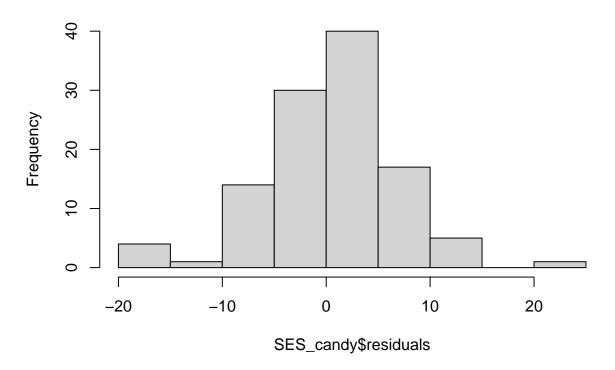
plot(SES\_candy\$residuals)



#### #Simple Smoothing

hist(SES\_candy\$residuals)

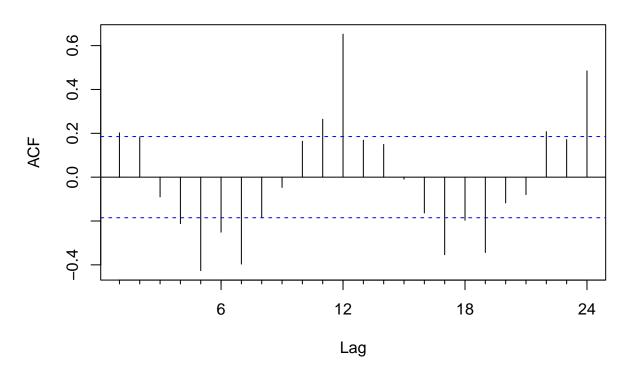
## **Histogram of SES\_candy\$residuals**



#Simple Smoothing

Acf(SES\_candy\$residuals)

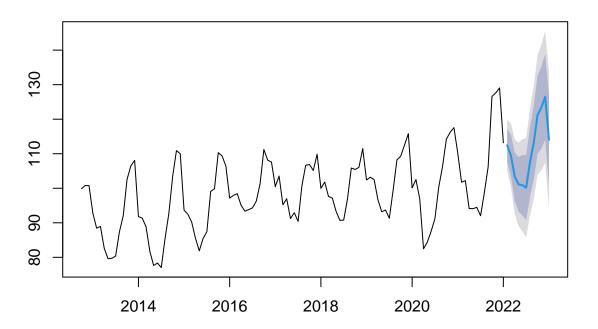
## Series SES\_candy\$residuals



 $\#\#\mbox{Overall}$  not good- seasonality and significant values

```
#Holt Winters
HW_candy <- HoltWinters(Window_candy_TS)
HW_candy_forecast <- forecast(HW_candy, h=12)
plot(HW_candy_forecast)</pre>
```

#### **Forecasts from HoltWinters**



```
#Holt Winters
HW_candy
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = Window_candy_TS)
##
## Smoothing parameters:
##
    alpha: 0.7506546
    beta: 0
##
##
    gamma: 0.4883202
##
## Coefficients:
##
               [,1]
## a
       110.70009616
## b
         0.02735169
         1.72180742
## s1
##
        -1.28486516
##
  s3
        -7.43820880
        -9.67567517
## s4
        -9.94871899
## s5
## s6
       -10.69053896
## s7
        -3.32792838
## s8
         2.30623793
        10.30389812
## s9
```

```
## s10 12.41027415
## s11 15.47849169
## s12 3.01602423
```

## From this we can see that value of alpha is 0.75, the value of beta is 0 and the value of gamma is 0.488.

##Alpha signifies the level of the smoothing - since it is .75, later values have more weight. ##Beta signifies the level for trend smoothing - since it is 0, earlier values have all teh weight. ##Gamma refers to the seasonal component of the timeseries since it is .48 this means that it is right in the middle of earlier and later values.

#### #Holt Winters

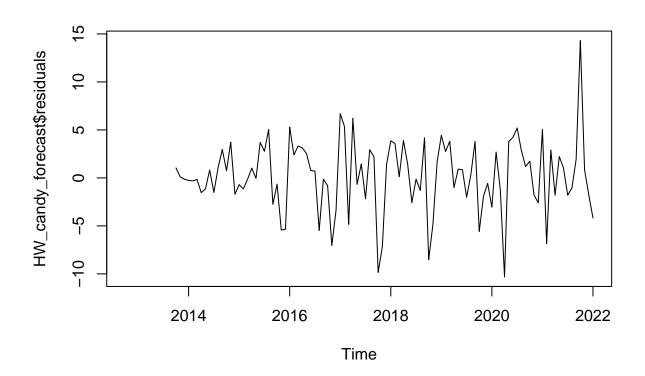
HW\_candy\$Sigma

## NULL

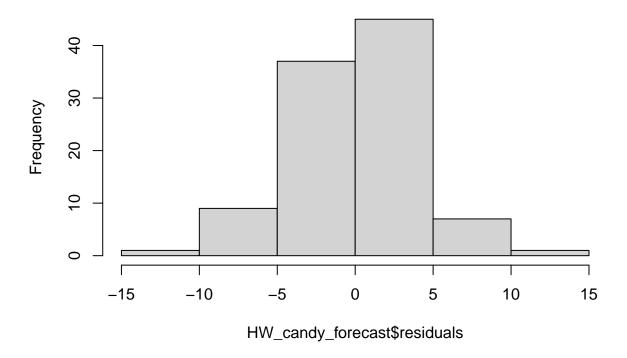
##The value of sigma is null

#### #ARIMA

plot(HW\_candy\_forecast\$residuals)



## Histogram of HW\_candy\_forecast\$residuals

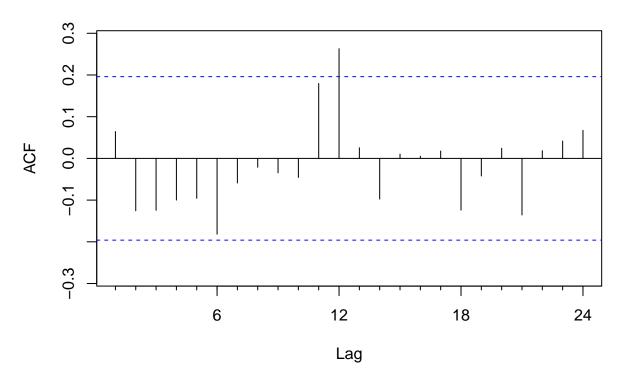


This shows there is a normal distribution in residuals

#HW

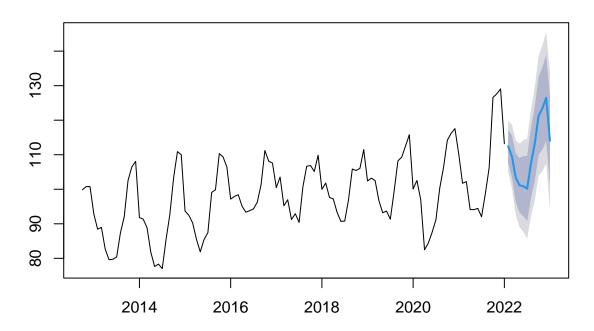
Acf(HW\_candy\_forecast\$residuals)

## Series HW\_candy\_forecast\$residuals



## TH is looks good, no trends, seasonality, all points are not significant

#### **Forecasts from HoltWinters**

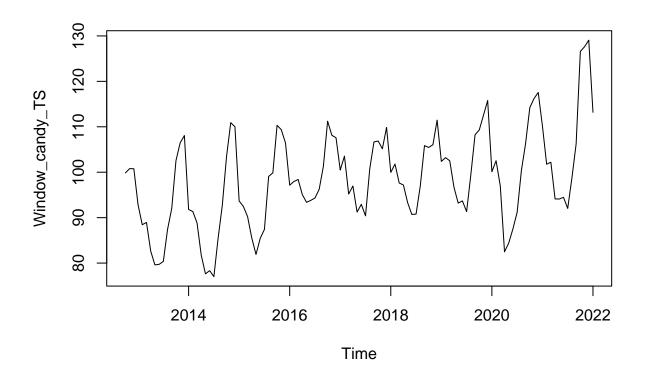


## #HW forecast(HW\_candy\_forecast, h=12)

```
##
            Point Forecast
                               Lo 80
                                        Hi 80
                                                  Lo 95
                                                            Hi 95
                  112.4493 107.62416 117.2744 105.06990 119.8286
## Feb 2022
## Mar 2022
                  109.4699 103.43667 115.5032 100.24285 118.6970
## Apr 2022
                  103.3439
                            96.30696 110.3809
                                               92.58181 114.1061
## May 2022
                  101.1338
                            93.21942 109.0482
                                               89.02979 113.2379
## Jun 2022
                            92.18431 109.5920
                                               87.57678 114.1995
                  100.8881
## Jul 2022
                  100.1737
                            90.74630 109.6010
                                               85.75575 114.5916
## Aug 2022
                  107.5636
                           97.46442 117.6628
                                               92.11822 123.0090
## Sep 2022
                  113.2251 102.49608 123.9542 96.81646 129.6338
## Oct 2022
                  121.2502 109.92622 132.5741 103.93169 138.5686
## Nov 2022
                  123.3839 111.49480 135.2730 105.20110 141.5667
## Dec 2022
                  126.4795 114.05090 138.9080 107.47161 145.4873
## Jan 2023
                  114.0443 101.09877 126.9899 94.24580 133.8429
```

##Overall, we can see that this a very good model. The model in a year is predicted to be 114.0443. We can tell this is a good model by the residuals.

```
#ARIMA
plot(Window_candy_TS)
```



```
#ARIMA
adf.test(Window_candy_TS)
## Warning in adf.test(Window_candy_TS): p-value smaller than printed p-value
##
    Augmented Dickey-Fuller Test
##
##
## data: Window_candy_TS
## Dickey-Fuller = -8.3398, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary
kpss.test(Window_candy_TS)
## Warning in kpss.test(Window_candy_TS): p-value smaller than printed p-value
##
##
    KPSS Test for Level Stationarity
##
## data: Window_candy_TS
## KPSS Level = 0.77215, Truncation lag parameter = 4, p-value = 0.01
```

The TS is stationary since when we run the KPSS test, the p-value is less than .05.

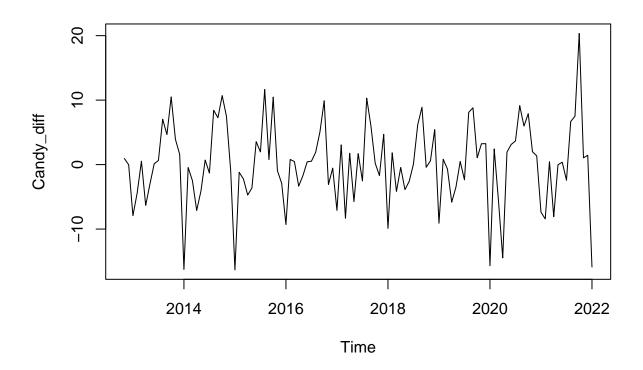
```
#ARIMA
nsdiffs(Window_candy_TS)
```

## [1] 1

From this we can see that the number of differences in order to make the data stationary is 1.

The seasonality component is needed since out time series has a seasonality component.

```
#ARIMA
Candy_diff <- diff(Window_candy_TS, differences=1)
plot(Candy_diff)</pre>
```

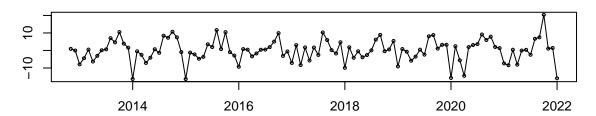


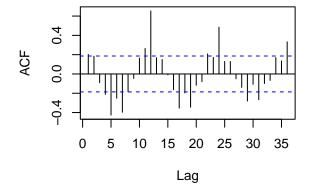
##This is our plot including the difference of 1.

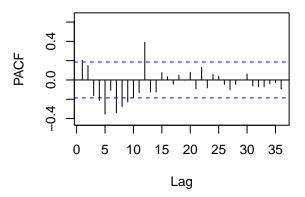
#### #ARIMA

tsdisplay(Candy\_diff)

## Candy\_diff







#### #ARIMA

```
fit1 <- auto.arima(candy_ts)
fit1</pre>
```

```
## Series: candy_ts
## ARIMA(1,0,0)(2,1,0)[12] with drift
##
## Coefficients:
##
            ar1
                                   drift
                   sar1
                            sar2
        0.6441
                -0.3042
                         -0.2351
                                  0.2083
##
                                  0.0579
## s.e. 0.0742
                 0.1040
                          0.1099
## sigma^2 = 14.95: log likelihood = -301.36
## AIC=612.72 AICc=613.31
                             BIC=626.18
```

#### From above, we can see that sigma $^2 = 14.95$ , AIC = 612.72 and BIC = 626.18

```
#ARIMA
fit3 <- auto.arima(Window_candy_TS,trace=TRUE, stepwise = FALSE )</pre>
##
##
   ARIMA(0,0,0)(0,1,0)[12]
                                              : 614.2527
  ARIMA(0,0,0)(0,1,0)[12] with drift
                                              : 598.8945
                                              : 616.2334
## ARIMA(0,0,0)(0,1,1)[12]
## ARIMA(0,0,0)(0,1,1)[12] with drift
                                              : 596.2502
## ARIMA(0,0,0)(0,1,2)[12]
                                              : 616.6361
## ARIMA(0,0,0)(0,1,2)[12] with drift
                                             : Inf
## ARIMA(0,0,0)(1,1,0)[12]
                                              : 616.2156
## ARIMA(0,0,0)(1,1,0)[12] with drift
                                              : 597.147
                                             : 618.2044
## ARIMA(0,0,0)(1,1,1)[12]
## ARIMA(0,0,0)(1,1,1)[12] with drift
                                             : Inf
## ARIMA(0,0,0)(1,1,2)[12]
                                              : 618.617
## ARIMA(0,0,0)(1,1,2)[12] with drift
                                              : Inf
## ARIMA(0,0,0)(2,1,0)[12]
                                              : 617.49
## ARIMA(0,0,0)(2,1,0)[12] with drift
                                              : 598.7375
## ARIMA(0,0,0)(2,1,1)[12]
                                              : 619.6502
                                              : Inf
## ARIMA(0,0,0)(2,1,1)[12] with drift
## ARIMA(0,0,0)(2,1,2)[12]
                                              : Inf
## ARIMA(0,0,0)(2,1,2)[12] with drift
                                              : Inf
## ARIMA(0,0,1)(0,1,0)[12]
                                              : 578.5893
## ARIMA(0,0,1)(0,1,0)[12] with drift
                                              : 569.7968
## ARIMA(0,0,1)(0,1,1)[12]
                                              : 578.8361
## ARIMA(0,0,1)(0,1,1)[12] with drift
                                              : Inf
## ARIMA(0,0,1)(0,1,2)[12]
                                              : 580.2324
## ARIMA(0,0,1)(0,1,2)[12] with drift
                                             : Inf
## ARIMA(0,0,1)(1,1,0)[12]
                                             : 578.5447
## ARIMA(0,0,1)(1,1,0)[12] with drift
                                             : 565.7557
## ARIMA(0,0,1)(1,1,1)[12]
                                              : 580.3731
## ARIMA(0,0,1)(1,1,1)[12] with drift
                                             : Inf
## ARIMA(0,0,1)(1,1,2)[12]
                                              : 582.0542
                                              : Inf
## ARIMA(0,0,1)(1,1,2)[12] with drift
## ARIMA(0,0,1)(2,1,0)[12]
                                              : 580.1977
## ARIMA(0,0,1)(2,1,0)[12] with drift
                                              : 567.6842
## ARIMA(0,0,1)(2,1,1)[12]
                                              : 582.4073
## ARIMA(0,0,1)(2,1,1)[12] with drift
                                              : Inf
                                              : Inf
## ARIMA(0,0,1)(2,1,2)[12]
## ARIMA(0,0,1)(2,1,2)[12] with drift
                                              : Inf
                                              : 569.2631
## ARIMA(0,0,2)(0,1,0)[12]
## ARIMA(0,0,2)(0,1,0)[12] with drift
                                              : 563.4987
## ARIMA(0,0,2)(0,1,1)[12]
                                              : 569.1028
## ARIMA(0,0,2)(0,1,1)[12] with drift
                                             : Inf
## ARIMA(0,0,2)(0,1,2)[12]
                                              : 571.0359
## ARIMA(0,0,2)(0,1,2)[12] with drift
                                              : Inf
## ARIMA(0,0,2)(1,1,0)[12]
                                              : 569.2359
## ARIMA(0,0,2)(1,1,0)[12] with drift
                                             : 560.5687
## ARIMA(0,0,2)(1,1,1)[12]
                                              : 570.4864
```

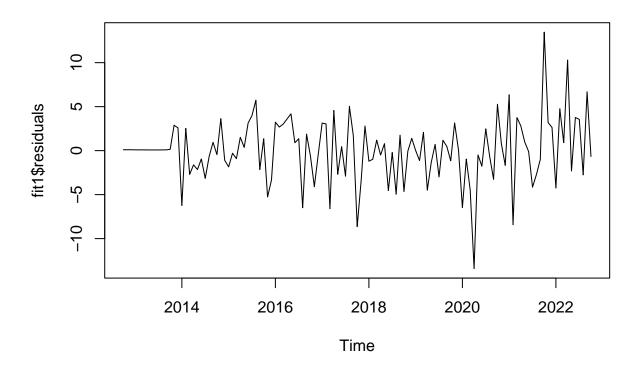
```
ARIMA(0,0,2)(1,1,1)[12] with drift
                                                : Inf
##
                                                : 572.7506
   ARIMA(0,0,2)(1,1,2)[12]
## ARIMA(0,0,2)(1,1,2)[12] with drift
                                                : Inf
                                                : 571.4252
## ARIMA(0,0,2)(2,1,0)[12]
##
   ARIMA(0,0,2)(2,1,0)[12] with drift
                                                : 561.8001
##
                                                : 572.7501
  ARIMA(0,0,2)(2,1,1)[12]
  ARIMA(0,0,2)(2,1,1)[12] with drift
                                               : Inf
                                                : 564.2611
## ARIMA(0,0,3)(0,1,0)[12]
##
   ARIMA(0,0,3)(0,1,0)[12] with drift
                                                : 560.9119
##
   ARIMA(0,0,3)(0,1,1)[12]
                                                : 563.2243
   ARIMA(0,0,3)(0,1,1)[12] with drift
                                                : Inf
                                                : 565.0771
##
   ARIMA(0,0,3)(0,1,2)[12]
##
   ARIMA(0,0,3)(0,1,2)[12] with drift
                                                : Inf
                                                : 563.4556
##
   ARIMA(0,0,3)(1,1,0)[12]
                                                : 557.7127
##
   ARIMA(0,0,3)(1,1,0)[12] with drift
##
   ARIMA(0,0,3)(1,1,1)[12]
                                                : 564.0822
##
                                                : Inf
   ARIMA(0,0,3)(1,1,1)[12] with drift
##
   ARIMA(0,0,3)(2,1,0)[12]
                                                : 565.6637
                                                : 559.3016
##
  ARIMA(0,0,3)(2,1,0)[12] with drift
   ARIMA(0,0,4)(0,1,0)[12]
                                                : 564.9765
##
   ARIMA(0,0,4)(0,1,0)[12] with drift
                                                : 562.6653
                                                : 563.1839
## ARIMA(0,0,4)(0,1,1)[12]
                                                : Inf
## ARIMA(0,0,4)(0,1,1)[12] with drift
                                                : 563.5343
##
   ARIMA(0,0,4)(1,1,0)[12]
                                                : 559.2561
## ARIMA(0,0,4)(1,1,0)[12] with drift
   ARIMA(0,0,5)(0,1,0)[12]
                                                : 567.041
##
   ARIMA(0,0,5)(0,1,0)[12] with drift
                                                : 564.1867
##
   ARIMA(1,0,0)(0,1,0)[12]
                                                : 560.4046
##
                                                : 558.1656
   ARIMA(1,0,0)(0,1,0)[12] with drift
  ARIMA(1,0,0)(0,1,1)[12]
                                                : 557.062
##
   ARIMA(1,0,0)(0,1,1)[12] with drift
                                                : Inf
##
   ARIMA(1,0,0)(0,1,2)[12]
                                                : 556.7227
##
   ARIMA(1,0,0)(0,1,2)[12] with drift
                                                : Inf
                                                : 557.8419
##
  ARIMA(1,0,0)(1,1,0)[12]
   ARIMA(1,0,0)(1,1,0)[12] with drift
                                                : 554.1541
##
                                                : Inf
   ARIMA(1,0,0)(1,1,1)[12]
  ARIMA(1,0,0)(1,1,1)[12] with drift
                                               : Inf
## ARIMA(1,0,0)(1,1,2)[12]
                                                : Inf
   ARIMA(1,0,0)(1,1,2)[12] with drift
                                                : Inf
##
## ARIMA(1,0,0)(2,1,0)[12]
                                                : 559.8259
  ARIMA(1,0,0)(2,1,0)[12] with drift
                                                : 555.6822
##
  ARIMA(1,0,0)(2,1,1)[12]
                                                : 562.0418
##
   ARIMA(1,0,0)(2,1,1)[12] with drift
                                                : 558.1768
##
                                                : Inf
   ARIMA(1,0,0)(2,1,2)[12]
  ARIMA(1,0,0)(2,1,2)[12] with drift
                                                : Inf
                                                : 562.3449
##
   ARIMA(1,0,1)(0,1,0)[12]
##
   ARIMA(1,0,1)(0,1,0)[12] with drift
                                                : 560.3232
##
   ARIMA(1,0,1)(0,1,1)[12]
                                                : 558.9252
  ARIMA(1,0,1)(0,1,1)[12] with drift
                                                : Inf
##
   ARIMA(1,0,1)(0,1,2)[12]
                                                : Inf
                                                : Inf
## ARIMA(1,0,1)(0,1,2)[12] with drift
## ARIMA(1,0,1)(1,1,0)[12]
                                                : 559.7744
## ARIMA(1,0,1)(1,1,0)[12] with drift
                                               : 556.3705
## ARIMA(1,0,1)(1,1,1)[12]
                                                : Inf
```

```
ARIMA(1,0,1)(1,1,1)[12] with drift
                                                : Inf
##
                                                : Inf
   ARIMA(1,0,1)(1,1,2)[12]
                                                : Inf
## ARIMA(1,0,1)(1,1,2)[12] with drift
                                                : 561.7711
## ARIMA(1,0,1)(2,1,0)[12]
##
   ARIMA(1,0,1)(2,1,0)[12] with drift
                                                : 557.9455
## ARIMA(1,0,1)(2,1,1)[12]
                                                : 563.9685
## ARIMA(1,0,1)(2,1,1)[12] with drift
                                                : 560.4787
## ARIMA(1,0,2)(0,1,0)[12]
                                                : 564.0932
##
   ARIMA(1,0,2)(0,1,0)[12] with drift
                                                : 561.8723
##
   ARIMA(1,0,2)(0,1,1)[12]
                                                : 561.1159
   ARIMA(1,0,2)(0,1,1)[12] with drift
                                                : Inf
                                                : Inf
##
   ARIMA(1,0,2)(0,1,2)[12]
##
   ARIMA(1,0,2)(0,1,2)[12] with drift
                                                : Inf
##
   ARIMA(1,0,2)(1,1,0)[12]
                                                : 561.9663
   ARIMA(1,0,2)(1,1,0)[12] with drift
                                                : 558.4588
##
##
   ARIMA(1,0,2)(1,1,1)[12]
                                                : Inf
                                                : Inf
##
   ARIMA(1,0,2)(1,1,1)[12] with drift
##
  ARIMA(1,0,2)(2,1,0)[12]
                                                : 563.9871
                                                : 559.9179
##
  ARIMA(1,0,2)(2,1,0)[12] with drift
   ARIMA(1,0,3)(0,1,0)[12]
                                                : 565.2932
##
   ARIMA(1,0,3)(0,1,0)[12] with drift
                                                : 562.8614
                                                : 563.0312
## ARIMA(1,0,3)(0,1,1)[12]
                                                : Inf
## ARIMA(1,0,3)(0,1,1)[12] with drift
                                                : 563.536
##
   ARIMA(1,0,3)(1,1,0)[12]
                                                : 559.4505
## ARIMA(1,0,3)(1,1,0)[12] with drift
   ARIMA(1,0,4)(0,1,0)[12]
                                                : 567.142
##
   ARIMA(1,0,4)(0,1,0)[12] with drift
                                                : 564.8129
##
   ARIMA(2,0,0)(0,1,0)[12]
                                                : 562.3127
##
                                                : 560.3192
   ARIMA(2,0,0)(0,1,0)[12] with drift
  ARIMA(2,0,0)(0,1,1)[12]
                                                : 558.9159
##
   ARIMA(2,0,0)(0,1,1)[12] with drift
                                                : Inf
##
   ARIMA(2,0,0)(0,1,2)[12]
                                                : Inf
##
   ARIMA(2,0,0)(0,1,2)[12] with drift
                                                : Inf
                                                : 559.7676
##
  ARIMA(2,0,0)(1,1,0)[12]
   ARIMA(2,0,0)(1,1,0)[12] with drift
                                                : 556.3704
                                                : Inf
##
   ARIMA(2,0,0)(1,1,1)[12]
   ARIMA(2,0,0)(1,1,1)[12] with drift
                                               : Inf
##
  ARIMA(2,0,0)(1,1,2)[12]
                                                : Inf
   ARIMA(2,0,0)(1,1,2)[12] with drift
                                                : Inf
##
##
                                                : 561.759
   ARIMA(2,0,0)(2,1,0)[12]
  ARIMA(2,0,0)(2,1,0)[12] with drift
                                                : Inf
##
  ARIMA(2,0,0)(2,1,1)[12]
                                                : Inf
##
   ARIMA(2,0,0)(2,1,1)[12] with drift
                                                : Inf
##
                                                : 564.4078
   ARIMA(2,0,1)(0,1,0)[12]
  ARIMA(2,0,1)(0,1,0)[12] with drift
                                                : 562.4507
                                                : 561.1317
##
   ARIMA(2,0,1)(0,1,1)[12]
##
   ARIMA(2,0,1)(0,1,1)[12] with drift
                                                : Inf
##
                                                : Inf
   ARIMA(2,0,1)(0,1,2)[12]
                                                : Inf
  ARIMA(2,0,1)(0,1,2)[12] with drift
##
   ARIMA(2,0,1)(1,1,0)[12]
                                                : 561.9841
                                                : 558.6319
## ARIMA(2,0,1)(1,1,0)[12] with drift
## ARIMA(2,0,1)(1,1,1)[12]
                                                : Inf
## ARIMA(2,0,1)(1,1,1)[12] with drift
                                                : Inf
## ARIMA(2,0,1)(2,1,0)[12]
                                                : Inf
```

```
ARIMA(2,0,1)(2,1,0)[12] with drift
                                               : 560.1475
                                               : 566.089
## ARIMA(2,0,2)(0,1,0)[12]
## ARIMA(2,0,2)(0,1,0)[12] with drift
                                               : 563.1382
## ARIMA(2,0,2)(0,1,1)[12]
                                               : 563.3754
## ARIMA(2,0,2)(0,1,1)[12] with drift
                                               : 564.2091
## ARIMA(2,0,2)(1,1,0)[12]
                                              : 560.1002
## ARIMA(2,0,2)(1,1,0)[12] with drift
## ARIMA(2,0,3)(0,1,0)[12]
                                               : 567.3445
##
   ARIMA(2,0,3)(0,1,0)[12] with drift
                                               : 564.098
## ARIMA(3,0,0)(0,1,0)[12]
                                               : 564.219
## ARIMA(3,0,0)(0,1,0)[12] with drift
                                               : 561.827
                                               : 561.1288
## ARIMA(3,0,0)(0,1,1)[12]
## ARIMA(3,0,0)(0,1,1)[12] with drift
                                               : Inf
## ARIMA(3,0,0)(0,1,2)[12]
                                               : Inf
                                               : Inf
## ARIMA(3,0,0)(0,1,2)[12] with drift
   ARIMA(3,0,0)(1,1,0)[12]
                                               : 561.9824
                                               : 558.4254
## ARIMA(3,0,0)(1,1,0)[12] with drift
## ARIMA(3,0,0)(1,1,1)[12]
                                               : Inf
## ARIMA(3,0,0)(1,1,1)[12] with drift
                                               : Inf
   ARIMA(3,0,0)(2,1,0)[12]
                                               : 564.012
## ARIMA(3,0,0)(2,1,0)[12] with drift
                                               : 559.8617
## ARIMA(3,0,1)(0,1,0)[12]
                                               : Inf
                                               : Inf
## ARIMA(3,0,1)(0,1,0)[12] with drift
                                               : Inf
## ARIMA(3,0,1)(0,1,1)[12]
                                               : Inf
## ARIMA(3,0,1)(0,1,1)[12] with drift
## ARIMA(3,0,1)(1,1,0)[12]
                                               : Inf
## ARIMA(3,0,1)(1,1,0)[12] with drift
                                               : 560.4603
## ARIMA(3,0,2)(0,1,0)[12]
                                               : Inf
## ARIMA(3,0,2)(0,1,0)[12] with drift
                                               : Inf
## ARIMA(4,0,0)(0,1,0)[12]
                                               : 566.2388
## ARIMA(4,0,0)(0,1,0)[12] with drift
                                               : 563.3861
## ARIMA(4,0,0)(0,1,1)[12]
                                               : 563.3083
## ARIMA(4,0,0)(0,1,1)[12] with drift
                                               : Inf
                                               : 564.0207
## ARIMA(4,0,0)(1,1,0)[12]
   ARIMA(4,0,0)(1,1,0)[12] with drift
                                               : 559.6753
                                              : Inf
## ARIMA(4,0,1)(0,1,0)[12]
## ARIMA(4,0,1)(0,1,0)[12] with drift
                                              : 565.6208
                                               : 567.6812
  ARIMA(5,0,0)(0,1,0)[12]
##
   ARIMA(5,0,0)(0,1,0)[12] with drift
                                               : 565.4329
##
##
##
   Best model: ARIMA(1,0,0)(1,1,0)[12] with drift
```

Based on the these auto arima functions run, we can see that the best model is ARIMA(1,0,0)(2,1,0)[12] with drift

```
#ARIMA
plot(fit1$residuals)
```

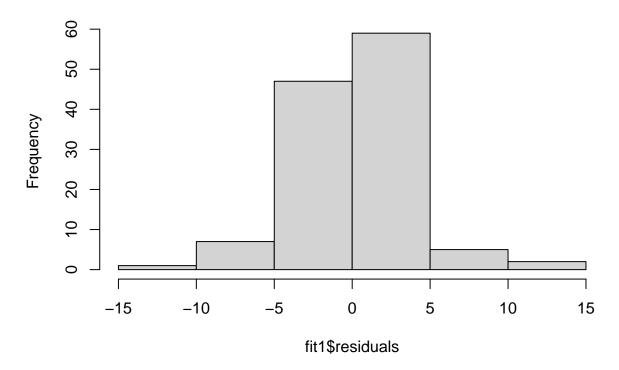


## These residuals looks very good since it appears to be white noise - There appears to be no seasonality or trend.

#### #ARIMA

hist(fit1\$residuals)

## Histogram of fit1\$residuals

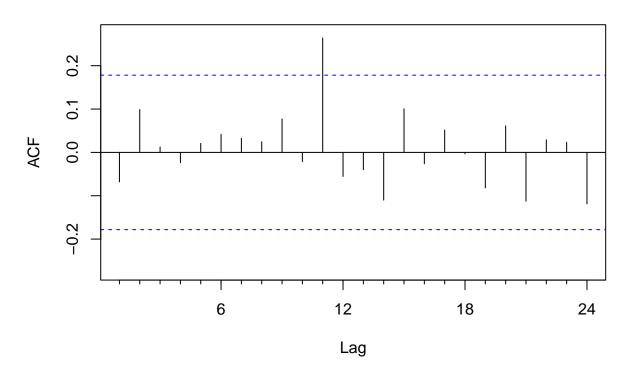


## This histogram plot seems to indicate that the data is normally distributed which is good for our residuals.

#### #ARIMA

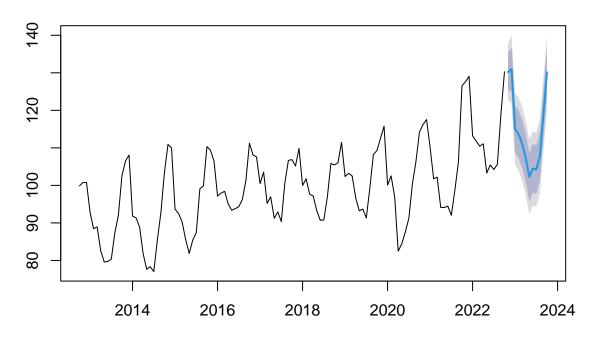
Acf(fit1\$residuals)

### Series fit1\$residuals



## This plot indicates that this plot is indeed the best because there is no trend or seasonality in the data. There values are also not statistically significant except for one and that appears to be a mistake.

#### Forecasts from ARIMA(1,0,0)(2,1,0)[12] with drift



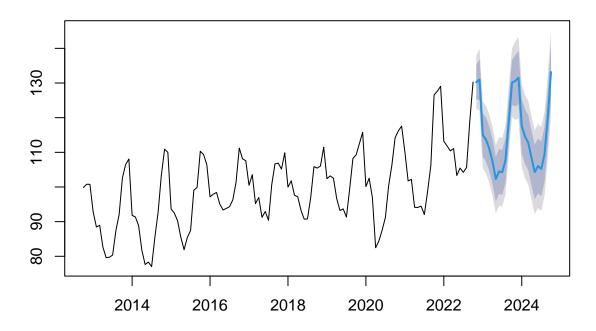
# #ARIMA oneyear\_arima

```
##
            Point Forecast
                               Lo 80
                                        Hi 80
                                                  Lo 95
                                                           Hi 95
## Nov 2022
                  130.2152 125.25972 135.1707 122.63645 137.7939
## Dec 2022
                  130.9781 125.08373 136.8725 121.96344 139.9928
## Jan 2023
                  115.0259 108.78339 121.2685 105.47879 124.5731
## Feb 2023
                  113.6240 107.24263 120.0054 103.86452 123.3835
                  111.0655 104.62735 117.5036 101.21922 120.9117
## Mar 2023
## Apr 2023
                  107.3725 100.91103 113.8341 97.49052 117.2546
## May 2023
                  102.3049
                           95.83376 108.7761 92.40812 112.2018
## Jun 2023
                  104.4700
                           97.99476 110.9451
                                               94.56700 114.3729
## Jul 2023
                  104.2670 97.79014 110.7439
                                               94.36150 114.1725
## Aug 2023
                  107.8069 101.32940 114.2845
                                              97.90040 117.7135
## Sep 2023
                  119.0309 112.55302 125.5087 109.12386 128.9378
## Oct 2023
                  130.1239 123.64593 136.6018 120.21671 140.0310
```

```
#ARIMA

twoyear_arima <- (forecast(fit1, h=24))
plot(twoyear_arima)</pre>
```

#### Forecasts from ARIMA(1,0,0)(2,1,0)[12] with drift



#### #ARIMA

twoyear\_arima

```
Point Forecast
                               Lo 80
                                        Hi 80
                                                   Lo 95
## Nov 2022
                  130.2152 125.25972 135.1707 122.63645 137.7939
## Dec 2022
                  130.9781 125.08373 136.8725 121.96344 139.9928
## Jan 2023
                  115.0259 108.78339 121.2685 105.47879 124.5731
## Feb 2023
                  113.6240 107.24263 120.0054 103.86452 123.3835
## Mar 2023
                  111.0655 104.62735 117.5036 101.21922 120.9117
## Apr 2023
                  107.3725 100.91103 113.8341
                                               97.49052 117.2546
## May 2023
                  102.3049
                            95.83376 108.7761
                                               92.40812 112.2018
## Jun 2023
                  104.4700
                            97.99476 110.9451
                                               94.56700 114.3729
## Jul 2023
                            97.79014 110.7439
                                               94.36150 114.1725
                  104.2670
## Aug 2023
                  107.8069 101.32940 114.2845
                                               97.90040 117.7135
                  119.0309 112.55302 125.5087 109.12386 128.9378
## Sep 2023
## Oct 2023
                  130.1239 123.64593 136.6018 120.21671 140.0310
## Nov 2023
                  130.6058 123.25537 137.9562 119.36428 141.8473
## Dec 2023
                  131.5482 123.86490 139.2316 119.79758 143.2989
## Jan 2024
                  117.6141 109.79684 125.4314 105.65861 129.5696
## Feb 2024
                  114.5620 106.68977 122.4341 102.52249 126.6014
## Mar 2024
                  112.7877 104.89290 120.6826 100.71362 124.8619
## Apr 2024
                  108.3628 100.45859 116.2670
                                               96.27435 120.4513
## May 2024
                  104.2936
                            96.38545 112.2017
                                               92.19915 116.3880
## Jun 2024
                  106.0342 98.12451 113.9440 93.93735 118.1311
```

```
## Jul 2024 105.2377 97.32733 113.1481 93.13982 117.3356

## Aug 2024 109.3693 101.45862 117.2800 97.27097 121.4676

## Sep 2024 119.8675 111.95676 127.7783 107.76904 131.9660

## Oct 2024 133.1484 125.23761 141.0593 121.04987 145.2470
```

We will see that in October 2023(a year from this point in time) the prediction is giving us 130 and in two years time(October 2024) we are getting 133.

Overall we can see that this forecasting technique is very good; the residuals are random and not significant and we can see the forecast is incorporating the positive trend as well as seasonality.